



ESF projekt Západočeské univerzity v Plzni reg. č. CZ.02.2.69/0.0/0.0/16 015/0002287

# KKY/USVP 5 Thermal Imaging

There are several companies producing thermal cameras. FLIR, Optris, Workswell.

In this lecture, we will work with a camera FLIR T640.

**Used library:** <a href="https://pypi.org/project/flirimageextractor/">https://pypi.org/project/flirimageextractor/</a>(<a href="https://pypi.org/project/flirimageextractor/">https://pypi.org/project/flirimageextractor/</a>),
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<a href="https://pypi.org/project/flirimageextractor/">https://pypi.org/project/flirimageextractor/</a>)</a>

Prerequisity: <a href="https://exiftool.org/index.html">https://exiftool.org/index.html</a> on linux Ubuntu just type sudo apt install exiftool into terminal

#### In [1]:

%pylab inline

Populating the interactive namespace from numpy and matplotlib

#### In [2]:

```
import flirimageextractor
from matplotlib import cm
import matplotlib.pyplot as plt
import numpy as np
```

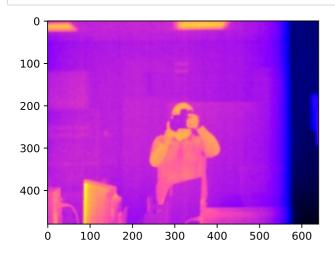
# How to load an image

### In [43]:

```
flir = flirimageextractor.FlirImageExtractor(palettes=[cm.jet, cm.bwr, cm.gist_ncar])
flir.process_image('./cviceni_5/FLIR0805.jpg')
```

### In [44]:

#### flir.plot()



Note that the glass behaves like a mirror in the infrared

## How to get thermal data

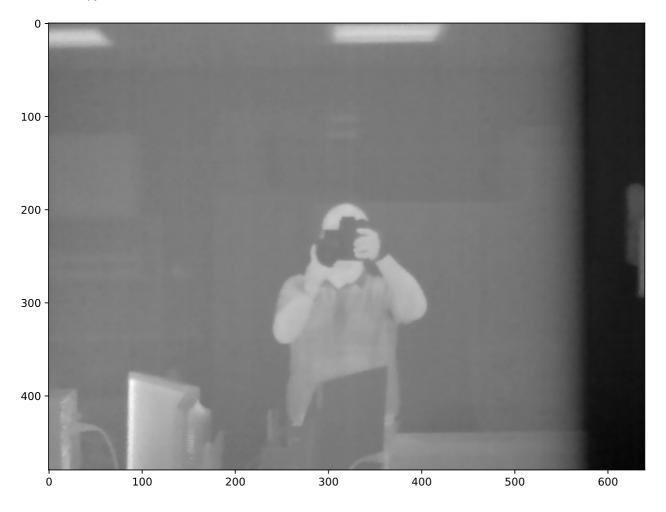
```
In [45]:
```

```
img = flir.get_thermal_np()
```

### In [46]:

```
plt.figure(1, figsize(10,10))
plt.imshow(img, cmap="gray")
print(type(img[0,0]), np.min(img), np.max(img))
```

<class 'numpy.float64'> 24.31294485740625 28.775005506518937



# How to get metadata

```
In [7]:
```

```
meta = flir.get_metadata('cviceni_5/FLIR0811.jpg')
```

### List of all metadata in the image file

```
In [8]:
 print(meta.kevs())
dict_keys(['SourceFile', 'ExifToolVersion', 'FileName', 'Directory', 'FileSize', 'FileModifyDat e', 'FileAccessDate', 'FileInodeChangeDate', 'FilePermissions', 'FileType', 'FileTypeExtension', 'MIMEType', 'JFIFVersion', 'ExifByteOrder', 'Make', 'Model', 'Orientation', 'XResolution', 'Y Resolution', 'ResolutionUnit', 'Software', 'ModifyDate', 'YCbCrPositioning', 'ExposureTime', 'E xifVersion', 'CreateDate', 'ComponentsConfiguration', 'SubjectDistance', 'FocalLength', 'ImageT emperatureMax', 'ImageTemperatureMin', 'FlashpixVersion', 'ColorSpace', 'ExifImageWidth', '
 ImageHeight', 'DigitalZoomRatio', 'ImageUniqueID', 'Compression', 'ThumbnailOffset', 'Thumbnail
Length', 'CreatorSoftware', 'Emissivity', 'ObjectDistance', 'ReflectedApparentTemperature', 'At mosphericTemperature', 'IRWindowTemperature', 'IRWindowTransmission', 'RelativeHumidity', 'Plan
ckR1', 'PlanckB', 'PlanckF', 'AtmosphericTransAlpha1', 'AtmosphericTransAlpha2', 'AtmosphericTransBeta1', 'AtmosphericTransBeta2', 'AtmosphericTransX', 'CameraTemperatureRangeMax', 'CameraTe
mperatureRangeMin', 'CameraTemperatureMaxClip', 'CameraTemperatureMinClip', 'CameraTemperatureM
axWarn', 'CameraTemperatureMinWarn', 'CameraTemperatureMaxSaturated', 'CameraTemperatureMinSaturated', 'CameraModel', 'CameraPartNumber', 'CameraSerialNumber', 'CameraSoftware', 'LensModel',
'LensPartNumber', 'LensSerialNumber', 'FieldOfView', 'FilterModel', 'FilterPartNumber', 'Filter SerialNumber', 'PlanckO', 'PlanckR2', 'RawValueMedian', 'RawValueRange', 'DateTimeOriginal', 'FocusStepCount', 'FocusDistance', 'FrameRate', 'PaletteColors', 'AboveColor', 'BelowColor', 'OverflowColor', 'UnderflowColor', 'Isotherm1Color', 'Isotherm2Color', 'PaletteMethod', 'PaletteStr
etch', 'PaletteFileName', 'PaletteName', 'Palette', 'RawThermalImageWidth', 'RawThermalImageHeight', 'RawThermalImageType', 'RawThermalImage', 'Real2IR', 'OffsetX', 'OffsetY', 'PiPX1', 'PiPX2', 'PiPY1', 'PiPY2', 'GPSMapDatum', 'EmbeddedImageWidth', 'EmbeddedImageHeight', 'EmbeddedImage
eType', 'EmbeddedImage', 'ImageWidth', 'ImageHeight', 'EncodingProcess', 'BitsPerSample', 'Colo
 rComponents', 'YCbCrSubSampling', 'ImageSize', 'Megapixels', 'PeakSpectralSensitivity', 'Shutte
 rSpeed', 'ThumbnailImage', 'FocalLength35efl'])
 In [9]:
 print(meta["Emissivity"])
0.95
 In [10]:
 print(meta["CameraTemperatureRangeMax"])
 150.0 C
 How to get a raw thermal data
 In [11]:
 raw_data = meta.get("RawThermalImage")
 In [12]:
 print(raw data)
 (Binary data 240492 bytes, use -b option to extract)
 In [13]:
 import io
 import os
 import subprocess
 from PIL import Image
 thermal_img_bytes = subprocess.check_output(["exiftool", "-RawThermalImage", "-b", 'cviceni 5/FLIR0811.jpg']
```

```
In [14]:
```

