

# $ExaGO^{TM}$ Users Manual

Version 1.5.1

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# Chapter 1

# Introduction

The Exascale Grid Optimization (ExaGO<sup>TM</sup>) toolkit is an open source package for solving large-scale power grid optimization problems on parallel and distributed architectures, particularly targeted for exascale machines with heteregenous architectures (GPU). ExaGO<sup>TM</sup> is written in C/C++ and makes heavy use of the functionality provided by the PETSc[1] library. It uses RAJA [3] and Umpire [4] libraries for execution on the GPU and can make use of several optimization solvers - Ipopt [7], HiOp [6, 5]- for solving the optimization problems.

All ExaGO<sup>TM</sup> applications use a nonlinear formulation based on full AC optimal power flow. The different applications available with ExaGO are listed in Table 1.1

Table 1.1: ExaGO applications

Application	Description	Notes
OPFLOW	AC optimal power flow	
SCOPFLOW	Security-constrained AC optimal power	Uses TCOPFLOW for multi-
	flow	period contingencies
TCOPFLOW	Multi-period AC optimal power flow	
SOPFLOW	Stochastic AC optimal power flow	Uses SCOPFLOW for multi-
		contingency scenarios

While ExaGO is targeted for making use of distributed computing environments and GPUs, its full support is still under development. Table 1.2 lists the architecture support for ExaGO applications.

Table 1.2: ExaGO application execution on different hardware

Application	CPU (serial)	CPU (parallel)	GPU
OPFLOW	Y	N	Y
SCOPFLOW	Y	Y	Y
SOPFLOW	Y	Y	Y
TCOPFLOW	Y	N	N

Together, these applications cater to problems spanning the dimensions of security (contingencies), stochasticity, and time as shown in Figure 1.1.

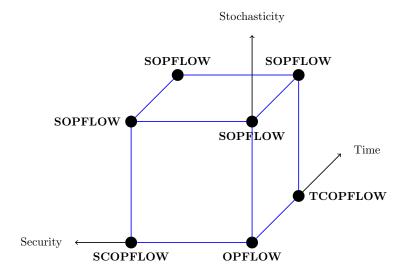


Figure 1.1: ExaGO provides applications along the dimensions of security (contingencies), time, and stochasticity. The label vertices denote different ExaGO applications available.

# Chapter 2

# Getting Started

## 2.1 System requirements

ExaGO is currently only built on 64b OSX and Linux machines, compiled with GCC >= 7.3. We build ExaGO on Intel, AMD, and IBM Power9 architectures.

# 2.2 Prerequisites

This section assumes that you already have the ExaGO source code, and that the environment variable EXAGODIR is the directory of the ExaGO source code. ExaGO may be acquired via the PNNL git repository linked here, like so:

```
> git clone https://gitlab.pnnl.gov/exasgd/frameworks/exago.git exago > export EXAGODIR=$PWD/exago
```

Paths to installations of third party software in examples are abbreviated with placeholder paths. For example, /path/to/cuda is a placeholder for a path to a valid CUDA Toolkit installation.

# 2.3 Dependencies

ExaGO at version 1.5.1 has the dependencies listed in table 2.1. The versions of dependencies listed are those we have tested with, though newer version may also be compatible.

Table 2.1: Dependency Table

Dependency	Version Constraints	Mandatory	Notes
PETSc [1]	3.16.x	✓	Core dependency
CMake	3.18	✓	Only a build dependency
MPI	4.1		Only tested with openmpi and spectrummpi
Ipopt [7]	3.12		
HiOp [6, 5]	0.7.1		Prefer dynamically linked
RAJA [3]	0.14.0		
Umpire [2]	6.0.0		Only when RAJA is enabled
MAGMA	2.6.1		Only when GPU acceleration is enabled
CUDA Toolkit	11.4		Only when GPU acceleration is enabled

These may all be toggled via CMake, which will be discussed in the section Building and installation.

#### 2.3.1 Notes on environment modules

Many of the dependencies are available via environment modules on institutional clusters. To get additional information on your institution's clusters, please ask your institution's system administrators. Some end-to-end examples in this document will use system-specific modules and are not expected to expected to run on other clusters.

For example, the modules needed to build and run ExaGO on Newell, an IBM Power9 PNNL cluster, are as follows:

```
> module load gcc/8.5.0
> module load openmpi/4.1.4
> module load cuda/11.4
> module load python/miniconda3.8
> module load cmake/3.19.6
```

#### 2.3.2 Additional Notes on GPU Accelerators

CUDA is currently the only GPU accelerator platform ExaGO fully supports.

### 2.3.3 Additional Notes on Umpire

Umpire is an implicit dependency of RAJA. If a user enables RAJA, they must also provide a valid installation of Umpire. Additionally, if a user would like to run ExaGO with RAJA and without CUDA, they must provide a CPU-only build of Umpire since an Umpire build with CUDA enabled will link against CUDA.

# 2.4 Building and installation

#### 2.4.1 Default Build

ExaGO may be built with a standard CMake workflow:

Listing 2.1: Example CMake workflow

```
> cd $EXAGODIR
> export BUILDDIR=$PWD/build INSTALLDIR=$PWD/install
> mkdir $BUILDDIR $INSTALLDIR
> cd $BUILDDIR
> cmake .. -DCMAKE_INSTALL_PREFIX=$INSTALLDIR
> make install
```

The following sections will assume the user is following the basic workflow outlined above.

**Note:** For changes to the CMake configuration to take effect, the code will have to be reconfigured using cmake and rebuilt using make.

#### 2.4.2 Additional Options

To enable additional options, CMake variables may be defined via CMake command line arguments, ccmake, or cmake-gui. CMake options specific to ExaGO have an EXAGO\_ prefix. For example, the following shell commands will build ExaGO with MPI:

```
> cmake .. -DCMAKE_INSTALL_PREFIX=$INSTALLDIR -DEXAGO_ENABLE_MPI=ON
```

ExaGO's CMake configuration will search the usual system locations for an MPI installation.

For dependencies not installed to a system-wide location, users may also directly specify the location of a dependency. For example, this will build ExaGO with IPOPT enabled and installed to a user directory:

```
> cmake .. \
    -DCMAKE_INSTALL_PREFIX=$INSTALLDIR \
    -DEXAGO_ENABLE_IPOPT=ON \
    -DIPOPT_DIR=/path/to/ipopt
```

Notice that the CMake variable IPOPT\_DIR does not have an EXAGO\_ prefix. This is because the variables specifying locations often belong to external CMake modules. CMake variables indicating installation directories do not have an EXAGO\_ prefix.

Some CMake options effect others. This is especially common when the user enables ExaGO's GPU options. For example, if the user enables EXAGO\_ENABLE\_GPU and EXAGO\_ENABLE\_RAJA, the user must provide a GPU-enabled RAJA installation. Umpire is also an implicit dependency of RAJA, so if the user enables EXAGO\_ENABLE\_GPU they must also provide a GPU-enabled Umpire installation.

Below is a complete shell session on PNNL's cluster Newell in which a more complicated ExaGO configuration is built, where each dependency installation is explicitly passed to CMake. Environment modules specific to Newell are provided to make the example thorough, even though they are not likely to work on another machine. However, similar modules (with different version numbers) are likely to be available on other platforms.

Listing 2.2: ExaGO build with all options enabled

```
> module load gcc/8.5.0
> module load openmpi/4.1.4
> module load cuda/11.4
> module load python/miniconda3.8
> module load cmake/3.19.6
> git clone https://gitlab.pnnl.gov/exasgd/frameworks/exago.git exago
> export EXAGODIR=$PWD/exago
> cd $EXAGODIR
> export BUILDDIR=$PWD/build INSTALLDIR=$PWD/install
> mkdir $BUILDDIR $INSTALLDIR
> cd $BUILDDIR
> cmake .. \
  -DCMAKE_INSTALL_PREFIX=$INSTALLDIR \
  -DCMAKE BUILD TYPE=Debug \
  -DEXAGO_ENABLE_GPU=ON \
  -DEXAGO_ENABLE_HIOP=ON \
  -DEXAGO_ENABLE_IPOPT=ON \
```

```
-DEXAGO_ENABLE_MPI=ON \
 -DEXAGO_ENABLE_PETSC=ON \
 -DEXAGO_RUN_TESTS=ON \
 -DEXAGO_ENABLE_RAJA=ON \
 -DEXAGO_ENABLE_IPOPT=ON \
 -DIPOPT_DIR=/path/to/ipopt \
 -DRAJA_DIR=/path/to/raja \
 -Dumpire_DIR=/path/to/umpire \
 -DHIOP_DIR=/path/to/hiop \
 -DMAGMA_DIR=/path/to/magma \
 -DPETSC_DIR=/path/to/petsc
> make -j 8 install
> # For the following commands, a job scheduler command may be needed.
> # Run test suite
> make test
> # Run an ExaGO application:
> $INSTALLDIR/bin/opflow
```

## 2.5 Usage

Each ExaGO application has the following format for execution

```
./app <app_options>
```

For OPFLOW for example:

```
./opflow -help
ExaGO 1.4.1 built on Jan 14 2022
Arguments for opflow:
        -help
                Print help message (type: flag)
        -version
                Print version information (type: flag)
        -config
                Print configuration options used to build ExaGO (type:
                   \hookrightarrow flag)
        -options_file /path/to/options_file
                Path to options file used to load additional ExaGO
                   → configuration options (type: string)
        -opflow_model (POWER_BALANCE_POLAR|POWER_BALANCE_HIOP|
           → PBPOLRAJAHIOP)
                OPFLOW model name (type: string)
```

```
-opflow_solver (IPOPT|HIOP|HIOPSPARSE)
        OPFLOW solver type (type: string)
-opflow_initialization (OPFLOWINIT_MIDPOINT|OPFLOWINIT_FROMFILE|
   → OPFLOWINIT_ACPF | OPFLOWINIT_FLATSTART)
        Type of OPFLOW initialization (type: string)
-opflow_objective (MIN_GEN_COST|MIN_GENSETPOINT_DEVIATION|NO_OBJ)
        Type of OPFLOW objective (type: string)
-opflow genbusvoltage (VARIABLE WITHIN BOUNDS|FIXED WITHIN QBOUNDS
   → | FIXED AT SETPOINT)
        Type of OPFLOW gen bus voltage control (type: string)
-opflow_has_gensetpoint 0
        Use set-points for generator real power (type: bool)
-opflow_use_agc 0
        Use automatic generation control (AGC) (type: bool)
-opflow_tolerance 1e-06
        Optimization tolerance (type: real)
-opflow_ignore_lineflow_constraints 0
        Ignore line flow constraints? (type: bool)
-opflow_include_loadloss_variables 0
        Ignore line flow constraints? (type: bool)
-opflow_loadloss_penalty 1000
        Penalty for load loss (type: real)
-opflow_include_powerimbalance_variables 0
        Allow power imbalance? (type: bool)
-opflow_powerimbalance_penalty 10000
        Power imbalance penalty (type: real)
-hiop_compute_mode (auto|cpu|hybrid|qpu)
        Set compute mode for HiOp solver (type: string)
-hiop_verbosity_level 0
        Set verbosity level for HiOp solver, between 0 and 12 (
           → type: int)
-hiop_ipopt_debug 0
        Flag enabling debugging HIOP code with IPOPT (type: bool)
```

ExaGO applications also have an option to print many options ExaGO was configured with, which aid in reproducing build environments that a given ExaGO source tree was built with.

```
./opflow -config
ExaGO version 1.3.0 built on Jan 14 2022
Built with the following command:
$ cmake -B /Users/manc568/workspace/exago/build -S /Users/manc568/
   → workspace/exago \
        -DEXAGO_ENABLE_RAJA:BOOL=OFF \
        -DEXAGO ENABLE PYTHON:BOOL=ON \
        -DEXAGO_ENABLE_HIP:BOOL=OFF \
        -DEXAGO_ENABLE_GPU:BOOL=OFF \
        -DEXAGO_ENABLE_HIOP_SPARSE:BOOL=ON \
        -DEXAGO_ENABLE_HIOP:BOOL=ON \
        -DEXAGO_ENABLE_IPOPT:BOOL=ON \
        -DEXAGO_ENABLE_MPI:BOOL=ON \
        -DEXAGO_BUILD_STATIC:BOOL=OFF \
        -DEXAGO_ENABLE_CUDA:BOOL=OFF \
        -DEXAGO_ENABLE_HIOP_DISTRIBUTED:BOOL=OFF \
        -DEXAGO_ENABLE_PETSC:BOOL=ON \
        -DEXAGO_BUILD_SHARED:BOOL=OFF \
        -DIPOPT_INCLUDES:STRING="" \
        -DIPOPT_ROOT_DIR:STRING="" \
        -DHiOp_DIR:STRING="/some/path" \
        -DPETSC DIR:STRING="/some/path" \
        -DCMAKE_CXX_COMPILER:STRING="/usr/local/bin/g++-11" \
        -DIPOPT_LIBRARIES:STRING="" \
        -DCMAKE_BUILD_TYPE:STRING="Debug" \
        -DPETSC_INCLUDES:STRING="" \
        -DCMAKE_C_COMPILER:STRING="/usr/local/bin/gcc-11" \
        -DCMAKE_INSTALL_PREFIX:STRING="/Users/manc568/workspace/exago/
           → install" \
        -DPETSC_LIBRARIES:STRING="" \
        -DEXAGO_OPTIONS_DIR:STRING="/Users/manc568/workspace/exago/install
           → /share/exago/options"
```

Here, app\_options are the command line options for the application. Each application has many options through which the input files and the control options can be set for the application. All application options have the form <code>-app\_option\_name</code> followed by the <code>app\_option\_value</code>. For instance,

```
./opflow -netfile case9mod.m -opflow_model POWER_BALANCE_POLAR \
-opflow_solver IPOPT
```

will execute the OPFLOW application using case9mod.m input file with the model POWER\_BALANCE\_POLAR and Ipopt [7]solver.

Options can also be passed to each application through an options file  $\neg$ optionsfile  $\prec$ optionfilename  $\hookrightarrow$ , or via command line or through a combination of the command line and options file. The option

specified via command line supersedes that given in in the options file. For example, if -options\_file 
→ opflowoptions specified -netfile case9mod.m within its settings:

```
./opflow -options_file opflowoptions # Uses case9mod.m
./opflow -netfile case118.m -options_file opflowoptions # Uses case118.m
```

# Chapter 3

# Optimal power flow (OPFLOW)

OPFLOW solves the full AC optimal power flow problem and provides various flexible features that can be toggled via run-time options. It has interfaces to different optimization solvers that can be executed on CPUs or on GPUs.

#### 3.1 Formulation

Optimal power flow is a general nonlinear programming problem with the following form

$$\min f(x) \tag{3.1}$$

s.t.

$$g(x) = 0 (3.2)$$

$$h(x) \le 0 \tag{3.3}$$

$$x^{\min} \le x \le x^{\max} \tag{3.4}$$

Here, x are the decision variables with lower and upper bounds  $x^{\min}$  and  $x^{\max}$ , respectively, f(x) is the objective function, g(x) and h(x) are the equality and inequality constraints, respectively. In the following sections we describe what constitutes these different terms as used by OPFLOW.

#### 3.1.1 Variables and bounds

The different variables used in OPFLOW formulation are described in Table 3.1.

Power imbalance variables are non-physical (slack) variables that measure the violation of power balance at buses. Having these variables (may) help in making the optimization problem easier to solve since they always ensure feasibility of the bus power balance constraints.

#### 3.1.2 Objective Function

The objective function for OPFLOW is given in (3.5)

min. 
$$C_{gen}(p^{g}) + C_{dev}(\Delta p^{g}) + C_{loss}(\Delta p^{l}, \Delta q^{l}) + C_{imb}(\Delta p^{+}, \Delta p^{-}, \Delta q^{+}, \Delta q^{-})$$
 (3.5)

Table 3.1: Optimal power flow (OPFLOW) variables

Symbol	Variable	Bounds	Notes
$p_j^{\mathrm{g}}$	Generator real power dispatch	$p_j^{\text{gmin}} \le p_j^{\text{g}} \le p_j^{\text{gmax}}$	
$q_j^{\mathrm{g}}$	Generator reactive power dispatch	$q_j^{\text{gmin}} \le q_j^{\text{g}} \le q_j^{\text{gmax}}$	
$\Delta p_j^{ m g}$	Generator real power deviation	$-p_j^{\mathrm{r}} \le \Delta p_j^{\mathrm{g}} \le p_j^{\mathrm{r}}$	• Only used when -opflow_has_gensetpoint or -opflow_use_agc option is active • $\Delta p_j^{\rm g}$ is the deviation from real power generation setpoint $p_j^{\rm gset}$ .
$p_j^{ m gset}$	Generator real power set-point	$p_j^{\text{gmin}} \leq p_j^{\text{gset}} \leq p_j^{\text{gmin}}$	Only used when -opflow_has_gensetpoint or -opflow_use_agc option is active.
$\Delta P$	System power ex- cess/deficit	Unbounded	Only used when -opflow_use_agc is active
$\theta_i$	Bus voltage angle	$-\pi \le \theta_i \le \pi$	• Used with power balance polar model (-opflow_model POWER_BALANCE_POLAR) • $\theta_i$ is unbounded, except reference bus angle $\theta_i^{\mathrm{ref}}$ which is fixed to 0
$v_i$	Bus voltage magnitude	$v_i^{\min} \le v_i \le v_i^{\max}$	$ \begin{array}{lll} \bullet \text{ Used} & \text{with} & \text{power} & \text{balance} & \text{polar} & \text{model} \\ & (-\texttt{opflow}\_\texttt{model} & \texttt{POWER}\_\texttt{BALANCE}\_\texttt{POLAR}) \\ \bullet & v_i^{\min} = v_i^{\max} = v_i^{\text{set}} & \text{if fixed generator set point voltage option is active } (-\texttt{opflow}\_\texttt{has}\_\texttt{gensetpoint}) \\ \end{array} $
$\Delta p_i^+, \Delta p_i^-$	Bus real power mismatch variables	$0 \le \Delta p_i^+, \Delta p_i^- \le \infty$	Used when power mismatch variable option is active (-opflow_include_powerimbalance_variables1)
$\Delta q_i^+, \Delta q_i^-$	Bus reactive power mismatch variables	$0 \le \Delta q_i^+, \Delta q_i^- \le \infty$	Used when power mismatch variable option is active (-opflow_include_powerimbalance_variables1)
$\Delta p_j^{ m l}$	Real power load loss	$0 \le \Delta p_j^{\mathbf{l}} \le p_j^{\mathbf{l}}$	Used when load loss variable option is active (-opflow_include_loadloss_variables1)
$\Delta q_j^{ m l}$	Reactive power load loss	$0 \le \Delta q_j^{\mathrm{l}} \le q_j^{\mathrm{l}}$	Used when load loss variable option is active (-opflow_include_loadloss_variables1)

## Total generation cost $C_{gen}(p^{\mathbf{g}})$

Needs option -opflow\_objective MIN\_GEN\_COST

$$C_{gen}(p^{g}) = \sum_{j \in J^{gen}} C_{j}^{g}(p_{j}^{g})$$

$$(3.6)$$

Here,  $C_j^{\rm g}$  is a quadratic function of the form  $C_j^{\rm g} = a_j^{\rm g} p_j^{\rm g^2} + b_j^{\rm g} p_j^{\rm g} + c_j^{\rm g}$ .

