Boost.Ratio 1.0.0

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Warning

Ratio is not part of the Boost libraries.

Overview

How to Use This Documentation

This documentation makes use of the following naming and formatting conventions.

- Code is in fixed width font and is syntax-highlighted.
- Replaceable text that you will need to supply is in italics.
- Free functions are rendered in the code font followed by (), as in free_function().



- If a name refers to a class template, it is specified like this: class_template<>; that is, it is in code font and its name is followed by <> to indicate that it is a class template.
- If a name refers to a function-like macro, it is specified like this: MACRO(); that is, it is uppercase in code font and its name is followed by () to indicate that it is a function-like macro. Object-like macros appear without the trailing ().
- Names that refer to concepts in the generic programming sense are specified in CamelCase.



Note

In addition, notes such as this one specify non-essential information that provides additional background or rationale.

Finally, you can mentally add the following to any code fragments in this document:

```
// Include all of Ratio files
#include <boost/ratio.hpp>
using namespace boost;
```

Motivation

Boost.Ratio aims to implement the compile time ratio facility in C++0x, as proposed in **N2661 - A Foundation to Sleep On**. That document provides background and motivation for key design decisions and is the source of a good deal of information in this documentation.

Description

The **Boost.Ratio** library provides:

- A class template, ratio, for specifying compile time rational constants such as 1/3 of a nanosecond or the number of inches per
 meter. ratio represents a compile time ratio of compile time constants with support for compile time arithmetic with overflow
 and division by zero protection
- It provides a textual representation of boost::ratio<N, D> in the form of a std::basic_string which can be useful for I/O.

User's Guide

Getting Started

Installing Ratio

Getting Boost.Ratio

You can get the last stable release of Boost.Ratio by downloading ratio.zip from the Boost Vault.

You can also access the latest (unstable?) state from the Boost Sandbox directories boost/ratio and libs/ratio. Just go to here and follow the instructions there for anonymous SVN access.

Where to install Boost.Ratio?

The simple way is to decompress (or checkout from SVN) the file in your BOOST_ROOT directory.

Othesewise, if you decompress in a different directory, you will need to comment some lines, and uncomment and change others in the build/Jamfile and test/Jamfile. Sorry for this, but I have not reached yet to write a Jamfile that is able to work in both environements and use the BOOST_ROOT variable. Any help is welcome.



Building Boost.Ratio

Boost.Ratio is a header only library, so no need to compile anything.

Requirements

Boost.Ratio depends on some Boost libraries. For these specific parts you must use either Boost version 1.39.0 or later (even if older versions should works also).

In particular, Boost.Ratio depends on:

Boost.Config for configuration purposes, ...

Boost.Integer for cstdint conformance, and integer traits ...

Boost.MPL for MPL Assert and bool, logical ...

Boost.StaticAssert for STATIC_ASSERT, ...

Boost.TypeTraits for is_base, is_convertible ...

Boost.Utility/EnableIf for enable_if, ...

Building an executable that uses Boost.Ratio

No link is needed.

Exception safety

All functions in the library are exception-neutral, providing the strong exception safety guarantee.

Thread safety

All functions in the library are thread-unsafe except when noted explicitly.

Tested compilers

Boost.Ratio should work with an C++03 conforming compiler. The current version has been tested on:

Windows with

- MSVC 10.0
- MSVC 9.0 Express
- MSVC 8.0

Scientific Linux with

• GCC 4.1.2

Cygwin with

- GCC 3.4.4
- GCC 4.3.2

MinGW with

- GCC 4.4.0
- GCC 4.5.0



Initial version was tested on:

MacOS with GCC 4.2.4

Ubuntu Linux with GCC 4.2.4



Note

Please let us know how this works on other platforms/compilers.



Note

Please send any questions, comments and bug reports to boost <at> lists <dot> boost <dot> org.

