See the Assessment Guide for information on how to interpret this report.

ASSESSMENT SUMMARY

```
Compilation: PASSED (0 errors, 3 warnings)
API:
              PASSED
SpotBugs:
             PASSED
PMD:
             PASSED
Checkstyle:
             PASSED
Correctness: 49/49 tests passed
Memory:
             133/133 tests passed
Timing:
             193/193 tests passed
Aggregate score: 100.00%
[ Compilation: 5%, API: 5%, Style: 0%, Correctness: 60%, Timing: 10%, Memory: 20% ]
```

ASSESSMENT DETAILS

```
The following files were submitted:
4.7K Nov 5 01:03 Deque.java
648 Nov 5 01:03 Permutation.java
4.8K Nov 5 01:03 RandomizedQueue.java
**********************************
  COMPILING
% javac Deque.java
% javac RandomizedQueue.java
RandomizedQueue.java:21: warning: [unchecked] unchecked cast
           this.arr = (Item[]) new Object[size()];
 required: Item[]
 found:
           Object[]
 where Item is a type-variable:
   Item extends Object declared in class RandomizedQueue
RandomizedQueue.java:57: warning: [unchecked] unchecked cast
       this.queue = (Item[]) new Object[16];
 required: Item[]
           Object[]
 found:
 where Item is a type-variable:
   Item extends Object declared in class RandomizedQueue
RandomizedQueue.java:140: warning: [unchecked] unchecked cast
       Item[] arr = (Item[]) new Object[capacity];
 required: Item[]
           Object[]
 found:
 where Item is a type-variable:
   Item extends Object declared in class RandomizedQueue
3 warnings
```

% javac Permutation.java *
Checking the APIs of your programs.
Deque:
RandomizedQueue:
Permutation:
=======================================

* CHECKING STYLE AND COMMON BUG PATTERNS ************************************
% spotbugs *.class
*
% pmd .
*
=======================================
% checkstyle *.java
*
% custom checkstyle checks for Deque.java *
% custom checkstyle checks for RandomizedQueue.java
*
% custom checkstyle checks for Permutation.java
*

