

Statistical Test Results for RQ1–RQ4 (COMPLEMENTS RESULTS in SECTION 5)

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Table 1. Statistical tests for **RQ1** comparing **AMPL-based variants** and **Python-based variants** based on (a) execution success rate (Success) and zero relative-error rates (#Zero/#Exec) using the Z-test; and (b) based on relative-error using the Mann-Whitney *U* test. Blue cells indicate significant improvements of AMPL-based over Python-based variants. No significant difference with Python-based variants outperforms AMPL-based variants.

(a) Comparing the variants based on the Success and #Zero/#Exec metrics										
Variant			PUBLIC				Industry			
LLM	Structuring	Refinement	Success		#Zero/#Exec		Success		#Zero/#Exec	
			Z	p-value	Z	p-value	Z	p-value	Z	p-value
Gemini 1.5-Flash	Unstructured	One-off	-5.31	1.00	3.15	0.00	-2.34	0.99	0.83	0.20
		Refinement	3.02	0.00	-1.64	0.95	-1.10	0.86	0.04	0.48
	Structured	One-off	-0.32	0.63	-0.67	0.75	-2.61	1.00	0.78	0.22
		Refinement	6.64	0.00	2.12	0.02	0.00	0.50	0.00	0.50
GPT-4o	Unstructured	One-off	-8.56	1.00	2.05	0.02	0.00	0.50	-0.94	0.83
		Refinement	-3.72	1.00	2.30	0.01	0.27	0.40	0.47	0.32
	Structured	One-off	-2.76	1.00	-3.60	1.00	-4.39	1.00	0.63	0.27
		Refinement	6.24	0.00	-2.74	1.00	-0.55	0.71	2.82	0.00
Gemini 2.5-Pro	Unstructured	One-off	-4.82	1.00	0.69	0.25	-1.39	0.92	-0.09	0.53
		Refinement	-1.06	0.86	-3.49	1.00	-0.47	0.68	-0.19	0.57
	Structured	One-off	-2.62	1.00	0.32	0.38	-2.09	0.98	1.65	0.05
		Refinement	2.20	0.01	2.68	0.00	0.00	0.50	-0.34	0.63
o4-mini	Unstructured	One-off	-4.33	1.00	3.73	0.00	-1.13	0.87	-0.69	0.76
		Refinement	0.26	0.40	1.15	0.13	0.31	0.38	-0.35	0.64
	Structured	One-off	3.71	0.00	-1.35	0.91	-0.55	0.71	0.51	0.30
		Refinement	7.77	0.00	-4.77	1.00	0.31	0.38	0.07	0.47

(b) Comparing the variants based on the relative-error metric						
Variant			PUBLIC Dataset		INDUSTRY Dataset	
LLM	Structuring	Refinement	p-value	\hat{A}_{12}	p-value	\hat{A}_{12}
Gemini 1.5-Flash	Unstructured	One-off	0.23	0.47	0.53	0.50
		Refinement	1.00	0.58	0.93	0.57
	Structured	One-off	0.99	0.58	0.86	0.54
		Refinement	0.00	0.41(S)	0.56	0.51
GPT-4o	Unstructured	One-off	0.13	0.46	0.57	0.51
		Refinement	0.04	0.45(N)	0.32	0.45
	Structured	One-off	1.00	0.60	0.50	0.48
		Refinement	0.98	0.56	0.01	0.32(M)
Gemini 2.5-Pro	Unstructured	One-off	0.23	0.48	0.84	0.56
		Refinement	1.00	0.57	0.51	0.50
	Structured	One-off	0.11	0.47	1.00	0.50
		Refinement	0.00	0.42(S)	0.72	0.53
o4-mini	Unstructured	One-off	0.01	0.45(N)	0.68	0.53
		Refinement	0.17	0.48	0.48	0.50
	Structured	One-off	0.82	0.52	0.17	0.47
		Refinement	1.00	0.59	0.49	0.50

Table 2. Statistical tests for **RQ2** comparing **structured variants** and **unstructured variants** based on (a) execution success rate (Success) and zero relative-error rates (#Zero/#Exec) using the Z-test; and (b) based on relative-error using the Mann-Whitney U test. Blue cells indicate significant improvements of structured over unstructured variants. No significant difference with unstructured variants outperforms structured variants.