#### Total generation setpoint deviation $C(\Delta p^{\mathbf{g}})$

Needs option -opflow\_objective MIN\_GENSETPOINT\_DEVIATION

$$C_{dev}(\Delta p^{g}) = \sum_{j \in J^{\text{gen}}} (\Delta p_{j}^{g^{2}})$$
(3.7)

This feature is only supported with IPOPT solver.

## Load loss $C(\Delta p^{\mathbf{l}}, \Delta q^{\mathbf{l}})$

This term gets added to the objective when -opflow\_include\_loadloss\_variables option is active.

$$C_{loss}(\Delta p^{l}, \Delta q^{l}) = \sum_{j \in I^{ld}} \sigma_{j}^{l}(\Delta p_{j}^{l} + \Delta q_{j}^{l})$$
(3.8)

The load loss penalty  $\sigma_j^l$  can be set via the option -opflow\_loadloss\_penalty. The default is 1000/MW for all loads.

## Power imbalance $C_{imb}(\Delta p^+, \Delta p^-, \Delta q^+, \Delta q^-)$

This term gets added to the objective when -opflow\_include\_powerimbalance\_variables option is active.

$$C_{imb}(\Delta p^+, \Delta p^-, \Delta q^+, \Delta q^-) = \sum_{i \in J^{bus}} \sigma_i(\Delta p^+ + \Delta p^- + \Delta q^+ + \Delta q^-)$$
(3.9)

The power imbalance cost  $\sigma_i$  can be set via the option -opflow\_powerimbalance\_penalty. The default is \$10,000/MW<sup>2</sup> for all buses. Though the power imbalance variables  $\Delta p^+, \Delta p^-, \Delta q^+, \Delta q^-$  are slack or non-physical, they can help in solving infeasible cases having no power flow solution, and thus provide a measure of the infeasibility.

#### Equality constraints 3.1.3

#### Nodal power balance

The nodal power balance equations for each bus i are given by

$$\sum_{\substack{j \in J^{\text{gen}} \\ A_{ij}^{\text{g}} \neq 0}} p_j^{\text{g}} = p_i^{\text{sh}} + \Delta p_i^+ - \Delta p_i^- + \sum_{\substack{j \in J^{\text{ld}} \\ A_{ij}^{\text{l}} \neq 0}} (p_j^{\text{l}} - \Delta p_j^{\text{l}}) + \sum_{\substack{j \in J^{\text{br}} \\ A_{oi}^{\text{br}} \neq 0}} p_{jod}^{\text{br}} + \sum_{\substack{j \in J^{\text{br}} \\ A_{id}^{\text{br}} \neq 0}} p_{jdo}^{\text{br}}$$
(3.10)

$$\sum_{\substack{j \in J^{\text{gen}} \\ A_{ij}^g \neq 0}} p_j^g = p_i^{\text{sh}} + \Delta p_i^+ - \Delta p_i^- + \sum_{\substack{j \in J^{\text{ld}} \\ A_{ij}^l \neq 0}} (p_j^l - \Delta p_j^l) + \sum_{\substack{j \in J^{\text{br}} \\ A_{oi}^{\text{br}} \neq 0}} p_{jod}^{\text{br}} + \sum_{\substack{j \in J^{\text{br}} \\ A_{id}^{\text{br}} \neq 0}} p_{jdo}^{\text{br}} \\
\sum_{\substack{j \in J^{\text{gen}} \\ A_{id}^g \neq 0}} q_j^g = q_i^{\text{sh}} + \Delta q_i^+ - \Delta q_i^- + \sum_{\substack{j \in J^{\text{ld}} \\ A_{ij}^l \neq 0}} (q_j^l - \Delta q_j^l) + \sum_{\substack{j \in J^{\text{br}} \\ A_{oi}^{\text{br}} \neq 0}} q_{jod}^{\text{br}} + \sum_{\substack{j \in J^{\text{br}} \\ A_{id}^{\text{br}} \neq 0}} q_{jdo}^{\text{br}}$$
(3.11)

(3.12)

where, the real and reactive power shunt consumption is given by (3.13) and (3.14)

The real and reactive power flow  $p_{j_{od}}^{\text{br}}$ ,  $q_{j_{od}}^{\text{br}}$  for line j from the origin bus o to destination bus d is given by (3.19) – (3.20) and from destination bus d to origin bus o is given by (3.21) – (3.22)

#### Shunt power

$$p_i^{\text{Sh}} = g_i^{\text{Sh}} v_i^2 \tag{3.13}$$

$$q_i^{\rm Sh} = -b_i^{\rm Sh} v_i^2 \tag{3.14}$$

#### Generator real power output

When using -opflow\_has\_gensetpoint, two extra variables  $p_j^{
m gset}$  and  $\Delta p_j^{
m g}$  are added for each generator. The generator real power output  $p_j^{\mathsf{g}}$  is related to the power deviation  $\Delta p_j^{\mathsf{g}}$  by the following relations

$$p_j^{\text{gset}} + \Delta p_j^{\text{g}} - p_j^{\text{g}} = 0 \tag{3.15}$$

$$p_j^{\text{gset}} - p_j^{g^*} = 0 (3.16)$$

The second equation sets the generator set-point  $p_j^{\text{gset}}$  to a fixed value  $p_j^{\text{g*}}$ . Here,  $p_j^{\text{g*}}$  is the set-point for the generator real power output, which can be thought of as an operator set or contractual agreement set-point.

#### 3.1.4Inequality constraints

#### MVA flow on branches

MVA flow limits at origin and destination buses for each line.

$$p_{j_{od}}^{\text{br}^2} + q_{j_{od}}^{\text{br}^2} \le s_j^{\text{rateA}^2}, \quad j \in J^{\text{br}}$$

$$p_{j_{do}}^{\text{br}^2} + q_{j_{do}}^{\text{br}^2} \le s_j^{\text{rateA}^2}, \quad j \in J^{\text{br}}$$
(3.17)

$$p_{j_{do}}^{\text{br}^2} + q_{j_{do}}^{\text{br}^2} \le s_j^{\text{rateA}^2}, \quad j \in J^{\text{br}}$$
 (3.18)

To reduce the number of inequality constraints, only lines that are in service and having MVA A rating  $s_i^{\mathrm{rate A}}$  less than 10000 MVA are considered.

#### **Branch flows**

In polar coordinates, the real and reactive power flow  $p_{j_{od}}^{br}$ ,  $q_{j_{od}}^{br}$  from bus o to bus d on line j is given by (3.19) - (3.20)

$$p_{j_{od}}^{\text{br}} = g_{oo}v_o^2 + v_o v_d (g_{od}\cos(\theta_o - \theta_d) + b_{od}\sin(\theta_o - \theta_d))$$
(3.19)

$$q_{j_{od}}^{\text{br}} = -b_{oo}v_o^2 + v_o v_d (-b_{od}\cos(\theta_o - \theta_d) + g_{od}\sin(\theta_o - \theta_d))$$
(3.20)

and from bus d to bus o is given by (3.21) - (3.22)

$$p_{j_{do}}^{\text{br}} = g_{dd}v_d^2 + v_d v_o(g_{do}\cos(\theta_d - \theta_o) + b_{do}\sin(\theta_d - \theta_o))$$
(3.21)

$$q_{ido}^{\text{br}} = -b_{dd}v_d^2 + v_d v_o (-b_{do}\cos(\theta_d - \theta_o) + g_{do}\sin(\theta_d - \theta_o))$$
 (3.22)

#### Automatic generation control (AGC)

With -opflow\_use\_agc, two additional constraints are added for each participating generator to enforce the proportional generator redispatch participation as done in automatic generation control (AGC). These two equations are

$$\left(\alpha_j^{\mathrm{g}} \Delta P - \Delta p_j^{\mathrm{g}}\right) \left(p_j^{\mathrm{g}} - p_j^{\mathrm{gmax}}\right) \ge 0$$

$$\left(\Delta p_j^{\mathrm{g}} - \alpha_j^{\mathrm{g}} \Delta P\right) \left(p_j^{\mathrm{gmin}} - p_j^{\mathrm{g}}\right) \ge 0$$
(3.23)

Eq. 3.23 forces the generator set-point deviation to be equal to the generation participation when the generator has head-room available  $p_j^{\text{gmin}} \leq p_j^{\text{g}} \leq p_j^{\text{gmax}}$ . Here,  $\alpha_j^{\text{g}}$  is the generator participation factor which is the proportion of the power deficit/excess  $\Delta P$  that the generator provides.

#### Generator bus voltage control

When the option <code>-opflow\_genbusvoltage FIXED\_WITHIN\_QBOUNDS</code> is used, the generator bus voltage is fixed when the total reactive power generation available at the bus is within bounds. When it reaches its bounds, the voltage varies with the generator reactive power fixed at its bound. To implement this behavior, two inequality constraints are added for each generator bus

$$(v_i^{\text{set}} - v_i)(q_i - q^{\max_i}) \ge 0$$
  
 $(v_i - v_i^{\text{set}})(q^{\min_i} - q_i) \ge 0$  (3.24)

Here,  $q_i$ ,  $q^{\max_i}$ , and  $q^{\min_i}$  are the generated, maximum, and minimum reactive power at the bus, respectively.

#### 3.2 Solvers

OPFLOW can be used with a few different solvers. All the solvers solve the optimization problem via a nonlinear interior-point algorithm.

- 1. Ipopt [7] is a popular open-source package for solving nonlinear optimization problems. It is the most robust of the solvers implemented for solving OPFLOW. However, it can be run only on a single process and does not have GPU support.
  - Option: -opflow\_solver IPOPT -opflow\_model POWER\_BALANCE\_POLAR
- 2. HiOp [6, 5] is a high-performance optimization library that implements an interior-point algorithm for solving nonlinear optimization problems. There are two solvers available from the HiOp [6, 5]library: Mixed sparse-dense formulation -opflow\_solver HIOP, and sparse formulation -opflow\_solver HIOPSPARSE. The library supports execution both on the CPU and the GPU. Options:

CPU: -opflow\_solver HIOP -opflow\_model POWER\_BALANCE\_HIOP -hiop\_compute\_mode CPU

GPU: -opflow\_solver HIOP -opflow\_model PBPOLRAJAHIOP -hiop\_compute\_mode GPU

#### 3.3 Models

A 'model' in ExaGO describes the representation of the underlying physics. All OPFLOW models use the power balance formulation in polar coordinates for the ACOPF equations. The difference between the different models arises from their specific implementation/interface. The different models available for OPFLOW are listed in Table 3.2. As discussed earlier, not every 'model' is compatible with every 'solver'. Table 3.3 lists the solver compatibility for the different models.

Table 3.2: OPFLOW models

Model type	OPFLOW option (-opflow_model )	Compatible solvers	CPU-GPU
Power balance with	POWER_BALANCE_POLAR	IPOPT,	CPU
polar coordinates		HIOPSPARSE	
Power balance with	POWER_BALANCE_HIOP	HiOp [6, 5]	CPU/GPU
polar coordinates used			
with HIOP			
Power balance with	PBPOLRAJAHIOP	HiOp [6, 5]	GPU
polar coordinates used			
with HIOP on GPU			

Table 3.3: OPFLOW Model-solver compatibility

Model Name	Ipopt [7]	HiOp [6, 5]	HIOPSPARSE
POWER_BALANCE_POLAR	✓		✓
POWER_BALANCE_HIOP		✓	
PBPOLRAJAHIOP		✓	

#### 3.3.1 Power balance polar

The power balance polar model (-opflow\_model POWER\_BALANCE\_POLAR) uses the power balance formulation with polar representation for the network voltages. It runs on CPU only and is compatible with Ipopt [7] and sparse HiOp [6, 5] solvers.

#### 3.3.2 Power balance with HiOp on CPU

This model (-opflow\_model POWER\_BALANCE\_HIOP) implements the power balance formulation with polar coordinates used with HiOp [6, 5]solver only. The model evaluation is done only on the CPU, but the HiOp [6, 5]solver can be executed either on the CPU (-hiop\_compute\_mode CPU) or GPU (-hiop\_compute\_mode HYBRID) by setting the -hiop\_compute\_mode option appropriately.

#### 3.3.3 Power balance with HiOp on GPU

The PBPOLRAJAHIOP model (-opflow\_model PBPOLRAJAHIOP) computes all the model and optimization calculations on the GPU. This model uses RAJA [3] and Umpire [4] libraries to run OPFLOW calculations (objective, constraints, etc.) on the GPU.

## 3.4 Input and Output

The current ExaGO version only supports reading network files in MATPOWER format and can (optionally) write the output back in MATPOWER data file format.

## 3.5 Usage

./opflow -netfile <netfilename> <opflowoptions>

# 3.6 Options

See table 3.4

Table 3.4: OPFLOW options

Option	Meaning	Values (Default value)	Compatibility
-netfile	Network file name	string < 4096 characters (case9mod.m)	
-print_output	Print output to screen	0 or 1 (0)	All solvers
-save_output	Save output to file	0 or 1 (0)	All solvers
$-opflow\_output\_format$	Solution file format	See Table 3.5 (MAT-POWER)	All solvers
-opflow_model	Representation of net- work balance equa- tions and bus voltages	See Table 3.3 (POWER_BALANCE_F	OLAR)
-opflow_solver	Optimization solver	See section 3.2	
$-opflow\_initialization$	Type of initialization	See Table 3.6 (MID-POINT)	All solvers
-opflow_has_gensetpoint	Uses generation set point and activates ramping variables	0 or 1 (0)	All models
-opflow_use_agc	Uses AGC formulation in OPF	0 or 1 (0)	POWER_BALANCE _POLAR only
-opflow_objective	type of objective function	See table 3.8 (MIN_GEN_COST)	All models
$-opflow\_genbusvoltage$	Type of generator bus voltage control	See Table 3.7 (VARI- ABLE_WITHIN _BOUNDS)	POWER_BALANCE _POLAR only
-opflow_ignore_lineflow_constraints	Ignore line flow constraints	0 or 1 (0)	All models
-opflow_monitor_line_kvlevels	Monitor line flows at these KV levels	comma separated list	All models
-opflow_include_loadloss_variables	Include load loss	0 or 1 (0)	All models
$-opflow\_include\_power imbalance\_variables$	Include power imbalance	0 or 1 (0)	All models
-opflow_loadloss_penality	\$ penalty for load loss	real (1000)	All models
$-opflow\_power imbalance\_penalty$	\$ penalty for power imbalance	real (10000)	All models
-opflow_tolerance	Optimization solver tolerance	real (1e-6)	All solvers

Table 3.5: OPFLOW solution output formats

Format name	Description
MATPOWER	Matlab format compatible with MATPOWER
CSV	Custom comma separated variable format
JSON	Javascript object notation, used for visualization
MINIMAL	Simple text file containing minimal information.

Table 3.6: OPFLOW initializations

Initialization type	Meaning
MIDPOINT	Use mid-point of bounds
FROMFILE	Use values from network file
ACPF	Run AC power flow
FLATSTART	Flat-start
DCOPF	Run DC optimal power flow

Table 3.7: OPFLOW generator bus voltage control modes

Voltage control type	Meaning	Compatibility
FIXED_WITHIN_QBOUNDS	Fixed within reactive power	POWER_BALANCE_POLAR only
	bounds	
VARIABLE_WITHIN_BOUNDS	Variable within voltage bounds	All models

Table 3.8: OPFLOW objective function types

Objective function	Meaning	Compatibility
MIN_GEN_COST	Minimize generation cost	All models
MIN_GENSETPOINT_DEVIATION	Minimize deviation (ramp up-down)	POWER_BALANCE_POLAR
	from generator set-point	model only
NO_OBJ	No objective function (only feasibil-	All models
	ity)	

# 3.7 Examples

Some OPFLOW example runs are provided with some sample output. Options values are the default values in table 3.4 unless otherwise specified. -print\_output is only used in the first example to save space. Sample output is generated by running examples from the installation directory.

