Lab 4: Scikit Learn, Classification and Clustering

Deadline Friday 4/29/22 11:59 pm

scikit-learn is a popular machine learning package that contains a variety of models and tools.

All objects within scikitt-learn share a uniform common basic API consisting of 3 interfaces: an *estimator* interface for building and fitting models, a *predictor* interface for making predictions, and a *transformer* interface for converting data.

The *estimator* interface defines object mechanism and a fit method for learning a model from training data. All supervised and unsupervised learning algorithms are offered as objects implementing this interface. Other machine learning tasks such as *feature extraction, feature selection,* and *dimensionality reduction* are provided as *estimators*.

For more information, check the scikit-learn API paper: [https://arxiv.org/pdf/1309.0238v1.pdf]

The general form of using models in scikit-learn:

```
clf = someModel( )
  clf.fit(x_train , y_tain)
For Example:

clf = LinearSVC( )
  clf.fit(x_train , y_tain)
```

The *predictor* adds a predict method that takes an array x_test and produces predictions for x_test, based on the learned parameters of the *estimator*. In supervised learning, this method typically return predicted labels or values computed by the model. Some unsupervised learning estimators may also implement the predict interface, such as **k-means**, where the predicted values are the cluster labels.

```
clf.predict(x_test)
```

transform method is used to modify or filter data before feeding it to a learning algorithm. It takes some new data as input and outputs a transformed version of that data. Preprocessing, feature selection, feature extraction and dimensionality reduction algorithms are all provided as *transformers* within the library.

This is usually done with **fit_transform** method. For example:

```
PCA = RandomizedPCA (n_components = 2)
x_train = PCA.fit_transform(x_train)
```

```
x test = PCA.fit transform(x test)
```

In the example above, we first **fit** the training set to find the PC components, then they are transformed.

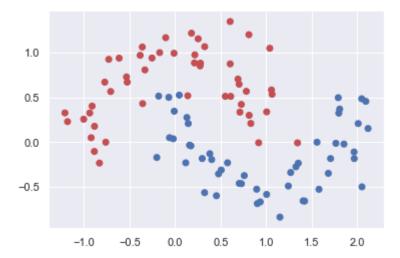
We can summarize the estimator as follows:

- In all estimators
 - model.fit() : fit training data. In supervised learning, fit will take two parameters: the data x and labels y. In unsupervised learning, fit will take a single parameter: the data x
- In supervised estimators
 - model.predict() : predict the label of new test data for the given model. Predict takes one parameter: the new test data and returns the learned label for each item in the test data
 - model.score() : Returns the score method for classification or regression methods.
- In unsupervised estimators
 - model.transform(): Tranform new data into new basis. Transform takes one parameter: new data and returns a new representation of that data based on the model

Classification: SVM

Support Vector Machines (SVM) are among the most useful and powerful supervised learning algorithm. Here we are going to look at an example of using SVM models in scikit-learn. Then, it will be your turn to try this model.

```
In [2]:
         %matplotlib inline
         import matplotlib.pyplot as plt
         import seaborn as sns; sns.set()
         import numpy as np
In [3]:
         from sklearn.model selection import train test split
         # Import make moons from scikit learn to generate synthetic data
         from sklearn.datasets import make moons
         # 2d classification dataset
         Xs , ys = make_moons( n_samples = 100, noise = 0.2 , random_state = 0)
         # train-test split
         Xs_train , Xs_test, ys_train, ys_test = train_test_split(Xs, ys , test_size = 0.15 )
         #plot the data
         colors = np.array(['r', 'b'])
         plt.scatter(Xs[:,0] , Xs[:,1] ,c = colors[ys] )
         plt.show()
```