(a) Comparing the variants based on the Success and #Zero/#Exec metrics

Variant			PUBLIC				INDUSTRY			
LLM	Language	Refinement	Success		#Zero/#Exec		Success		#Zero/#Exec	
			Z	p-value	Z	p-value	Z	p-value	Z	p-value
Gemini 1.5-Flash	AMPL	One-off	2.63	0.00	-2.98	1.00	0.00	0.50	0.00	0.50
		Refinement	0.96	0.17	6.06	0.00	1.69	0.04	-0.21	0.58
	Python	One-off	-2.39	0.99	0.75	0.22	0.29	0.39	0.07	0.47
		Refinement	-2.79	1.00	1.88	0.03	0.61	0.27	-0.18	0.57
GPT-4o	AMPL	One-off	2.44	0.00	-2.65	1.00	-1.39	0.92	0.21	0.41
		Refinement	5.73	0.00	-3.58	1.00	0.00	0.50	1.91	0.03
	Python	One-off	-3.53	1.00	3.02	0.00	3.16	0.00	-1.50	0.93
		Refinement	-4.25	1.00	1.47	0.07	0.81	0.21	-0.49	0.69
Gemini 2.5-Pro	AMPL	One-off	0.67	0.25	-3.65	1.00	-1.06	0.85	1.83	0.03
		Refinement	0.31	0.38	3.13	0.00	0.38	0.35	0.42	0.34
	Python	One-off	-1.62	0.95	-3.54	1.00	-0.33	0.63	0.23	0.41
		Refinement	-2.92	1.00	-3.04	1.00	-0.09	0.53	0.58	0.28
o4-mini	AMPL	One-off	1.92	0.03	-2.15	0.98	0.00	0.50	1.44	0.07
		Refinement	2.15	0.02	-2.95	1.00	0.00	0.50	0.00	0.50
	Python	One-off	-6.07	1.00	2.89	0.00	-0.58	0.72	0.37	0.36
		Refinement	-5.80	1.00	3.14	0.00	0.00	0.50	0.41	0.34

(b) Comparing the variants based on the relative-error metric

Variant			PUBLIC Dataset		INDUSTRY Dataset	
LLM	Language	Refinement	p-value	\hat{A}_{12}	p-value	\hat{A}_{12}
Gemini 1.5-Flash	AMPL	One-off	1.00	0.54	1.00	0.50
		Refinement	0.00	0.34(M)	0.04	0.41(S)
	Python	One-off	0.49	0.50	0.34	0.47
		Refinement	0.11	0.47	0.58	0.51
GPT-4o	AMPL	One-off	0.95	0.56	1.00	0.50
		Refinement	1.00	0.57	0.07	0.39
	Python	One-off	0.01	0.44(S)	0.79	0.57
		Refinement	0.17	0.47	0.78	0.57
Gemini 2.5-Pro	AMPL	One-off	1.00	0.58	0.18	0.46
		Refinement	0.00	0.42(S)	0.55	0.51
	Python	One-off	1.00	0.59	0.48	0.50
		Refinement	1.00	0.58	0.32	0.47
o4-mini	AMPL	One-off	0.99	0.55	0.54	0.50
		Refinement	1.00	0.56	0.44	0.49
	Python	One-off	0.07	0.46	0.85	0.53
		Refinement	0.03	0.46(N)	0.52	0.50

Table 3. Statistical tests for **RQ3** comparing **refinement variants** and **one-off variants** based on (a) execution success rate (Success %) and zero relative-error rates (#Zero/#Exec) using the Z-test; and (b) based on relative-error using the Mann-Whitney U test. Blue cells indicate significant improvements of refinement over one-off variants. No significant difference with one-off variants outperforms refinement variants.

(a) Comparing the variants based on the Success % and #Zero/#Exec metrics

Variant			PUBLIC				INDUSTRY			
LLM	Language	Structuring	Success %		#Zero/#Exec		Success %		#Zero/#Exec	
			Z	p-value	Z	p-value	Z	p-value	Z	p-value
Gemini 1.5-Flash	AMPL	Unstructured	10.68	0.00	-4.91	1.00	1.55	0.06	-1.00	0.84
		Structured	9.10	0.00	3.49	0.00	3.16	0.00	-1.19	0.88
	Python	Unstructured	2.71	0.00	-0.31	0.62	0.29	0.39	-0.30	0.62
		Structured	2.30	0.01	0.69	0.24	0.61	0.27	-0.56	0.71
GPT-4o	AMPL	Unstructured	7.13	0.00	-0.63	0.73	1.81	0.03	-0.11	0.58
		Structured	10.15	0.00	-0.77	0.78	3.13	0.00	1.13	0.13
	Python	Unstructured	2.23	0.01	-0.60	0.73	1.50	0.06	-1.58	0.94
		Structured	1.48	0.07	-2.13	0.98	-0.89	0.81	-0.72	0.76
Gemini 2.5-Pro	AMPL	Unstructured	5.13	0.00	-3.74	1.00	0.79	0.21	-0.69	0.75
		Structured	4.80	0.00	3.04	0.00	2.19	0.01	-2.04	0.98
	Python	Unstructured	1.43	0.08	0.25	0.40	-0.15	0.56	-0.66	0.75
		Structured	0.08	0.47	0.75	0.22	0.09	0.46	-0.30	0.62
o4-mini	AMPL	Unstructured	5.45	0.00	-0.29	0.62	1.43	0.08	0.37	0.36
		Structured	5.53	0.00	-0.88	0.81	1.43	0.08	-1.16	0.88
	Python	Unstructured	0.92	0.18	2.53	0.01	0.00	0.50	-0.41	0.66
		Structured	1.15	0.12	2.43	0.01	0.58	0.28	-0.37	0.64

