

9/04/20

Assignment

Ans

### ① Master's Theorem

If  $f(n)$  and  $\Theta(n^d)$  are  $f(n) = c n^d$  where  $d \geq 0$

Recurrence  $T(n) = aT(n/b) + f(n)$  (then)

$$T(n) = \begin{cases} \Theta(n^d) & \text{if } a < b^d \\ \Theta(n^d \log n) & \text{if } a = b^d \\ \Theta(n^{\log_b a}) & \text{if } a > b^d \end{cases}$$

$$T(n) = 8T(n/2) + 1000n^2$$

$$T(n) = aT(n/b) + f(n)$$

$$a = 8, b = 2 \quad f(n) = c n^d$$

$$= 1000 n^2$$

$$c = 1000, d = 2$$

$$\text{Since } a > b^d$$

$$\text{i.e. } 8 > 2^2$$

Master theorem case ③ is fulfilled

$$T(n) = \Theta(n^{\log_b a})$$

$$= \Theta(n^{\log_2 8})$$

$$\boxed{T(n) = \Theta(n^3)}$$

$$\textcircled{2} \quad T(n) = 2T(n/2) + n^2$$

$$a = 2, b = 2, c = 1, d = 2$$

$$\text{Since } a < b^d$$

$$2 < 2^2$$

$$\text{Case ① } T(n) = \Theta(n^d)$$

$$T(n) = \Theta(n^2)$$



$$3) \quad T(n) = 2T(n/2) + 10n$$

$$a = 2, \quad b = 2, \quad c = 10, \quad d = 1$$

$$\text{since } a = b^d$$

$$2 = 2^1$$

case ②

$$\text{i.e. } T(n) = \Theta(n^d \log n)$$

$$T(n) = \Theta(n \log n)$$

x

x