We will perform both linear and nonlinear SVM on this synthetic dataset:

```
In [24]:

def meshGrid (x , y , h):
    '''x is data for x-axis meshgrid
    y is data for y-axis meshgrid
    h is stepsize
    ...
    x_min, x_max = x.min() - 1 , x.max() + 1
    y_min, y_max = y.min() - 1 , y.max() + 1
    xx, yy = np.meshgrid(np.arange(x_min, x_max, h), np.arange(y_min, y_max, h))
    return xx , yy

In []:

In [5]: #Import SVM
```

```
#Import SVM
from sklearn import svm
from matplotlib.colors import ListedColormap
from sklearn import metrics
cmap_light = ListedColormap(['#FBBBB9', '#82CAFF'])
cmap_bold = ListedColormap(['#CA226B', '#2B65EC'])
cmap_test = ListedColormap(['#8E35EF', '#659EC7'])
cmap predict = ListedColormap(['#FCDFFF', '#E0FFFF'])
# clf1 is a linear svm classifier
clf1 = svm.SVC(kernel = 'linear')
# Fit data
clf1.fit(Xs_train, ys_train)
# Predict
ys_predict = clf1.predict(Xs_test)
#Display the outcome of classification
print(metrics.classification_report(ys_test, ys_predict))
print(metrics.confusion_matrix(ys_test, ys_predict))
```

```
# Display the svm
xx , yy = meshGrid(Xs[:,0], Xs[:,1], 0.01)

Z = Clf1.predict(np.c_[xx.ravel(), yy.ravel()])
Z = Z.reshape(xx.shape)

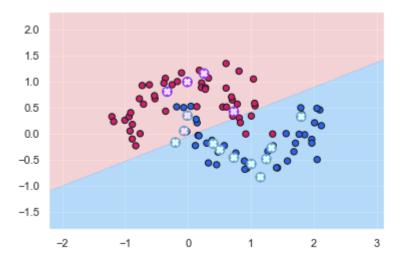
plt.figure()
plt.contourf(xx, yy, Z, cmap=cmap_light ,levels=[-1, 0, 1] ,alpha = 0.5)

# For plotting all data use the following line
#plt.scatter(Xs[:, 0], Xs[:, 1], c=ys, cmap=cmap_bold, edgecolor='k', s=50)

# For plotting train and test and prediction separatley
plt.scatter(Xs_train[:, 0], Xs_train[:, 1], c=ys_train, cmap=cmap_bold,edgecolor='k', s
plt.scatter(Xs_test[:, 0], Xs_test[:, 1], alpha=1.0,c = ys_test, cmap=cmap_test,linewid
plt.scatter(Xs_test[:, 0], Xs_test[:, 1], alpha=1.0,c = ys_predict, cmap=cmap_predict ,
plt.xlim(xx.min(), xx.max())
plt.ylim(yy.min(), yy.max())

plt.show()
```

support	f1-score	recall	precision	
4	0.80	1.00	0.67	0
11	0.90	0.82	1.00	1
15	0.87	0.87	0.91	avg / total
				[[4 0] [2 9]]

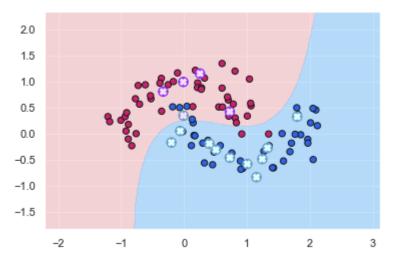


Now we apply a non-linear sym classifier

```
In [6]: # clf2 is a nonlinear svm classifier
    clf2 = svm.SVC(kernel = 'rbf')
# Fit data
```

```
clf2.fit(Xs_train, ys_train)
# Predict
ys_predict2 = clf2.predict(Xs_test)
#Display the outcome of classification
print(metrics.classification_report(ys_test, ys_predict2))
print(metrics.confusion matrix(ys test, ys predict2))
# Display the svm
xx, yy = meshGrid(Xs[:,0], Xs[:,1], 0.01)
Z = clf2.predict(np.c_[xx.ravel(), yy.ravel()])
Z = Z.reshape(xx.shape)
plt.figure()
plt.contourf(xx, yy, Z, cmap=cmap_light ,levels=[-1, 0, 1] ,alpha = 0.5)
# For plotting all data use the following line
#plt.scatter(Xs[:, 0], Xs[:, 1], c=ys, cmap=cmap_bold, edgecolor='k', s=50)
# For plotting train and test and prediction separatley
plt.scatter(Xs_train[:, 0], Xs_train[:, 1], c=ys_train, cmap=cmap_bold,edgecolor='k', s
plt.scatter(Xs_test[:, 0], Xs_test[:, 1], alpha=1.0,c = ys_test, cmap=cmap_test,linewid
plt.scatter(Xs_test[:, 0], Xs_test[:, 1], alpha=1.0,c = ys_predict2, cmap=cmap_predict
plt.xlim(xx.min(), xx.max())
plt.ylim(yy.min(), yy.max())
plt.show()
```