Example using the Ipopt [7] solver:

```
This is Ipopt version 3.12.10, running with linear solver ma27.
Number of nonzeros in equality constraint Jacobian...:
                                                            114
Number of nonzeros in inequality constraint Jacobian.:
                                                             72
Number of nonzeros in Lagrangian Hessian....:
                                                             96
Total number of variables....:
                                                             2.4
                     variables with only lower bounds:
                                                              0
                variables with lower and upper bounds:
                                                             16
                     variables with only upper bounds:
                                                             0
Total number of equality constraints....:
                                                             18
Total number of inequality constraints....:
                                                             18
        inequality constraints with only lower bounds:
                                                              0
   inequality constraints with lower and upper bounds:
                                                             18
        inequality constraints with only upper bounds:
                                                              0
iter
                     inf_pr inf_du lq(mu) ||d|| lq(rq) alpha_du
        objective
   → alpha_pr ls
   0 1.0318125e+04 1.80e+00 1.00e+02 -1.0 0.00e+00 - 0.00e+00 0.00e
      \hookrightarrow +00
   1 7.7157691e+03 1.17e+00 1.03e+02 -1.0 1.08e+00
                                                        - 6.27e-01 3.50e
      \hookrightarrow -01f 1
   2 7.6608235e+03 1.15e+00 1.01e+02 -1.0 6.28e+00 - 1.20e-02 1.37e
      \hookrightarrow -02f 1
                                                       - 4.15e-03 5.81e
   3 7.4466686e+03 1.09e+00 3.06e+02 -1.0 3.74e+00
      \hookrightarrow -02f 1
   4 5.4292675e+03 3.92e-01 4.83e+03 -1.0 7.34e-01 - 3.34e-03 6.40e
     \hookrightarrow -01f 1
   5 4.5792834e+03 2.24e-01 1.51e+03 -1.0 6.46e-01
                                                       2.0 8.77e-03 7.37e
      \hookrightarrow -01f 1
   6 4.2907579e+03 1.20e-02 3.57e+02 -1.0 3.36e-01 - 5.37e-01 1.00e
      \hookrightarrow +00f 1
   7 4.1690456e+03 4.40e-02 5.31e+01 -1.0 3.31e-01 - 9.22e-01 1.00e
      → +00f 1
    4.1687926e+03 4.88e-04 1.93e+00 -1.0 4.79e-02
                                                       1.5 1.00e+00 1.00e
      \hookrightarrow +00h 1
   9 4.1497176e+03 1.19e-02 9.92e+00 -2.5 1.87e-01 - 8.38e-01 1.00e
      \hookrightarrow +00f 1
       objective
                     inf_pr inf_du lg(mu) ||d|| lg(rg) alpha_du
iter
   \hookrightarrow alpha_pr ls
  10 4.1463942e+03 1.09e-02 5.09e-01 -2.5 1.15e-01 - 8.71e-01 1.00e
    \rightarrow +00h 1
  11 4.1449657e+03 1.47e-03 1.79e-02 -2.5 2.75e-02
                                                       - 1.00e+00 1.00e
  12 4.1445415e+03 6.63e-04 9.12e-02 -3.8 1.48e-02 - 1.00e+00 6.30e
    \hookrightarrow -01h 1
  13 4.1444705e+03 3.43e-04 4.96e-02 -3.8 2.08e-02 - 1.00e+00 8.93e
```

```
\hookrightarrow -01h 1
  14 4.1444809e+03 4.48e-05 1.79e-04 -3.8 6.82e-03 - 1.00e+00 1.00e
    \rightarrow +00f 1
  15 4.1444611e+03 1.96e-05 4.55e-03 -5.7 4.57e-03 - 1.00e+00 9.34e
    \hookrightarrow -01h 1
 16 4.1444607e+03 6.49e-06 1.17e-05 -5.7 2.60e-03 - 1.00e+00 1.00e
  17 4.1444605e+03 1.19e-06 2.07e-06 -7.0 1.11e-03 - 1.00e+00 1.00e
    \hookrightarrow +00h 1
 18 4.1444605e+03 1.58e-07 3.29e-07 -7.0 4.06e-04 - 1.00e+00 1.00e
    \hookrightarrow +00h 1
Number of Iterations...: 18
                                 (scaled)
                                                        (unscaled)
Objective...... 9.2925122354655841e+01 4.1444604570176507e
  → +03
Dual infeasibility.....: 3.2927387965389691e-07
                                                 1.4685615032563802e
  \hookrightarrow -05
Constraint violation...: 2.6639677713768961e-08 2.6639677713768961e
  \hookrightarrow -08
Complementarity..... 4.7840038622596930e-07
                                                 2.1336657225678232e
  \hookrightarrow -05
Overall NLP error....: 4.7840038622596930e-07 2.1336657225678232e
  \hookrightarrow -0.5
Number of objective function evaluations
                                                = 19
Number of objective gradient evaluations
                                                = 19
Number of equality constraint evaluations
Number of inequality constraint evaluations
Number of equality constraint Jacobian evaluations = 19
Number of inequality constraint Jacobian evaluations = 19
Number of Lagrangian Hessian evaluations
                                                = 18
Total CPU secs in IPOPT (w/o function evaluations) =
                                                        0.025
Total CPU secs in NLP function evaluations
                                                        0.002
EXIT: Optimal Solution Found.
______
Optimal Power Flow
_____
Model
                                 POWER BALANCE POLAR
Solver
                                 IPOPT
Objective
                                 MIN GEN COST
Initialization
                                 MIDPOINT
Gen. bus voltage mode
                                 VARIABLE WITHIN BOUNDS
Load loss allowed
                                 NΟ
```

Power i	imba	alance allowed	NC
Ignore	lir	ne flow constraints	NC
Number	of	variables	24
Number	of	equality constraints	18
Number	of	inequality constraints	18

Convergence status CONVERGED Objective value 4144.46

1	s Pd → Pslack			Va	mult_Pmis	mult_Qmis
1	0.00 → 0.00		1.100	0.000	2102.91	0.00
2		0.00	1.095	3.928	2059.18	-0.00
3	0.00 → 0.00		1.087	2.120	2065.15	-0.00
4	0.00 → 0.00		1.097	-1.993	2103.16	0.08
5	75.00 → 0.00		1.079	-3.060	2113.45	7.29
6	90.00 → 0.00		1.087	-3.927	2129.85	1.62
7	0.00 → 0.00		1.100	0.535	2059.57	-0.04
8	100.00 → 0.00		1.089	-1.720	2079.34	2.99
9	0.00 → 0.00		1.100	-0.135	2065.43	-0.09

$\hookrightarrow$							
From	То	Status	Sft	Stf	Slim	mult_Sf	mult_St
$\hookrightarrow$							
1	4	1	73.18	72.98	380.00	-0.00	-0.00
2	7	1	114.18	114.68	250.00	-0.00	-0.00
3	9	1	83.57	84.60	300.00	-0.00	-0.00
4	5	1	29.68	40.50	250.00	-0.00	-0.00
4	6	1	44.86	46.03	250.00	-0.00	-0.00
5	7	1	51.29	49.04	250.00	-0.00	-0.00
6	9	1	48.94	51.43	150.00	-0.00	-0.00
7	8	1	66.61	68.11	250.00	-0.00	-0.00
8	9	1	38.86	34.15	150.00	-0.00	-0.00

Ge		Status Qmax	Fuel	Pg	Qg	Pmin	Pmax	Qmin	
	$\hookrightarrow$								
1		1	UNDEFINED	72.86	6.79	10.00	350.00	-300.00	
	$\hookrightarrow$	300.00							
2		1	UNDEFINED	114.07	-5.13	10.00	300.00	-300.00	
	$\hookrightarrow$	300.00							
3		1	UNDEFINED	80.21	-23.47	10.00	270.00	-300.00	
	$\hookrightarrow$	300.00							
[E	xaG(	O] Finaliz	ing opflow a	application	on.				

#### Example using the HiOp [6, 5] solver on the CPU with ACPF initialization:

```
./bin/opflow -opflow_solver HIOP -opflow_model POWER_BALANCE_HIOP -netfile
   → $EXAGO_DIR/datafiles/case9/case9mod.m -opflow_initialization ACPF -
   → hiop_compute CPU -hiop_verbosity_level 3 -print_output
[ExaGO] Creating OPFlow
[Warning] Detected 1 fixed variables out of a total of 24.
_____
Hiop SOLVER
_____
Using 1 MPI ranks.
_____
Problem Summary
_____
Total number of variables: 24
     lower/upper/lower_and_upper bounds: 16 / 16 / 16
Total number of equality constraints: 18
Total number of inequality constraints: 18
     lower/upper/lower_and_upper bounds: 18 / 18 / 18
                                inf_du
iter
       objective
                     inf_pr
                                        lg(mu) alpha_du
                                                         alpha_pr
   → linesrch
   0 4.6670737e+03 3.714e-11 2.891e+03 -1.00 0.000e+00
                                                          0.000e+00
     \hookrightarrow - (-)
    4.6431205e+03 3.373e-04 2.791e+03 -1.00 3.013e-01 3.498e-02
                                                                    1(f
   2 4.4461241e+03 6.595e-02 2.105e+03 -1.00 4.910e-01 2.467e-01
                                                                     1 (s
   3 4.1942969e+03 6.464e-02 5.808e+02 -1.00 5.986e-01
                                                          8.573e-01
                                                                     1 (s
   4 4.1615434e+03 8.234e-03 1.159e+02 -1.00 7.556e-01 1.000e+00
                                                                     1 (s
     \hookrightarrow )
   5 4.1471588e+03 4.414e-03 1.291e+02 -1.00 1.000e+00 1.000e+00
                                                                     1 (s
```

```
\hookrightarrow )
   6 4.1441777e+03 2.959e-02 7.889e+01 -1.00 4.818e-01 4.030e-01 1(s
  7 4.1448270e+03 7.926e-03 4.949e+01 -1.00 1.000e+00 1.000e+00 1(s
   8 4.1448562e+03 1.506e-03 2.576e-01 -1.00 1.000e+00 1.000e+00 1(s
   9 4.1444966e+03 3.576e-04 2.859e+00 -3.82 9.631e-01 6.968e-01 1(s
     \hookrightarrow )
iter objective inf_pr inf_du lg(mu) alpha_du alpha_pr
  → linesrch
  10 4.1444617e+03 1.671e-04 2.747e+00 -3.82 9.520e-01 7.537e-01 1(s
 11 4.1444597e+03 5.733e-05 1.190e-01 -3.82 9.716e-01 1.000e+00 1(s
    \hookrightarrow )
  12 4.1444610e+03 6.929e-06 5.005e-04 -3.82 1.000e+00 1.000e+00 1(s
    \hookrightarrow )
  13 4.1444605e+03 1.681e-06 1.400e-04 -5.73 1.000e+00 1.000e+00 1(h
 14 4.1444605e+03 2.574e-07 2.377e-05 -5.73 1.000e+00 1.000e+00 1(h
    \hookrightarrow )
 15 4.1444604e+03 1.411e-08 1.319e-06 -5.73 1.000e+00 1.000e+00 1(h
    \hookrightarrow )
 16 4.1444604e+03 2.396e-10 2.047e-08 -7.00 1.000e+00 1.000e+00 1(h
Successfull termination.
Total time 0.933 sec
Hiop internal time: total 0.932 sec avg iter 0.058 sec
   internal total std dev across ranks 0.000 percent
Fcn/deriv time: total=0.001 sec (obj=0.000 grad=0.000 cons=0.000 Jac
  \hookrightarrow =0.000 Hess=0.001)
   Fcn/deriv total std dev across ranks 0.000 percent
Fcn/deriv #: obj 18 grad 18 eg cons 18 ineg cons 18 eg Jac 18 ineg Jac 18
Total KKT time 0.931 sec
update init 0.848sec update linsys 0.000 sec fact 0.071 sec
solve rhs-manip 0.000 sec triangular solve 0.012 sec
______
Optimal Power Flow
______
Model
                                 POWER BALANCE HIOP
Solver
                                 HIOP
Objective
                                 MIN GEN COST
Initialization
Gen. bus voltage mode
                                 VARIABLE_WITHIN_BOUNDS
Load loss allowed
                                 NO
Power imbalance allowed
                                 NO
```

Ignore	line	flow	constraints	NO

Number of variables 24
Number of equality constraints 18
Number of inequality constraints 18

Convergence status CONVERGED Objective value 4144.46

	s Pd → Pslack			Va	mult_Pmis	mult_Qmis
1	0.00 → 0.00		1.100	-0.000	2102.91	0.00
2		0.00	1.095	3.928	2059.18	-0.00
3		0.00	1.087	2.120	2065.15	-0.00
4	0.00 → 0.00		1.097	-1.993	2103.17	0.07
5	75.00 → 0.00		1.079	-3.060	2113.46	7.29
6	90.00 → 0.00		1.087	-3.927	2129.85	1.62
7	0.00 → 0.00		1.100	0.535	2059.57	-0.04
8	100.00 → 0.00		1.089	-1.720	2079.34	2.99
9	0.00 → 0.00		1.100	-0.135	2065.43	-0.09

<pre>←→ From </pre>	То	Status	Sft	Stf	Slim	mult_Sf	mult_St
$\hookrightarrow$							
1	4	1	73.18	72.98	380.00	-0.00	-0.00
2	7	1	114.18	114.68	250.00	-0.00	-0.00
3	9	1	83.58	84.61	300.00	-0.00	-0.00
4	5	1	29.69	40.50	250.00	-0.00	-0.00
4	6	1	44.86	46.03	250.00	-0.00	-0.00
5	7	1	51.29	49.04	250.00	-0.00	-0.00
6	9	1	48.94	51.43	150.00	-0.00	-0.00
7	8	1	66.61	68.11	250.00	-0.00	-0.00
8	9	1	38.87	34.15	150.00	-0.00	-0.00

Gen	→ Status	Fuel	Pg	Qg	Pmin	Pmax	Qmin
	 →						
1	1	UNDEFINED	72.86	6.80	10.00	350.00	-300.00
_	→ 300.00						
2	1	UNDEFINED	114.07	-5.13	10.00	300.00	-300.00
_	→ 300.00						
3	1	UNDEFINED	80.21	-23.48	10.00	270.00	-300.00
_	→ 300.00						
[Exa	GO] Finaliz	ing opflow a	application	on.			

Example with HIOP solver on GPU with load loss activated. In this example, the load at bus 5 is increased to 750 MW leading to an infeasible power flow. Activating the load loss causes shedding of load at bus 5 and as a result makes the optimization converge.

```
./opflow -opflow_solver HIOP -opflow_model PBPOLRAJAHIOP -netfile

→ $EXAGO_DIR/datafiles/case9/case9mod_loadloss.m -hiop_compute_mode

   → GPU -hiop_verbosity_level 3 -print_output -
   → opflow_include_loadloss_variables
[ExaGO] Creating OPFlow
[Warning] Detected 1 fixed variables out of a total of 30.
==========
Hiop SOLVER
_____
Using 1 MPI ranks.
_____
Problem Summary
_____
Total number of variables: 30
     lower/upper/lower_and_upper bounds: 22 / 22 / 22
Total number of equality constraints: 18
Total number of inequality constraints: 18
     lower/upper/lower_and_upper bounds: 18 / 18 / 18
iter
        objective
                      inf_pr
                                 inf_du
                                          lg(mu)
                                                 alpha_du
                                                             alpha_pr
   → linesrch
   0 1.4867531e+04 7.490e+00
                             1.000e+05
                                         -1.00
                                                0.000e+00
                                                            0.000e+00
      \hookrightarrow - (-)
     1.3403771e+04 7.490e+00 1.000e+05 -1.00 2.729e-04
                                                           1.702e-05
                                                                      1 (s
     1.1742043e+04 7.489e+00
                              9.993e+04
                                         -1.00
                                                5.655e-03
                                                           1.102e-04
                                                                       1 (s
     1.0453140e+04 7.484e+00 8.993e+04 -1.00
                                                1.258e-01
                                                           6.948e-04
                                                                       1 (s
      \hookrightarrow )
     1.0933710e+04 7.247e+00 8.722e+04 -1.00 3.011e-02
                                                           3.073e-02
                                                                       1 (s
```

```
\hookrightarrow )
   5 1.2262728e+04 6.691e+00 1.217e+05 -1.00 3.642e-04 7.537e-02 1(s
   6 1.2718100e+04 6.509e+00 1.303e+05 -1.00 2.837e-04 2.663e-02 1(s
   7 1.2721404e+04 6.508e+00 1.302e+05 -1.00 1.583e-02 1.930e-04 1(s
   8 1.6122803e+04 5.696e+00 7.620e+04 -1.00 1.954e-03 1.492e-01 1(S
      \hookrightarrow )
   9 1.6366303e+04 5.692e+00 7.616e+04 -1.00 9.924e-02 8.075e-04 1(s
iter objective inf_pr
                                inf_du lg(mu) alpha_du alpha_pr
   → linesrch
  10 1.7501119e+04 5.671e+00 7.587e+04 -1.00 3.082e-03 3.708e-03 1(s
     \hookrightarrow )
  11 1.7624878e+04 5.668e+00 8.682e+04 -1.00 9.630e-02 3.944e-04 1(s
     \hookrightarrow )
  12 2.2838548e+04 5.575e+00 8.354e+04 -1.00 1.071e-03 1.646e-02 1(s
     \hookrightarrow )
  . . .
  47 \quad 7.4002786e+05 \quad 5.392e-03 \quad 5.252e+05 \quad -1.00 \quad 1.365e-04 \quad 4.401e-03 \quad 1 \text{ (s}
     \hookrightarrow )
  48 7.4002761e+05 5.391e-03 5.332e+05 -1.00 2.888e-02 1.880e-03 1(s
  49 7.4003537e+05 3.310e-03 4.892e+05 -1.00 3.124e-03 1.000e+00 1(s
     \hookrightarrow )
iter
       objective inf_pr inf_du lg(mu) alpha_du alpha_pr
   → linesrch
  50 \quad 7.4002879e + 05 \quad 3.234e - 03 \quad 3.147e + 05 \quad -1.00 \quad 1.000e + 00 \quad 2.273e - 02 \quad 1 \text{ (s}
     \hookrightarrow )
  51 7.4003883e+05 1.340e-05 2.982e+03 -1.00 6.601e-01 1.000e+00 1(s
     \hookrightarrow )
  52 7.4003471e+05 3.828e-04 1.015e+01 -1.00 1.000e+00 1.000e+00 1(f
  53 7.4003556e+05 2.461e-08 2.164e-01 -3.82 9.883e-01 1.000e+00 1(h
     \hookrightarrow )
  54 7.4003556e+05 2.665e-14 5.489e-07 -5.73 1.000e+00 1.000e+00 1(f
     \hookrightarrow )
Successfull termination.
Total time 1.527 sec
Hiop internal time: total 1.465 sec avg iter 0.027 sec
    internal total std dev across ranks 0.000 percent
Fcn/deriv time:
                  total=0.052 sec (obj=0.009 grad=0.003 cons=0.012 Jac
   \rightarrow =0.011 Hess=0.018)
   Fcn/deriv total std dev across ranks 0.000 percent
Fcn/deriv #: obj 97 grad 56 eq cons 97 ineq cons 97 eq Jac 56 ineq Jac 56
```

Total KKT time 1.249 sec

update init 0.773sec update linsys 0.029 sec fact 0.237 sec solve rhs-manip 0.172 sec triangular solve 0.038 sec

\_\_\_\_\_\_

Optimal Power Flow

\_\_\_\_\_

Model PBPOLRAJAHIOP Solver HIOP Objective MIN\_GEN\_COST Initialization MIDPOINT Gen. bus voltage mode VARIABLE\_WITHIN\_BOUNDS Load loss allowed YES Load loss penalty (\$) 1000. Power imbalance allowed NO Ignore line flow constraints NO Number of variables 30 Number of equality constraints 18

Convergence status CONVERGED Objective value 740035.56

Number of inequality constraints

Bu	s Pd	Qd	Vm	Va	mult_Pmis	mult_Qmis
	→ Pslack	Qsl	ack			
1	0.00 → 0.00		1.100	0.000	4182.05	0.00
2		0.00	1.100	12.398	4028.36	0.00
3		0.00	1.100	16.811	6041.35	0.00
4		0.00	1.021	-4.918	5930.37	19899.38
5		109.68	0.900	-15.480	100000.00	100000.00
6		30.00	1.018	-2.414	7827.64	16824.43
7	0.00 → 0.00	0.00	1.052	5.271	19366.68	29169.45
8	100.00 → 0.00	35.00	1.053	5.150	15594.67	21709.27
9		0.00	1.083	9.964	7193.17	9437.04

_	$\rightarrow$						
From	То	Status	Sft	Stf	Slim	mult_S:	f mult_St
	→						
1	4	1	230.52	213.89	380.00	-0.00	-0.00
2	7	1	250.00	239.12	250.00	2404.19	0.00
3	9	1	246.68	242.96	300.00	0.00	0.00
4	5	1	250.00	227.52	250.00	14113.38	0.00
4	6	1	47.20	50.98	250.00	-0.00	-0.00
5	7	1	210.17	239.03	250.00	0.00	0.00
6	9	1	137.83	144.52	150.00	0.00	0.00
7	8	1	10.10	7.53	250.00	-0.00	-0.00
8	9	1	100.92	98.82	150.00	-0.00	-0.00
	 →						
Gen	Status	Fuel	Pa	Oq	Pmin	Pmax	Omin
	→ Qmax		,	~ 3			~
	<b>→</b>		4.65 05	150 50	10.00	0.50	
		UNDEFINED	167.37	158.52	10.00	350.00	-300.00
	→ 300.00						
		UNDEFINED	229.90	98.21	10.00	300.00	-300.00
	→ 300.00						
		UNDEFINED	242.50	45.19	10.00	270.00	-300.00
	→ 300.00						
[Exa	GOJ Finaliz	ing opflow a	applicatio	n.			