Tutorial

Ratio

ratio is a general purpose utility inspired by Walter Brown allowing one to easily and safely compute rational values at compile time. The ratio class catches all errors (such as divide by zero and overflow) at compile time. It is used in the duration and time_point classes to efficiently create units of time. It can also be used in other "quantity" libraries or anywhere there is a rational constant which is known at compile time. The use of this utility can greatly reduce the chances of run time overflow because the ratio (and any ratios resulting from ratio arithmetic) are always reduced to lowest terms.

ratio is a template taking two intmax_ts, with the second defaulted to 1. In addition to copy constructors and assignment, it only has two public members, both of which are static const intmax_t. One is the numerator of the ratio and the other is the denominator. The ratio is always normalized such that it is expressed in lowest terms, and the denominator is always positive. When the numerator is 0, the denominator is always 1.

Example:

```
typedef ratio<5, 3> five_thirds;
// five_thirds::num == 5, five_thirds::den == 3

typedef ratio<25, 15> also_five_thirds;
// also_five_thirds::num == 5, also_five_thirds::den == 3

typedef ratio_divide<five_thirds, also_five_thirds>::type one;
// one::num == 1, one::den == 1
```

This facility also includes convenience typedefs for the SI prefixes atto through exa corresponding to their internationally recognized definitions (in terms of ratio). This is a tremendous syntactic convenience. It will prevent errors in specifying constants as one no longer has to double count the number of zeros when trying to write millions or billions.

Example:



```
typedef ratio_multiply<ratio<5>, giga>::type _5giga;
// _5giga::num == 50000000000, _5giga::den == 1

typedef ratio_multiply<ratio<5>, nano>::type _5nano;
// _5nano::num == 1, _5nano::den == 200000000
```

Ratio I/O

For each ratio<N, D> there exists a ratio_string<ratio<N, D>, CharT> for which you can query two strings: short_name and long_name. For those ratio's that correspond to an SI prefix long_name corresponds to the internationally recognized prefix, stored as a basic_string<CharT>. For example ratio_string<mega, char>::long_name() returns string("mega"). For those ratio's that correspond to an SI prefix short_name corresponds to the internationally recognized symbol, stored as a basic_string<CharT>. For example ratio_string<mega, char>::short_name() returns string("M"). For all other ratio's, both long_name() and short_name() return a basic_string containing "[ratio::num/ratio::den]".

ratio_string<ratio<N, D>, CharT> is only defined for four character types:

- char: UTF-8
- char16_t: UTF-16
- char32_t: UTF-32
- wchar_t: UTF-16 (if wchar_t is 16 bits) or UTF-32

When the character is char, UTF-8 will be used to encode the names. When the character is char16_t, UTF-16 will be used to encode the names. When the character is char32_t, UTF-32 will be used to encode the names. When the character is wchar_t, the encoding will be UTF-16 if wchar_t is 16 bits, and otherwise UTF-32.

The short_name for micro is defined by Unicode to be U+00B5.

Examples:

```
#include <boost/ratio/ratio_io.hpp>
#include <iostream>
int main()
    using namespace std;
    using namespace boost;
    cout << "ratio_string<deca, char>::long_name() = "
         << ratio_string<deca, char>::long_name() << '\n';
    cout << "ratio_string<deca, char>::short_name() = '
         << ratio_string<deca, char>::short_name() << '\n';</pre>
    cout << "ratio_string<giga, char>::long_name() = "
             ratio_string<giga, char>::long_name() << '\n';</pre>
    cout << "ratio_string<giga, char>::short_name() = "
         << ratio_string<giga, char>::short_name() << '\n';
    cout << "ratio_string<ratio<4, 6>, char>::long_name() = "
         << ratio_string<ratio<4, 6>, char>::long_name() << '\n';</pre>
    cout << "ratio_string<ratio<4, 6>, char>::short_name() = "
         << ratio_string<ratio<4, 6>, char>::short_name() << '\n';</pre>
```

The output will be



```
ratio_string<deca, char>::long_name() = deca
ratio_string<deca, char>::short_name() = da
ratio_string<giga, char>::long_name() = giga
ratio_string<giga, char>::short_name() = G
ratio_string<ratio<4, 6>, char>::long_name() = [2/3]
ratio_string<ratio<4, 6>, char>::short_name() = [2/3]
```

Example

SI units

This example illustrates the use of type-safe physics code interoperating with boost::chrono::duration types, taking advantage of the **Boost.Ratio** infrastructure and design philosophy.