	precision	recall	f1-score	support
0 1	0.80 1.00	1.00 0.91	0.89 0.95	4 11
avg / total	0.95	0.93	0.94	15
[[4 0] [1 10]]				



CS418-Lab4 4/29/22, 9:11 PM

SVM on Wine quality dataset

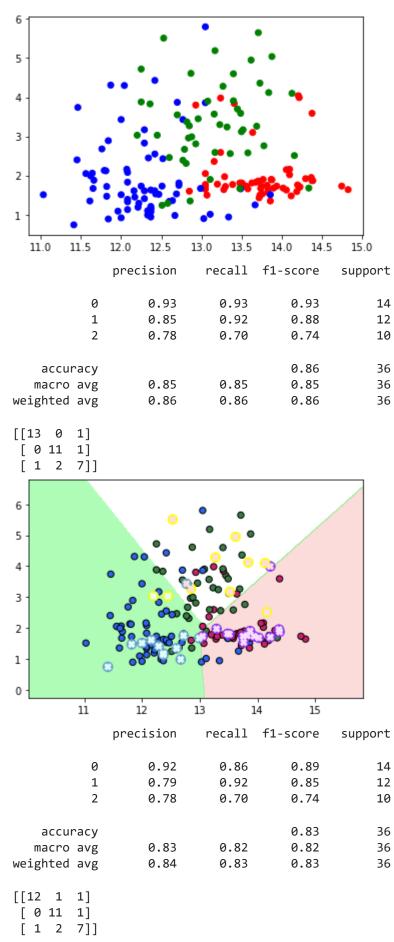
Exercise 4.1 (30 pts)

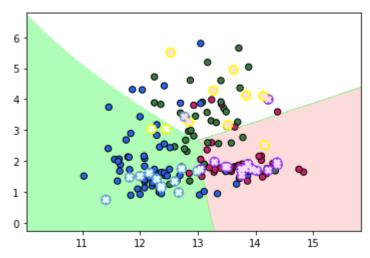
Now it's your turn to work with SVM. The wine data set is loaded below. You can learn more about the dataset by using datasett.DESCR. Here, you need to work with the first two features to train your model.