print(thermal img bytes)

 $9d \times 03 \times d2 \times 1c \times d3 \times fb \times 9c \times 95 \times 8b \times ca \vee 2b \times 17 \times c0 \times b8E \times 99, ` \times 021 \times f3 \times 00 \times a2 \times e8. S= \times b6, ' ' \times 92 \times 0b \times 01 \times 8c \times d04 \times 98 \times 9als \times 01g \times b0. @S \times ba \times e9 \times 87 \times 89 \times 01 \times a5 \times f8 \times ec \times a7p \times e0 \times 9d \times 5xca \times 8b \times e2 \times b9 \times 2xca \times 8a \times 08 \times cdp_ \times 9d \times 9d \times 2xca \times 2xc$ 

```
 U \times 3 \times 5 \times 6 \times 10^{3} \times 10
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17GH\x9c\x06\xe9-\{\xe3\x9b\x9f\x0bh\x02\}\xc1\x98>T\x8a\xbe\x87\x075!\xdb\x99z\x85!s\x13\xc5\t;=
\xb3\xbbu^\xb1\x8d0\xfcd\xd4R-%V\x0bq\x94\xe3A\x9d\x0c\\p`|+M\x96\x86\xdb\xc3C\x1cJ\xc1N\xca\xe
6\xf8\x00\xe8X\xc6l\x1dQ\xf8\x03\xd6[\x93\xb8\xfaQ \xf7\x13\xc48|\xae\x04>\xb6\x8d\x04p\n\x0b\x
ac9\xfe\xd6\xc5\xb7\xad\xfe\xc2.\x81<u\xfa\xb1]-\xfc\xd8\x8e\xde\xbe\xac\xe7\xee\x0b\xd3\x06\xc
6\xf1\xcc>\x95\x93\xc7\x02\xb9<\xf1\xsf1\xbf1\xcc9\x0e\x8e\xfc1\xf3\xfd
xce\xb0\xb5\x03\x90\xd6V\xdfX\x8f\x8d9\x9b\xef\xae(8\xb2\x80\xea\xa7\xcd\x08\xa0\x92\xdctA\xbb\xea\xae(8\xb2\xbae)
x9c\x9eN}\xf2k\xaa\x98\xe3\xb0U\xd0\xcfR\x92\x86\x96~\x05\x01U\xac\xd4\x90&$06\xc9\x918\x87\x17
\xab\xe4,h\xa2\xc6\xc1\x1b\xd9{g\x8dC\x8fQ\xc6\x89\xa3\xc6t\xcc \x08\xd2\x82\x03BRIX\xc2\xa2\xb
d\x16\xd5\xbD\xc0=a\xc3e\x02\xf6\xb6\x01\x97\xdb\xb8X\x87\x1b<\xaaA=\x0cD\xa0\xd1"\xdb[\xd3\xf6\xd5]
6K_Z \times 9a \times b2 \times 91G \times 91X \times 8c3 \times
xa2\t\xdeaD3M\xb7\xb3\xfao .\x0e\xe3\xa8\x18b\x94\xd2"\x8d\xf9\xd1\x07o\xf9\xa5\x88\xe11W;\xb3;
\\\x9b\xa6|F7a\xc3>G\x97\x1f3\x8a\xe3\x00&\xe8\x01\x91\x01\x8f\xea\xab*\xe1p\x89\xcc\xad\x85\x8
b\xe3\xed\xf3>X*H1\x01\xe3\xb6\xed\x91\x9a\x0f\xd5\x06\x08c\x04\x00fH\x01D\xbc\x95k\x89\xa5-\x8
aVzKr: \x1a\xa0\xa0r\xea\xd7\xca\x93a^\xbf\x07"xT\xea\xcf\xec\xc8+\xb7\x1e\xe8\x8a\x1d\thM\xc5k
\xea\xfd\xd1m\x8fA\#\x9b8\xd2V\xa0\xc2\t\x183/g\xf7\x9288\x80\xf6\xf8t\xeb\x9a\xa9\xa6j\x04\x15\
 x7fQ0M \times a6[2\times e1\times 8c\times 1di\times c2\times a6\times 06a\times 11\times 87\times 12\times 07\times 9d\times 14V\times 8c\times a3\times c20\times c5b\times bd\times 02\times 9b\times 12\times 07\times 9d\times 14V\times 8c\times a3\times c20\times c5b\times bd\times 02\times c3b\times 
x82\x12[\x04(th\xc7\x0f\xdd\xa0\xc2\x96\xfe\xda\x1e\xd4\xe4\x0cu|\x94\xc4\x02\xb3ZD;\xf6q{X}\x82
 \x1aa\xf1h\xc9"\xec\x9a\x14\xf1\xbcn\xeb\xe5\xa5\xa7\x9f>k%`\xe1B-Ib\x9a\x82\x84\xa6pd\xc2\x89\
xb0`)\x86\xfe\xf5\xd5F@\xc33L\xa7\x1d\xb2H\xe9]5N\x0b\xea)\x12A\x8d0\xe4,\xdd\x1c\x01\x190\xb7\xd5F@\xc32L\xa7\xdd\xb2H\xe9]
 x0c + x02 \times 16 \times e^{xf2 \times 3} 
e7$eSaQ;\xd6\xc2#\x0b\xb1\x9a\xa3\x8a\x1b\x92HJ\xa5\x8d(H\xbb\xe9\x9c\xc5\xa5~|y\xc7\x87\xc4\x9