Let's start by defining a length class template that mimics boost::chrono::duration, which represents a time duration in various units, but restricts the representation to double and uses **Boost.Ratio** for length unit conversions:

```
template <class Ratio>
class length {
private:
   double len_;
public:
    typedef Ratio ratio;
    length() : len_(1) {}
    length(const double& len) : len_(len) {}
    template <class R>
    length(const length<R>& d)
            : len_(d.count() * boost::ratio_divide<Ratio, R>::type::den /
                               boost::ratio_divide<Ratio, R>::type::num) {}
    double count() const {return len_;}
    length& operator+=(const length& d) {len_ += d.count(); return *this;}
    length& operator==(const length& d) {len_ -= d.count(); return *this;}
    length operator+() const {return *this;}
    length operator-() const {return length(-len_);}
    length& operator*=(double rhs) {len_ *= rhs; return *this;}
    length& operator/=(double rhs) {len_ /= rhs; return *this;}
```

Here's a small sampling of length units:

Note that since length's template parameter is actually a generic ratio type, so we can use boost::ratio allowing for more complex length units:

```
typedef length<boost::ratio_multiply<boost::ratio<12>, inch::ratio>::type> foot; // 12 inchs
typedef length<boost::ratio_multiply<boost::ratio<5280>, foot::ratio>::type> mile; // 5280 feet
```

Now we need a floating point-based definition of seconds:



```
typedef boost::chrono::duration<double> seconds; // unity
```

We can even support sub-nanosecond durations:

```
typedef boost::chrono::duration<double, boost::pico> picosecond; // 10^-12 seconds
typedef boost::chrono::duration<double, boost::femto> femtosecond; // 10^-15 seconds
typedef boost::chrono::duration<double, boost::atto> attosecond; // 10^-18 seconds
```

Finally, we can write a proof-of-concept of an SI units library, hard-wired for meters and floating point seconds, though it will accept other units:

```
template <class R1, class R2>
class quantity
    double q_;
public:
    typedef R1 time_dim;
    typedef R2 distance_dim;
    quantity() : q_(1) {}
    double get() const {return q_;}
    void set(double q) {q_ = q;}
};
template <>
class quantity<boost::ratio<1>, boost::ratio<0> >
    double q_;
public:
    quantity() : q_(1) {}
    quantity(seconds d) : q_(d.count())  {} // note: only User1::seconds needed here
    double get() const {return q_;}
    void set(double q) {q_ = q;}
};
template <>
class quantity<boost::ratio<0>, boost::ratio<1> >
    double q_;
public:
    quantity() : q_(1) \{ \}
    quantity(meter d) : q_(d.count()) {} // note: only User1::meter needed here
    double get() const {return q_;}
    void set(double q) {q_ = q;}
};
template <>
class quantity<boost::ratio<0>, boost::ratio<0> >
    double q_;
public:
    \mathtt{quantity()} \; : \; \mathtt{q}_{-}(1) \; \left\{ \, \right\}
    quantity(double d) : q_(d) {}
    double get() const {return q_;}
    void set(double q) {q_ = q;}
};
```

That allows us to create some useful SI-based unit types:



To make quantity useful, we need to be able to do arithmetic:

```
template <class R1, class R2, class R3, class R4>
quantity<typename boost::ratio_subtract<R1, R3>::type,
         typename boost::ratio_subtract<R2, R4>::type>
operator/(const quantity<R1, R2>& x, const quantity<R3, R4>& y)
    typedef quantity<typename boost::ratio_subtract<R1, R3>::type,
                    typename boost::ratio_subtract<R2, R4>::type> R;
    Rr;
    r.set(x.get() / y.get());
    return r;
template <class R1, class R2, class R3, class R4>
quantity<typename boost::ratio_add<R1, R3>::type,
         typename boost::ratio_add<R2, R4>::type>
operator*(const quantity<R1, R2>& x, const quantity<R3, R4>& y)
    typedef quantity<typename boost::ratio_add<R1, R3>::type,
                     typename boost::ratio_add<R2, R4>::type> R;
   r.set(x.get() * y.get());
    return r;
template <class R1, class R2>
quantity<R1, R2>
operator + (const \ quantity < R1 \ , \ R2 > \& \ x \ , \ const \ quantity < R1 \ , \ R2 > \& \ y)
{
    typedef quantity<R1, R2> R;
    Rr;
    r.set(x.get() + y.get());
    return r;
template <class R1, class R2>
quantity<R1, R2>
operator-(const quantity<R1, R2>& x, const quantity<R1, R2>& y)
    typedef quantity<R1, R2> R;
    Rri
    r.set(x.get() - y.get());
    return r;
```

