

# Model Based Testing

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Dr Michael Foster

*Based on material from Professor Rob Hierons*

- Formal models of systems (FSMs)

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- Testing from finite state machines

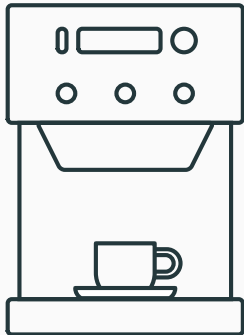
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  - The *W* method

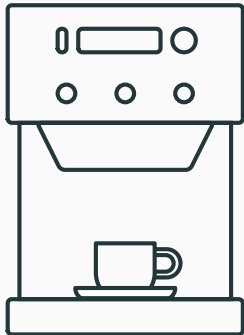
## Motivating Example - Simple Drinks Machine



- Select a drink

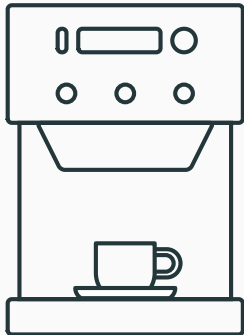


# Motivating Example - Simple Drinks Machine



- Select a drink
- Insert coins

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- Select a drink
- Insert coins
- Press “vend” to dispense drink

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- Generate tests according to code components

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# Formal Models of Systems

There are lots of different modelling notations (Z, B, state machines)

We will introduce MBT with state machines

An FSM (Mealy machine) is a six tuple  $(S, s_0, X, Y, \delta, \lambda)$  where

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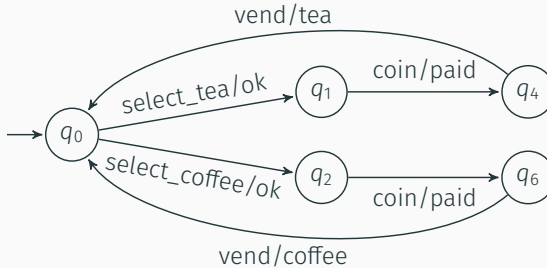
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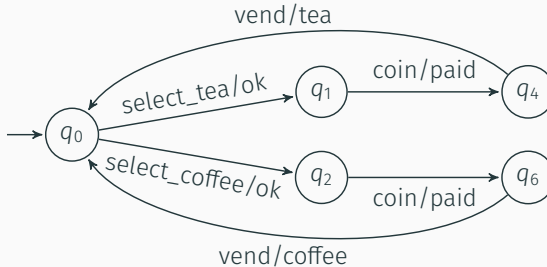
# FSM of the Drinks Machine



- We give the system inputs and it changes state and gives us outputs

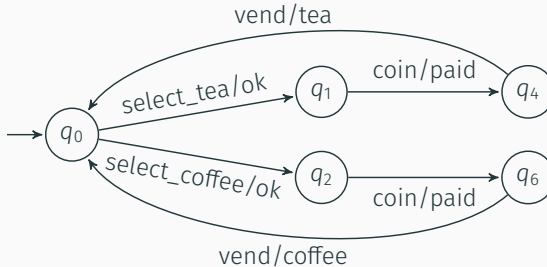


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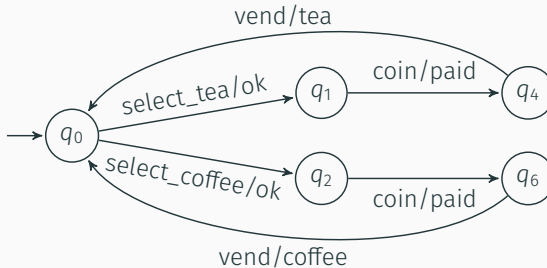
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  - inputs `select_tea`, `coin`, `vend`, gives us outputs `ok`, `paid`, `tea`
  - Machine follows path  $q_0 \rightarrow q_1 \rightarrow q_4 \rightarrow q_0$

# Terminology (sorry!)

We will focus on FSM testing with *deterministic*, *minimal*, and *completely specified* models