5V5\xef\xdb\xfb0\xc7/\xc35?o4\xb8k\x96z\xf7\xe6\x8ea+\xa9\x93\xc7\xfe`8\xba\x7f\xbf\xee\xff\xc5
c0+h\&\xo=u=0$\x1aAME\x05\x16\x95\&\x08R\x80j\nhq\x91{\x11\x81\xc1\x8d\xd0\x19jfL\xfb\xc8\xcbT>w=0}
L) o \times d a \times 96 \times 13k \times xa4 
07\xf8\xf1\xd3\xdb7Eyr\x13\xe1\xf3~M\xcch\xb2G\xe1\xd3\xe5\x1dk\xf5\xc4~\x04\xb7\xe7]?\x1e7~%)\
\xdc\x87\xdd\xc1\x98U\x05I\xa1\x95S\x0b"\xb4\x07\x8c\xd5W\x05\xa3j\xcfx\xc8]\xf0\x96D\xa1,\xb4\
xe4\x9eFM\x0f\xa0\xcf\xd5\x8c\x13\x82k\xe1\xac\c\xc3\x10\x0epr\xdf5\xf4Y\xb8\x80G\xee\xac\x86\x
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5\xb0Y\xf8\x93$\n\xf7\xc7\x93\xf7\xf8\xb7\r&\x92\x02I\x85\xa4\xae\x01\xd0%m\x1e\xf2\xd0\x00.\xa
b\xae\x05:\xdf\xe7\xa2\xb5\xa8PY\x85\x0b\x89-+\xb0R\x1a\xd1\x8a\xc6p[\x1c\x08!\xf8\xd2\xda\x84\
x96\x0f\xe1\xba*?\xf4\xee\xe3\x15o\xa8\xb0B>\xb1\xc7\xd2^\xbd\r\xee\xdd^\xc0WP9\x9d>\xbc0\xd7/B
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5n\xe2UK\x95\xbb\x85\x1dl\x03\xaf\xebAT\x86\n\xc8\x01\xaf~\xea\xa5W\x8c50@\xf1\xfdMD\xbb\x02g=\
\x13@\x9f\xe1\x19\xd0U\xbeGF]\x10\xb7\xfa\x82w\xd7\xaeZMe\xa5\xb4U !\xf9\xc1m\x9ad7 \xb35AK \x1
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e92\xf9\xd9\x80\%\xb20\xadH\xaeq\xae\x90N\x8e\xa0!\xbc8ki\xbewV\xfb\xac\x0b\x1a\x9f+8\x03[\x02\xd]
80\r0\x87\xec\xc6\xadN1\x96\xa7\xe5\x14\xaa \x1e\xbe\xa4\xee\xea\#HB\xd1j,\I\xe3\xb9\xe8m[[\x82]]
98b \times d3 \times da1^x fa_{-xf3} \times 0b \times 17 \times c7 \times b2 \times 13 \times da1^x fa_{-xf3} \times 0b \times 17 \times c7 \times b2 \times 13 \times da1^x fa_{-xf3} \times 0b \times 17 \times c7 \times b2 \times 13 \times da1^x fa_{-xf3} \times 0b \times 17 \times c7 \times b2 \times 13 \times da1^x fa_{-xf3} \times 0b \times 17 \times c7 \times b2 \times 13 \times da1^x fa_{-xf3} \times 0b \times 17 \times c7 \times b2 \times 13 \times da1^x fa_{-xf3} \times 0b \times 17 \times c7 \times b2 \times 13 \times da1^x fa_{-xf3} \times 0b \times 17 \times c7 \times b2 \times 13 \times da1^x fa_{-xf3} \times 0b \times 17 \times c7 \times b2 \times 13 \times da1^x fa_{-xf3} \times 0b \times 17 \times c7 \times b2 \times da1^x fa_{-xf3} \times 0b \times 17 \times c7 \times b2 \times da1^x fa_{-xf3} \times 0b \times 17 \times c7 \times b2 \times da1^x fa_{-xf3} \times 0b \times 17 \times c7 \times b2 \times da1^x fa_{-xf3} \times 0b \times 17 \times c7 \times b2 \times da1^x fa_{-xf3} \times 0b \times 17 \times 
b\times94\times60\timesf9\times85n\times89\timesb7\xf4YQ\xbf\xf5\x1c\x17\x1c\x93\x1b~LSm+\x812u\x17\xb9Z\x15\xe7\xdb\
xaaM^Qjl\\x19Bj\\x89g\\xba\\xa2\\x0b\\xe1\\xf3X\\x1c\\x08\\xa5-B\\xb0\\xb7\\xd9e>\\x84[\\xf8l\\xdbQ>G;4\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\xa6\\r\\
94\x0b\xd5B<\xdc\xa9.=[i_J\xb0\xa7\xbeX\xd7gA\xa1\xdbX&\xf0\x93\xe2\xfc\xcc\x1e\x83%M?\xbd\xa3(
-fq.\xac\xb9\x94\r8\x80\xe4o@\x961\xcb\xbbX\xf5\xbeR58[\xba\xc4L+\x17Z\x00\x16Ss`\xfd\xaa\x15\xbeR5R[\xba\xc4L+\x17Z\x00]