With all of the foregoing scaffolding, we can now write an exemplar of a type-safe physics function:



```
Distance
compute_distance(Speed v0, Time t, Acceleration a)
{
    return v0 * t + Scalar(.5) * a * t * t; // if a units mistake is made here it won't compile
}
```

Finally, we can exercise what we've created, even using custom time durations (User1::seconds) as well as Boost time durations (boost::chrono::hours). The input can be in arbitrary, though type-safe, units, the output is always in SI units. (A complete Units library would support other units, of course.)

```
int main()
    typedef boost::ratio<8, BOOST_INTMAX_C(0x7FFFFFFFD)> R1;
    typedef boost::ratio<3, BOOST_INTMAX_C(0x7FFFFFFD)> R2;
    typedef User1::quantity<boost::ratio_subtract<boost::ratio<0>, boost::ratio<1> >::type,
                           boost::ratio_subtract<boost::ratio<1>, boost::ratio<0> >::type > RR;
    typedef boost::ratio_subtract<R1, R2>::type RS;
    std::cout << RS::num << '/' << RS::den << '\n';
    std::cout << "*********\n";
    std::cout << "* testUser1 *\n";</pre>
    std::cout << "*********\n";
    User1::Distance d( User1::mile(110) );
    User1::Time t( boost::chrono::hours(2) );
    RR r=d / t;
    //r.set(d.get() / t.get());
    User1::Speed rc= r;
    User1::Speed s = d / t;
    std::cout << "Speed = " << s.get() << " meters/sec\n";
   User1::Acceleration a = User1::Distance( User1::foot(32.2) ) / User1::Time() / User1::Time();
    std::cout << "Acceleration = " << a.get() << " meters/sec^2\n";</pre>
    User1::Distance df = compute_distance(s, User1::Time( User1::seconds(0.5) ), a);
    std::cout << "Distance = " << df.get() << " meters\n";
    std::cout << "There are "
        << User1::mile::ratio::den << '/' << User1::mile::ratio::num << " miles/meter";</pre>
    User1::meter mt = 1;
    User1::mile mi = mt;
    std::cout << " which is approximately " << mi.count() << '\n';</pre>
    std::cout << "There are "
        << User1::mile::ratio::num << '/' << User1::mile::ratio::den << " meters/mile";</pre>
    mi = 1;
    std::cout << " which is approximately " << mt.count() << '\n';</pre>
    User1::attosecond as(1);
    User1::seconds sec = as;
    std::cout << "1 attosecond is " << sec.count() << " seconds\n";</pre>
    std::cout << "sec = as; // compiles\n";</pre>
    sec = User1::seconds(1);
    as = sec;
    std::cout << "1 second is " << as.count() << " attoseconds\n";</pre>
    std::cout << "as = sec; // compiles\n";</pre>
    std::cout << "\n";
    return 0;
```

See the source file example/si_physics.cpp



External Resources

C++ Standards Committee's current Working Paper

The most authoritative reference material for the library is the C++ Standards Committee's current Working Paper (WP). 20.6 Compile-time rational arithmetic "ratio"

N2661 - A Foundation to Sleep On

From Howard E. Hinnant, Walter E. Brown, Jeff Garland and Marc Paterno. Is very informative and provides motivation for key design decisions

LWG 1281. CopyConstruction and Assignment between ratios having the same normalized form

From Vicente Juan Botet Escriba.