# Chapter 4

# Multi-period optimal power flow (TCOPFLOW)

TCOPFLOW solves a full AC multi-period optimal power flow problem with the objective of minimizing the total cost over the given time horizon while adhering to constraints for each period and between consecutive time-periods (ramping constraints).

#### 4.1 Formulation

The multi-period optimal power flow problem is a series of optimal power flow problems coupled via temporal constraints. The generator real power deviation  $(p_{jt}^g - p_{jt-\Delta t}^g)$  constrained within the ramp limits form the temporal constraints. An illustration of the temporal constraints is shown in Fig. 4.1 with four time steps. Each time-step t is coupled with its preceding time  $t - \Delta t$ , where  $\Delta t$  is the time-step where the objective is to find a least cost dispatch for the given time horizon.

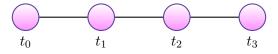


Figure 4.1: Multi-period optimal power flow example with four time-steps. The lines connecting the different time-periods denote the coupling between them.

In general form, the equations for multi-period optimal power flow are given by (4.1) – (4.5). TCOPFLOW solves to minimize the total generation cost  $\sum_{t=0}^{N_t-1} f(x_t)$  over the time horizon, where  $N_t$  is the number of time-steps. At each time-step, the equality constraints  $(g(x_t))$ , inequality  $h(x_t)$ , and the lower/upper limit  $(x^-, x^+)$  constraints need to be satisfied. Equation (4.5) represents the coupling between the consecutive time-steps. It is the most common form of coupling that limits the deviation of the real power generation at time t from its preceding time-step  $t - \Delta t$  to within its ramping capability  $\Delta x_t$ .

$$\min \sum_{t=0}^{N_t - 1} f(x_t) \tag{4.1}$$

s.t.

$$g(x_t) = 0, t \in [0, N_t - 1] (4.2)$$

$$h(x_t) \le 0,$$
  $t \in [0, N_t - 1]$  (4.3)

$$x^{-} \le x_t \le x^{+},$$
  $t \in [0, N_t - 1]$  (4.4)

$$-\Delta x_t \le x_t - x_{t-\Delta t} \le \Delta x_t, \qquad t \in [1, N_t - 1] \tag{4.5}$$

#### 4.2 Solvers

Currently, Exago only supports solving TCOPFLOW using Ipopt [7] on on a single rank.

## 4.3 Input and Output

- **Network file:** The network file describing the network details. Only MATPOWER format files are currently supported.
- Load data: One file for load real power and one for reactive power. The files need to be in CSV format. An example of the format for the 9-bus case is here.
- Wind generation: The wind generation time-series described in CSV format. See an example of the format here.

If the load data and/or wind generation profiles are not set then a flat profile is assumed, i.e., the load and wind generation for all hours is constant.

The TCOPFLOW output is saved to a directory named tcopflowout. This directory contains  $N_t$  files, one for each time-step, in MATPOWER data file format.

# 4.4 Usage

```
Ipopt is released as open source code under the Eclipse Public License (
    \hookrightarrow EPL).
        For more information visit http://projects.coin-or.org/Ipopt
*************************
This is Ipopt version 3.12.10, running with linear solver ma27.
Number of nonzeros in equality constraint Jacobian...:
                                                           798
Number of nonzeros in inequality constraint Jacobian.:
                                                           540
Number of nonzeros in Lagrangian Hessian....:
                                                           672
Total number of variables.....
                                                           168
                    variables with only lower bounds:
                                                             0
                variables with lower and upper bounds:
                                                           112
                    variables with only upper bounds:
                                                             0
Total number of equality constraints....:
                                                           126
Total number of inequality constraints....:
                                                           144
        inequality constraints with only lower bounds:
                                                             0
   inequality constraints with lower and upper bounds:
                                                           144
        inequality constraints with only upper bounds:
                                                             0
iter
       objective
                    inf_pr inf_du lg(mu) ||d|| lg(rg) alpha_du
   → alpha_pr ls
                                                         0.00e+00 0.00e
   0 7.2226875e+04 1.80e+00 1.00e+02 -1.0 0.00e+00
     \hookrightarrow +00
   1 5.1460539e+04 1.04e+00 1.60e+02 -1.0 1.08e+00
                                                         6.27e-01 4.21e
     \rightarrow -01f 1
   2 4.8692257e+04 9.13e-01 1.60e+03 -1.0 1.42e+00
                                                      2.0 2.84e-03 1.29e
     \hookrightarrow -01f 1
   3 4.1695179e+04 5.82e-01 8.63e+02 -1.0 1.09e+00 - 3.86e-03 3.78e
     \hookrightarrow -01f 1
   4 3.8223523e+04 4.01e-01 5.86e+02 -1.7 7.91e-01
                                                      - 2.00e-01 3.10e
     \hookrightarrow -01f 1
    3.1081047e+04 9.06e-02 1.98e+03 -1.7 5.58e-01
                                                       - 4.80e-01 1.00e
      \hookrightarrow +00f 1
   6 3.0468392e+04 1.83e-01 1.34e+02 -1.7 5.84e-01
                                                       - 2.75e-01 1.00e
      \hookrightarrow +00f 1
     3.0405940e+04 9.33e-02 4.47e+00 -1.7 3.04e-01
                                                       - 4.96e-01 1.00e
     \hookrightarrow +00f 1
   8 3.0382232e+04 3.12e-02 7.07e-01 -2.5 1.76e-01
                                                       - 7.33e-01 1.00e
     \rightarrow +00h 1
   9 3.0369124e+04 2.45e-03 4.69e-02 -2.5 4.46e-02 - 1.00e+00 1.00e
      \hookrightarrow +00h 1
       objective
                   inf_pr inf_du lg(mu) ||d|| lg(rg) alpha_du
iter
   → alpha_pr ls
```

```
10 3.0364520e+04 9.81e-04 7.50e-02 -3.8 2.34e-02 - 9.84e-01 6.75e
    \hookrightarrow -01h 1
  11 3.0364301e+04 1.91e-04 1.14e-02 -3.8 1.67e-02 - 8.91e-01 9.19e
    → -01h 1
 12 3.0364426e+04 4.32e-05 9.33e-05 -3.8 6.82e-03 - 1.00e+00 1.00e
    \rightarrow +00f 1
  13 3.0364326e+04 1.45e-05 4.77e-03 -5.7 3.90e-03
                                                    - 1.00e+00 9.44e
    \hookrightarrow -01h 1
 14 3.0364329e+04 1.12e-06 2.32e-06 -5.7 1.10e-03 - 1.00e+00 1.00e
    \hookrightarrow +00h 1
 15 3.0364328e+04 7.91e-09 3.33e-08 -7.0 9.28e-05 - 1.00e+00 1.00e
    \hookrightarrow +00h 1
Number of Iterations....: 15
                                 (scaled)
                                                         (unscaled)
Objective..... 6.8081453631121144e+02 3.0364328319480031e
  \hookrightarrow +04
Dual infeasibility....: 3.3330834427063850e-08
                                                  1.4865552154470478e
  \hookrightarrow -06
Constraint violation...: 1.5610245006347778e-09
                                                  1.5610245006347778e
  \hookrightarrow -09
Complementarity.....: 1.0802025033126202e-07 4.8177031647742860e
  \hookrightarrow -06
Overall NLP error....: 1.0802025033126202e-07
                                                 4.8177031647742860e
  → -06
Number of objective function evaluations
                                                 = 16
Number of objective gradient evaluations
                                                 = 16
Number of equality constraint evaluations
                                                 = 16
Number of inequality constraint evaluations
                                                 = 16
Number of equality constraint Jacobian evaluations = 16
Number of inequality constraint Jacobian evaluations = 16
Number of Lagrangian Hessian evaluations
                                                 = 15
Total CPU secs in IPOPT (w/o function evaluations) =
                                                         0.036
Total CPU secs in NLP function evaluations
                                                         0.014
EXIT: Optimal Solution Found.
_____
Multi-Period Optimal Power Flow
_____
OPFLOW Model
                                  POWER BALANCE POLAR
Solver
                                 IPOPT
Duration (minutes)
                                  30.00
Time-step (minutes)
                                 5.00
Number of steps
```

Active power demand profile /people/abhy245/projects/exaSGD/exago/ → datafiles/case9/load\_P.csv Rective power demand profile /people/abhy245/projects/exaSGD/exago/ → datafiles/case9/load\_Q.csv Wind generation profile NOT SET Load loss allowed NO Power imbalance allowed NO Ignore line flow constraints NO Number of variables 168 Number of equality constraints 126 Number of inequality constraints 126 Number of coupling constraints Convergence status CONVERGED Objective value 30364.33

Bus	Pd	Qd	Vm	Va	mult_Pmis	mult_Qmis
	→ Pslack	Qsl	ack			
	0.00 → 0.00		1.089	0.000	2102.34	-0.00
2	0.00	0.00	1.092	3.904	2059.04	-0.00
3	0.00	0.00	1.087	2.077	2065.00	-0.00
4		0.00	1.095	-2.016	2102.60	-0.04
	→ 0.00 75.00		1.088	-3.150	2112.60	1.16
1	→ 0.00 90.00		1.085	-3.962	2129.51	1.68
7	→ 0.00 0.00		1.100	0.501	2059.43	-0.06
_	→ 0.00	0.00			2079.19	2.98
_	→ 0.00	0.00				
1	0.00 → 0.00		1.100	-0.176	2065.27	-0.09

$\hookrightarrow$								
From	To	Status	Sft	Stf	Slim	mult_Sf	mult_St	
$\hookrightarrow$								
1	4	1	73.35	73.70	380.00	-0.00	-0.00	
2	7	1	114.60	115.46	250.00	-0.00	-0.00	

3 4 4 5 6 7 8	9 5 6 7 9 8 9	1 1 1 1 1 1	83.29 28.85 44.89 49.16 49.36 66.70 38.80	50.83 51.07	300.00 250.00 250.00 250.00 150.00 250.00	-0.00 -0.00 -0.00 -0.00	-0.00 -0.00 -0.00 -0.00 -0.00	
Ger	↔ n Status ↔ Qmax	Fuel	Pg	Qg	Pmin	Pmax	Qmin	
1 2	→ 300.00  1	UNDEFINED UNDEFINED		-8.69 -11.12			-300.00 -300.00	
3 [Ex	→ 300.00 1 → 300.00 ×aGO] Finaliz	UNDEFINED			10.00	270.00	-300.00	

## Chapter 5

# Security-constrained optimal power flow (SCOPFLOW)

SCOPFLOW solves a contingency-constrained optimal power flow problem. The problem is set up as a two-stage optimization problem where the first-stage (base-case) represents the normal operation of the grid and the second-stage comprises  $N_c$  contingency scenarios. Each contingency scenario can be single or multi-period.

#### 5.1 Formulation

#### 5.1.1 Single-period

The contingency-constrained optimal power flow (popularly termed as security-constrained optimal power flow (SCOPF) in power system parlance) attempts to find a least cost dispatch for the base case (or no contingency) while ensuring that if any of contingencies do occur then the system will be secure. This is illustrated in Fig. 5.1 for a SCOPF with a base-case  $c_0$  and three contingencies.

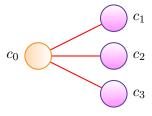


Figure 5.1: Contingency constrained optimal power flow example with three contingencies.  $c_0$  represents the base case (or no contingency case).  $c_1$ ,  $c_2$ ,  $c_3$  are the three contingency cases. Each of the contingency states is coupled with the base-case through ramping constraints (denoted by red lines)

In general form, the equations for contingency-constrained optimal power flow are given by (5.1) – (5.5). This is a two-stage stochastic optimization problem where the first stage is the base case  $c_0$  and each of the contingency states  $c_i$ ,  $i \in [1, N_c]$  are second-stage subproblems. SCOPFLOW aims to minimize the objective  $\sum_{c=0}^{N_c} f(x_c)$ , while adhering to the equality  $g_c(x_c)$ , inequality  $h_c(x_c)$ , and the lower/upper bound  $(x^-, x^+)$  constraints. Equation (5.5) represents the coupling between the base-case  $c_0$  and each of the contingency states  $c_i$ . Equation (5.5) is the most typical form of coupling that limits the deviation of the contingency variables  $x_c$  from the base  $x_0$  to within  $\Delta x_c$ . An example of this

constraint could be the allowed real power output deviation for the generators constrained by their ramp limit, which is currently the only constraint SCOPFLOW supports.

$$\min \sum_{c=0}^{N_c} f_c(x_c) \tag{5.1}$$

s.t.

$$g_c(x_c) = 0, \qquad c \in [0, N_c] \tag{5.2}$$

$$h_c(x_c) \le 0, \qquad c \in [0, N_c] \tag{5.3}$$

$$x^- \le x_c \le x^+, \qquad c \in [0, N_c] \tag{5.4}$$

$$-\Delta x_c \le x_c - x_0 \le \Delta x_c, \qquad c \in [1, N_c] \tag{5.5}$$

#### 5.1.2 Multiperiod

In the multi-period version, each contingency is comprised of multiple time-periods. The multiple periods have variables and constraints as described in chapter 4. An example of multi-contingency multi-period optimal power flow is illustrated in Fig. 5.2 for multi-period SCOPFLOW with three contingencies  $c_1$ ,  $c_2$ , and  $c_3$  coupled to the base case  $c_0$ . Each state is multi-period with two time-periods. Each time-step is coupled with its adjacent one through ramping constraints. We assume that the contingency is incident at the first time-step, i.e. at  $t_0$ . This results in the coupling between the contingency cases  $c_i$ ,  $i \in [1, N_c]$  and the base-case  $c_0$  only at time-step  $t_0$ .



Figure 5.2: Multi-period contingency constrained optimal power flow example with two contingencies  $c_0$  and  $c_1$ , each with two time-periods  $t_0$ ,  $t_1$ . State  $c_0$  represents the base case (no contingency) case. The contingency states  $c_1, c_2, c_3$  are coupled with the no-contingency state  $c_0$ . The red line denotes the coupling between the contingencies.

The overall objective of this contingency-constrained multi-period optimal power flow is to find a secure dispatch for base-case  $c_0$  while adhering to contingency and temporal constraints. The general formulation of this problem is given in Eqs. (5.6) - (5.12).

$$\min \sum_{c=0}^{N_c} \sum_{t=0}^{N_t - 1} f_{ct}(x_{c,t}) \tag{5.6}$$

s.t.

$$g_{ct}(x_{c,t}) = 0,$$
  $c \in [0, N_c], t \in [0, N_t - 1]$  (5.7)

$$h_{ct}(x_{c,t}) \le 0,$$
  $c \in [0, N_c], t \in [0, N_t - 1]$  (5.8)

$$x^{-} \le x_{c,t} \le x^{+},$$
  $c \in [0, N_c], t \in [0, N_t - 1]$  (5.9)

$$-\Delta x_t \le x_{c,t} - x_{c,t-\Delta t} \le \Delta x_t, \qquad c \in [0, N_c], t \in [1, N_t - 1]$$
 (5.10)

$$-\Delta x_c \le x_{c,0} - x_{0,0} \le \Delta x_c, \qquad c \in [1, N_c] \tag{5.11}$$

(5.12)

In this formulation, the objective is to reduce the cost for the base-case time horizon, where  $f(x_{0,t})$  is the objective cost for contingency  $c_0$  at time t. Equation (5.12) represents the coupling between the base case  $c_0$  and each contingency  $c_i$  at time-step  $t_0$ . We use a simple box constraint  $\Delta x_c$  to restrict the deviation of decision variables  $x_{c,0}$  from the base-case  $x_{0,0}$ . The bound  $\Delta x_c$  could represent here, for example, the allowable reserve for each generator.

#### 5.2 Solvers

SCOPFLOW supports solving the optimization problem via Ipopt [7], HiOp [6, 5], or EMPAR. Ipopt [7]can solve SCOPFLOW on single rank only. HiOp [6, 5] supports solving the problem in parallel using a primal-decomposition algorithm. With HIOP, one can solve the subproblem either on the CPU or GPU by selecting the appropriate subproblem model and solver (see options table below). However, note that ExaGO needs to be built with Ipopt [7]even when using HiOp [6, 5]solver. The EMPAR solver does not solve the security-constrained ACOPF problem, it only solves the base-case and the contingencies independently with OPFLOW. It distributes the contingencies to different processes when executed in parallel.

#### 5.3 Input and Output

To execute SCOPFLOW, the following files are required:

- **Network file:** The network file describing the network details. Only MATPOWER format files are currently supported.
- Contingency file: The file describing the contingencies. Contingencies can be single or multiple outages. The contingency file needs to be described in PTI format.

If the multi-period option is chosen, then additional files describing the load and wind generation can be (optionally) set.

- Load data: One file for load real power and one for reactive power. The files need to be in CSV format. An example of the format for the 9-bus case is here.
- Wind generation: The wind generation time-series described in CSV format. See an example of the format here.

The SCOPFLOW output is saved to a directory named scopflowout. This directory contains  $N_c$  files to save the solution for each contingency in MATPOWER datafile format. Each file has the name cont\_xx where xx is the contingency number.

If the multi-period option is chosen then  $N_c$  subdirectories are created (one for each contingency), and each subdirectory contains  $N_t$  output files, one for each time-period. The subdirectories have the naming convention cont\_xx and the output file are named as t\_yy where yy is the time-step number.

#### 5.4 Usage

```
./scopflow -netfile <netfilename> -ctgcfile <ctgcfilename> \
<scopflowoptions> [-scopflow_enable_multiperiod 1]
```

#### 5.5 Options

See table 5.1. In addition, all OPFLOW options in Table 3.4 and TCOPFLOW options in Table ?? can be used.