99\x06\x93M\x9d\nn\x0c\xddb(\xf5\x88\xfa\xd1\xd4\xa6\x91\xe4#\xa0\x04\x98\xce\x16\xd6\x08\x08\
e\x1b\xf8\#\x0b\xfe7NoX\xb03-\x05\x1f\xdc\x00\xbc*\x8f\xb4\x1f\x1b\r\xda\x04\x1d\x92\xb3\x82\x90
 -E1\x7f\xa1\xa8J\x07\'Z\xb42IR\xd7\xf1s$\xd2;\x9b\xa3\xb3\x9d\xd7y\xb7\x01\xdd\xb5\xe7\xa5\xd1]
][5A\x11\xce\xb4\xf1\xde9{\xff\xaaM\xca\xe9\xfa\xb4Ji\x8ac\xdcV\xf2\n\x0e\x9c\xdd/\xadW1\xe1\xe
2\xb0X\x1cq\xc9\#\xbc\xb1\x92\xd1I\xc1\x89\xb8,\xccq.\xef\xe8\x19\%\x9c\x17\x869\x19\x8c\xe1\x8fV
\xd9\xb1\xe5\x056\xc6\x8d\{u\xdf\xbe\xce\xc7\xaf=I\xc6\x0e\x85\xc6B4\xad\xa0\x0cy\xecb\x042D
\x83\x04\xf4\xadE\x1c\xc0=\'\xf4\x12\x04\x9d\x9b\xf3\xee\x96:m\x85\x984\xaa\x16u\xe9f\xc8\x9b\x
e5H^\times08B\times1dNP\timesb5\times91\timese4Xp)\\ 8\times f5\times bd\times d0\times b3\times e46-\times c0\times13Y\times dc\times7f\times a4\times 9d\times12\times00\times174DW\times b3\times e46-\times c0\times13Y\times dc\times7f\times a4\times e4Xp)\\ 8\times f5\times bd\times d0\times b3\times e46-\times c0\times13Y\times dc\times7f\times a4\times e4Xp)\\ 8\times f5\times bd\times d0\times b3\times e46-\times c0\times13Y\times dc\times7f\times a4\times e4Xp)\\ 8\times f5\times bd\times d0\times b3\times e46-\times c0\times13Y\times dc\times7f\times a4\times e4Xp)\\ 8\times f5\times bd\times d0\times b3\times e46-\times c0\times13Y\times dc\times7f\times a4\times e4Xp)\\ 8\times f5\times bd\times d0\times b3\times e46-\times c0\times13Y\times dc\times7f\times a4\times e4Xp)\\ 8\times f5\times bd\times d0\times e4Xp)\\ 8\times f5\times bd\times e4Xp)\\ 8\times bd\times e4Xp)\\ 8\times f5\times bd\times e4Xp)\\ 8\times bd\times e4Xp)
x9a/ s\xc3\xae\xd1\x87\xa8\#\xfb\x18\x16\x8c\x08\xcb\x1d5E\x08Cb-\xd6\x0c\x0f\x84]\x1c)\xfcQ\xe8
\xbdk\x1bt\x98\x94\xc1\x19\x94\xc8\xde\x1bN\x1d\x94\xe1\x050\x13b\xec\x19\xc9\xb8\xd8\xcbq\x8cq
```

```
P\x00\x1e\x8ex+\xe0P\xf0\xe1\xf2\xfa\xd6\x1a=\xbd\x81\x06\x17\xbe\x97\xbe\xc7=\x19\xbd\x8a\xa6
\x82\x06\x07n"XX\x16\xe4\xfd\x02\xf9#\x0b|\xf7\x9e~\xfa\xf2s\xd3\xca/0\x17\xad\x9b\x1a\x8f\x89\
xeb\xfb\xaf0U\xbd\tG\xdb\x8cHf\xea\xf4\xfc\x85E\xf1\xe5\x87\xbb\n\xeb \x0b\xa0V\x11{\x8f6\xcdj+
\xa3:\x9b\x9b\xa3\xed\x9cv\xa8\xd2d\xd6\x80\x9a,]\xd2\x84\x05\xc7X\x06\xac!\x84\x93Hz\xce\xa1\x
\x86\xc1\xa3\x8f\xa9\xa3\xc9Z\x0f\xf7h\x15\xd0\n H\xae\xb6\xb0\xea\x15\x82\xfcGS\x1a8\x82\'\xfe
\xc9\x15\xca\xb5\xdb\xa7\xa9A\x8dsL\xf2\xc8\x0bC\overline{4}\x97\x0cp\xaa\r$;S?\x92A\xc4c\xab [\x84\x10\xb]
\label{lem:ccx8dxd4yA} $$ c\x0<xbd\x08\xa8\xc60\xf1m\x95.\x89\xf1KV\x8f\x06(\x1c\xa9\xe2i\x07JY\x06) $$
40\xc6\'\xc3\x8dM\xab\xd1\xefBW\x9aM\x12\xde\xc9b\xf6\x88$\x85\x11]Xb\x1d\j5=\x16\xa2\xdd\x04@2=
 -\x7f\xa0\xe5\x17;\x98KH\x9dP\xdc\xbd\xbf
\xb0\xa3?\x14\x90B\xd5\xc9sJ\x80\xb6\xeb\x99i\xd1\xe0\x9e$\xb0Z\xcf2\x1c\x1a\x0f \\\xfb\x15o^\x
\xa4t\xac5K\xc6\xd4\xaeM\x9b8\xf7\x8bZ\x1aI\xde\\\x1f\xb0\xe5\xe0[t\x0b\xd6Q\xe0@\xcf\xed)\x80\
xbe\\x0c\\xe976\\xd2\\x8d\\xe5\\xab\\xa7\\xb7\\x17P\\xb0\\xc2-\\xd0\\x93\\xef\\xf6\\x9d\\x97\\xef=D!\\xae\\x85P\\;