Reference

Header <boost/ratio_fwd.hpp>

This header provides forward declarations for the <boost/ratio.hpp> file.



```
namespace boost {
    template <boost::intmax_t N, boost::intmax_t D = 1> class ratio;
    // ratio arithmetic
    template <class R1, class R2> struct ratio_add;
    template <class R1, class R2> struct ratio_subtract;
    template <class R1, class R2> struct ratio_multiply;
    template <class R1, class R2> struct ratio_divide;
    // ratio comparison
    template <class R1, class R2> struct ratio_equal;
    template <class R1, class R2> struct ratio_not_equal;
    template <class R1, class R2> struct ratio_less;
    template <class R1, class R2> struct ratio_less_equal;
    template <class R1, class R2> struct ratio_greater;
    template <class R1, class R2> struct ratio_greater_equal;
    // convenience SI typedefs
    typedef ratio<1LL, 100000000000000000LL> atto;
    typedef ratio<1LL, 100000000000000LL> femto;
                        1000000000000LL> pico;
    typedef ratio<1LL,
                            1000000000LL> nano;
    typedef ratio<1LL,
   typedef ratio<1LL,
                                1000000LL> micro;
    typedef ratio<1LL,
                                    1000LL> milli;
    typedef ratio<1LL,
                                      100LL> centi;
                                      10LL> deci;
    typedef ratio<1LL,
                                 10LL, 1LL> deca;
    typedef ratio<
    typedef ratio<
                                100LL, 1LL> hecto;
    typedef ratio<
                               1000LL, 1LL> kilo;
                           1000000LL, 1LL> mega;
    typedef ratio<
                       1000000000LL, 1LL> giga;
    typedef ratio<
    typedef ratio< 10000000000LL, 1LL> tera;
    typedef ratio< 100000000000000LL, 1LL> peta;
    typedef ratio<100000000000000000LL, 1LL> exa;
```

Header <boost/ratio.hpp>

ratio is a facility which is useful in specifying compile time rational constants. Compile time rational arithmetic is supported with protection against overflow and divide by zero. Such a facility is very handy when needing to efficiently represent 1/3 of a nanosecond, or specifying an inch in terms of meters (for example 254/10000 meters - which ratio will reduce to 127/5000 meters).

```
// configuration macros
#define BOOST_RATIO_USES_STATIC_ASSERT
#define BOOST_RATIO_USES_MPL_ASSERT
#define BOOST_RATIO_USES_ARRAY_ASSERT
```

Configuration Macros

When BOOST_NO_STATIC_ASSERT is defined, the user can select the way static assertions are reported. Define

- BOOST_RATIO_USES_STATIC_ASSERT to use Boost.StaticAssert
- BOOST_RATIO_USES_MPL_ASSERT to use Boost.MPL static assertions
- BOOST_RATIO_USES_RATIO_ASSERT to use Boost.Ratio static assertions

The default behavior is as if BOOST_RATIO_USES_ARRAY_ASSERT is defined.



When BOOST_RATIO_USES_MPL_ASSERT is not defined the following symbols are defined as shown:

```
#define BOOST_RATIO_OVERFLOW_IN_ADD "overflow in ratio add"
#define BOOST_RATIO_OVERFLOW_IN_SUB "overflow in ratio sub"
#define BOOST_RATIO_OVERFLOW_IN_MUL "overflow in ratio mul"
#define BOOST_RATIO_OVERFLOW_IN_DIV "overflow in ratio div"
#define BOOST_RATIO_NUMERATOR_IS_OUT_OF_RANGE "ratio numerator is out of range"
#define BOOST_RATIO_DIVIDE_BY_0 "ratio divide by 0"
#define BOOST_RATIO_DENOMINATOR_IS_OUT_OF_RANGE "ratio denominator is out of range"
```

Depending upon the static assertion system used, a hint as to the failing assertion will appear in some form in the compiler diagnostic output.

Class Template ratio<>

```
template <boost::intmax_t N, boost::intmax_t D>
class ratio {
public:
    static const boost::intmax_t num;
    static const boost::intmax_t den;
    typedef ratio<num, den> type;

    ratio() = default;

    template <intmax_t _N2, intmax_t _D2>
    ratio(const ratio<_N2, _D2>&);

    template <intmax_t _N2, intmax_t _D2>
    ratio& operator=(const ratio<_N2, _D2>&) {return *this;}
};
```

A diagnostic will be emitted if ratio is instantiated with D = 0, or if the absolute value of N or D can not be represented. **Note:** These rules ensure that infinite ratios are avoided and that for any negative input, there exists a representable value of its absolute value which is positive. In a two's complement representation, this excludes the most negative value.