* TESTING CORRECTNESS ***********************************
Testing correctness of Deque
*
Running 19 total tests.
Tests 1-8 make random intermixed calls to addFirst(), addLast(), removeFirst(), removeLast(), isEmpty(), and size(), and iterator().
The probabilities of each operation are (p1, p2, p3, p4, p5, p6, p7), respectively.
Test 1: check random calls to addFirst(), addLast(), and size() * 5 random calls (0.4, 0.4, 0.0, 0.0, 0.0, 0.2, 0.0)

```
50 random calls (0.4, 0.4, 0.0, 0.0, 0.0, 0.2, 0.0)
     500 random calls (0.4, 0.4, 0.0, 0.0, 0.0, 0.2, 0.0)
  * 1000 random calls (0.4, 0.4, 0.0, 0.0, 0.0, 0.2, 0.0)
==> passed
Test 2: check random calls to addFirst(), removeFirst(), and isEmpty()
      5 random calls (0.8, 0.0, 0.1, 0.0, 0.1, 0.0, 0.0)
      50 random calls (0.8, 0.0, 0.1, 0.0, 0.1, 0.0, 0.0)
     500 random calls (0.8, 0.0, 0.1, 0.0, 0.1, 0.0, 0.0)
   1000 random calls (0.8, 0.0, 0.1, 0.0, 0.1, 0.0, 0.0)
      5 random calls (0.1, 0.0, 0.8, 0.0, 0.1, 0.0, 0.0)
      50 random calls (0.1, 0.0, 0.8, 0.0, 0.1, 0.0, 0.0)
     500 random calls (0.1, 0.0, 0.8, 0.0, 0.1, 0.0, 0.0)
  * 1000 random calls (0.1, 0.0, 0.8, 0.0, 0.1, 0.0, 0.0)
==> passed
Test 3: check random calls to addFirst(), removeLast(), and isEmpty()
      5 random calls (0.8, 0.0, 0.0, 0.1, 0.1, 0.0, 0.0)
      50 random calls (0.8, 0.0, 0.0, 0.1, 0.1, 0.0, 0.0)
     500 random calls (0.8, 0.0, 0.0, 0.1, 0.1, 0.0, 0.0)
   1000 random calls (0.8, 0.0, 0.0, 0.1, 0.1, 0.0, 0.0)
      5 random calls (0.1, 0.0, 0.0, 0.8, 0.1, 0.0, 0.0)
     50 random calls (0.1, 0.0, 0.0, 0.8, 0.1, 0.0, 0.0)
     500 random calls (0.1, 0.0, 0.0, 0.8, 0.1, 0.0, 0.0)
  * 1000 random calls (0.1, 0.0, 0.0, 0.8, 0.1, 0.0, 0.0)
==> passed
Test 4: check random calls to addLast(), removeLast(), and isEmpty()
      5 random calls (0.0, 0.8, 0.0, 0.1, 0.1, 0.0, 0.0)
      50 random calls (0.0, 0.8, 0.0, 0.1, 0.1, 0.0, 0.0)
     500 random calls (0.0, 0.8, 0.0, 0.1, 0.1, 0.0, 0.0)
   1000 random calls (0.0, 0.8, 0.0, 0.1, 0.1, 0.0, 0.0)
      5 random calls (0.0, 0.1, 0.0, 0.8, 0.1, 0.0, 0.0)
      50 random calls (0.0, 0.1, 0.0, 0.8, 0.1, 0.0, 0.0)
     500 random calls (0.0, 0.1, 0.0, 0.8, 0.1, 0.0, 0.0)
  * 1000 random calls (0.0, 0.1, 0.0, 0.8, 0.1, 0.0, 0.0)
==> passed
Test 5: check random calls to addLast(), removeFirst(), and isEmpty()
       5 random calls (0.0, 0.8, 0.1, 0.0, 0.1, 0.0, 0.0)
      50 random calls (0.0, 0.8, 0.1, 0.0, 0.1, 0.0, 0.0)
     500 random calls (0.0, 0.8, 0.1, 0.0, 0.1, 0.0, 0.0)
   1000 random calls (0.0, 0.8, 0.1, 0.0, 0.1, 0.0, 0.0)
      5 random calls (0.0, 0.1, 0.8, 0.0, 0.1, 0.0, 0.0)
      50 random calls (0.0, 0.1, 0.8, 0.0, 0.1, 0.0, 0.0)
     500 random calls (0.0, 0.1, 0.8, 0.0, 0.1, 0.0, 0.0)
  * 1000 random calls (0.0, 0.1, 0.8, 0.0, 0.1, 0.0, 0.0)
==> passed
Test 6: check random calls to addFirst(), removeFirst(), and iterator()
       5 random calls (0.8, 0.0, 0.1, 0.0, 0.0, 0.0, 0.1)
      50 random calls (0.8, 0.0, 0.1, 0.0, 0.0, 0.0, 0.1)
     500 random calls (0.8, 0.0, 0.1, 0.0, 0.0, 0.0, 0.1)
   1000 random calls (0.8, 0.0, 0.1, 0.0, 0.0, 0.0, 0.1)
       5 random calls (0.1, 0.0, 0.8, 0.0, 0.0, 0.0, 0.1)
      50 random calls (0.1, 0.0, 0.8, 0.0, 0.0, 0.0, 0.1)
     500 random calls (0.1, 0.0, 0.8, 0.0, 0.0, 0.0, 0.1)
  * 1000 random calls (0.1, 0.0, 0.8, 0.0, 0.0, 0.0, 0.1)
==> passed
Test 7: check random calls to all methods except iterator()
       5 random calls (0.3, 0.3, 0.1, 0.1, 0.1, 0.0)
      50 random calls (0.3, 0.3, 0.1, 0.1, 0.1, 0.0)
     500 random calls (0.3, 0.3, 0.1, 0.1, 0.1, 0.0)
   1000 random calls (0.3, 0.3, 0.1, 0.1, 0.1, 0.0)
       5 random calls (0.1, 0.1, 0.3, 0.3, 0.1, 0.1, 0.0)
      50 random calls (0.1, 0.1, 0.3, 0.3, 0.1, 0.1, 0.0)
     500 random calls (0.1, 0.1, 0.3, 0.3, 0.1, 0.1, 0.0)
  * 1000 random calls (0.1, 0.1, 0.3, 0.3, 0.1, 0.1, 0.0)
```

```
==> passed
Test 8: check random calls to all methods, including iterator()
      5 random calls (0.2, 0.2, 0.1, 0.1, 0.1, 0.2)
     50 random calls (0.2, 0.2, 0.1, 0.1, 0.1, 0.1, 0.2)
     500 random calls (0.2, 0.2, 0.1, 0.1, 0.1, 0.2)
  * 1000 random calls (0.2, 0.2, 0.1, 0.1, 0.1, 0.1, 0.2)
      5 random calls (0.1, 0.1, 0.2, 0.2, 0.1, 0.1, 0.2)
     50 random calls (0.1, 0.1, 0.2, 0.2, 0.1, 0.1, 0.2)
    500 random calls (0.1, 0.1, 0.2, 0.2, 0.1, 0.1, 0.2)
 * 1000 random calls (0.1, 0.1, 0.2, 0.2, 0.1, 0.1, 0.2)
==> passed
Test 9: check removeFirst() and removeLast() from an empty deque
  * removeFirst()
 * removeLast()
==> passed
Test 10: check whether two Deque objects can be created at the same time
  * n = 10
  * n = 1000
==> passed
Test 11: check iterator() after n calls to addFirst()
  * n = 10
 * n = 50
==> passed
Test 12: check iterator() after random calls to addFirst(), addLast(),
         removeFirst(), and removeLast() with probabilities (p1, p2, p3, p4)
 * 20 random operations (0.8, 0.0, 0.2, 0.0)
 * 20 random operations (0.8, 0.0, 0.0, 0.2)
 * 20 random operations (0.0, 0.8, 0.0, 0.2)
 * 20 random operations (0.0, 0.8, 0.2, 0.0)
 * 20 random operations (0.4, 0.4, 0.1, 0.1)
 * 20 random operations (0.2, 0.0, 0.8, 0.0)
 * 20 random operations (0.2, 0.0, 0.0, 0.8)
 * 20 random operations (0.0, 0.2, 0.0, 0.8)
 * 20 random operations (0.0, 0.2, 0.8, 0.0)
 * 20 random operations (0.1, 0.1, 0.4, 0.4)
 * 100 random operations (0.4, 0.4, 0.1, 0.1)
 * 1000 random operations (0.4, 0.4, 0.1, 0.1)
==> passed
Test 13: create two nested iterators to same deque of size n
 * n = 10
 * n = 50
==> passed
Test 14: create two parallel iterators to same deque of size n
  * n = 10
 * n = 50
==> passed
Test 15: create an iterator and check calls to next() and hasNext()
 * 10 consecutive calls to hasNext() on a deque of size 10
 * 10 consecutive calls to next() on a deque of size 10
 * 50 random intermixed calls to next() and hasNext() on a deque of size 10
 * 1000 random intermixed calls to next() and hasNext() on a deque of size 100
==> passed
Test 16: create Deque objects of different parameterized types
==> passed
Test 17: call addFirst() and addLast() with null argument
==> passed
Test 18: check that remove() and next() throw the specified exceptions in iterator()
==> passed
```