- Select the first two features for your X
- Split the dataset in two sets of training and testing data. Use 80% of the data for training and 20% for testing
- Perform linear and non-linear SVM on the dataset
- Display the classification report and accuracy for both models

```
In [100...
          from sklearn.datasets import load_wine
          import pandas as pd
          import seaborn as sns
          import matplotlib.pyplot as plt
          import numpy as np
          from sklearn.model_selection import train_test_split
          from sklearn import svm
          from matplotlib.colors import ListedColormap
          from sklearn import metrics
          Xwine_full , ywine = load_wine(return_X_y = True)
          #Your code here
          Xc = Xwine full [:, :2]
          X_train,X_test,y_train,y_test = train_test_split(Xc, ywine, test_size = 0.20)
          colors = np.array(['r' , 'b', 'g'])
          plt.scatter(Xc[:,0] , Xc[:,1] ,c = colors[ywine])
          plt.show()
          cmap_light = ListedColormap(['#FBBBB9', '#82CAFF', '#5EFB6E'])
          cmap_bold = ListedColormap(['#CA226B', '#2B65EC', '#387C44'])
          cmap_test = ListedColormap(['#8E35EF', '#659EC7', '#FFFF00'])
          cmap_predict = ListedColormap(['#FCDFFF', '#E0FFFF', '#FFE0E0'])
          # clf1 is a linear svm classifier
          clf1 = svm.SVC(kernel = 'linear')
          # Fit data
          clf1.fit(X train, y train)
          # Predict
          ys_predict = clf1.predict(X_test)
          #Display the outcome of classification
          print(metrics.classification_report(y_test, ys_predict))
          print(metrics.confusion_matrix(y_test, ys_predict))
          # Display the svm
```

```
xx, yy = meshGrid(Xc[:,0], Xc[:,1], 0.01)
Z = clf1.predict(np.c [xx.ravel(), yy.ravel()])
Z = Z.reshape(xx.shape)
plt.figure()
plt.contourf(xx, yy, Z, cmap=cmap_light ,levels=[-1, 0, 1] ,alpha = 0.5)
# For plotting all data use the following line
#plt.scatter(Xs[:, 0], Xs[:, 1], c=ys, cmap=cmap_bold, edgecolor='k', s=50)
# For plotting train and test and prediction separatley
plt.scatter(X train[:, 0], X train[:, 1], c=y train, cmap=cmap bold,edgecolor='k', s=40
plt.scatter(X_test[:, 0], X_test[:, 1], alpha=1.0,c = y_test, cmap=cmap_test,linewidth=
plt.scatter(X_test[:, 0], X_test[:, 1], alpha=1.0,c = ys_predict, cmap=cmap_predict ,li
plt.xlim(xx.min(), xx.max())
plt.ylim(yy.min(), yy.max())
plt.show()
clf2 = svm.SVC(kernel = 'rbf')
# Fit data
clf2.fit(X_train, y_train)
# Predict
ys predict2 = clf2.predict(X test)
#Display the outcome of classification
print(metrics.classification_report(y_test, ys_predict2))
print(metrics.confusion_matrix(y_test, ys_predict2))
# Display the svm
xx1, yy1 = meshGrid(Xc[:,0], Xc[:,1], 0.01)
Z1 = clf2.predict(np.c_[xx1.ravel(), yy1.ravel()])
Z1 = Z1.reshape(xx1.shape)
plt.figure()
plt.contourf(xx1, yy1, Z1, cmap=cmap light ,levels=[-1, 0, 1] ,alpha = 0.5)
# For plotting all data use the following line
#plt.scatter(Xs[:, 0], Xs[:, 1], c=ys, cmap=cmap_bold, edgecolor='k', s=50)
# For plotting train and test and prediction separatley
plt.scatter(X_train[:, 0], X_train[:, 1], c=y_train, cmap=cmap_bold,edgecolor='k', s=40
plt.scatter(X_test[:, 0], X_test[:, 1], alpha=1.0,c = y_test, cmap=cmap_test,linewidth=
plt.scatter(X_test[:, 0], X_test[:, 1], alpha=1.0,c = ys_predict2, cmap=cmap_predict ,1
plt.xlim(xx1.min(), xx1.max())
plt.ylim(yy1.min(), yy1.max())
plt.show()
```





Exercise 4.2 (10 pts)

Scaling features is another step that can affect the performance of your classifier. For the wine data, scale the features using StandardScaler and perform linear SVM. Display the classification report and accuracy. Did scaling data affect the classifier performance?