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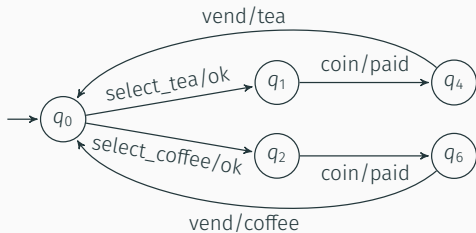
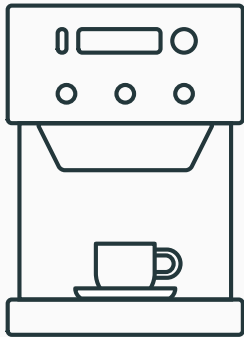
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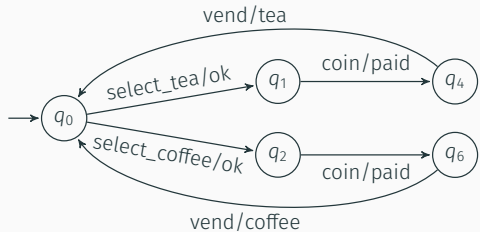
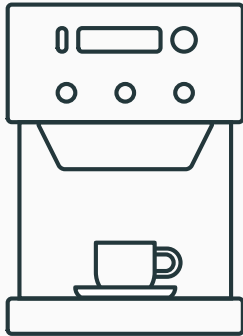


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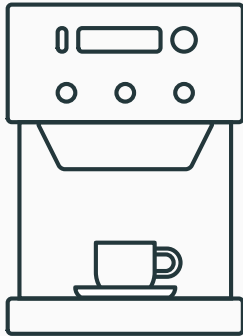
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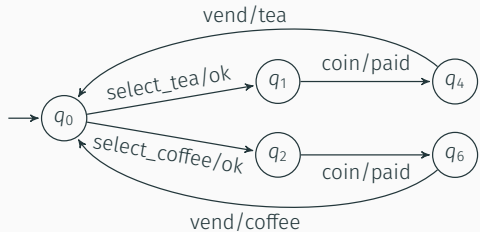


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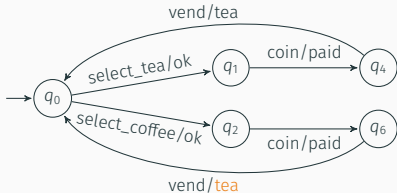


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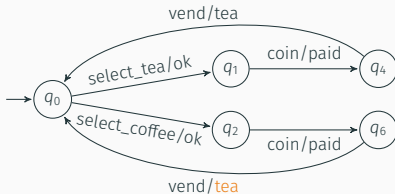


- Assume the software behaves like an FSM model
- Submit inputs to the FSM and software in parallel
- Observe and compare the outputs

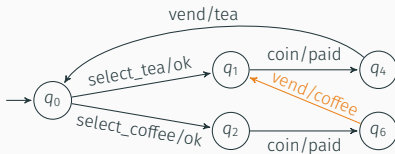
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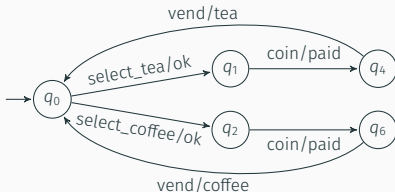


**State transfer faults:** A transition goes to the wrong state



# Transition Tour

Assume no state transfer faults, then we can test by just executing every transition



The input sequence *select\_tea, coin, vend, select\_coffee, coin, vend* will do that for us

We validate that the output sequence is *ok, paid, tea, ok, paid, coffee*

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- Output faults may also be masked
- We want to explicitly check for state transfer faults

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## Challenges

**Controllability:** How do we get the FSM to  $q_i$ ?

**Observability:** How do we know the FSM is in  $q_j$ ?



## Controllability

Find a sequence that gets the *specification* to the desired state.

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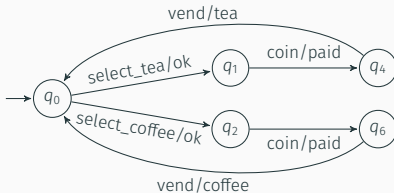
Characterise states in terms of the I/O actions they can perform:

- Distinguishing sequences
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- Characterising set

# Distinguishing Sequences

A distinguishing sequence is an input sequence that produces a different output for **each state**.

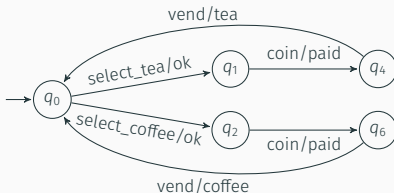
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Yes! (assuming we know when an input has been refused)

*select\_tea, coin, vend*

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  - $\bar{y}$  represents a *sequence* of outputs
- Not all FSMs have these either!