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Test 19: call iterator() when the deque is empty
==> passed
Total: 19/19 tests passed!
______
Testing correctness of RandomizedQueue
Running 21 total tests.
Tests 1-6 make random intermixed calls to enqueue(), dequeue(), sample(),
isEmpty(), size(), and iterator(). The probabilities of each operation
are (p1, p2, p3, p4, p5, p6), respectively.
Test 1: check random calls to enqueue() and size()
      5 random calls (0.8, 0.0, 0.0, 0.0, 0.2, 0.0)
     50 random calls (0.8, 0.0, 0.0, 0.0, 0.2, 0.0)
    500 random calls (0.8, 0.0, 0.0, 0.0, 0.2, 0.0)
 * 1000 random calls (0.8, 0.0, 0.0, 0.0, 0.2, 0.0)
==> passed
Test 2: check random calls to enqueue() and dequeue()
      5 random calls (0.7, 0.1, 0.0, 0.1, 0.1, 0.0)
     50 random calls (0.7, 0.1, 0.0, 0.1, 0.1, 0.0)
    500 random calls (0.7, 0.1, 0.0, 0.1, 0.1, 0.0)
  * 1000 random calls (0.7, 0.1, 0.0, 0.1, 0.1, 0.0)
      5 random calls (0.1, 0.7, 0.0, 0.1, 0.1, 0.0)
     50 random calls (0.1, 0.7, 0.0, 0.1, 0.1, 0.0)
    500 random calls (0.1, 0.7, 0.0, 0.1, 0.1, 0.0)
 * 1000 random calls (0.1, 0.7, 0.0, 0.1, 0.1, 0.0)
==> passed
Test 3: check random calls to enqueue() and sample()
      5 random calls (0.8, 0.0, 0.2, 0.0, 0.0, 0.0)
     50 random calls (0.8, 0.0, 0.2, 0.0, 0.0, 0.0)
    500 random calls (0.8, 0.0, 0.2, 0.0, 0.0, 0.0)
 * 1000 random calls (0.8, 0.0, 0.2, 0.0, 0.0, 0.0)
      5 random calls (0.2, 0.0, 0.8, 0.0, 0.0, 0.0)
     50 random calls (0.2, 0.0, 0.8, 0.0, 0.0, 0.0)
    500 random calls (0.2, 0.0, 0.8, 0.0, 0.0, 0.0)
 * 1000 random calls (0.2, 0.0, 0.8, 0.0, 0.0, 0.0)
==> passed
Test 4: check random calls to enqueue() and iterator()
      5 random calls (0.8, 0.0, 0.0, 0.0, 0.0, 0.2)
     50 random calls (0.8, 0.0, 0.0, 0.0, 0.0, 0.2)
    500 random calls (0.8, 0.0, 0.0, 0.0, 0.0, 0.2)
 * 1000 random calls (0.8, 0.0, 0.0, 0.0, 0.0, 0.2)
==> passed
Test 5: check random calls to all methods except iterator()
      5 random calls (0.6, 0.1, 0.1, 0.1, 0.0)
     50 random calls (0.6, 0.1, 0.1, 0.1, 0.0)
    500 random calls (0.6, 0.1, 0.1, 0.1, 0.0)
 * 1000 random calls (0.6, 0.1, 0.1, 0.1, 0.0)
      5 random calls (0.1, 0.6, 0.1, 0.1, 0.0)
     50 random calls (0.1, 0.6, 0.1, 0.1, 0.0)
    500 random calls (0.1, 0.6, 0.1, 0.1, 0.0)
  * 1000 random calls (0.1, 0.6, 0.1, 0.1, 0.0)
==> passed
Test 6: check random calls to all methods, including iterator()
      5 random calls (0.5, 0.1, 0.1, 0.1, 0.1)
     50 random calls (0.5, 0.1, 0.1, 0.1, 0.1)
    500 random calls (0.5, 0.1, 0.1, 0.1, 0.1)
  * 1000 random calls (0.5, 0.1, 0.1, 0.1, 0.1, 0.1)
```

