

3.4

HW #9

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33.

$$A = \begin{bmatrix} 1 & 1 \\ 1 & 2 \end{bmatrix} \quad B = \begin{bmatrix} 2 & -1 \\ -2 & 3 \end{bmatrix}$$

$$|A| = 1(2) - 1(1)$$

$$|A| = 1$$

$$|B| = 2(3) - (-2)(-1)$$

$$|B| = 4$$

$$|A| + |B| = 5$$

$$A + B = \begin{bmatrix} 3 & 0 \\ -1 & 5 \end{bmatrix}$$

$$|A+B| = 3(5) - (-1)(0)$$

$$|A+B| = 15$$

$$\therefore |A+B| \neq |A| + |B|$$

34.

$$A = \begin{bmatrix} 1 & 3 \\ 3 & 1 \end{bmatrix} \quad B = \begin{bmatrix} 3 & 1 \\ 1 & 3 \end{bmatrix}$$

$$|A| = (1)(1) - 3(3)$$

$$= -8$$

$$|B| = 3(3) - 1(1)$$

$$= 8$$

$$|A| + |B| = 0$$

$$|A+B| = \begin{bmatrix} 4 & 4 \\ 4 & 4 \end{bmatrix}$$

$$= 4(4) - 4(4)$$

$$= 0$$

$$\therefore |A+B| \leq |A| + |B|$$

$$39. \quad x + 2y = 2$$

$$2x + 5y = 0$$

$$x_1 = \frac{A_1}{A} = \frac{10}{1} = 10$$

$$x_2 = \frac{A_2}{A} = \frac{-4}{1} = -4$$

$$A = \begin{bmatrix} 1 & 2 \\ 2 & 5 \end{bmatrix} = 1(5) - 2(2) = 1$$

$$A_1 = \begin{bmatrix} 2 & 2 \\ 0 & 5 \end{bmatrix} = 2(5) - 0(2) = 10$$

$$A_2 = \begin{bmatrix} 1 & 2 \\ 2 & 0 \end{bmatrix} = 1(0) - 2(2) = -4$$

$$\boxed{x = 10, y = -4}$$

W is a subspace of V, W is a vector space