Table 5.1: SCOPFLOW options

Option	Meaning	Values (Default value)	Compatibility
-netfile	Network file name	string < 4096 characters (case9mod_gen3_wind.m)	
-ctgcfile	Contingency file name	string < 4096 characters (case9.cont)	
-print_output	Print output to screen	0 or 1 (0)	
-save_output	Save output to directory	0 or 1 (0)	Format determined by OPFLOW option.
-scopflow_output_directory	Output directory path	"scopflowout"	
-scopflow_model	SCOPFLOW model type	GENRAMP, GENRAMPT (GENRAMP)	
-scopflow_solver	Set solver for scopflow	IPOPT, HIOP, or EMPAR (IPOPT)	
-scopflow_subproblem_solver	Set solver for subprob- lem	IPOPT or HIOP (IPOPT)	Only when using HIOP solver for SCOPFLOW
-scopflow_subproblem_model	Set model for subprob- lem	See OPFLOW chapter	Only when using HIOP solver for SCOPFLOW
-scopflow_Nc	Number of contingencies	int (0. Passing -1 results in all contingencies in the file used)	
-scopflow_mode	Operation mode: Preventive or corrective	0 or 1 (0)	
$-scopflow\_enable\_multiperiod$	Multi-period SCOPFLOW	0 or 1 (0)	IPOPT solver only
-scopflow_ploadprofile	Real power load profile	string (load_P.csv)	
$-scopflow\_qloadprofile$	Reactive power load profile	string (load_Q.csv)	
-scopflow_windgenprofile	Wind generation pro- file	string (case9/scenarios_9bus.csv)	
-scopflow_dT	Length of time-step (minutes)	double (5.0)	
-scopflow_duration	Total duration (hours)	double $(0.5)$	
-scopflow_tolerance	Optimization solver tolerance	double (1e-6)	

Depending on the value chosen for <code>-scopflow\_mode</code>, SCOPFLOW can operate either in preventive (mode = 0) or corrective (mode = 1) mode. In the preventive mode, the PV and PQ generator real power is fixed to its corresponding base-case values. The generators at the reference bus pick up any make-up power required for the contingency. The corrective mode allows deviation of the PV and PQ generator real power from the base-case dispatch constrained by its 30-min. ramp rate capability. The optimization decides the optimal redispatch. One can have AGC control instead of having the generators proportionally share the deficit/excess power by using the option (-opflow use agc).

The option -scopflow\_enable\_multiperiod 1 must be used in order to enable any of the options listed in table 5.1 for multiperiod analysis.

#### 5.6 Examples

Some SCOPFLOW example runs are provided with some sample output. Options are the default options given in table 3.4, ?? and 5.1 unless otherwise specified. Sample output is generated by running examples in the installation directory.

Example using the Ipopt [7]solver:

```
./bin/scopflow -netfile $EXAGO_DIR/datafiles/case9/case9mod.m -ctqcfile
   → $EXAGO_DIR/datafiles/case9/case9.cont -scopflow_Nc 4 -
   → scopflow_solver IPOPT -print_output
[ExaGO] SCOPFLOW: Application created
[ExaGO] SCOPFLOW running with 5 subproblems (base case + 4 contingencies)
[ExaGO] SCOPFLOW: Using IPOPT solver
[ExaGO] SCOPFLOW: Setup completed
**************************
This program contains Ipopt, a library for large-scale nonlinear
  \hookrightarrow optimization.
Ipopt is released as open source code under the Eclipse Public License (
   \hookrightarrow EPL).
        For more information visit http://projects.coin-or.org/Ipopt
************************
This is Ipopt version 3.12.10, running with linear solver ma27.
Number of nonzeros in equality constraint Jacobian...:
                                                        598
Number of nonzeros in inequality constraint Jacobian.:
                                                        328
Number of nonzeros in Lagrangian Hessian....:
                                                        660
Total number of variables....:
                                                        144
                   variables with only lower bounds:
                                                          0
               variables with lower and upper bounds:
                                                        104
                   variables with only upper bounds:
                                                          0
Total number of equality constraints....:
                                                        114
Total number of inequality constraints....:
                                                         82
       inequality constraints with only lower bounds:
                                                          0
   inequality constraints with lower and upper bounds:
                                                         82
       inequality constraints with only upper bounds:
                                                          0
       objective
                   inf_pr
                            inf_du lg(mu) ||d|| lg(rg) alpha_du
iter
   \hookrightarrow alpha_pr ls
   0 1.0318125e+04 1.80e+00 1.00e+02 -1.0 0.00e+00
                                                    - 0.00e+00 0.00e
   1 9.2868867e+03 1.56e+00 8.62e+01 -1.0 1.08e+00
                                                    - 6.27e-01 1.31e
     \hookrightarrow -01f 1
    9.0292788e+03 1.50e+00 3.50e+02 -1.0 2.60e+00 - 1.37e-03 4.28e
```

```
\rightarrow -02f 1
   3 6.8151659e+03 9.02e-01 3.07e+03 -1.0 1.03e+00 - 4.57e-02 4.09e
      \rightarrow -01f 1
   4 5.6911245e+03 5.63e-01 2.09e+03 -1.0 7.85e-01 2.0 1.22e-01 3.87e
   5 5.6219674e+03 5.39e-01 2.00e+03 -1.0 8.34e-01 - 1.99e-01 4.29e
      \rightarrow -02f 1
   6 \quad 4.7820782e+03 \quad 2.34e-01 \quad 7.42e+02 \quad -1.0 \quad 7.27e-01 \quad - \quad 5.45e-01 \quad 5.75e
      \rightarrow -01f 1
   7 4.1986838e+03 3.84e-02 2.59e+02 -1.7 4.11e-01 - 3.64e-01 1.00e
      \hookrightarrow +00f 1
   8 4.1593634e+03 6.26e-02 1.52e+01 -1.7 3.77e-01 - 5.76e-01 1.00e
      \hookrightarrow +00f 1
   9 4.1598457e+03 3.63e-04 1.53e+00 -2.5 4.57e-02 1.5 8.25e-01 1.00e
      \hookrightarrow +00h 1
                    inf_pr inf_du lg(mu) ||d|| lg(rg) alpha_du
iter
      objective
  → alpha_pr ls
  10 4.1472241e+03 4.61e-02 5.44e+00 -3.8 1.15e-01 - 3.15e-01 1.00e
     → +00f 1
 11 4.1437514e+03 3.32e-02 3.50e+00 -3.8 1.95e-01 - 5.75e-01 3.47e
     \hookrightarrow -01h 1
 12 4.1440398e+03 1.07e-02 1.64e+00 -3.8 7.68e-02 - 2.42e-01 6.18e
     → -01h 1
 13 4.1444455e+03 1.33e-03 4.38e-02 -3.8 3.29e-02 - 9.49e-01 1.00e
    \rightarrow +00h 1
  14 4.1444954e+03 5.41e-06 2.57e-02 -3.8 2.31e-03 1.0 1.00e+00 1.00e
     \hookrightarrow +00h 1
 15 4.1444778e+03 1.47e-05 1.41e-02 -3.8 3.80e-03 0.6 1.00e+00 1.00e
     → +00h
  16 4.1444804e+03 1.82e-05 4.42e-03 -3.8 3.58e-03 0.1 1.00e+00 1.00e
     \rightarrow +00h
  17 4.1444799e+03 9.05e-05 3.06e-03 -3.8 7.43e-03 -0.4 1.00e+00 1.00e
    \rightarrow +00h 1
 18 4.1444616e+03 1.08e-05 5.76e-03 -5.7 3.72e-03 -0.9 1.00e+00 9.26e
     \hookrightarrow -01h 1
  19 4.1444608e+03 5.66e-06 1.11e-04 -5.7 2.43e-03 -1.3 1.00e+00 1.00e
    \rightarrow +00h 1
        objective
                    inf_pr inf_du lg(mu) ||d|| lg(rg) alpha_du
iter
  → alpha_pr ls
  20 4.1444608e+03 2.21e-08 3.62e-05 -5.7 2.38e-03 -1.8 1.00e+00 1.00e
     → +00H 1
  21 4.1444608e+03 3.35e-07 2.93e-05 -5.7 5.76e-03 -2.3 1.00e+00 1.00e
     → +00H
  22 4.1444608e+03 2.25e-04 1.95e-05 -5.7 1.15e-02 -2.8 1.00e+00 1.00e
     \rightarrow +00h
  23 4.1444608e+03 5.41e-04 1.11e-05 -5.7 1.96e-02 -3.2 1.00e+00 1.00e
     → +00h 1
```

```
24 4.1444608e+03 2.03e-02 1.22e-04 -5.7 1.15e-01 -3.7 1.00e+00 1.00e
     \hookrightarrow +00h 1
  25 4.1444608e+03 8.07e-04 2.02e-05 -5.7 2.32e-02 -3.3 1.00e+00 1.00e
     → +00h
  26 4.1444608e+03 6.02e-03 3.97e-05 -5.7 6.75e-02 -3.8 1.00e+00 1.00e
     \hookrightarrow +00h 1
  27 4.1444608e+03 1.93e-02 1.75e-04 -5.7 1.17e-01 -4.3 1.00e+00 1.00e
     → +00h
  28 4.1444608e+03 4.88e-02 7.07e-05 -5.7 1.71e-01 -4.7 1.00e+00 1.00e
     → +00h 1
  29 4.1444608e+03 8.42e-04 6.07e-06 -5.7 3.53e-02 -4.3 1.00e+00 1.00e
    \hookrightarrow +00h 1
      objective inf_pr inf_du lg(mu) ||d|| lg(rg) alpha_du
iter
  → alpha_pr ls
  30 4.1444608e+03 1.16e-02 4.10e-06 -5.7 1.11e-01 -4.8 1.00e+00 1.00e
     \hookrightarrow +00h 1
  31 4.1444608e+03 1.54e-03 1.71e-06 -5.7 3.87e-02 -4.4 1.00e+00 1.00e
     \rightarrow +00h 1
  32 4.1444608e+03 2.12e-02 9.93e-06 -5.7 1.38e-01 -4.8 1.00e+00 1.00e
     \rightarrow +00h 1
  33 4.1444608e+03 1.52e-01 8.57e-05 -5.7 5.25e-01 -5.3 1.00e+00 1.00e
     \rightarrow +00h 1
  34 4.1444608e+03 5.89e-03 2.06e-05 -5.7 1.27e-01 -4.9 1.00e+00 1.00e
     \hookrightarrow +00h 1
  35 4.1444608e+03 2.60e-01 1.06e-04 -5.7 1.23e+00 - 7.38e-01 1.00e
    → +00H 1
  36 4.1444608e+03 4.78e-02 3.16e-05 -5.7 3.18e-01 - 1.00e+00 1.00e
     \rightarrow +00h 1
  37 4.1444608e+03 1.18e-03 3.22e-07 -5.7 7.50e-02 - 1.00e+00 1.00e
     \rightarrow +00h 1
  38 4.1444608e+03 3.36e-05 2.96e-09 -5.7 1.62e-02 - 1.00e+00 1.00e
    \rightarrow +00h 1
  39 4.1444608e+03 3.14e-10 5.68e-13 -5.7 5.87e-05 - 1.00e+00 1.00e
     → +00h 1
       objective
                    inf_pr inf_du lg(mu) ||d|| lg(rg) alpha_du
   → alpha_pr ls
  40 4.1444605e+03 7.54e-08 1.83e-07 -7.0 2.81e-04 - 1.00e+00 1.00e
     \hookrightarrow +00h 1
Number of Iterations....: 40
                                    (scaled)
                                                             (unscaled)
Objective...... 9.2925124417578417e+01 4.1444605490239974e
   \rightarrow +03
Dual infeasibility....: 1.8347495281748061e-07 8.1829828956596351e
  \rightarrow -06
Constraint violation...: 1.3290786859965209e-08 1.3290786859965209e
```

```
\hookrightarrow -08
Complementarity..... 2.6885276874539710e-07 1.1990833486044711e
  \hookrightarrow -05
Overall NLP error....: 2.6885276874539710e-07 1.1990833486044711e
 \hookrightarrow -05
Number of objective function evaluations
                                          = 44
Number of objective gradient evaluations
                                          = 41
Number of equality constraint evaluations
                                          = 44
Number of inequality constraint evaluations
                                          = 44
Number of equality constraint Jacobian evaluations = 41
Number of inequality constraint Jacobian evaluations = 41
Number of Lagrangian Hessian evaluations = 40
Total CPU secs in IPOPT (w/o function evaluations) = 0.078
Total CPU secs in NLP function evaluations = 0.026
EXIT: Optimal Solution Found.
______
Security-Constrained Optimal Power Flow
_____
Number of contingencies
Multi-period contingencies?
                            NO
Solver
                             IPOPT
Initialization
                             MIDPOINT
Load loss allowed
                            NO
Power imbalance allowed
                             NO
Ignore line flow constraints
                            NO
Convergence status
                          CONVERGED
Objective value (base)
                             4144.46
Bus Pd Qd Vm Va mult_Pmis mult_Qmis
 \hookrightarrow Pslack
              Qslack
1 0.00 0.00 1.100 0.000 2102.91
                                                0.00
 \hookrightarrow 0.00 0.00
2
   0.00 0.00 1.095 3.928 2059.18
                                                -0.00
 \hookrightarrow 0.00
              0.00
       0.00 0.00 1.087 2.120 2065.15
                                                -0.00
           0.00
  \hookrightarrow 0.00
  0.00 0.00 1.097 -1.993 2103.17 0.08 \rightarrow 0.00
```

75.00 50.00 1.079 -3.060 2113.46

 $\hookrightarrow$  0.00

0.00

7.29

6		90.00		.087 -3.9	27 23	129.85	1.6	2	
7		0.00	0.00 1	.100 0.5	35 2	059.57	-0.0	4	
8		100.00	35.00 1	.089 -1.7	20 2	079.34	2.9	9	
9		0.00	0.00 1	.100 -0.1	35 2	065.43	-0.0	9	
	$\hookrightarrow$								
Fro	mc	То	Status	Sft	Stf	Slim	mult_S	f mult_St	
	$\hookrightarrow$								
1		4	1	73.18	72.98	380.00	-0.00	-0.00	
2		7	1	114.18	114.68	250.00	-0.00	-0.00	
3		9	1	83.58	84.61	300.00	-0.00	-0.00	
4		5	1	29.69	40.50	250.00	-0.00	-0.00	
4		6	1	44.86	46.03	250.00	-0.00	-0.00	
5		7	1	51.29	49.04	250.00	-0.00	-0.00	
6		9		48.94				-0.00	
7		8		66.61					
8		9		38.87					
	$\hookrightarrow$								
Gei		Status Qmax	Fuel	Pg	Qg	Pmin	Pmax	Qmin	
	$\hookrightarrow$								
1			UNDEFINED	72.86	6.79	10.00	350.00	-300.00	
		300.00							
2		1	UNDEFINED	114.07	-5.13	10.00	300.00	-300.00	
	$\hookrightarrow$	300.00							
3		1	UNDEFINED	80.21	-23.48	10.00	270.00	-300.00	
		300.00							
[E:	xaG(	O] Finaliz	ing scopflo	w applicat	ion.				