```
5 random calls (0.1, 0.5, 0.1, 0.1, 0.1, 0.1)
     50 random calls (0.1, 0.5, 0.1, 0.1, 0.1, 0.1)
  * 500 random calls (0.1, 0.5, 0.1, 0.1, 0.1, 0.1)
 * 1000 random calls (0.1, 0.5, 0.1, 0.1, 0.1, 0.1)
==> passed
Test 7: call dequeue() and sample() from an empty randomized queue
  * dequeue()
 * sample()
==> passed
Test 8: create multiple randomized queue objects at the same time
 * n = 10
 * n = 100
==> passed
Test 9: check that iterator() returns correct items after a sequence
        of n enqueue() operations
 * n = 10
 * n = 50
==> passed
Test 10: check that iterator() returns correct items after intermixed
        sequence of m enqueue() and dequeue() operations
 * m = 10
 * m = 1000
==> passed
Test 11: create two nested iterators over the same randomized queue of size n
 * n = 10
 * n = 50
==> passed
Test 12: create two parallel iterators over the same randomized queue of size n
 * n = 10
 * n = 50
==> passed
Test 13: create two iterators over different randomized queues,
        each of length 10
==> passed
Test 14: create an iterator and check calls to next() and hasNext()
 * 10 consecutive calls to hasNext() on a deque of size 10
 * 10 consecutive calls to next() on a deque of size 10
 * 50 random intermixed calls to next() and hasNext() on a deque of size 10
 * 1000 random intermixed calls to next() and hasNext() on a deque of size 100
==> passed
Test 15: create RandomizedQueue objects of different parameterized types
==> passed
Test 16: check randomness of sample() by enqueueing n items, repeatedly calling
        sample(), and counting the frequency of each item
 * n = 3, trials = 12000
 * n = 5, trials = 12000
 * n = 8, trials = 12000
 * n = 10, trials = 12000
==> passed
Test 17: check randomness of dequeue() by enqueueing n items, dequeueing n items,
        and seeing whether each of the n! permutations is equally likely
 * n = 2, trials = 12000
 * n = 3, trials = 12000
 * n = 4, trials = 12000
 * n = 5, trials = 12000
==> passed
```

Test 18: check randomness of iterator() by enqueueing n items, iterating over those

```
n items, and seeing whether each of the n! permutations is equally likely
 * n = 2, trials = 12000
 * n = 3, trials = 12000
 * n = 4, trials = 12000
 * n = 5, trials = 12000
==> passed
Test 19: call enqueue() with a null argument
==> passed
Test 20: check that remove() and next() throw the specified exceptions in iterator()
==> passed
Test 21: call iterator() when randomized queue is empty
==> passed
Total: 21/21 tests passed!
______
******************************
* TESTING CORRECTNESS (substituting reference RandomizedQueue and Deque)
*************************
Testing correctness of Permutation
      ______
Tests 1-5 call the main() function directly, resetting standard input
before each call.
Running 9 total tests.
Test 1a: check formatting for sample inputs from assignment specification
 % java Permutation 3 < distinct.txt</pre>
 Ι
 C
 В
 % java Permutation 3 < distinct.txt</pre>
 D
 Ι
 C
 % java Permutation 8 < duplicates.txt</pre>
 AA
 BB
 BB
 BB
 BB
 CC
 CC
 BB
==> passed
Test 1b: check formatting for other inputs
 % java Permutation 8 < mediumTale.txt</pre>
 times
 age
 the
 wisdom
 of
 was
 it
 times
 % java Permutation 0 < distinct.txt</pre>
 [no output]
```

```
==> passed
Test 2: check that main() reads all data from standard input
 * filename = distinct.txt, k = 3
 * filename = distinct.txt, k = 3
 * filename = duplicates.txt, k = 8
 * filename = mediumTale.txt, k = 8
==> passed
Test 3a: check that main() prints each item from the sequence at most once
        (for inputs with no duplicate strings)
 * filename = distinct.txt, k = 3
 * filename = distinct.txt, k = 1
 * filename = distinct.txt, k = 9
 * filename = permutation6.txt, k = 6
 * filename = permutation10.txt, k = 10
==> passed
Test 3b: check that main() prints each item from the sequence at most once
        (for inputs with duplicate strings)
 * filename = duplicates.txt, k = 8
 * filename = duplicates.txt, k = 3
 * filename = permutation8.txt, k = 6
 * filename = permutation8.txt, k = 2
 * filename = tinyTale.txt, k = 10
==> passed
Test 3c: check that main() prints each item from the sequence at most once
        (for inputs with newlines)
 * filename = mediumTale.txt, k = 10
 * filename = mediumTale.txt, k = 20
 * filename = tale.txt, k = 10
 * filename = tale.txt, k = 50
==> passed
Test 4: check main() when k = 0
 * filename = distinct.txt, k = 0
 * filename = distinct.txt, k = 0
==> passed
Test 5a: check that permutations are uniformly random
        (for inputs with no duplicate strings)
 * filename = permutation4.txt, k = 1
 * filename = permutation4.txt, k = 2
 * filename = permutation4.txt, k = 3
 * filename = permutation4.txt, k = 4
 * filename = permutation6.txt, k = 2
==> passed
Test 5b: check that permutations are uniformly random
        (for inputs with duplicate strings)
 * filename = permutation5.txt, k = 1
 * filename = permutation5.txt, k = 2
 * filename = permutation5.txt, k = 3
 * filename = duplicates.txt, k = 3
 * filename = permutation8.txt, k = 2
==> passed
Total: 9/9 tests passed!
______
**********************************
* TIMING (substituting reference RandomizedQueue and Deque)
************************************
Timing Permutation
*-----
Running 23 total tests.
```