 'm\xc4\x1fi\xcb\xe0\xb8\xf3\xe0\x08A\xdb\x88\x02\xe9+w\x0cTHo\\<\x01\x0e\x17xz\x0f\x8b<\xef+\xa
\xb9@\xd48\xb0er\x9e[K\x1e9.\xf4\xb1c\xd6\xcb%r\x83\xac\x99}\xb8\xde1)\xc7\xb3\x17\xfaFA\t0\xf1
P%\xee\xbc\xb1\x0f\xdb\x18\xbf\xa9\xb0\xab\xbf6\YE\x83\xf6\xda\x01\{l\xc659\xc2\#\xda\V0\xb5\xa5\W\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf\xa6\xbf
f2\xb5\xd5\xd7-\x88\xf9\r\xdb\x1eaH\x8b.YI7\xb8\xc3Y\xa9\x03\x06Y\x99-\xb9s\xf3,\xb8\x13>\x93S\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\xf3,\xb8\x8\xf3,\xb8\xf3,\xb8\x8\x8\x8\x8\x8\x8\x8\x8\x8\x8
x1d\xc4\xe3\xd8\xec\x90\x07\x0f8Q\tm\xfc\xadp\xc57-\x0b\x16P\xdb8U\x7f,v\xd8;\x0epHsMN\x0fn[&a\x0epHsMN\x0fn]
e\xef\xc4.d\xa3)\t\xd9\x0c\xc7\xbc\xa1\x11\xf0m\xc2\xfc\xd0\xbc\x08\x05\x8f0.\x0c\x9a\x1f1\xecW
\xb4m\x87\xa3\xd5>\x94\x9f==\xbao\xe9^q\xf5\xbb\'\x1c]6\xcb\xfa\xe0z.\x92\xb8\xa9\x98r\xad\x93h
\x1cp\xcb\x94\x00\x07\x0c\x1c\xe7\x98GS0\x018\x95\\\x02\x16j\x0f\x06\xa0\x84B\x8e!+\xe1EayA\x15
\xc8`M -~\x1b\xb5j\x89\xf8\x84\xa7\xf2\xe0^\x85\xc9\xc5\xc1\x8b\xcb_\x01p\xfd\x14\xa8)\xc0\xb9&
\x0eZ\xf8D\xa5\xdc\n/(\x06\xad\x0c\nx\xb2\x14\xa7\xcd\xf9s\x9e}\xb8\xb6U\xf5\x1e\xc0\xd3\xbf\xeq
cL\xe9M\xdaQ)\x94\x92\xed\xc8\x9e\xb8\xc3\x1b\x1a\xde\xf7\xdf_2\x1cP\x96\x85L\xb4\\xe6\xf8\xe9
\xd3\xf7\x9f>~\xf9\xba\xf33\x03\x95\xcb\x00\x1e\xf2\xdaR\xaf\xed\x02%\x87\x9e!S\x85I\xbf}\xc1\x
8b\rB\xa84yU\xbb\xe1\xc4CL\x85\xce*\xb8\xea\x05\xlbg\xee\xbf\xda\x14\x10\n\x15\xf6\xc1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\xcb\xd1\x
xa4W\x7f\x16\xc2I\xa5\x8d\x1f\x12\xb0IV\tZ.\r9F\xe3\xb4\x07\xbe\xd5\x02;x}\xcf}\xcf\}\xb2USy\xf2\xe7
@\x90\x05\xe6qgr\xee1a\xce\xb3n\t\xb4:\xbdc\x90G\x0bl\x93F\xa3\xcb\xd9\xaa#\xb4\xc3mr\x08M\xb9\
xba\xcb\xc1\xb3\x85\xa5\x16\xe3\xf2\x10n\x9aN\xc2\x13\xcax\x85%\xc8\xc0U\xf8(\x04\xf0\x94$\xd3\
xabPs\r^*\xfb\x84w<\xa7yc\x98gFc\xf3t\x9d\xff\x99\xe7\x84v\xf6\xd5?l\x1a\x89\xc7\xf2\x8c\xa3\x07
z\x02!\x8bf\x194!\x9f}\xee\xf4\x91pA\xe4Z5I\{\&\x9c\xa4\xbb\xfb:\xe57\xbd\|b\xbf\xb8E\xa3I\xae>i\xbexeq.
\x8c\x1e\xf4\xafL\xad\x06\x00\x00\t\xd7IDAT\x1b\xc3\xf7\xf4\xb8\x04\xf9\xe1\xf5\xb9a{\xb1\xcc\x
 x1c\\x89\\xc3h\\x16"\\xc1\\x1cB- \\x1e\\xee\\x98"\\xd5\\x12\\xd87*z\\xad\\xc3\\x08\\\\x01\\xd6\\xb4\\xa4\\x99
f(xf9) xbb(xa7w) x8d(x9f(x7f(xb1*xf0)xa33)x8d(xe5)xa3)x8d(xb3)xd6G6(xbd(xb51)xf7)xe1(xfd(xa2L)xaagv)xe5(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)xe3(xe5)
\x96$0\xee\xd7\xff\xc7&\xf1G\xf7\xf9\xab\xd9MH\x98\xbc\xab\xbc\xc6\x90\'\xbdp\xcf\n\x16\x82
\x0b;\xe0Qp\x16JWs\xee\t\xd1x\xcf\xd6\xc9\x1f\xbf=\xee\x02\x15Z*\xe8\xf4)M\x93\x0cJ\xd8\xa8\x00
eT\xe6\xda\xfb\xb20W.\xdb\x9d\xe0>\x1d\x0fVRss\&\xf7:p\xa0\xb8U*\xb8o\x01\x1a\xf1\x88Ba\xc9\x7f8
<P\xceGp\xe2X\x12W\x15A\x8a\x80d\xba]\x98\xc8\x8f\xf8\x12\xdb\xe1\xe8\xe0\x9c6I=J/\xef\xe0\xbc\
xbe_?\xfc\x1b\xc9Y\xc7\xb4\xd3\x8fT<\x89\x84q\xe7\x0c\x0b\xa7\x89,\xef\x08\x0bt\xfd\xd7\'\xd7P\