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- There are polynomial time algorithms to generate  $W$  sets
- We can minimise every FSM

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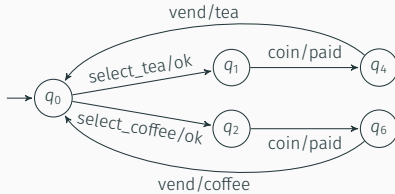
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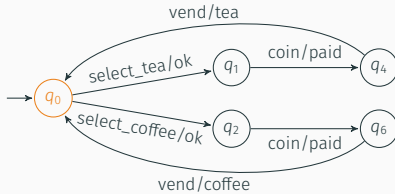
A *state cover*  $V$  is a set of input sequences such that each state of an FSM  $M$  is reached from  $s_0$  by a sequence from  $V$ , and  $V$  also contains the empty input sequence.

# The $W$ Method for Drinks



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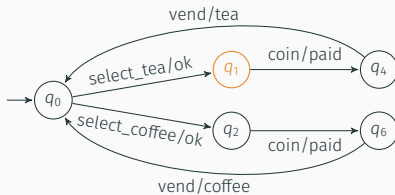


$W = \{[select\_tea, coin, vend]\}$

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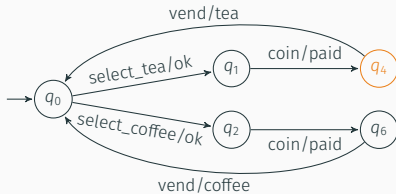
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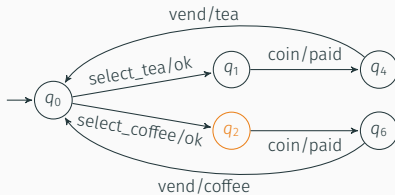
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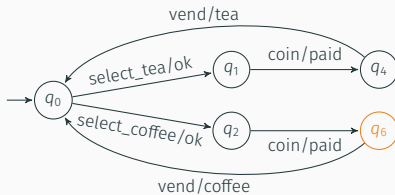
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# Applying the $W$ Method

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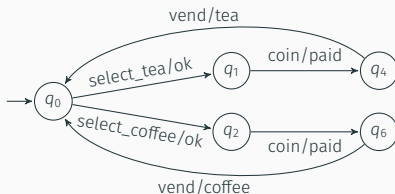
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Make sure you reset before each sequence!



# Applying the $W$ Method to Drinks

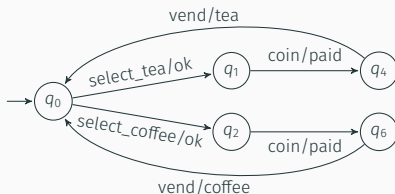


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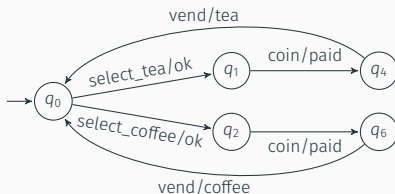


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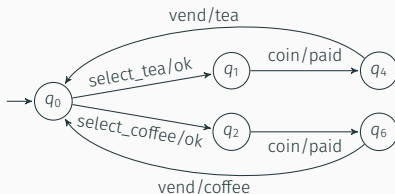


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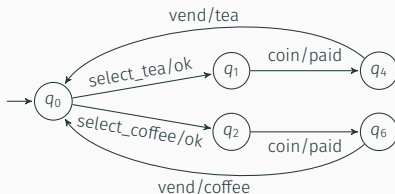


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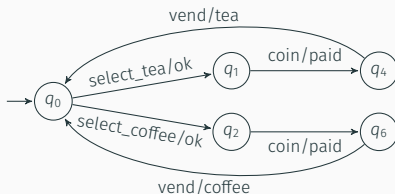


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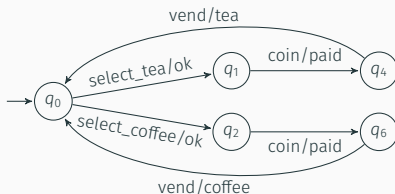


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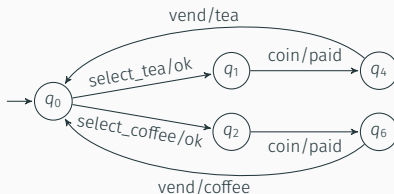