#### Example using HIOP solver with IPOPT subproblem solver.

```
bin/scopflow -netfile $EXAGO_DIR/datafiles/case9/case9mod.m -ctgcfile

$EXAGO_DIR/datafiles/case9/case9.cont -scopflow_Nc 4 -

$copflow_solver IPOPT -print_output -scopflow_solver HIOP -

$copflow_subproblem_solver IPOPT -scopflow_subproblem_model

$POWER_BALANCE_POLAR

[ExaGO] SCOPFLOW: Application created

[ExaGO] SCOPFLOW running with 5 subproblems (base case + 4 contingencies)

[ExaGO] SCOPFLOW: Using HIOP solver
```

```
Failed to read option file 'hiop_pridec.options'. Hiop will use default
  \hookrightarrow options.
[ExaGO] SCOPFLOW: Setup completed
total number of recourse problems
************************
This program contains Ipopt, a library for large-scale nonlinear
  → optimization.
Ipopt is released as open source code under the Eclipse Public License (
   \hookrightarrow EPL).
        For more information visit http://projects.coin-or.org/Ipopt
*************************
This is Ipopt version 3.12.10, running with linear solver ma27.
Number of nonzeros in equality constraint Jacobian ...:
                                                          114
Number of nonzeros in inequality constraint Jacobian.:
                                                          72
Number of nonzeros in Lagrangian Hessian....:
                                                           96
Total number of variables.....
                                                           2.4
                    variables with only lower bounds:
                                                           0
               variables with lower and upper bounds:
                                                           16
                    variables with only upper bounds:
                                                           0
Total number of equality constraints....:
                                                          18
Total number of inequality constraints....:
                                                           18
       inequality constraints with only lower bounds:
                                                           0
   inequality constraints with lower and upper bounds:
                                                           18
       inequality constraints with only upper bounds:
                                                            0
                    inf_pr inf_du lg(mu) ||d|| lg(rg) alpha_du
iter
       objective
  → alpha_pr ls
   0 1.0318125e+04 1.80e+00 1.00e+02 -1.0 0.00e+00 - 0.00e+00 0.00e
   1 7.7157691e+03 1.17e+00 1.03e+02 -1.0 1.08e+00
                                                      - 6.27e-01 3.50e
     \hookrightarrow -01f 1
   2 7.6608235e+03 1.15e+00 1.01e+02 -1.0 6.28e+00
                                                      - 1.20e-02 1.37e
     \rightarrow -02f 1
   3 \quad 7.4466686e+03 \quad 1.09e+00 \quad 3.06e+02 \quad -1.0 \quad 3.74e+00 \quad -4.15e-03 \quad 5.81e
     \hookrightarrow -02f 1
   4 5.4292675e+03 3.92e-01 4.83e+03 -1.0 7.34e-01 - 3.34e-03 6.40e
     \hookrightarrow -01f 1
   5 4.5792834e+03 2.24e-01 1.51e+03 -1.0 6.46e-01 2.0 8.77e-03 7.37e
     \hookrightarrow -01f 1
   6 4.2907579e+03 1.20e-02 3.57e+02 -1.0 3.36e-01 - 5.37e-01 1.00e
     → +00f 1
```

```
7 \quad 4.1690456e+03 \quad 4.40e-02 \quad 5.31e+01 \quad -1.0 \quad 3.31e-01 \quad -9.22e-01 \quad 1.00e
      \rightarrow +00f 1
   8 4.1687926e+03 4.88e-04 1.93e+00 -1.0 4.79e-02 1.5 1.00e+00 1.00e
      \hookrightarrow +00h 1
   9 4.1497176e+03 1.19e-02 9.92e+00 -2.5 1.87e-01 - 8.38e-01 1.00e
      → +00f 1
iter
       objective
                    inf_pr inf_du lg(mu) ||d|| lg(rg) alpha_du
   \hookrightarrow alpha_pr ls
  10 4.1463942e+03 1.09e-02 5.09e-01 -2.5 1.15e-01 - 8.71e-01 1.00e
     \hookrightarrow +00h 1
  11 4.1449657e+03 1.47e-03 1.79e-02 -2.5 2.75e-02 - 1.00e+00 1.00e
     \hookrightarrow +00h 1
  12 4.1445415e+03 6.63e-04 9.12e-02 -3.8 1.48e-02 - 1.00e+00 6.30e
  13 4.1444705e+03 3.43e-04 4.96e-02 -3.8 2.08e-02 - 1.00e+00 8.93e
     \hookrightarrow -01h 1
  14 4.1444809e+03 4.48e-05 1.79e-04 -3.8 6.82e-03 - 1.00e+00 1.00e
     → +00f 1
  15 4.1444611e+03 1.96e-05 4.55e-03 -5.7 4.57e-03 - 1.00e+00 9.34e
     \hookrightarrow -01h 1
  16 4.1444607e+03 6.49e-06 1.17e-05 -5.7 2.60e-03
                                                        - 1.00e+00 1.00e
     \hookrightarrow +00h 1
  17 4.1444605e+03 1.19e-06 2.07e-06 -7.0 1.11e-03 - 1.00e+00 1.00e
     \hookrightarrow +00h 1
  18 4.1444605e+03 1.58e-07 3.29e-07 -7.0 4.06e-04 - 1.00e+00 1.00e
     \hookrightarrow +00h 1
Number of Iterations....: 18
                                    (scaled)
                                                              (unscaled)
Objective..... 9.2925122354655841e+01 4.1444604570176507e
  → +03
Dual infeasibility.....: 3.2927387965389691e-07
                                                      1.4685615032563802e
   \hookrightarrow -05
Constraint violation...: 2.6639677713768961e-08
                                                      2.6639677713768961e
   → -08
Complementarity.....: 4.7840038622596930e-07 2.1336657225678232e
Overall NLP error....: 4.7840038622596930e-07 2.1336657225678232e
  \hookrightarrow -05
Number of objective function evaluations
                                                     = 19
Number of objective gradient evaluations
                                                     = 19
Number of equality constraint evaluations
                                                     = 19
Number of inequality constraint evaluations
                                                     = 19
Number of equality constraint Jacobian evaluations = 19
```

```
Number of inequality constraint Jacobian evaluations = 19
Number of Lagrangian Hessian evaluations
                                                      = 18
Total CPU secs in IPOPT (w/o function evaluations) =
                                                             0.027
Total CPU secs in NLP function evaluations
                                                             0.002
EXIT: Optimal Solution Found.
This is Ipopt version 3.12.10, running with linear solver ma27.
Number of nonzeros in equality constraint Jacobian...:
                                                             118
Number of nonzeros in inequality constraint Jacobian.:
                                                              64
Number of nonzeros in Lagrangian Hessian....:
                                                             141
Total number of variables.....
                                                              30
                     variables with only lower bounds:
                                                              0
                variables with lower and upper bounds:
                                                              22
                     variables with only upper bounds:
                                                               0
Total number of equality constraints....:
                                                              24
Total number of inequality constraints....:
                                                              16
        inequality constraints with only lower bounds:
                                                              0
   inequality constraints with lower and upper bounds:
                                                              16
        inequality constraints with only upper bounds:
                                                               0
iter
        objective
                     inf_pr inf_du lg(mu) ||d|| lg(rg) alpha_du
   \hookrightarrow alpha_pr ls
                                                         - 0.00e+00 0.00e
   0 0.0000000e+00 1.80e+00 0.00e+00 -1.0 0.00e+00
      \hookrightarrow +00
   1 0.0000000e+00 1.41e+00 3.55e+01 -1.0 9.96e-01
                                                         - 6.48e-01 2.16e
      \hookrightarrow -01h 1
   0.00000000e+001.36e+005.74e+01-1.03.86e+00
                                                         - 3.79e-03 3.37e
      \hookrightarrow -02f 1
   3 0.0000000e+00 1.12e+00 3.23e+02 -1.0 1.01e+00
                                                         - 1.98e-02 1.76e
      \hookrightarrow -01f 1
   4 0.0000000e+00 4.03e-01 7.31e+02 -1.0 7.32e-01
                                                        - 2.71e-02 9.03e
      \hookrightarrow -01f 1
   5 0.0000000e+00 8.41e-02 1.58e+02 -1.0 6.95e-01
                                                         - 4.70e-01 8.52e
      \hookrightarrow -01h 1
   6 0.0000000e+00 4.93e-03 3.36e+01 -1.0 1.85e-01
                                                       - 1.00e+00 1.00e
     0.0000000e+00 2.20e-02 2.50e+01 -1.0 6.50e-01
                                                         - 4.45e-01 2.50e
      \hookrightarrow -01h 3
   8 0.0000000e+00 1.07e-01 5.13e+00 -1.0 3.57e-01 0.0 1.00e+00 1.00e
      \hookrightarrow +00h 1
   9 0.0000000e+00 1.07e-01 4.86e+00 -1.7 9.45e-01 - 3.30e-01 1.98e
      \rightarrow -01h 2
       objective
                     inf_pr inf_du lg(mu) ||d|| lg(rg) alpha_du
iter
   \hookrightarrow alpha pr ls
  10 0.0000000e+00 9.21e-03 3.47e+00 -1.7 1.17e-01 -0.5 8.84e-01 1.00e
```

```
\hookrightarrow +00h 1
  11 0.0000000e+00 2.70e-02 9.88e-01 -1.7 1.67e-01 - 1.00e+00 1.00e
    \rightarrow +00h
  12 0.0000000e+00 8.46e-03 1.62e-01 -1.7 1.58e-01 -1.0 1.00e+00 1.00e
     \rightarrow +00h 1
  13 0.0000000e+00 7.11e-04 1.09e-01 -2.5 4.58e-02 -1.4 1.00e+00 1.00e
  14 0.0000000e+00 1.11e-01 9.70e-02 -2.5 1.43e+00 - 1.00e+00 1.00e
     \hookrightarrow +00H 1
  15 0.0000000e+00 2.40e-02 5.99e-02 -2.5 2.27e-01 -1.9 1.00e+00 1.00e
     \hookrightarrow +00h 1
  16 0.0000000e+00 3.45e-02 2.41e-01 -2.5 3.69e-01 - 5.82e-01 1.00e
     \rightarrow +00h 1
  17 0.0000000e+00 1.85e-02 1.46e-01 -2.5 3.58e-01 - 1.00e+00 1.00e
    \hookrightarrow +00h 1
  18 0.0000000e+00 8.37e-03 2.78e-02 -2.5 9.85e-02 - 1.00e+00 1.00e
     \hookrightarrow +00h 1
  19 0.0000000e+00 6.33e-06 5.45e-04 -3.8 6.81e-03 - 1.00e+00 1.00e
    \rightarrow +00h 1
     objective inf_pr inf_du lg(mu) ||d|| lg(rg) alpha_du
iter
  → alpha_pr ls
  20 0.0000000e+00 1.42e-07 2.95e-06 -5.7 1.02e-03 - 1.00e+00 1.00e
    \rightarrow +00h 1
  21 0.0000000e+00 1.44e-06 1.25e-07 -7.0 3.43e-03 - 1.00e+00 1.00e
    \hookrightarrow +00h 1
Number of Iterations....: 21
                                   (scaled)
                                                            (unscaled)
\hookrightarrow +00
Dual infeasibility....: 1.2466133995485293e-07
                                                     1.2466133995485293e
   \hookrightarrow -07
Constraint violation...: 1.8383034489088956e-07 1.8383034489088956e
   \hookrightarrow -07
Complementarity..... 1.0156847334169061e-07
                                                     1.0156847334169061e
   \hookrightarrow -07
Overall NLP error....: 1.8383034489088956e-07 1.8383034489088956e
   \hookrightarrow -07
Number of objective function evaluations
                                                    = 28
Number of objective gradient evaluations
                                                    = 22
Number of equality constraint evaluations
Number of inequality constraint evaluations
Number of equality constraint Jacobian evaluations = 22
Number of inequality constraint Jacobian evaluations = 22
```

Number of Lagrangian Hessian evaluations

Total CPU secs in IPOPT (w/o function evaluations) = 0.032

0.003

EXIT: Optimal Solution Found.

. . . . . .

\_\_\_\_\_

#### Security-Constrained Optimal Power Flow

\_\_\_\_\_

Number of contingencies Multi-period contingencies? NO Solver HIOP Initialization MIDPOINT Load loss allowed NO Power imbalance allowed NO Ignore line flow constraints NO

Convergence status CONVERGED Objective value (base) 4144.46

1				Va	mult_Pmis	mult_Qmis
	→ Pslack	Qsl 	ack 			
1	0.00 → 0.00		1.100	0.000	2102.91	0.00
2		0.00	1.095	3.928	2059.18	-0.00
3	0.00 → 0.00		1.087	2.120	2065.15	-0.00
4	0.00 → 0.00		1.097	-1.993	2103.16	0.08
5	75.00 → 0.00		1.079	-3.060	2113.45	7.29
6	90.00 → 0.00		1.087	-3.927	2129.85	1.62
7	0.00 → 0.00		1.100	0.535	2059.57	-0.04
8	100.00 → 0.00		1.089	-1.720	2079.34	2.99
9		0.00	1.100	-0.135	2065.43	-0.09

$\hookrightarrow$								
From	То	Status	Sft	Stf	Slim	mult_S:	f mult_St	
1	4	1	73.18	72.98	380.00	-0.00	-0.00	
2	7	1	114.18	114.68	250.00	-0.00	-0.00	
3	9	1	83.57	84.60	300.00	-0.00	-0.00	
4	5	1	29.68	40.50	250.00	-0.00	-0.00	
4	6	1	44.86	46.03	250.00	-0.00	-0.00	
5	7	1	51.29	49.04	250.00	-0.00	-0.00	
6	9	1	48.94	51.43	150.00	-0.00	-0.00	
7	8	1	66.61	68.11	250.00	-0.00	-0.00	
8	9	1	38.86	34.15	150.00	-0.00	-0.00	
$\hookrightarrow$								
Gen	Status	Fuel	Pa	0a	Pmin	Pmax	Omin	
	Qmax		3	~ 3			~	
$\hookrightarrow$								
		UNDEFINED	72.86	6.79	10.00	350.00 -	-300.00	
$\hookrightarrow$	300.00							
2	1	UNDEFINED	114.07	-5.13	10.00	300.00	-300.00	
	300.00							
3	1	UNDEFINED	80.21	-23.47	10.00	270.00	-300.00	
$\hookrightarrow$	300.00							
[FvaC(	Ol Finaliz	ing scopflow	applicat	ion.				

## Chapter 6

# Stochastic optimal power flow (SOPFLOW)

SOPFLOW solves a stochastic security-constrained multi-period optimal power flow problem. The problem is set up as a two-stage optimization problem where the first-stage (base-case) represents the normal operation of the grid (or the most likely forecast) and the second-stage comprises  $N_s$  scenarios of forecast deviation. Each scenario can have multiple contingencies and each contingency can be multi-period.

#### 6.1 Formulation

An illustration of SOPFLOW is shown in Fig. 6.1 for a case with two scenarios  $s_0$  and  $s_1$  with three contingencies each, and each scenario/contingency with two time-periods. We assume that any contingency is incident at the first time-step, i.e., at  $t_0$ .

The full formulation for the stochastic security-constrained multi-period optimal power flow is given in (6.1) – (6.7). In this formulation, the objective is to reduce the expected cost, where  $f(x_{s,c,t})$  is the cost for scenario s with contingency c at time t.  $\pi_s$  is the probability of scenario s.

$$\min \sum_{s=0}^{N_s-1} \pi_s \sum_{c=0}^{N_c-1} \sum_{t=0}^{N_t-1} f(x_{s,c,t})$$
(6.1)

s.t.

$$g(x_{s,c,t}) = 0,$$
  $s \in [1, N_s - 1], c \in [0, N_c - 1], t \in [0, N_t - 1]$  (6.2)

$$h(x_{s,c,t}) \le 0,$$
  $s \in [1, N_s - 1], c \in [0, N_c - 1], t \in [0, N_t - 1]$  (6.3)

$$x^{-} \le x_{s,c,t} \le x^{+},$$
  $s \in [1, N_s - 1], c \in [0, N_c - 1], t \in [0, N_t - 1]$  (6.4)

$$-\Delta x_t \le x_{s,c,t} - x_{s,c,t-\Delta t} \le \Delta x_t, \qquad s \in [1, N_s - 1], c \in [0, N_c - 1], t \in [1, N_t - 1]$$
(6.5)

$$-\Delta x_c \le x_{s,c,0} - x_{s,0,0} \le \Delta x_c, \qquad s \in [1, N_s - 1], c \in [1, N_c - 1]$$
(6.6)

$$-\Delta x_s \le x_{s,0,0} - x_{0,0,0} \le \Delta x_s, \qquad s \in [1, N_s - 1] \tag{6.7}$$

The modeling details used for an optimial power flow problem are also used for a SOPFLOW problem, i.e., each of the circles shown in Fig. 6.1 has the modeling details of an optimal power flow problem (OPFLOW). Incorporating the probabilities  $\pi_s$  for each scenario is not implemented yet which leads to each scenario having an equal probability.

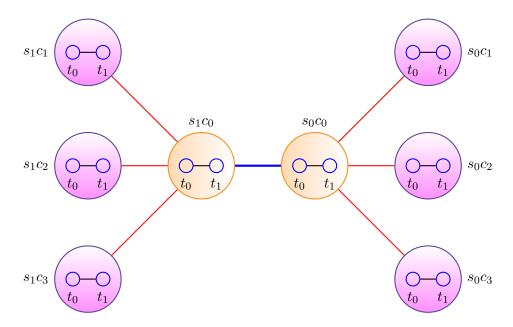


Figure 6.1: Stochastic multi-period contingency constrained structure with two scenarios  $s_0$  and  $s_1$ . Each scenario has three contingencies  $c_1,c_2,$  and  $c_3$ .  $s_0c_0$  and  $s_1c_0$  denote the base-cases for the two scenarios. Each scenario and contingency has two time-periods  $t_0$ , and  $t_2$ ,  $t_2$ . The red line denotes the coupling between the contingencies and their respective base-case scenarios. The blue line denotes the coupling between the scenarios

Depending on the options selected, SOPFLOW can be used to solve

- Single-period stochastic optimal power flow : No contingencies or time-periods
- Single-period contingency-constrained stochastic optimal power flow: No time-periods
- Multi-period security-constrained stochastic optimal power flow: Full formulation

Currently, SOPFLOW uses wind power generation as the stochastic variables and each scenario is a realization of the power output from wind generators. A zero fuel cost is used for wind power generation to ensure wind generation would be the dispatched to the given target level (upper limit).

For the contingecy-constrained stochastic optimal power flow, SOPFLOW flattens out the contingencies and scenarios to a two-level formulation. In this formulation, all the scenarios (and their contingencies) are coupled to a base scenario problem.

For contingencies, SOPFLOW supports generation and/or transmission outages. A contingency can have multiple outages, but, it should not cause any islanding. The coupling between the no-contingency and the contingency case for each scenario is also the difference in real power output  $(p_{jsct}^g - p_{js0t}^g, j \in J^{\text{gen}})$  that must be within the 30 minute generator ramp rate. Refer to 5 for details on the contingency modeling.

For multi time-period, we use ramping constraints on the generator real power output between successive time steps.

SOPFLOW can be run in two modes: preventive and corrective. In the preventive mode, generator real power output is fixed to the base-case values for generators at PV bus(es). In this mode, the generators at the reference bus provide/absorb any deficit/surplus power. The corrective mode allows deviation of the PV and PQ generator real power from the base-case dispatch constrained by its 30-min.

ramp rate capability. Note that the preventive/corrective mode is only applied at the first step  $t_0$ . In the successive time-steps, the generator dispatch is dictated by the previous step dispatch and the ramp limits.

#### 6.2 Solvers

SOPFLOW supports solving the optimization problem via Ipopt [7], HiOp [6, 5], or EMPAR. Ipopt [7]can solve SOPFLOW on single rank only. HiOp [6, 5] supports solving the problem in parallel using a primal-decomposition algorithm. With HIOP, one can solve the subproblem either on the CPU or GPU by selecting the appropriate subproblem model and solver (see options table below). However, note that ExaGO needs to be built with Ipopt [7]even when using HiOp [6, 5]solver. The EMPAR solver does not solve the stochastic ACOPF problem, but it only solves the base-case and the stochastic scenarios independently with OPFLOW. It distributes the scenarios and contingencies to different processes when executed in parallel. Table 6.1 lists the compatibility of the different solvers for different variations of SOPFLOW.

Solver	Stochastic scenarios	Include contingencies	Include multi-period								
IPOPT	Y	Y	Y								
HIOP	Y	Y	N								
EMPAR	Y	Y	Y								

Table 6.1: SOPFLOW solver compatibility

#### 6.3 Input and Output

The following files are needed for executing SOPFLOW.

- **Network file:** The network file describing the network details. Only MATPOWER format files are currently supported.
- Scenario file: SOPFLOW only supports reading wind generation scenarios in a CSV format. An example of this format for the 9-bus case is here.
- Contingency file: Contingencies can be specified via PTI format file as described in chapter 5. The option -sopflow\_enable\_multicontingency should be set for multi-contingency problems.
- Load data: One file for load real power and one for reactive power. The files need to be in CSV format. An example of the format for the 9-bus case is here.

The SOPFLOW output is saved to a directory named sopflowout. This directory contains  $N_s$  subdirectories to save the solution for each scenario. Each of these subdirectories contain  $N_c$  subdirectories, one for each contingency. Each contingency subdirectory has  $N_t$  MATPOWER format files to store the output for each time-period for the given contingency and scenario. The subdirectories have the directory name format scen\_x where x is the scenario number, cont\_y where y is the contingency number, and the output files have the file name format t\_z where z is the time-step number.

