Work-out Problems

Study tip: Show all your work!

Exercise 1. Let x denote the input variable and y denote the output variable. Determine which of the following gives y as a function of x.

1.
$$\{(-1,0), (0,-3), (2,-3), (3,0), (4,5)\}$$

2.
$$\{(6,10), (-7,3), (0,4), (6,-4)\}$$

3.
$$y = x^2 + 1$$

4.
$$y^2 = x + 1$$

$$5. \ x^2 + y^2 = 4$$

Exercise 2. Given $f(x) = -6x^2 + ax - 7$ and $g(x) = -x^2 - \frac{4}{5}x$ evaluate each of the following.

- 1. f(-10)
- 2. f(0)
- 3. f(t)
- 4. f(t+1)
- 5. f(x+1)
- 6. f(x) + 1
- $7. \ g(x+h)$
- 8. $g(x^2 5)$

Exercise 3. Express the following sets of numbers using interval notation.

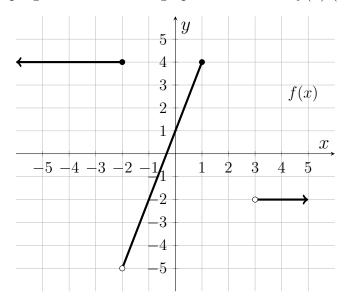
1.
$$\{x \mid x \ge \frac{1}{2} \text{ and } x \ne \pm \sqrt{7}\}$$

2.
$$\{x \mid \frac{11}{5} > x \text{ or } \frac{11}{5} \le x < 26\}$$

3.
$$\{x \mid x < -4 \text{ and } 2x + 5 > 21\}$$

4.
$$\{x \mid x \ge -3 \text{ and } x \le 0\} \cup \{(x+2)(x-5) \ne 0 \text{ and } 0 < x \le 6\} \cup \{x > 8 \text{ and } x \ge 10\}$$

Exercise 4. The graph given below is the graph of a function f(x) (why?).



Determine the following.

- 1. The domain of f (in interval notation)
- 2. The range of f (in interval notation)
- 3. f(-3)
- 4. f(-2)
- 5. f(2)
- 6. All zeros of f
- 7. Where f(x) = -2

Exercise 5. Anakin Skywalker, the consultant for the company "It's Lit!" determines that if the company sells x lightsabers, their demand equation (where x is the number of lightsabers demanded and p is the price in dollars) is the function $p(x) = -\frac{1}{50}x + 1000$.

1. Determine the company's revenue equation.

2. Find the number of lightsabers that should be produced to yield a maximum revenue. Round to the nearest whole number, if necessary. Answer with a complete sentence, using the correct units.

3. Calculate the maximum revenue of the company in dollars. Round your answer to 2 decimal places, if necessary. Answer with a complete sentence, using the correct units.

4. Find the price at which each lightsaber should be sold to maximize their revenue. Round your answer to 2 decimal places, if necessary. Answer with a complete sentence, using the correct units.

5. The company's cost equation is given by $C(x) = \frac{1568}{5}x + 1{,}139{,}950$. How many lightsabers should Anakin sell to break even?

Exercise 6. A degree 3 polynomial $f(x) = ax^3 + bx^2 + cx + d$ has y-intercept (0, -4) and exactly three real zeros at x = 8, x = -3, and $x = \frac{1}{2}$.

- 1. Find the equation of f.
- 2. Describe the end behavior of the graph of f(x) (both symbolically and with a quick sketch).
- 3. What is the domain of f?

Exercise 7. Determine if each of the following is a polynomial. If it is a polynomial, specify its degree, leading coefficient, end behavior, and domain. If it is not a polynomial, state a reason for your answer.

1.
$$f(x) = 3x^{1/2} + x\sqrt{2}$$

2.
$$q(x) = x + 2x^{-1}$$

3.
$$h(x) = x^3 + 2x + \frac{\sqrt{6}}{7}$$

4.
$$j(x) = 130x - \frac{5^{2/3}}{4}\sqrt{3}x^{23} + 17x^{12}$$

5.
$$k(x) = ax^6 + bx^{58} - cx^5 + dx^{11} + 18x^2$$
 where $a < 0, b < 0, c < 0, and $d > 0$.$

Exercise 8. Given $y = -5x^2 + 10x - 4$, without graphing determine the vertex, axis of symmetry, maximum value, minimum value, domain, range, y-intercept, and x-intercept(s) of the function.

Exercise 9. Let $f(x) = -x^2 + 3x$. Find and simplify the following completely.

$$\frac{f(x+h) - f(x)}{h}$$

This expression is called a <u>difference quotient</u>. This important concept is introduced in Section 5.2 and we will see it throughout Chapter 5.

Multiple Choice Problems

Study tip: Write out all your work when you complete the multiple-choice problems.

Multiple Choice 1. It has been determined that the revenue function for a stapler is given by $R(x) = -0.025x^2 + 8.25x$ and the cost function is given by C(x) = 1.25x + 500 where R(x) and C(x) are in dollars and x represents the number of staplers produced and sold. What is the selling price of the stapler when the profit is maximized? (Answers are given to the nearest penny.)

- (a) \$140.00
- (b) \$4.75
- (c) \$4.13
- (d) \$10.00
- (e) None of these

Multiple Choice 2. What is the range of the function

$$h(x) = -(x-3)^2 + 18 ?$$

- (a) $(-\infty, \infty)$
- (b) $[18, \infty)$
- (c) $(-\infty, 3]$
- (d) $(-\infty, 18]$
- (e) $(-\infty, 18)$

Multiple Choice 3. Find all the exact zeros of the quadratic function:

$$f(x) = 10x^2 - 3x - 4$$

- (a) $x = \frac{4}{5}, -\frac{1}{2}$
- (b) $x = -\frac{4}{5}, \frac{1}{2}$
- (c) $x = \frac{3}{20}$
- (d) x = -4
- (e) None of the given answer choices are correct.

Multiple Choice 4. Let h be the function $h(x) = -5x^8 + 85x^7 + 45x^6 - 6345x^5 + 15120x^4 + 121500x^3 - 349920x^2$ which factors into:

$$h(x) = -5(x-0)^{2}(x+6)^{2}(x-3)(x-9)^{2}(x-6).$$

Which of the following statements is **FALSE**?

- (a) The domain of the function is $(-\infty, \infty)$.
- (b) h(9) = 0
- (c) The function h(x) is a polynomial.
- (d) $h(x) \to \infty$ as $x \to -\infty$.
- (e) The function h(x) has zeros at x = -6, 0, 3, 6, 9.

Multiple Choice 5. Elena's Biking Company manufactures and sells bikes. Each bike costs \$40 to make and the company's fixed costs are \$5000. Elena knows that the company's cost is given by a linear function, and that the unit price (in dollars) of each bike is a linear function of the number of bikes sold. Based on her sales data, when the unit price of a bike is \$280, she knows that 10 bikes will be sold, and if the unit price drops by \$60, then 40 bikes will be sold. Which of the following statements is FALSE? (All answers are rounded to the nearest whole number).

- (a) Elena's cost equation is given by C(x) = 40x + 5000, x denotes the number of bikes sold
- (b) The graph of the profit equation is a parabola that opens downward.
- (c) (x, p) = (40, 60) is a point on the graph of the linear demand function where the unit price p is a function of number of bikes sold, x
- (d) Elena will maximize her profit if 65 bikes are sold
- (e) To break even, Elena should sell approximately 23 bikes or 107 bikes.