```
Test 1: count calls to methods in StdIn
```

- * java Permutation 5 < distinct.txt
- * java Permutation 10 < permutation10.txt
- * java Permutation 1 < mediumTale.txt
- * java Permutation 20 < tale.txt
- * java Permutation 100 < tale.txt
- * java Permutation 16412 < tale.txt
- ==> passed

Test 2: count calls to methods in Deque and RandomizedQueue

- * java Permutation 5 < distinct.txt
- * java Permutation 10 < permutation10.txt
- * java Permutation 1 < mediumTale.txt
- * java Permutation 20 < tale.txt
- * java Permutation 100 < tale.txt
- * java Permutation 16412 < tale.txt
- ==> passed

Test 3: count calls to methods in StdRandom

- * java Permutation 5 < distinct.txt
- * java Permutation 10 < permutation10.txt
- * java Permutation 1 < mediumTale.txt
- * java Permutation 20 < tale.txt
- * java Permutation 100 < tale.txt
- * java Permutation 16412 < tale.txt
- ==> passed

Test 4: Time main() with k = 5, for inputs containing n random strings

		n	seconds
=>	passed	1000	0.00
=>	passed	2000	0.00
=>	passed	4000	0.00
=>	passed	8000	0.00
=>	passed	16000	0.01
=>	passed	32000	0.01
=>	passed	64000	0.02
=>	passed	128000	0.04
=>	passed	256000	0.08
=>	passed	512000	0.16
==:	> 10/10	tests passed	

Test 5: Time main() with k = 1000, for inputs containing n random strings

	n	seconds
=> passed	1000	0.00
=> passed	2000	0.00
=> passed	4000	0.00
=> passed	8000	0.00
=> passed	16000	0.01
=> passed	32000	0.01
=> passed	64000	0.02
=> passed	128000	0.04
=> passed	256000	0.08
=> passed	512000	0.16
==> 10/10	tests passed	t

Total: 23/23 tests passed!

```
**********************************
* MFMORY
******************************
Analyzing memory of Permutation
*_____
Running 2 total tests.
Test 1: check that only one Deque or RandomizedQueue object is created
 * filename = distinct.txt, n = 9, k = 1
 * filename = distinct.txt, n = 9, k = 2
 * filename = distinct.txt, n = 9, k = 4
 * filename = tinyTale.txt, n = 12, k = 10
 * filename = tale.txt, n = 138653, k = 50
==> passed
Test 2: check that the maximum size of any Deque or RandomizedQueue object
      created is between k and n
 * filename = distinct.txt, n = 9, k = 1
 * filename = distinct.txt, n = 9, k = 2
 * filename = distinct.txt, n = 9, k = 4
 * filename = tinyTale.txt, n = 12, k = 10
 * filename = tale.txt, n = 138653, k = 5
 * filename = tale.txt, n = 138653, k = 50
 * filename = tale.txt, n = 138653, k = 500
 * filename = tale.txt, n = 138653, k = 5000
 * filename = tale.txt, n = 138653, k = 50000
==> passed
Test 3 (bonus): check that maximum size of any or Deque or RandomizedQueue object
             created is equal to k
 * filename = tale.txt, n = 138653, k = 5
   - max size of RandomizedQueue object = 138653
 * filename = tale.txt, n = 138653, k = 50
   - max size of RandomizedQueue object = 138653
 * filename = tale.txt, n = 138653, k = 500
   - max size of RandomizedQueue object = 138653
 * filename = tale.txt, n = 138653, k = 5000
   - max size of RandomizedQueue object = 138653
 * filename = tale.txt, n = 138653, k = 50000
   - max size of RandomizedQueue object = 138653
==> FAILED
Total: 2/2 tests passed!
_____
*****************************
********************************
Analyzing memory of Deque
                     _____
For tests 1-4, the maximum amount of memory allowed for a Deque
containing n items is 48n + 192.
Running 49 total tests.
Test 1a-1i: total memory usage after inserting n items,
          where n is a power of 2
```

	n	bytes	
=> passed => passed	32 64	1576 3112	
=> passed	128	6184	
<pre>=> passed => passed</pre>	256 512	12328 24616	
<pre>=> passed => passed</pre>	1024 2048	49192 98344	
<pre>-> passed -> passed</pre>	4096 8192	196648 393256	
==> 9/9 tests	_	333230	

Memory: $48.00 \text{ n} + 40.00 \text{ (R}^2 = 1.000)$

Test 2a-2i: Total memory usage after inserting n items, when n is one more than a power of 2.

	n	bytes	
=> passed	33	1624	
=> passed	65	3160	
=> passed	129	6232	
=> passed	257	12376	
=> passed	513	24664	
=> passed	1025	49240	
=> passed	2049	98392	
=> passed	4097	196696	
=> passed	8193	393304	
==> 9/9 tests	passed		

Memory: $48.00 \text{ n} + 40.00 \text{ (R}^2 = 1.000)$

Test 3a-3i: Total memory usage after inserting 2n-1 items, and then deleting n-1 items, when n is one more than a power of 2.

	n	bytes
=> passed => passed	33 65 129 257 513 1025 2049 4097	1624 3160 6232 12376 24664 49240 98392 196696
<pre>=> passed ==> 9/9 tests</pre>	8193 passed	393304

Memory: $48.00 \text{ n} + 40.00 \text{ (R}^2 = 1.000)$

Test 4a-4e: Total memory usage after inserting n items, and then deleting all but one item (should not grow with n or be too large of a constant).

		n	bytes	
=>	passed	32	88	
=>	passed	64	88	
=>	passed	128	88	
=>	passed	256	88	
=>	passed	512	88	
=>	passed	1024	88	
=>	passed	2048	88	
=>	passed	4096	88	
=>	passed	8192	88	

```
==> 9/9 tests passed
```

```
Memory: 88.00 (R<sup>2</sup> = 1.000)
```

Test 5a-5e: Total memory usage of iterator after inserting n items (should not grow with n or be too large of a constant).