xb3\xa6\xbf\xde{\x94=\x19\xec/\xb0\xff7\xfd\x93\t:LK\xc9\xc5[T\xa9\xf4\xa5\x02s\x9e\x84\xf00\xeq]
f(\xba\x845\x9a\xb4\xa3\xa3T+\xb8\xd3+\xady\xdd3\xcd\xd3\x97\x9b\x12\x1d\r\xo1\xc2u\xb1\xc5T\x
 x9f(xf5)xf7(xa3)x15(xb3)xd1(x075)x08(xbc%(x81)xc0(xcb)xf8(xa8)xfb (rR(x88), xbd(xd3)x820(x9d)xd20(xb)xf8(xa8)xfb (rR(x88), xbd(xd3)x820(x9d)xd20(xb)xf8(xa8)xfb (rR(x88), xbd(xd3)x820(x9d)xd20(xb)xf8(xa8)xfb (rR(x88), xbd(xd3)x820(x9d)xd20(xb)xf8(xa8)xfb (rR(x88), xbd(xd3)x820(x9d)xd20(xb)xf8(xa8)xfb (rR(x88), xbd(xd3)x820(xbd)xd20(xbd)xf8(xa8)xfb (rR(x88), xbd(xd3)x820(xbd)xd20(xbd)xf8(xa8)xfb (rR(x88), xbd(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd)xd20(xbd
7\xae\x10\x1e\xffZ\xddw\xfe\xe8\x82\xdf\xe5\xf4\xff\xee\xba\x9d\xda\xe8\xb9e!\xc1\xxcd\x14\x96\x
ac}\x8b\x16\'\xb2\x15\xc9\xba\x9d\x10\xa9p\xf7\xd0K\xb2\n5\xc0AJ\x15ckM\xf8/t\xe0BK\xbc\x83\#\x8B
b \times 05 \times x05 \times x
\x11/\xfd\xf5v\x94\xed\xf70\xdd\xfb\xb0j\xb4<\x1b\x1fP\xc5Z.\x13\xdd\xb3\xbd\x84\x8a\x98Z\
xa1\x89\x830\xbe\t\x13\xce8\x97L\xe9l\x8dv.M\xa314\x92\xf1\xf7;\x87\x0c\xfc\xa7Y\xc8\xc0\x1f\x1
a\xf0u\xd7\xf4\xdcU\xdc5\xd8q\xfa\xc4\x05\x84\'\x85\xb4\xaa5\xdd\xba*\xa1^U\x0eX-\xf5^\x84\xf1x
a\xf8\xabHx\xecZh<\xf0\xf6\xc2\x16\x9c\xee^\x9d\xe7[\x19?\xb2\xb60\xef>\xf0\xf7\xed\xef\xo7]
6\x07\xfb\x08\x02\xe1\xfb\xc6\xc1\x96\x99\x18\x9a\x16\xc7*\x0c!\W8\x000\xef\x0f8\x1f\xa0R\x
xdc\\x8eA\\xcb\\xad\\xad\\xca\\x04Z\\xbc\\x1cm\\xc0I0\\xa610\\x11\\\\x04\\xaa\\x80\\\\x81\\x8f\\x8f\\x17\\x90\\xa90\\)
\xb8l-\x9b\xaa\xd1\\\x81G\xde4\xd25\xb0l\xbf\x9a\xa3\xfa\xd3\x04\xbe-k\xb0&\x07(4\xe1\x89>\xe8\
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 $xb7P dV\x83\x9b\xb4\x93\x10\x10\x05a\xf5\x80q\x0f\xab\xfa\x1f\xdd\xb0\xd4\xa4\xc9\xe4\x8c\&\x84I$ \xba\xa5\'}\x0b@x\xc30}\xd3\xca\x9a]\xb9\xc8f\xb5\xa5\x0eFK\xbe\xb8\xed\x9c5B\x19M8\xcf\xb9,a \xe0\x8a\xa5\xe0)\x9b\x90B\x8b0\xe0/\xeb\n<\x90\x95\x14U\x8a\xa4\x97\xeaC\xd6\xa3\xd3\xba5\xc1;  $6.\x0b\x0b\x0c1\x13,b\x90W\x11\xc20\xf4+e\xc3\x16\xbd\x91\xcaB\x90\#\xb4)0\x1d\xc1\xabq1\xe4\x8$ 2\x02\x17\xa7\xfb\x83?\x17(\xd0\n\xfb\x8e:G\x96<\xa7\xdeUR\xd6\x96%4KV8D3K\xb0)9\n.\x07\xd6k\xb 96\xdb\x00\xf3\xe2\xb6\x90\xe0\x91\xbd\x8dA+n"D\x07\xa50(1\xd0FI\x95=\xd3X\xa5\x88\x80\xe5\x85?  $a \times c9 \times 96 + xba \times e10 \times 87 \times d5 + j \times c2 \times 8f \times 11 \times d0 \times b0 \times e2 \times 877 \times e9 \times c7 \times 83 \times 84 y \times 83 \times 98 \times t \times 98 \times b1 \times e10 \times e1$  $xd9F\x81V\xb3/9<\x92\xa4\xedI\xecg[Y\xe9\x1e\xc6lqr\xf7\xd5C+2\xda\xf6\xf2\xe2\xee\xca\x7fl\xa5$  $\x87/N\x7f\xd5(\xb2\xe4m2\r\x81A\xb2\x82\xbc\xecKm\x04\&|*\xc3\&\x95k\x8b1\xec`\xd3Ym\xb4\xc6\x9c$ \xf5>FJI]S\x8b\xe5#@\xd5\x0e\\\xa853\x038X:\'\xbfy\xbc\xb5q\xb4I\xe8\x9d\xb8R\xd5\x1ew\xea\x11A  $bf>x1b\\x86I\\x8b\\x17\\x179\\xd8\\x81\\xb6pwh\\x88\\xeb\\xe1\\xce\\n-@\\xdf{xe5\\xba\\x1b\\xfaiF\\x1a\\x1$  $\label{lem:dc_xd3k_q_x92_xc3_xa8_x15_xea_106.