The members num and den will be normalized values of the template arguments N and D computed as follows. Let gcd denote the greatest common divisor of N's absolute value and of D's absolute value. Then:

- num has the value sign(N) * sign(D) * abs(N)/gcd.
- den has the value abs(D)/gcd.

The nested typedef type denotes the normalized form of this ratio type. It should be used when the normalized form of the template arguments are required, since the arguments are not necessarily normalized.

Two ratio classes ratio<N1,D1> and ratio<N2,D2> have the same normalized form if ratio<N1,D1>::type is the same type as ratio<N2,D2>::type

Construction and Assignment

```
template <intmax_t N2, intmax_t D2>
  ratio(const ratio<N2, D2>& r);
```

Effects: Constructs a ratio object.

Remarks: This constructor will not participate in overload resolution unless r has the same normalized form as *this.



```
template <intmax_t N2, intmax_t D2>
  ratio& operator=(const ratio<N2, D2>& r);
```

Effects: Assigns a ratio object.

Returns: *this.

Remarks: This operator will not participate in overload resolution unless r has the same normalized form as *this.

ratio Arithmetic

For each of the class templates in this section, each template parameter refers to a ratio. If the implementation is unable to form the indicated ratio due to overflow, a diagnostic will be issued.

ratio_add<>

```
template <class R1, class R2> struct ratio_add {
  typedef [/see below] type;
};
```

The nested typedef type is a synonym for ratio<R1::num * R2::den + R2::num * R1::den , R1::den * R2::den>::type.

ratio_subtract<>

```
template <class R1, class R2> struct ratio_subtract {
  typedef [/see below] type;
};
```

The nested typedef type is a synonym for ratio<R1::num * R2::den - R2::num * R1::den, R1::den * R2::den>::type.

ratio_multiply<>

```
template <class R1, class R2> struct ratio_multiply {
  typedef [/see below] type;
};
```

The nested typedef type is a synonym for ratio<R1::num * R2::num, R1::den * R2::den>::type.

ratio_divide<>

```
template <class R1, class R2> struct ratio_divide {
   typedef [/see below] type;
};
```

The nested typedef type is a synonym for ratio<R1::num * R2::den, R2::num * R1::den>::type.

ratio Comparison

ratio_equal<>

If R1::num = R2::num && R1::den = R2::den, ratio_equal derives from true_type, else derives from false_type.



ratio_not_equal<>

ratio_less<>

```
template <class R1, class R2>
struct ratio_less
   : public boost::integral_constant<bool, [/see below] > {};
```

If R1::num * R2::den < R2::num * R1::den, ratio_less derives from true_type, else derives from false_type.

ratio_less_equal<>

ratio greater<>

ratio_greater_equal<>

SI typedefs

The International System of Units specifies twenty SI prefixes. Boost.Ratio defines all except youto, zepto, zetta, and yotta

```
// convenience SI typedefs
typedef ratio<1LL, 1000000000000000000LL> atto;
typedef ratio<1LL, 100000000000000LL> femto;
typedef ratio<1LL, 100000000000LL> pico;
typedef ratio<1LL,
                           1000000000LL> nano;
typedef ratio<1LL,
                              1000000LL> micro;
typedef ratio<1LL,
                                 1000LL> milli;
                                  100LL> centi;
typedef ratio<1LL,
typedef ratio<1LL,</pre>
                                   10LL> deci;
typedef ratio<
                              10LL, 1LL> deca;
                             100LL, 1LL> hecto;
typedef ratio<
typedef ratio<
                            1000LL, 1LL> kilo;
typedef ratio<
                        1000000LL, 1LL> mega;
typedef ratio<
                     1000000000LL, 1LL> giga;
                  10000000000000LL, 1LL> tera;
typedef ratio<
typedef ratio< 100000000000000LL, 1LL> peta;
typedef ratio<100000000000000000LL, 1LL> exa;
```

Limitations and Extensions

The following are limitations of Boost.Ratio relative to the specification in the C++0x draft standard:

• Four of the SI units typedefs -- yocto, zepto, zetta, and yotta -- are to be conditionally supported, if the range of intmax_t allows, but are not supported by **Boost.Ratio**.