```
n
                   bytes
______
=> passed 32
                      32
=> passed
           64
                      32
=> passed
          128
                      32
          256
                     32
=> passed
        256
512
1024
2048
                     32
=> passed
                     32
=> passed
                     32
=> passed
        409ь
8192
          4096
                      32
=> passed
=> passed
                      32
==> 9/9 tests passed
```

Memory: 32.00 (R² = 1.000)

```
Test 6a: Insert n strings; delete them one at a time, checking for loitering after each deletion. The probabilities of addFirst() and addLast() are (p1, p2), respectively. The probabilities of removeFirst() and removeLast() are (q1, q2), respectively.
```

- st 100 random insertions (1.0, 0.0) and 100 random deletions (1.0, 0.0)
- * 100 random insertions (1.0, 0.0) and 100 random deletions (0.0, 1.0)
- * 100 random insertions (0.0, 1.0) and 100 random deletions (1.0, 0.0)
- * 100 random insertions (0.0, 1.0) and 100 random deletions (0.0, 1.0)
- * 100 random insertions (0.5, 0.5) and 100 random deletions (0.5, 0.5)

==> passed

```
Test 6b: Perform random operations, checking for loitering after each operation. The probabilities of addFirst(), addLast(), removeFirst(), and removeLast() are (p1, p2, p3, p4), respectively.
```

- * 100 random operations (0.8, 0.0, 0.2, 0.0)
- * 100 random operations (0.8, 0.0, 0.0, 0.2)
- * 100 random operations (0.0, 0.8, 0.2, 0.0)
- * 100 random operations (0.0, 0.8, 0.0, 0.2)
- * 100 random operations (0.4, 0.4, 0.1, 0.1)
- * 100 random operations (0.2, 0.2, 0.3, 0.3)
- ==> passed

Test 7: Perform m random add/remove operations in the deque and check that only constant memory is allocated/deallocated per operation

- * m = 128
- * m = 256
- * m = 512
- ==> passed

Test 8: Insert m items into deque; then iterate over deque and check that only constant memory is allocated/deallocated per operation

- * m = 64
- * m = 128
- * m = 256
- ==> passed