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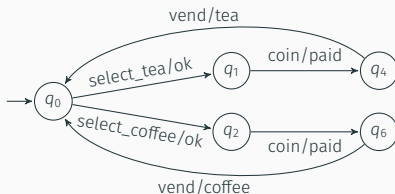
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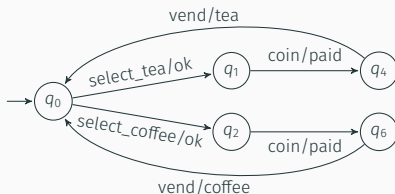


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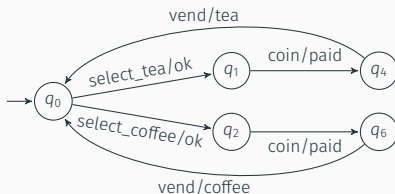


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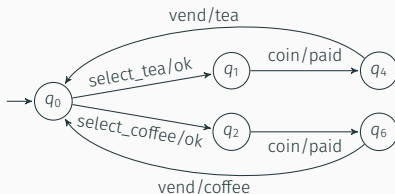


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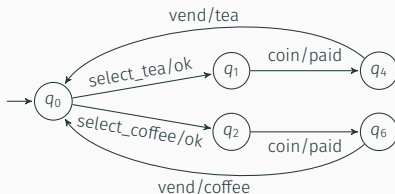


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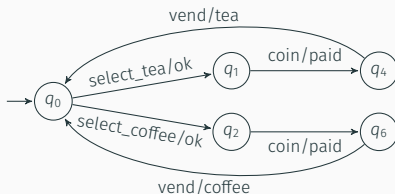


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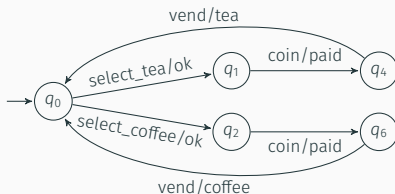


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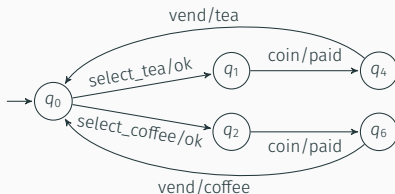


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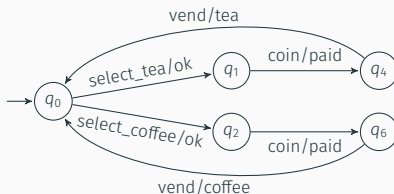
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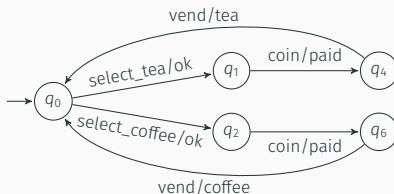


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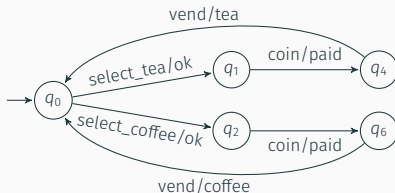


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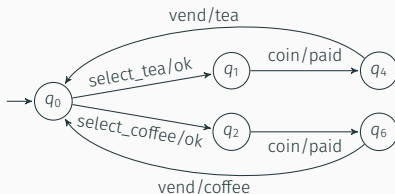


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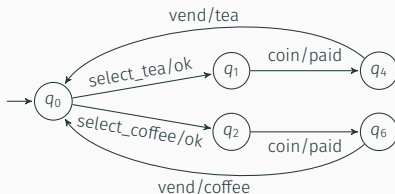


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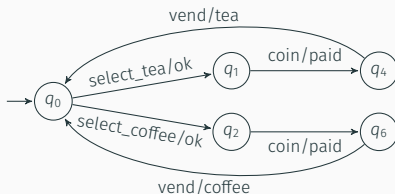


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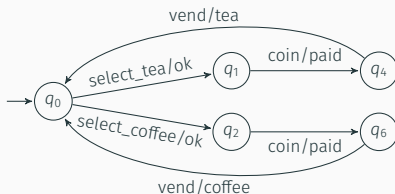


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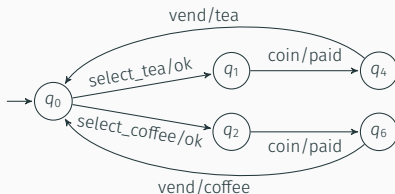


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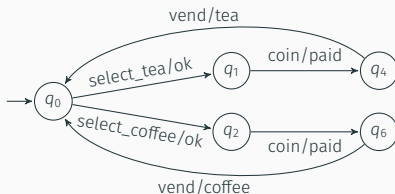
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