#### 6.4 Usage

```
./sopflow -netfile <netfilename> -windgen <wind_scenario_filename> \
[-sopflow_enable_multicontingency 1] <sopflowoptions>
```

#### 6.5 Options

Table 6.2: SOPFLOW options

Option	Meaning	Values (Default value)	Compatibility
-netfile	Network file name	string 4096 characters	
		$(case9mod\_gen3\_wind.m)$	
-windgen	Scenario file name	string 4096 characters	
		(case9/10scenarios_9bus.csv)	
-ctgcfile	Contingency file name	string (case9.cont)	
-save_output	Save output to direc-	0 or 1 (0)	Format determined by
	tory		OPFLOW option.
$-sopflow\_output\_directory$	Output directory path	"sopflowout"	
-sopflow_mode	Operation mode: Pre-	0 or 1 (0)	
	ventive or corrective		
-sopflow_model	Set model for	GENRAMP, GENRAMPC	
	SOPFLOW	(GENRAMP)	
-sopflow_solver	Set solver for	IPOPT, HIOP, or EMPAR	
	SOPFLOW		
$-sopflow\_subproblem\_solver$	Set solver for subprob-	IPOPT or HIOP (IPOPT)	Only when using
	lem		HIOP solver for
			SOPFLOW
$-sopflow\_subproblem\_model$	Set model for subprob-	See OPFLOW chapter	Only when using
	lem		HIOP solver for
			SOPFLOW
$-sopflow\_enable\_multicontingency$	Multi-contingency	0 or 1 (0)	
	SOPFLOW		
-sopflow_flatten_contingencies	Flatten contingencies	0 or 1 (1)	
	for SOPFLOW		
$-sopflow_Ns$	Number of scenarios	int (Default 0. Use -1 to select all	
		scenarios from the scenario file)	
$-sopflow_Nc$	Number of contingen-	int (0. Passing -1 results in all	
	cies	contingencies in the file used)	

#### 6.6 Examples

Some SOPFLOW example runs are provided with some sample output. Options are the default options given in Tables 3.4, ??, 5.1 and 6.2 unless otherwise specified. Sample output is generated by running examples in the installation directory.

Example using the Ipopt [7] solver:

```
bin/sopflow -netfile $EXAGO_DIR/datafiles/case9/case9mod.m -windgen 

→ $EXAGO_DIR/datafiles/case9/10_scenarios_9bus.csv -sopflow_Ns 4 -
```

```
→ sopflow_enable_multicontingency 0 -sopflow_solver IPOPT -
   → print_output
[ExaGO] SOPFLOW: Application created
Rank[0], s = 0, scen_num = 0
Rank[0], s = 1, scen_num = 1
Rank[0], s = 2, scen_num = 2
Rank[0], s = 3, scen_num = 3
[ExaGO] SOPFLOW: Using IPOPT solver
[ExaGO] SOPFLOW: Setup completed
*************************
  \hookrightarrow
This program contains Ipopt, a library for large-scale nonlinear
  \hookrightarrow optimization.
Ipopt is released as open source code under the Eclipse Public License (
   \hookrightarrow EPL).
        For more information visit http://projects.coin-or.org/Ipopt
************************
This is Ipopt version 3.12.10, running with linear solver ma27.
Number of nonzeros in equality constraint Jacobian...:
                                                          513
Number of nonzeros in inequality constraint Jacobian .:
                                                          288
Number of nonzeros in Lagrangian Hessian....:
                                                          564
Total number of variables....:
                                                          120
                    variables with only lower bounds:
                                                           0
               variables with lower and upper bounds:
                                                          88
                    variables with only upper bounds:
                                                           0
Total number of equality constraints....:
                                                           96
Total number of inequality constraints....:
                                                          72
       inequality constraints with only lower bounds:
                                                           0
   inequality constraints with lower and upper bounds:
                                                           72
       inequality constraints with only upper bounds:
                                                           0
iter
                    inf_pr inf_du lg(mu) ||d|| lg(rg) alpha_du
       objective
   \hookrightarrow alpha_pr ls
   0 3.2548812e+04 1.80e+00 1.00e+02 -1.0 0.00e+00
                                                     - 0.00e+00 0.00e
     \hookrightarrow +00
   1 2.6023632e+04 1.18e+00 1.21e+02 -1.0 1.07e+00
                                                      - 5.64e-02 3.40e
     \rightarrow -01f 1
   2 2.0106844e+04 4.83e-01 2.57e+03 -1.0 6.99e-01
                                                     2.0 1.02e-02 6.07e
     \hookrightarrow -01f 1
   3 2.0011119e+04 4.70e-01 2.50e+03 -1.0 5.84e-01
                                                    2.4 1.32e-01 2.67e
     \hookrightarrow -02f 1
   4 1.9372689e+04 3.88e-01 1.99e+03 -1.0 7.94e-01 1.9 2.37e-01 1.97e
```

```
\hookrightarrow -01f 1
 18 1.6587232e+04 4.15e-05 1.21e+03 -5.7 5.76e-03 - 1.00e+00 9.18e
    → -01h 1
 19 1.6587229e+04 8.62e-06 1.55e-05 -5.7 3.00e-03 - 1.00e+00 1.00e
    \hookrightarrow +00h 1
iter
      objective
                  inf_pr inf_du lg(mu) ||d|| lg(rg) alpha_du
  → alpha_pr ls
  20 1.6587228e+04 1.50e-06 2.56e-06 -7.0 1.25e-03 - 1.00e+00 1.00e
  21 1.6587228e+04 2.18e-07 4.53e-07 -7.0 4.77e-04 - 1.00e+00 1.00e
    \hookrightarrow +00h 1
Number of Iterations....: 21
                                 (scaled)
                                                        (unscaled)
Objective...... 3.7191094895317639e+02 1.6587228323311669e
  \hookrightarrow +04
Dual infeasibility.....: 4.5286779256921672e-07
                                                 2.0197903548587065e
  \hookrightarrow -05
Constraint violation...: 3.6703967934426096e-08
                                                 3.6703967934426096e
  \hookrightarrow -08
Complementarity.....: 6.2406713469536533e-07 2.7833394207413294e
Overall NLP error....: 6.2406713469536533e-07 2.78333394207413294e
  \hookrightarrow -05
Number of objective function evaluations
                                                 = 22
Number of objective gradient evaluations
                                                = 22
Number of equality constraint evaluations
Number of inequality constraint evaluations
                                                = 22
Number of equality constraint Jacobian evaluations = 22
Number of inequality constraint Jacobian evaluations = 22
Number of Lagrangian Hessian evaluations
                                                = 21
Total CPU secs in IPOPT (w/o function evaluations) =
                                                        0.043
Total CPU secs in NLP function evaluations
                                                        0.013
EXIT: Optimal Solution Found.
_____
Stochastic Optimal Power Flow
_____
Number of scenarios
Multi-contingency scenarios?
                                 NO
Solver
                                 IPOPT
Initialization
                                 MIDPOINT
Load loss allowed
                                 NO
```

Power imbalance allowed NO Ignore line flow constraints NO

Convergence status Objective value (base)				ONVERGED 149.15				
Bus	Pd Pslack	Qd Qsl	Vm ack	Va	mu	lt_Pmis	mult_Qı	mis
1	0.00	0.00	1.100	0.00	0 2	152.67	0.00	
	<pre>     0.00     0.00     0.00 </pre>		1.095	3.93	5 2	108.81	-0.00	
3	0.00	0.00	1.087	1.63	7 2	117.68	-0.00	
4	0.00	0.00		-2.05	4 2	152.95	0.18	
5	75.00 0.00 90.00	50.00	1.079					
	90.00		1.087	-4.08	4 2	181.34	1.69	
	0.00			0.45	5 2	109.21	-0.04	
8	100.00	35.00	1.089	-1.90	7 2	130.61	3.09	
	0.00		1.100	-0.47	1 2	117.94	-0.09	
 From		Stat	115	 Sft		Slim	mult Sf	mult St
<u>د</u> ; 1	4	1		75.41	75.22	380.00	-0.00	-0.00
2 3	7 9	1 1	1.	17.10 78.55	117.61 79.51	250.00 300.00	-0.00 -0.00	-0.00 -0.00
4	5	1		29.85	40.63	250.00	-0.00	-0.00
4	6	1	4	46.99	47.91	250.00	-0.00	-0.00
5	7	1		51.14	48.90	250.00	-0.00	-0.00
6	9	1		47.20	49.41	150.00	-0.00	-0.00
7 8	8 9	1		69.69 36.50	70.99	250.00 150.00	-0.00 -0.00	-0.00 -0.00
Gen	Status	Fuel	. Po	<b>a</b>	Qg	Pmin	Pmax	Qmin

```
\hookrightarrow Qmax
                                          6.61
1
                 UNDEFINED
                               75.12
                                                   10.00
                                                            350.00
                                                                     -300.00
   → 300.00
                              116.99
                                         -5.04
                                                   10.00
                                                            300.00
                                                                     -300.00
                 UNDEFINED
   → 300.00
                                        -23.36
3
                 UNDEFINED
                               75.00
                                                   10.00
                                                             85.00
                                                                     -300.00
            1
   → 300.00
[ExaGO] Finalizing sopflow application.
```

#### Example using the *IPOPT* solver with multicontingency enabled:

```
bin/sopflow -netfile $EXAGO_DIR/datafiles/case9/case9mod.m -windgen
   → $EXAGO DIR/datafiles/case9/10 scenarios 9bus.csv -sopflow Ns 4 -
   → sopflow_enable_multicontingency 1 -sopflow_solver IPOPT -
   → print_output -sopflow_Nc 4 -ctgcfile $EXAGO_DIR/datafiles/case9/
   → case9.cont -sopflow_Nc 4
[ExaGO] SOPFLOW: Application created
Rank[0], s = 0, scen_num = 0, cont_num = 0
Rank[0], s = 1, scen_num = 0, cont_num = 1
Rank[0], s = 2, scen_num = 0, cont_num = 2
Rank[0], s = 3, scen_num = 0, cont_num = 3
Rank[0], s = 4, scen_num = 0, cont_num = 4
Rank[0], s = 5, scen_num = 1, cont_num = 0
Rank[0], s = 6, scen_num = 1, cont_num = 1
Rank[0], s = 7, scen_num = 1, cont_num = 2
Rank[0], s = 8, scen_num = 1, cont_num = 3
Rank[0], s = 9, scen_num = 1, cont_num = 4
Rank[0], s = 10, scen_num = 2, cont_num = 0
Rank[0], s = 11, scen_num = 2, cont_num = 1
Rank[0], s = 12, scen_num = 2, cont_num = 2
Rank[0], s = 13, scen_num = 2, cont_num = 3
Rank[0], s = 14, scen_num = 2, cont_num = 4
Rank[0], s = 15, scen_num = 3, cont_num = 0
Rank[0], s = 16, scen_num = 3, cont_num = 1
Rank[0], s = 17, scen_num = 3, cont_num = 2
Rank[0], s = 18, scen_num = 3, cont_num = 3
Rank[0], s = 19, scen_num = 3, cont_num = 4
[ExaGO] SOPFLOW: Using IPOPT solver
[ExaGO] SOPFLOW: Setup completed
***********************
   \hookrightarrow
This program contains Ipopt, a library for large-scale nonlinear
   \hookrightarrow optimization.
 Ipopt is released as open source code under the Eclipse Public License (
   \hookrightarrow EPL).
```

```
For more information visit http://projects.coin-or.org/Ipopt
************************
This is Ipopt version 3.12.10, running with linear solver ma27.
Number of nonzeros in equality constraint Jacobian...:
                                                         2449
Number of nonzeros in inequality constraint Jacobian.:
                                                         1312
Number of nonzeros in Lagrangian Hessian....:
                                                         2820
Total number of variables....:
                                                          600
                    variables with only lower bounds:
                                                           0
               variables with lower and upper bounds:
                                                          440
                    variables with only upper bounds:
                                                            0
Total number of equality constraints....:
                                                          480
Total number of inequality constraints....:
                                                          328
        inequality constraints with only lower bounds:
                                                            0
   inequality constraints with lower and upper bounds:
                                                          328
       inequality constraints with only upper bounds:
                                                            0
       objective
iter
                    inf_pr inf_du lg(mu) ||d|| lg(rg) alpha_du
   → alpha_pr ls
   0 1.6274406e+05 1.80e+00 1.00e+02 -1.0 0.00e+00 - 0.00e+00 0.00e
   1 1.4901965e+05 1.56e+00 8.69e+01 -1.0 1.07e+00
                                                     - 1.73e-01 1.31e
     \hookrightarrow -01f 1
   2 1.4480394e+05 1.49e+00 1.32e+02 -1.0 1.80e+00
                                                      - 1.34e-03 4.72e
     \hookrightarrow -02f 1
   3 1.3529809e+05 1.31e+00 1.15e+02 -1.0 1.22e+00
                                                      - 4.90e-02 1.18e
     \hookrightarrow -01f 1
   4 1.1656024e+05 9.25e-01 9.13e+01 -1.0 8.50e-01
                                                      - 9.55e-02 2.99e
     → -01f 1
   5 1.0783333e+05 7.18e-01 9.48e+01 -1.7 7.97e-01
                                                     - 2.05e-01 2.24e
     \hookrightarrow -01f 1
   6 9.9954510e+04 5.10e-01 9.64e+01 -1.7 7.94e-01
                                                      - 3.55e-01 2.89e
     \hookrightarrow -01f 1
   7 9.3292251e+04 3.16e-01 9.31e+01 -1.7 7.35e-01 - 3.05e-01 3.78e
     \hookrightarrow -01f 1
   8 9.2973069e+04 3.05e-01 9.00e+01 -1.7 4.70e-01
                                                     2.0 3.84e-02 3.33e
     \rightarrow -02f 1
  30 8.3618318e+04 1.07e-05 1.74e+03 -5.7 3.88e-03
                                                     - 1.00e+00 8.83e
    \hookrightarrow -01f 1
  31 8.3618280e+04 5.27e-06 2.36e-04 -5.7 2.35e-03 - 1.00e+00 1.00e
     \hookrightarrow +00h 1
  32 8.3618280e+04 6.40e-07 1.28e-06 -5.7 8.17e-04 - 1.00e+00 1.00e
    → +00h 1
```

```
33 8.3618274e+04 1.95e-07 1.70e-06 -7.0 4.52e-04 - 1.00e+00 1.00e
    \hookrightarrow +00h 1
 34 8.3618274e+04 8.21e-09 1.71e-08 -7.0 9.25e-05 - 1.00e+00 1.00e
    \hookrightarrow +00h 1
Number of Iterations....: 34
                                                    (unscaled)
                              (scaled)
Objective...... 1.8748492036555979e+03 8.3618274483039670e
  \hookrightarrow +04
Dual infeasibility....: 1.7101740512915904e-08
                                              7.6273762687604936e
  \hookrightarrow -07
Constraint violation...: 1.3811524007811826e-09 1.3811524007811826e
  \hookrightarrow -09
Complementarity.....: 1.1101524615042143e-07
                                              4.9512799783087964e
Overall NLP error....: 1.1101524615042143e-07 4.9512799783087964e
  \hookrightarrow -06
Number of objective function evaluations
                                             = 35
Number of objective gradient evaluations
                                             = 35
Number of equality constraint evaluations
                                             = 35
Number of inequality constraint evaluations
                                             = 35
Number of equality constraint Jacobian evaluations = 35
Number of inequality constraint Jacobian evaluations = 35
Number of Lagrangian Hessian evaluations
                                             = 34
Total CPU secs in IPOPT (w/o function evaluations) = 0.135
Total CPU secs in NLP function evaluations
EXIT: Optimal Solution Found.
_____
Stochastic Optimal Power Flow
_____
Number of scenarios
                              4
Multi-contingency scenarios?
                              YES
Contingencies per scenario
                              4
Solver
                               IPOPT
Initialization
                              MIDPOINT
Load loss allowed
                              NO
Power imbalance allowed
                              NO
Ignore line flow constraints
                              NO
Convergence status
                              CONVERGED
Objective value (base)
                              4149.15
_____
```

$\hookrightarrow$	Pslack	Qd Qslack	<u>.</u>	mu	lt_Pmis	mult_	Qmis
1		0.00 1.		) 2	 152 <b>.</b> 67	0.0	0
2	0.00	0.00 1.	095 3.935	5 2	108.81	-0.0	0
3	0.00	0.00 1.	087 1.637	2	117.68	-0.0	0
4	0.00	0.00 1.	097 -2.054	. 2	152.95	0.1	8
5	75.00	50.00 1.	079 -3.127	2	163.77	7.5	3
6	90.00	30.00 1.	087 -4.084	2	181.34	1.6	9
7		0.00 1.	100 0.455	5 2	109.22	-0.0	4
8	100.00	35.00 1.	089 -1.907	2	130.61	3.0	9
9	0.00	0.00 1.	100 -0.471	. 2	117.94	-0.0	9
$\hookrightarrow$	0.00	0.00					
		Status	S f+	C+ f	Slim	m111+ S	f mult St
		1					-0.00
2 3	7 9		117.10 78.55				
4 4	5 6		29.85 46.99				
5 6	7	1	51.14 47.20	48.90	250.00	-0.00	-0.00
7 8	8 9		69.69	70.99	250.00		-0.00
				JI. 01			
		Fuel	Pg	Qg	Pmin	Pmax	Qmin
		IINDEETNED	75 10	6 61	10 00	350 00	_300 00
	300.00	UNDEFINED	13.12	0.01	10.00	330.00	-300.00

3 1 UNDEFINED 75.00 -23.36 10.00 85.00 -300.00

→ 300.00

[ExaGO] Finalizing sopflow application.

### Chapter 7

## Python Bindings

The ExaGO Python bindings are a wrapper around the C++ API to provide an interface to ExaGO in Python. This interface aims to provide equivalent functionality between the ExaGO C++ API and the Python API.

The wrapper uses an object-oriented API slightly different from the C++ API. The C++ API uses the application type in uppercase as the prefix for its methods, where they are native methods in Python. ExaGO Python instances must be destroyed, using del, before calling exago.finalize(), like calling \*Destroy() with the C++ API. Failure to do so will cause segmentation faults or other memory errors. In section 7.3, are tables that detail the mappings between functions and objects in the Python vs C++.