```
Min observed memory for Deque: 48.00 \text{ n} + 40.00 \text{ (R}^2 = 1.000)
Max observed memory for Deque: 48.00 \text{ n} + 40.00 \text{ (R}^2 = 1.000)
```

Total: 49/49 tests passed!

Analyzing memory of RandomizedQueue

*_____

For Tests 1-5, the maximum amount of memory allowed for a RandomizedQueue containing n items is 48n + 192.

For Test 6, the maximum amount of memory allowed for a RandomizedQueue iterator over n items is 8n + 72.

Test 1a-1i: Total memory usage after inserting n items when n is a power of 2.

	n	bytes	
=> passed	32	568	
=> passed	64	1080	
=> passed	128	2104	
=> passed	256	4152	
=> passed	512	8248	
=> passed	1024	16440	
=> passed	2048	32824	
=> passed	4096	65592	
=> passed	8192	131128	
==> 9/9 tests	passed		

Memory: $16.00 \text{ n} + 56.00 \text{ (R}^2 = 1.000)$

Test 2a-2i: Total memory usage after inserting n items, when n is one more than a power of 2.

	n	bytes	
=> passed	33	568	
=> passed	65	1080	
=> passed	129	2104	
=> passed	257	4152	
=> passed	513	8248	
=> passed	1025	16440	
=> passed	2049	32824	
=> passed	4097	65592	
=> passed	8193	131128	
==> 9/9 tests	passed		

Memory: $16.00 \text{ n} + 40.00 \text{ (R}^2 = 1.000)$

Test 3a-3i: Total memory usage after inserting 2n-1 items, and then deleting n-1 items, when n is one more than a power of 2.

	n	bytes	
=> passed	33 65 129 257 513 1025	1080 2104 4152 8248 16440 32824	
=> passed => passed => passed => 9/9 tests	2049 4097 8193	65592 131128 262200	

Memory: $32.00 \text{ n} + 24.00 \text{ (R}^2 = 1.000)$

Test 4a-4i: Total memory usage after inserting n items, deleting n items,

then inserting n times, when n is a power of 2.

	n	bytes	
-> paggd	22	гсо	
=> passed	32	568	
=> passed	64	1080	
=> passed	128	2104	
=> passed	256	4152	
=> passed	512	8248	
=> passed	1024	16440	
=> passed	2048	32824	
=> passed	4096	65592	
=> passed	8192	131128	
==> 9/9 te	sts passed		

Memory: $16.00 \text{ n} + 56.00 \text{ (R}^2 = 1.000)$

Test 5a-5i: Total memory usage after inserting n items, and then deleting all but one item.

	n	bytes	
=> passed	32	72	
=> passed	64	72	
=> passed	128	72	
=> passed	256	72	
=> passed	512	72	
=> passed	1024	72	
=> passed	2048	72	
=> passed	4096	72	
=> passed	8192	72	
==> 9/9 tests	passed		

Memory: 72.00 (R² = 1.000)

Test 6a-6i: Total memory usage of iterator after inserting n items.

	n	bytes	
=> passed => passed => passed => passed => passed	32 64 128 256 512	320 576 1088 2112 4160	
<pre>=> passed => passed => passed => passed => passed</pre>	1024 2048 4096 8192 passed	8256 16448 32832 65600	

Memory: $8.00 \text{ n} + 64.00 \text{ (R}^2 = 1.000)$

Test 6j-6r: Total memory usage of iterator after inserting n items.

		n	bytes
=>	passed	34	336
	passed	66	592
=>	passed	130	1104
=>	passed	258	2128
=>	passed	514	4176
=>	passed	1026	8272
=>	passed	2050	16464
=>	passed	4098	32848
=>	passed	8194	65616
==;	9/9 tests	passed	

Memory: $8.00 \text{ n} + 64.00 \quad (R^2 = 1.000)$

Test 7a: Insert 100 strings; delete them one at a time, checking for loitering after each deletion.

==> passed

Test 7b: Perform random operations, checking for loitering after each operation. The probabilities of enqueue(), dequeue(), and sample() are (p1, p2, p3), respectively.

- * 200 random operations (0.8, 0.2, 0.0)
- * 200 random operations (0.2, 0.8, 0.0)
- * 200 random operations (0.6, 0.2, 0.2)
- * 200 random operations (0.2, 0.4, 0.4)

==> passed

Test 8: Insert m items into queue; then iterate over deque and check that only constant memory is allocated/deallocated per operation

- * m = 64
- * m = 128
- * m = 256
- ==> passed

Test 9: Total memory usage after inserting n items, seeking to identify values of n where memory usage is minimized as a function of n.

	n	bytes	
=> passed	31 63 127 255 511 1023 2047	312 568 1080 2104 4152 8248 16440	
==> 7/7 tests	passed		

Memory: $8.00 \text{ n} + 64.00 \text{ (R}^2 = 1.000)$

Test 10: Total memory usage after inserting 4096 items, then successively deleting items, seeking values of n where memory usage is maximized as a function of n

	n	bytes	
=> passed	2049	65592	
=> passed	1025	32824	
=> passed	513	16440	
=> passed	257	8248	
=> passed	129	4152	
=> passed	65	2104	
=> passed	33	1080	
=> passed	17	568	
=> passed	9	312	
==> 9/9 tests	passed		

Memory: $32.00 \text{ n} + 24.00 \text{ (R}^2 = 1.000)$

Min observed memory for RandomizedQueue: $8.00 \text{ n} + 64.00 \text{ (R}^2 = 1.000)$ Max observed memory for RandomizedQueue: $32.00 \text{ n} + 24.00 \text{ (R}^2 = 1.000)$

Running 82 total tests.

Total: 82/82 tests passed!

```
******************************
* TIMING
******************************
Timing Deque
*----
Running 103 total tests.
Test 1a-1k: make n calls to addFirst() followed by n calls to removeFirst()
                     n seconds
-----
=> passed 1024 0.00
=> passed 2048 0.00
=> passed 4096 0.00
=> passed 8192 0.00
=> passed 16384 0.00
=> passed 32768 0.00
=> passed 65536 0.00
=> passed 128000 0.00
=> passed 256000 0.00
=> passed 512000 0.01
=> passed 1024000 0.02
==> 11/11 tests passed
Test 2a-2k: make n calls to addLast() followed by n calls to removeLast()
                 n seconds
-----
=> passed 1024 0.00
=> passed 2048 0.00
=> passed 4096 0.00
=> passed 8192 0.00
=> passed 16384 0.00
=> passed 32768 0.00
=> passed 65536 0.00
=> passed 128000 0.01
=> passed 512000 0.01
=> passed 1024000 0.02
==> 11/11 tests passed
==> 11/11 tests passed
Test 3a-3k: make n calls to addFirst() followed by n calls to removeLast()
              n seconds
-----
=> passed 1024 0.00
=> passed 2048 0.00
=> passed 4096 0.00
=> passed 8192 0.00
=> passed 16384 0.00
=> passed 32768 0.00
=> passed 65536 0.00
=> passed 128000 0.00
=> passed 512000 0.01
=> passed 1024000 0.02
==> 11/11 tests passed
==> 11/11 tests passed
Test 4a-4k: make n calls to addLast() followed by n calls to removeFirst()
                    n seconds
```