} $$ dc_xd_xe21_xea_x80oL_xb4_xfc_xe8_x93_x0e_xac_1_xea_x80oL_xb4_xfc_xe8_x93_x0e_xac_1_xea_x60_xe21_xea_x80oL_xb4_xfc_xe8_x93_x0e_xac_1_xea_x80oL_xb4_xfc_xe8_x93_x0e_xac_1_xea_x80oL_xb4_xfc_xe8_x93_x0e_xac_1_xea_x80oL_xb4_xfc_xe8_x93_x0e_xac_1_xea_x80oL_xb4_xfc_xe8_x93_x0e_xac_1_xea_x80oL_xb4_xfc_xe8_x93_x0e_xac_1_xea_x80oL_xb4_xfc_xe8_x93_x0e_xac_1_xea_x80oL_xb4_xfc_xe8_x93_x0e_xac_1_xea_x80oL_xb4_xfc_xe8_x93_x0e_xac_1_xea_x80oL_xb4_xfc_xe8_x93_x0e_xac_1_xea_x80oL_xb4_xfc_xe8_x93_x0e_xac_1_xea_x80oL_xb4_xfc_xe8_x93_x0e_xac_1_xea_x80oL_xb4_xfc_xe8_x93_x0e_xac_1_xea_x80oL_xb4_xfc_xe8_x93_x0e_xac_1_xea_x80oL_xb4_xfc_xe8_x93_x0e_xac_1_xea_x80oL_xb4_xfc_xe8_x93_x0e_xac_1_xea_x80oL_xb4_xfc_xe8_x93_x0e_xac_1_xea_x80oL_xb4_xfc_xe8_x93_x0e_xac_1_xea_x80oL_xb4_xfc_xe8_x93_x0e_xac_1_xea_x80oL_xb4_xfc_xe8_x93_x0e_xac_1_xea_x80oL_xb4_xfc_xe8_x93_x0e_xac_1_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80oL_xb4_xea_x80o$  $\xe1E\xe3b\x10 \xd5\x93\x04\\\xc9\xb6\xd5\xbb\x17\xf7\x87)\xe8\xb2XC^\xof\x04\xbdg\xce\x93\\\h$  $\x96\x86\x69\xc4\xc1\xc0\x1d;?\x0e\xb7\x11\x03\x87q\&\xfdf\x03vJ\#\xce\xee\x1bn\xb6\xe5\%\xc4\xb0$ \xfa~\x16\x82\xecU\xbb\xc7\x9e\xbc+\xd5\x1b\xdb\xb2t\xe7\x06\xa4 \x9eGc\x02{\x96\x8e\xe7k\xcf\x 9dC\x836\xf90\x810r\xc2;\xcd\x84Ha\xc2\xc8\xfah\x89\xf3\x97\x8b\x82%\xc4mP\xda\xe8\x90V4p\x04\x  $05\x85F\x98\xd4\x83\xbd\xfd\xe2\xb0\xe0\xc6\xce\xa4\xa4W\#\xe8\xe7\x1dT6\x171\x16\xdd\xa6q\x7f\x$  $e9\\x13N\\xe8F\\xe0\\xcb\\xdb\\xd3\\xbb\\xd$  $8W\xdd\xa8=\x8b\xf8\x0f\xb5\xf8\xd8zA\xe6\x077\x8aD\xf3\xf1\xbd\xb7;\xf9c+\'\x1e\xd9\xf5\xafy$  $\x1c\xe7\x10@\xb8\x05\xa1(\x06\x11\x83\x83Iu\x94\xba\x84cP \xc2:\x1e<)0\xe4\xee\x1a\#@Xl\x0en\x1$  $5\xb4\xa0\x840/\xef2\xe1\xa9\n\xc8\x8d3"\xo5\t\xa9F\xa2PN\x83\x9f\xo3\xfa\x1b+\xa8k\'\xf7\xcb\$  $x0f\x9c\xdb\xea\x96\xb2\xdf\x08e\ c\xc6\xdd0\xd1\x04\c p(\x17\xde2\x11\xc9\x98H\xff\xaa\x10\xdcd\xd$ b8\x8c\x8a\x0f\x9f\x1d\xe7xLl\x7f\x18\xa5\xd3\x99\x173YS\xc5\x9bi<m\x90\xcdb\xc1\x8d\xe5\xa2w]\  $6`\\ xb1\x10\xef\x8b\x94L\x7f\x8d+\x1d\xd0,\x12\x82\x1e\r\x80\x90\xb1q\x85\x8eU\xc2\{\xaf\x8d+\x1d\xd0,\x1d\x8d+\x1d\xd0,\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8d+\x1d\x8$ \xdf\x8e\xea!\x98\xc1\xeb\xc8\xa6Y\x9e\x1c\xb9\xd2\x11rP\x10\x08\x8c\x93.i\x8a\xb4\xc6-1\xe0T\x e3  $x0c\xc3P\x18\xce\xceM8=\xd7a\xe2\x001H\x88\x81\x01\xfc\xe5W\x96Vj\x9c\xd8~v\x1c\xd7\xaeT\x9$  $b6\x06.S\xbb\xda\xa0\xd0\xc6\x98\x0e\xac\xbc\xa6\xa6\x89\x12\x0e\xfb\xafm\x13\x04\xcb\xab\xc8$  $g\\xe7\\xa10\\x07W(\\x14\\xf2\\xcc\\Wa=\\x8c \\xcc\\x17\\xe2-\\|x9a\\x0bM\\xe3\\xe9p\\x10\\xea3k!\\xaf\\xb0\\xd8\\x8$  $e\xcd\xaa\{\xc2\x96\x88-\xf9\xa6g4q\xe5\xe9x\x1dK\xd2QiG\\ \x13T\xe3\xc6J\xb4\x83\t^e\xb6\xfc@Y\$  $x8b \times f(07) \times 99] \times b4 \times f(0x) = x61 \times f(0x) \times f(0x)$ 

#### In [15]:

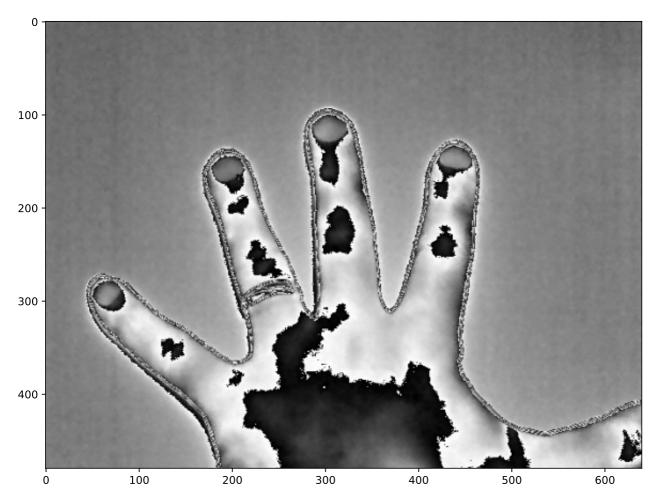
```
thermal_img_stream = io.BytesIO(thermal_img_bytes)
thermal_img_stream.seek(0)