#### 7.1 Code Comparison

Below is a comparison of what solving an OPF looks like through the C++ and Python APIs. C++:

```
#include <opflow.h>
#include <exago_config.h>

static char help[] = "User example calling OPFLOW.\n";
static char appname[] = "opflow";

int main(int argc, char** argv) {

    /* Initialize ExaGO application */
    PetscErrorCode ierr;
    OPFLOW opflow;
    MPI.Comm comm = MPI.COMM_WORLD;
    ierr = ExaGOInitialize(comm, &argc, &argv, appname, help);

    /* Create OPFLOW object */
    ierr = OPFLOWCreate(comm, &opflow);
    ExaGOCheckError(ierr);

    /* Read network data */
```

```
ierr = OPFLOWReadMatPowerData(opflow, "datafiles/case9/case9mod.m");
ExaGOCheckError(ierr);

/* Solve */
ierr = OPFLOWSolve(opflow);
ExaGOCheckError(ierr);

/* Print solution */
ierr = OPFLOWPrintSolution(opflow);
ExaGOCheckError(ierr);

/* Destroy OPFLOW object */
ierr = OPFLOWDestroy(&opflow);
ExaGOCheckError(ierr);

/* Clean up resources */
ExaGOFinalize();
return 0;
}
```

#### Python:

```
import exago
exago.initialize("opflow")
opf = exago.OPFLOW()
opf.read_mat_power_data('datafiles/case9/case9mod.m')
opf.solve()
opf.print_solution()
del opf
exago.finalize()
```

### 7.2 Building with MPI

ExaGO depends on mpi4py when running through the Python interface. When running ExaGO, you may need to disable threading through mpi4py before importing exago:

```
import mpi4py.rc
mpi4py.rc.threads = False
from mpi4py import MPI
import exago
comm = MPI.COMM_WORLD
exago.initialize("app", comm)
# ...
exago.finalize()
```

Additionally linting tools may re-order your imports, and so you may need to add appropriate comments (# noqa) in order to avoid this:

```
import mpi4py.rc
mpi4py.rc.threads = False
from mpi4py import MPI # noqa
import exago # noqa
```

#### 7.3 Bindings Tables

#### 7.3.1 ExaGO

Table 7.1: ExaGO Python Bindings

C++ API	Python API	Notes
ExaGOInitialize	exago.initialize	
ExaGOFinalize	exago.finalize	
	exago_prefix	Returns the path to the installation directory of ExaGO (for finding mat power data files, etc)
OutputFormat enum	exago.OutputFormat enum	Output format type for functions like save_solution_ Possible values for this enum can be found in 7.4

#### 7.3.2 PFLOW

The functions in the following table could be called by a pflow object (i.e. pflow = exago.PFLOW(); pflow.solve();).

Table 7.2: PFLOW Python Bindings

C++ API	Python API	Notes
PFLOW	exago.PFLOW class	
PFLOWReadMatPowerData	read_mat_power_data	
PFLOWSolve	solve	

#### **7.3.3 OPFLOW**

The functions in the following table could be called by a opflow object (i.e. opflow = exago.OPFLOW(); opflow.solve();).

Table 7.3: OPFLOW Python Bindings

C++ API	Python API	Notes
OPFLOW	exago.OPFLOW class	
OPFLOWObjectiveType enum	exago.OPFLOWObjectiveType	More details and possible values for
	enum	this enum can be found in 7.4
OPFLOWInitializationType enum	exago.OPFLOWInitializationType	More details and possible values for
	enum	this enum can be found in 7.4
OPFLOWGenBusVoltageType enum	exago.OPFLOWGenBusVoltageType	More details and possible values for
	enum	this enum can be found in 7.4
OPFLOWSetObjectiveType	set_objective_type	
OPFLOWSetInitializationType	set_initialization_type	
OPFLOWSetGenBusVoltageType	set_gen_bus_voltage_type	

Table 7.3: OPFLOW Python Bindings (cont.)

C++ API	Python API	Notes
OPFLOWSetModel	set_model	options are "PBPOLRAJAHIOP", "POWER_BALANCE_HIOP", and "POWER_BALANCE_POLAR"
OPFLOWSetSolver	set_solver	options are "IPOPT", "HIOP", and "HIOPSPARSE"
OPFLOWHasGenSetPoint	set_has_gen_set_point	
OPFLOWSetHIOPComputeMode	set_hiop_compute_mode	options are "CPU" or "GPU"
OPFLOWSetHIOPMemSpace	set_hiop_mem_space	options are "DEFAULT", "HOST", "UM", and "DEVICE"
OPFLOWHasLoadLoss	set_has_load_loss	
OPFLOWIgnoreLineflowConstraints	set_ignore_lineflow_constraints	
OPFLOWHasBusPowerImbalance	set_has_bus_power_imbalance	
OPFLOWUseAGC	set_use_agc	
OPFLOWSetHIOPVerbosityLevel	set_hiop_verbosity_level	integer between 0 and 10
OPFLOWSetLoadLossPenalty	set_loadloss_penalty	
OPFLOWSetBusPowerImbalancePenalty	set_bus_power_imbalance_penalty	
OPFLOWSetTolerance	set_tolerance	
OPFLOWSetWeight	set_weight	
PSSetGenPowerLimits	ps_set_gen_power_limits	
OPFLOWGetTolerance	get_tolerance	
OPFLOWGetHIOPComputeMode	get_hiop_compute_mode	
OPFLOWGetHIOPMemSpace	get_hiop_mem_space	
OPFLOWGetModel	get_model	
OPFLOWGetSolver	get_solver	
	-	
OPFLOWGetConvergenceStatus	get_convergence_status	
OPFLOWGetObjectiveType	get_objective_type	
OPFLOWGetInitializationType	get_initialization_type	
OPFLOWGetGenBusVoltageType	get_gen_bus_voltage_type	
OPFLOWGetHasGenSetPoint	get_has_gen_set_point	
OPFLOWGetLoadlossPenalty	get_loadloss_penalty	
OPFLOWGetIgnoreLineflowConstraints	get_ignore_lineflow_constraints	
OPFLOWGetHasLoadloss	get_has_loadloss	
OPFLOWGetHasBusPowerImbalance	get_has_bus_power_imbalance	
OPFLOWGetUseAGC	get_use_agc	
OPFLOWGetHIOPVerbosityLevel	get_hiop_verbosity_level	
OPFLOWGetBusPowerImbalancePenalty	get_bus_power_imbalance_penalty	
PSGetGenDispatch	get_gen_dispatch	
OPFLOWGetObjectiveTypes	get_objective_types	
OPFLOWGetInitializationTypes	get_initialization_types	
OPFLOWGetGenBusVoltage	get_gen_bus_voltage	
OPFLOWGetObjective	get_objective	
OPFLOWSolve	solve	
OPFLOWPrintSolution	print_solution	
OPFLOWSaveSolution	save_solution	
OPFLOWReadMatPowerData	read_mat_power_data	
OPFLOWSolutionToPS	solution_to_ps	
OPFLOWSetUpPS	set_up_ps	
OPFLOWSkipOptions	skip_options	
OPFLOWSetLinesMonitored	set_lines_monitored	implemented as two different methods
	set_lines_monitored([])	Specify a list of line kvlevels (type float) to monitor

Table 7.3: OPFLOW Python Bindings (cont.)

C++ API	Python API	Notes
	<pre>set_lines_monitored(n, "file")</pre>	Read n line kvlevels from a file (n=-1 for all)_

#### 7.3.4 SCOPFLOW

The functions in the following table could be called by a scopflow object (i.e. scopflow = exago.SCOPFLOW(); scopflow.solve();)

Table 7.4: SCOPFLOW Python Bindings

C++ API	Python API	Notes
SCOPFLOW	exago.SCOPFLOW class	
ContingencyFileInputFormat enum	exago.ContingencyFileInputFormat enum	More details and possible values for this enum can be found in the 7.4. Currently, this is only be used as a Python enum. A string representation is not available.
SCOPFLOWSetModel	set_model	
SCOPFLOWSetNetworkData	set_network_data	
SCOPFLOWSetLoadProfiles	set_load_profiles	
SCOPFLOWSetNumContingencies	set_num_contingencies	
SCOPFLOWSetContingencyData	set_contingency_data	
SCOPFLOWSetPLoadData	set_pload_data	
SCOPFLOWSetQLoadData	set_qload_data	
SCOPFLOWSetWindGenProfile	set_wind_gen_profile	
SCOPFLOWSetTimeStep	set_time_step	
SCOPFLOWSetDuration	set_duration	
SCOPFLOWSetTimeStepandDuration	set_time_step_and_duration	
SCOPFLOWSetTolerance	set_tolerance	
SCOPFLOWSetVerbosityLevel	set_verbosity_level	
SCOPFLOWSetComputeMode	set_compute_mode	
SCOPFLOWSetSolver	set_solver	
SCOPFLOWSetSubproblemModel	set_subproblem_model	
SCOPFLOWSetSubproblemSolver	set_subproblem_solver	
SCOPFLOWSetInitilizationType	set_initialization_type	
SCOPFLOWSetGenBusVoltageType	set_gen_bus_voltage_type	
SCOPFLOWEnableMultiPeriod	enable_multi_period	
SCOPFLOWEnablePowerImbalanceVariables	enable_power_imbalance_variables	
SCOPFLOWIgnoreLineflowConstraints	ignore_lineflow_constraints	
SCOPFLOWGetTolerance	get_tolerance	
SCOPFLOWGetNumIterations	get_num_iterations	
SCOPFLOWGetConvergenceStatus	get_convergence_status	
SCOPFLOWGetTotalObjective	get_total_objective	
SCOPFLOWGetBaseObjective	get_base_objective	
SCOPFLOWSetUp	set_up	
SCOPFLOWSolve	solve	
SCOPFLOWPrintSolution	print_solution	
SCOPFLOWSaveSolution	save_solution	
SCOPFLOWSaveSolutionDefault	save_solution_default	
SCOPFLOWSaveSolutionAll	save_solution_all	
SCOPFLOWSaveSolutionAllDefault	save_solution_all_default	

#### 7.3.5 SOPFLOW

The functions in the following table could be called by a sopflow object (i.e. sopflow = exago.SOPFLOW(); sopflow.solve();)

Table 7.5: SOPFLOW Python Bindings

C++ API	Python API	Notes
SCOPFLOW	exago.SCOPFLOW class	
ScenarioFileInputFormat enum	ScenarioFileInputFormat enum	More details and possible values for this enum can be found in 7.4. Cur- rently, this is only be used as a Python enum. A string representa- tion is not available.
ScenarioUncertaintyType enum	ScenarioUncertaintyType enum	More details and possible values for this enum can be found in the 7.4. Currently, this is only be used as a Python enum. A string representa- tion is not available.
SOPFLOWSetModel	set_model	
SOPFLOWSetNetworkData	set_network_data	
SOPFLOWSetContingencyData	set_contingency_data	
SOPFLOWSetNumContingencies	set_num_contingencies	
SOPFLOWSetScenarioData	set_scenario_data	
SOPFLOWSetNumScenarios	set_num_scenarios	
SOPFLOWSetWindGenProfile	set_wind_gen_profile	
SOPFLOWSetTimeStepandDuration	set_time_step_and_duration	
SOPFLOWSetTolerance	set_tolerance	
SOPFLOWSetSubproblemVerbosityLevel	set_subproblem_verbosity_level	
SOPFLOWSetSubproblemComputeMode	set_subproblem_compute_mode	
SOPFLOWSetSubproblemModel	set_subproblem_model	
SOPFLOWSetSubproblemSolver	set_subproblem_solver	
SOPFLOWSetSolver	set_solver	
SOPFLOWSetInitializationType	set_initialization_type	
SOPFLOWSetGenBusVoltageType	set_gen_bus_voltage_type	
SOPFLOWSetLoadProfiles	set_load_profiles	
SOPFLOWSetLoadProfiles	set_ignore_lineflow_constraints	
SOPFLOWEnableMultiContingency	enable_multi_contingency	
SOPFLOWFlattenContingencies	flatten_contingencies	
SOPFLOWGetNumScenarios	get_num_scenarios	
SOPFLOWGetNumIterations	get_num_iterations	
SOPFLOWGetConvergenceStatus	get_convergence_status	
SOPFLOWGetTotalObjective	get_total_objective	
SOPFLOWGetConvergenceStatus	get_converged_status	
SOPFLOWGetTolerance	get_tolerance	
SOPFLOWSetUp	setup	
SOPFLOWSolve	solve	
SOPFLOWPrintSolution	print_solution	
SOPFLOWSaveSolution	save_solution	
SOPFLOWSaveSolutionAll	save_solution_all	

#### 7.4 Enums

The enums in ExaGO serve as integer mapped values for certain settings within the application. Several type settings, OPFLOWObjectiveType, OPFLOWInitializationType, and OPFLOWGenBusVolt-

ageType, are specific to OPFLOW.

Instances can be constructed directly through the ExaGO library (i.e. exago.OutputFormat.CSV). The possible values for the current enums are as follows:

Possible Values		
OPFLOWObjectiveType	OPFLOWInitializationType	OPFLOWGenBusVoltageType
- MIN_GEN_COST	- OPFLOWINIT_FROMFILE	- VARIABLE_WITHIN_BOUNDS
- MIN_GENSETPOINT_DEVIATION	- OPFLOWINIT_MIDPOINT	- FIXED_WITHIN_QBOUNDS
- NO_OBJ	- OPFLOWINIT_ACPF	- FIXED_AT_SETPOINT
	- OPFLOW_FLATSTART	

Possible Values			
OutputFormat	ContingencyFileInputFormat	ScenarioFileInputFormat	ScenarioUncertaintyType
- CSV	- NATIVE	- NATIVE_SINGLEPERIOD	- NONE
- MATPOWER	- PSSE	- NATIVE_MULTIPERIOD	- WIND
- JSON			- LOAD
- MINIMAL			

Note: getters for the possible values of ContingencyFileInputeFormat, ScenarioFileInputFormat, ScenarioUncertaintyType are not currently available.

Instances can be constructed directly through the exago library (i.e. exago.OPFLOWObjectiveType.MIN\_GEN\_COST or exago.MIN\_GEN\_COST)

Setter functions for these OPFLOW Type configurations can take an integer, an instance of the exago enum, or a string that describes the enum (i.e. 'MIN\_GEN\_COST'). The rest currently only accept an instance of the exago enum. The possible values for these OPFLOW Type enums can be retrieved through opflow.get\_xxx\_types() (i.e. opflow.get\_gen\_bus\_voltage\_types()). The opflow.get\_xxx\_types functions yield a list of the enum values.

The next section covers some code examples on how to get and use these values.

#### 7.4.1 Code Examples

#### Set with a string

```
>>> opflow.set_initialization_type('OPFLOWINIT_FROMFILE')
>>> opflow.get_initialization_type()
OPFLOWINitializationType.OPFLOWINIT_FROMFILE
```

#### Set with an integer

```
>>> opflow.set_initialization_type(1)
>>> opflow.get_initialization_type()
OPFLOWInitializationType.OPFLOWINIT_FROMFILE
```

#### Set with an enum instance

```
>>> opflow.set_initialization_type(exago.OPFLOWInitializationType.

\( \to \) OPFLOWINIT_FROMFILE)

>>> opflow.get_initialization_type()

OPFLOWInitializationType.OPFLOWINIT_FROMFILE
```

#### Set via getter function

#### 7.5 History

Exago pre v1.1 had optional Python bindings, implemented with ctypes, that could be enabled. HiOp [6, 5], a critical dependency, updated to Umpire v6 when GPU and RAJA options were enabled. Because Umpire after v6 ships with CUDA device code, a final device link step was required for any other libraries or executables. This drastically complicated the ctypes Python bindings, which relied on calling out to the shared library directly.

ExaGO v1.2.1 was the first version to ship Python bindings that used Pybind11, which creates a shared library directly importable from Python, which simplified the user experience and made it possible to call ExaGO from Python when only static libraries are generated.

## Appendices

## Appendix A

## Symbol reference

Units of measurement are given in Table (A.1), indices and index sets in Table (A.2), subsets in Table (A.3), special set elements in Table (A.4), and real-valued parameters in Table (A.5).

Table A.1: Units of measurement

Symbol	Description
1	dimensionless. Dimensionless real number quantities are indicated by a unit of 1.
USD	US dollar. Cost, penalty, and objective values are expressed in USD.
h	hour. Time is expressed in h.
pu	per unit. Voltage magnitude is expressed in a per unit system under given base values, and the unit is denoted by pu
rad	radian. Voltage angles are expressed in rad.
MW	megawatt. Real power is expressed in MW.
MVar	megavolt-ampere-reactive. Reactive power is expressed in MVar.
MVA	megavolt-ampere. Apparent power is expressed in MVA.
MW at 1 pu	megawatt at unit voltage. Conductance is expressed in MW at 1 pu, meaning the conductance is such as to yield a real power flow equal to the indicated amount when the voltage is equal to 1 pu
MVar at 1 pu	megavolt-ampere-reactive at unit voltage. Susceptance is expressed in MVar at 1 pu, meaning the susceptance is such as to yield a reactive power flow equal to the indicated amount when the voltage is equal to 1 pu

Table A.2: Index sets

Symbol	Description
$a \in A$ $i \in I$	areas buses

Table A.2: Continued

Symbol	Description
$j \in J$	bus-connected grid components, i.e. loads, shunts, generators, stochastic resources, branches
$k \in K$	security contingencies, i.e. NERC $(n-1)$ - or $(n-k)$ -style contingencies, different from
$s \in S$	the severe event we are modeling stochastic scenarios
$t \in T$	time periods

Table A.3: Subsets

Symbol	Description
$J^{\mathrm{gen}} \subset J$	generators
$J^{\mathrm{ld}}\subset J$	loads
$J^{\mathrm{br}}\subset J$	branches, i.e. lines, transformers
$J^{\operatorname{sh}}\subset J$	shunts
$J_i^{\mathrm{o}} \subset J$	branches with origin bus at bus $i$
$J_i^{\mathrm{d}} \subset J$	branches with destination bus at bus $i$

Table A.4: Special set elements

Symbol	Description
$a_i \in A$	area of bus $i$
$i_j^{\mathrm{d}} \in I$	destination bus of branch $j \in J$
$i_j^{\mathrm{o}} \in I$	origin bus of branch $j \in J^{\text{br}}$

 ${\bf Table~A.5:} \quad {\bf Real-valued~parameters}$ 

Symbol	Description
$b_j^{\max}$	maximum susceptance for shunt $j \in J^{\text{sh}}$ (MVar at 1 pu)

Table A.5: Continued

Symbol	Description
$b_j^{\min}$	minimum susceptance for shunt $j \in J^{\text{sh}}$ (MVar at 1 pu)
$b_j^{ m ch}$	charging susceptance for branch $j \in J^{\text{br}}$ (MVar at 1 pu)
$b_j^{ m s}$	series susceptance for branch $j \in J^{\text{br}}$ (MVar at 1 pu)
$p_j^{ m gset}$	real power set point of generator $j \in J^{\text{gen}}$ (MW)
$p_j^{ m gmax}$	maximum real power output for generator $j \in J^{\text{gen}}$ (MW)
$p_j^{ m gmin}$	minimum real power output for generator $j \in J^{\text{gen}}$ (MW)
$p_j^{ m r}$	maximum ramp rate for generator $j \in J^{\text{gen}}$ (MW/h)
$q_j^{\mathrm{gmax}}$	maximum reactive power output for generator $j \in J^{\text{gen}}$ (MVar)
$q_j^{ m gmin}$	minimum reactive power output for generator $j \in J^{\text{gen}}$ (MVar)
$v_i^{\max}$	maximum voltage magnitude for bus $i \in I$ (pu)
$v_i^{\min}$	minimum voltage magnitude for bus $i \in I$ (pu)
$\pi_s$	probability of scenario $s$ (1)

## **Bibliography**

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