```
8192
16384
32768
65536
128000
               8192
                      0.00
=> passed
=> passed
                         0.00
=> passed
                         0.00
=> passed
                         0.00
=> passed
                         0.00
             256000
                       0.00
=> passed
=> passed
             512000
                       0.01
          1024000
=> passed
                         0.02
==> 11/11 tests passed
```

			n	seconds
=>	passed	1	024	0.00
=>	passed	2	048	0.00
=>	passed	4	096	0.00
=>	passed	8	192	0.00
=>	passed	16	384	0.00
=>	passed	32	768	0.00
=>	passed	65	536	0.00
=>	passed	128	000	0.00
=>	passed	256	000	0.01
=>	passed	512	000	0.01
=>	passed	1024	000	0.03
=>	passed	2048	000	0.06
==:	> 12/12	tests pa	ssed	

	n	seconds
=> passed	1024	0.00
=> passed	2048	0.00
=> passed	4096	0.00
=> passed	8192	0.00
=> passed	16384	0.00
=> passed	32768	0.00
=> passed	65536	0.00
=> passed	128000	0.00
=> passed	256000	0.01
=> passed	512000	0.02
=> passed	1024000	0.03
=> passed	2048000	0.06
==> 12/12	tests passed	

Test 7a-7g: make n random calls to addFirst(), addLast(), removeFirst(), removeLast(), isEmpty(), and size() with probabilities (0.3, 0.3, 0.1, 0.1, 0.1)

	n	seconas
=> passed	l 1024	0.00
=> passed	l 2048	0.00
=> passed	l 4096	0.00
=> passed	l 8192	0.00
=> passed	l 16384	0.00
=> passed	l 32768	0.00
=> passed	l 65536	0.00
=> passed	128000	0.00
=> passed	l 256000	0.01
=> passed	l 512000	0.02
=> passed	1024000	0.04
=> passed	l 2048000	0.07
==> 12/12	tests passe	d

		n	seconds
=>	passed	1024	0.00
=>	passed	2048	0.00
=>	passed	4096	0.00
=>	passed	8192	0.00
=>	passed	16384	0.00
=>	passed	32768	0.00
=>	passed	65536	0.00
=>	passed	128000	0.00
=>	passed	256000	0.00
=>	passed	512000	0.01
=>	passed	1024000	0.02
=>	passed	2048000	0.04
==>	12/12	tests passed	

	n	seconds
=> passed	1025	0.00
=> passed	2049	0.00
=> passed	4097	0.00
=> passed	8193	0.00
=> passed	16385	0.00
=> passed	32769	0.00
=> passed	65537	0.01
=> passed	128001	0.01
=> passed	256001	0.01
=> passed	512001	0.03
=> passed	1024001	0.05
==> 11/11	tests passed	

Total: 103/103 tests passed!

* n = 10

```
Timing RandomizedQueue
*-----
Running 67 total tests.
Test 1: make n calls to enqueue() followed by n calls to dequeue();
       count calls to StdRandom
 * n = 10
 * n = 100
 * n = 1000
==> passed
Test 2: make n calls to enqueue() follwed by n calls to sample();
       count calls to StdRandom
 * n = 10
 * n = 100
 * n = 1000
==> passed
Test 3: make n calls to enqueue() and iterate over the n items;
       count calls to StdRandom
```

```
* n = 1000
==> passed
```

Test 4a-k: make n calls to enqueue() followed by n calls to dequeue()

	n	seconds
=> passed	1024	0.00
=> passed	2048	0.00
=> passed	4096	0.00
=> passed	8192	0.00
=> passed	16384	0.00
=> passed	32768	0.00
=> passed	65536	0.01
=> passed	128000	0.01
=> passed	256000	0.02
=> passed	512000	0.01
=> passed	1024000	0.03
==> 11/11	tests passed	l

	n	seconds
=> passed	1024	0.00
=> passed	2048	0.00
=> passed	4096	0.00
=> passed	8192	0.00
=> passed	16384	0.00
=> passed	32768	0.00
=> passed	65536	0.01
=> passed	128000	0.01
=> passed	256000	0.02
=> passed	512000	0.04
=> passed	1024000	0.10
==> 11/11	tests passed	

	n	seconds
=> passed	1024	0.00
=> passed	2048	0.00
=> passed	4096	0.00
=> passed	8192	0.00
=> passed	16384	0.00
=> passed	32768	0.00
=> passed	65536	0.00
=> passed	128000	0.01
=> passed	256000	0.01
=> passed	512000	0.03
=> passed	1024000	0.07
==> 11/11	tests passed	l

		n	seconds	
=>	passed	1024	0.00	
=>	passed	2048	0.00	

```
4096
                           0.00
=> passed
           4096
8192
16384
32768
65536
128000
                           0.00
=> passed
                           0.00
=> passed
                           0.00
=> passed
                         0.00
=> passed
=> passed
                           0.01
              256000
=> passed
                           0.02
=> passed
              512000
                           0.05
           1024000
=> passed
                           0.12
==> 11/11 tests passed
```

	n	seconds
=> passed	1024	0.00
=> passed	2048	0.00
=> passed	4096	0.00
=> passed	8192	0.00
=> passed	16384	0.00
=> passed	32768	0.00
=> passed	65536	0.00
=> passed	128000	0.01
=> passed	256000	0.01
=> passed	512000	0.02
=> passed	1024000	0.04
==> 11/11	tests passed	

Test 9a-i: make 100 calls to enqueue; 99 calls to dequeue; n calls to enqueue(); then call dequeue() three times, followed by enqueue() three times, and repeat n times.

	n	seconds			
=> passed	1024	0.00			
=> passed	2048	0.00			
=> passed	4096	0.00			
=> passed	8192	0.00			
=> passed	16384	0.00			
=> passed	32768	0.00			
=> passed	65536	0.01			
=> passed	128000	0.02			
=> passed	256000	0.05			
==> 9/9 tests passed					

Total: 67/67 tests passed!