thermal_img = Image.open(thermal_img_stream)
thermal_np = np.array(thermal_img)
```

### In [16]:

```
plt.figure(1, figsize(10,10))
plt.imshow(thermal_np, cmap="gray")
print(type(thermal_np[0,0]), np.min(thermal_np), np.max(thermal_np))
```

<class 'numpy.int32'> 56 65339



# How to transform RAW values into temperature

### In [17]:

```
args = [
    "exiftool",
    "-Emissivity",
    "-SubjectDistance",
    "-AtmosphericTemperature",
    "-ReflectedApparentTemperature",
    "-IRWindowTemperature",
    "-IRWindowTransmission",
    "-RelativeHumidity",
    "-PlanckR1",
    "-PlanckB",
    "-PlanckB",
    "-PlanckF",
    "-PlanckO",
    "-PlanckC2",
    "-j",
    "-j",
    "-",
    "-",
}
```

```
def raw2temp(
        raw,
        E=1,
        0D=1,
        RTemp=20,
        ATemp=20,
        IRWTemp=20,
        IRT=1,
        RH=50.
        PR1=21106.77,
        PB=1501,
        PF=1,
P0=-7340,
        PR2=0.012545258.
    ):
        convert raw values from the flir sensor to temperatures in C
        # this calculation has been ported to python from
        # https://github.com/gtatters/Thermimage/blob/master/R/raw2temp.R
        # a detailed explanation of what is going on here can be found there
        # constants
        ATA1 = 0.006569
        ATA2 = 0.01262
        ATB1 = -0.002276
        ATB2 = -0.00667
        ATX = 1.9
        # transmission through window (calibrated)
        emiss wind = 1 - IRT
        refl_wind = 0
        # transmission through the air
        h2o = (RH / 100) * exp(
            1.5587
            + 0.06939 * (ATemp)
             - 0.00027816 * (ATemp) ** 2
            + 0.00000068455 * (ATemp) ** 3
        tau1 = ATX * exp(-sqrt(0D / 2) * (ATA1 + ATB1 * sqrt(h2o))) + (1 - ATX) * exp(
             -\operatorname{sqrt}(OD / 2) * (ATA2 + ATB2 * \operatorname{sqrt}(h2o))
        tau2 = ATX * exp(-sqrt(0D / 2) * (ATA1 + ATB1 * sqrt(h2o))) + (1 - ATX) * exp(
            -\operatorname{sqrt}(OD / 2) * (ATA2 + ATB2 * \operatorname{sqrt}(h2o))
        )
        # radiance from the environment
        raw_refl1 = PR1 / (PR2 * (exp(PB / (RTemp + 273.15)) - PF)) - PO
        raw_refl1_attn = (1 - E) / E * raw_refl1
        raw atm1 = PR1 / (PR2 * (exp(PB / (ATemp + 273.15)) - PF)) - PO
        raw_atm1_attn = (1 - tau1) / E / tau1 * raw_atm1
        raw\_wind = PR1 / (PR2 * (exp(PB / (IRWTemp + 273.15)) - PF)) - PO
        raw_wind_attn = emiss_wind / E / tau1 / IRT * raw_wind
        raw_refl2 = PR1 / (PR2 * (exp(PB / (RTemp + 273.15)) - PF)) - PO
        raw_refl2_attn = refl_wind / E / tau1 / IRT * raw_refl2
raw_atm2 = PR1 / (PR2 * (exp(PB / (ATemp + 273.15)) - PF)) - PO
        raw_atm2_attn = (1 - tau2) / E / tau1 / IRT / tau2 * raw_atm2
        raw obj = (
            raw / E / tau1 / IRT / tau2
             - raw_atm1_attn
            raw_atm2_attn
            - raw wind attn
             - raw_refl1_attn
             raw_refl2_attn
        # temperature from radiance
        temp celcius = PB / np.log(PR1 / (PR2 * (raw obj + P0)) + PF) - 273.15
        return temp_celcius
```