(b) Comparing the variants based on the relative-error metric

Variant			PUBLIC Dataset		INDUSTRY Dataset		
LLM	Language	Structuring	p-value	\hat{A}_{12}	p-value	\hat{A}_{12}	
Gemini 1.5-Flash	AMPL	Unstructured	1.00	0.64	0.86	0.58	
		Structured	0.00	0.41(S)	0.82	0.56	
	Python	Unstructured	0.68	0.51	0.69	0.53	
		Structured	0.26	0.48	0.63	0.53	
GPT-4o	AMPL	Unstructured	0.72	0.52	0.40	0.47	
		Structured	0.78	0.52	0.16	0.41	
	Python	Unstructured	0.78	0.52	0.88	0.61	
		Structured	0.99	0.56	0.79	0.56	
Gemini 2.5-Pro	AMPL	Unstructured	1.00	0.58	0.72	0.54	
		Structured	0.00	0.43(S)	0.98	0.38	
	Python	Unstructured	0.38	0.49	0.77	0.54	
		Structured	0.21	0.48	0.62	0.52	
o4-mini	AMPL	Unstructured	0.65	0.51	0.38	0.48	
		Structured	0.78	0.52	0.88	0.56	
	Python	Unstructured	0.07	0.47	0.64	0.52	
		Structured	0.01	0.45(N)	0.67	0.52	

Table 4. Statistical tests for **RQ4** comparing EXEOS variants when instantiated with **reasoning** LLMs, i.e., Gemini 2.5-Pro and o4-mini, versus when instantiated with **instruction-following** LLMs, i.e., Gemini 1.5-Flash and GPT-4o, based on (a) execution success rate (Success) and zero relative-error rates (#Zero/#Exec) using the Z-test, and (b) relative-error using the Mann-Whitney U test. Blue cells indicate significant improvements in results obtained with reasoning LLMs over those obtained with instruction-following LLMs. No significant difference where instruction-following LLMs outperforms reasoning LLMs.

(a) Comparing the variants based on the Success and #Zero/#Exec metrics

Language	Variant		PUBLIC				INDUSTRY			
	Structuring	Refinement	Success %		#Zero/#Exec		Success %		#Zero/#Exec	
			Z	p-value	Z	p-value	Z	p-value	Z	p-value
AMPL	Unstructured	One-off	12.78	0.00	1.34	0.09	2.30	0.01	-0.02	0.51
		Refinement	8.02	0.00	4.07	0.00	1.99	0.02	0.65	0.26
	Structured	One-off	11.23	0.00	2.51	0.01	2.58	0.00	1.66	0.05
		Refinement	4.10	0.00	2.38	0.01	1.07	0.14	-0.27	0.60
Python	Unstructured	One-off	9.79	0.00	3.09	0.00	2.59	0.00	0.18	0.43
		Refinement	8.03	0.00	5.84	0.00	1.65	0.05	1.00	0.16
	Structured	One-off	8.04	0.00	-0.41	0.66	-0.42	0.66	1.92	0.03
		Refinement	11.35	0.00	-0.03	0.51	0.43	0.33	2.28	0.01

(b) Comparing the variants based on the relative-error metric

Variant			PUBLIC Dataset		INDUSTRY Dataset	
Language	Structuring	Refinement	p-value	\hat{A}_{12}	p-value	\hat{A}_{12}
AMPL	Unstructured	One-off	0.04	0.47(N)	0.40	0.49
		Refinement	0.00	0.42(S)	0.38	0.48
	Structured	One-off	0.01	0.45(N)	0.05	0.44
		Refinement	0.01	0.47(N)	0.60	0.51
Python	Unstructured	One-off	0.00	0.45(N)	0.41	0.49
		Refinement	0.00	0.42(S)	0.19	0.46
	Structured	One-off	0.76	0.51	0.03	0.42(S)
		Refinement	0.62	0.51	0.01	0.39(M)