- Ratio values should be of type static constexpr intmax_t (see Ratio values should be constexpr), but no compiler supports constexpr today, so **Boost.Ratio** uses static const intmax_t instead.
- Rational arithmetic should use template aliases (see Rational Arithmetic should use template aliases), but those are not available in C++03, so inheritance is used instead.

The current implementation extends the requirements of the C++0x draft standard by making the copy constructor and copy assignment operator have the same normalized form (see copy constructor and assignment between ratios having the same normalized form).

Header <boost/ratio_io.hpp>

This header provides ratio_string<> which can generate a textual representation of a ratio<> in the form of a std::ba-sic_string<>. These strings can be useful for I/O."

```
namespace boost {
   template <class Ratio, class CharT>
   struct ratio_string
   {
      static std::basic_string<CharT> short_name();
      static std::basic_string<CharT> long_name();
   };
}
```

Appendices

Appendix A: History

Version 1.0.0, ?? ??, 2010

Appendix B: Rationale

Why ratio needs CopyConstruction and Assignment from ratios having the same normalized form

Current N3000 doesn't allows to copy-construct or assign ratio instances of ratio classes having the same normalized form.

This simple example

```
ratio<1,3> r1;
ratio<3,9> r2;
r1 = r2; // (1)
```

fails to compile in (1). Other example

```
ratio<1,3> r1;
ratio_subtract<ratio<2,3>,ratio<1,3> > r2=r1; // (2)
```

The type of $ratio_subtract< ratio<2,3>, ratio<1,3>> could be <math>ratio<3,9>$ so the compilation could fail in (2). It could also be ratio<1,3> and the compilation succeeds.



Why ratio needs the nested normalizer typedef type

The current resolution of issue LWG 1281 acknowledges the need for a nested type typedef, so Boost.Ratio is tracking the likely final version of std::ratio.

Appendix C: Implementation Notes

How Boost.Ratio manage with compile-time rational arithmetic overflow?

When the result is representable, but a simple application of arithmetic rules would result in overflow, e.g. ratio_multiply<ratio<INTMAX_MAX,2>,ratio<2,INTMAX_MAX>> can be reduced to ratio<1,1>, but the direct result of ratio<INTMAX_MAX*2,INT-MAX_MAX*2> would result in overflow.

Boost.Ratio implementes some simplifications in order to reduce the possibility of overflow. The general ideas are:

- The num and den ratio<> fields are normalized.
- Use the gcd of some of the possible products that can overflow, and simplify before doing the product.
- Use some equivalences relations that avoid addition or subtraction that can overflow or underflow.

The following subsections cover each case in more detail.

ratio_add

In

```
(n1/d1)+(n2/d2)=(n1*d2+n2*d1)/(d1*d2)
```

either n1*d2+n2*d1 or d1*d2 can overflow.

```
( (n1 * d2) + (n2 * d1) )
------(d1 * d2)
```

Dividing by gcd(d1,d2) on both num and den

```
( (n1 * (d2/gcd(d1,d2))) + (n2 * (d1/gcd(d1,d2))) )
------
((d1 * d2) / gcd(d1,d2))
```

Multipliying and diving by gcd(n1,n2) in numerator

Factorizing gcd(n1,n2)



Regrouping

```
( gcd(n1,n2) *
  ( ((n1/gcd(n1,n2)) * (d2/gcd(d1,d2))) + ((n2/gcd(n1,n2)) * (d1/gcd(d1,d2))) )
)
( (d1 / gcd(d1,d2)) * d2 )
```

Dividing by (d1 / gcd(d1,d2))

```
( ( gcd(n1,n2) / (d1 / gcd(d1,d2)) ) *
  ( ((n1/gcd(n1,n2)) * (d2/gcd(d1,d2))) + ((n2/gcd(n1,n2)) * (d1/gcd(d1,d2))) )
)
d2
```

Dividing by d2

This expression correspond to the multiply of two ratios that have less risk of overflow as the initial numerators and denomitators appear now in most of the cases divided by a gcd.

For ratio_subtract the reasoning is the same

ratio_multiply

In

```
(n1/d1)*(n2/d2)=((n1*n2)/(d1*d2))
```

either n1*n2 or d1*d2 can overflow.

Dividing by gcc(n1,d2) numerator and denominator

```
(((n1/gcc(n1,d2))*n2)
-----(d1*(d2/gcc(n1,d2))))
```

Dividing by gcc(n2,d1)

```
((n1/gcc(n1,d2))*(n2/gcc(n2,d1)))
-----((d1/gcc(n2,d1))*(d2/gcc(n1,d2)))
```

And now all the initial numerator and denominators have been reduced, avoiding the overflow.

For ratio_divide the reasoning is similar.



ratio_less

In order to evaluate

```
(n1/d1) < (n2/d2)
```

without moving to floating point numbers, two techniques are used:

• First compare the sign of the numerators

If sign(n1) < sign(n2) the result is true.

If sign(n1) == sign(n2) the result depends on the following after making the numerators positive

When the sign is equal the technique used is to work with integer division and modulo when the signs are equal.

Let call Qi the integer division of ni and di and Mi the modulo of ni and di.

```
ni = Qi * di + Mi and Mi < di
```

Form

```
((n1*d2)<(d1*n2))
```

we get

```
(((Q1 * d1 + M1)*d2)<(d1*((Q2 * d2 + M2))))
```

Developing

```
((Q1 * d1 * d2)+ (M1*d2))<((d1 * Q2 * d2) + (d1*M2))
```

Dividing by d1*d2

$$Q1 + (M1/d1) < Q2 + (M2/d2)$$

If Q1=Q2 the result depends on

```
(M1/d1) < (M2/d2)
```

If M1=0=M2 the result is false

If M1=0 M2!=0 the result is true

If M1!0 M2=0 the result is false

If M1!=0 M2!=0 the result depends on

If Q1!=Q2, the result of



```
Q1 + (M1/d1) < Q2 + (M2/d2)
```

depends only on Q1 and Q2 as Qi are integers and (Mi/di) <1 because Mi<di.

```
if Q1>Q2, Q1==Q2+k, k>=1
```

but the difference between two numbers between 0 and 1 can not be greater than 1, so the result is false.

if Q2>Q1, Q2==Q1+
$$k$$
, $k>=1$

```
\begin{array}{l} Q1 \ + \ (M1/d1) \ < \ Q1+k \ + \ (M2/d2) \\ (M1/d1) \ < \ k \ + \ (M2/d2) \\ (M1/d1) \ - \ (M2/d2) \ < \ k \end{array}
```

which is always true, so the result is true.

The following table recapitulates this analisys

ratio <n1,d1></n1,d1>	ratio <n2,d2></n2,d2>	Q1	Q2	M1	M2	Result
ratio <n1,d1></n1,d1>	ratio <n2,d2></n2,d2>	Q1	Q2	!=0	!=0	Q1 < Q2
ratio <n1,d1></n1,d1>	ratio <n2,d2></n2,d2>	Q	Q	0	0	false
ratio <n1,d1></n1,d1>	ratio <n2,d2></n2,d2>	Q	Q	0	!=0	true
ratio <n1,d1></n1,d1>	ratio <n2,d2></n2,d2>	Q	Q	!=0	0	false
ratio <n1,d1></n1,d1>	ratio <n2,d2></n2,d2>	Q	Q	!=0	!=0	ratio_less <ratio<d2,m2>, ratio<d1 m1="">></d1></ratio<d2,m2>

Appendix D: FAQ

Appendix E: Acknowledgements

The library's code was derived from Howard Hinnant's time2_demo prototype. Many thanks to Howard for making his code available under the Boost license. The original code was modified by Beman Dawes to conform to Boost conventions.

time2_demo contained this comment:

Much thanks to Andrei Alexandrescu, Walter Brown, Peter Dimov, Jeff Garland, Terry Golubiewski, Daniel Krugler, Anthony Williams.

The ratio.hpp source has been adapted from the experimental header <ratio_io> from Howard Hinnant.

Thanks to Adrew Chinnoff for his help polishing the documentation.

Appendix F: Future Plans

For later releases

• Use constexpr on compilers providing it



- Use template aliases on compiler providing it
- Implement multiple arguments ratio arithmetic.