Yes, Scaling data made the performance better and it gave the higher accuracy output at some extent.

```
from sklearn.preprocessing import StandardScaler
scaler = StandardScaler()

#Your code here

X_train_new = scaler.fit_transform(X_train)
X_test_new = scaler.transform(X_test)

# clf1 is a linear svm classifier
clf3 = svm.SVC(kernel = 'linear')

# Fit data
clf3.fit(X_train_new, y_train)

# Predict
ys_predict3 = clf3.predict(X_test_new)

#Display the outcome of classification
print(metrics.classification_report(y_test, ys_predict3))
print(metrics.confusion_matrix(y_test, ys_predict3))
```

	precision	recall	f1-score	support
•	2 22	4 00		
0	0.93	1.00	0.97	14
1	0.85	0.92	0.88	12
2	0.88	0.70	0.78	10
accuracy			0.89	36
macro avg	0.88	0.87	0.87	36

```
weighted avg 0.89 0.89 0.88 36

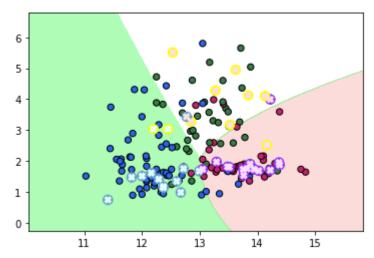
[[14 0 0]
  [ 0 11 1]
  [ 1 2 7]]
```

Exercise 4.3 (10 pts)

scikit-learn has many other classifiers. Pick another classifier of your choice (KNN, DecisionTree, NaiveBayes, ...) and apply it to the wine dataset. Display the classification report and accuracy.

```
In [102...
          #Your code goes here
          from sklearn.naive bayes import GaussianNB
          model = GaussianNB()
          model.fit(X_train, y_train)
          model predict = model.predict(X test)
          #Display the outcome of classification
          print(metrics.classification_report(y_test, model_predict))
          print(metrics.confusion matrix(y test, model predict))
          # Display the svm
          xx4, yy4 = meshGrid(Xc[:,0], Xc[:,1], 0.01)
          Z4 = model.predict(np.c_[xx4.ravel(), yy4.ravel()])
          Z4 = Z4.reshape(xx4.shape)
          plt.figure()
          plt.contourf(xx4, yy4, Z4, cmap=cmap light , levels=[-1, 0, 1] , alpha = 0.5)
          # For plotting all data use the following line
          #plt.scatter(Xs[:, 0], Xs[:, 1], c=ys, cmap=cmap_bold, edgecolor='k', s=50)
          # For plotting train and test and prediction separatley
          plt.scatter(X_train[:, 0], X_train[:, 1], c=y_train, cmap=cmap_bold,edgecolor='k', s=40
          plt.scatter(X_test[:, 0], X_test[:, 1], alpha=1.0,c = y_test, cmap=cmap_test,linewidth=
          plt.scatter(X_test[:, 0], X_test[:, 1], alpha=1.0,c = model_predict, cmap=cmap_predict
          plt.xlim(xx4.min(), xx4.max())
          plt.ylim(yy4.min(), yy4.max())
          plt.show()
```

```
precision
                           recall f1-score
                                              support
           0
                   0.93
                             0.93
                                       0.93
                                                   14
           1
                             0.92
                                       0.88
                   0.85
                                                   12
                   0.78
                             0.70
                                       0.74
                                                   10
                                       0.86
                                                   36
    accuracy
                   0.85
                             0.85
                                       0.85
                                                   36
   macro avg
weighted avg
                   0.86
                             0.86
                                       0.86
                                                   36
[[13 0 1]
 [ 0 11 1]
 [1 2 7]]
```



Clustering

You have already seen an example of clustering using scikit-learn in lecture. In this section, you will apply KMeans algorithm to the wine dataset.

Exercise 4.4 (30 pts)

- First choose the first two features and apply kmeans clustering.
- Display cluster evaluation metrics homogeneity_score and completeness_score (both belong to sklearn.metrics)
- Plot the clusters and centroids. You have the "ground truth" or labels of your data points, your
 plot should create a meshgrid to display the decision boundary of your model, and add the
 datapoints and their true labels. (This is to observe how good your model performs on the
 data)

Note: For displaying decision boundaries and data points follow these steps:

- 1. Use meshGrid function to get the mesh for your attributes
- 2. Obtain labels for each point in mesh and reshape it. (Z = kmeans.predict(....))
- 3. Put the results into a color plot
 - Plot the colormesh --> plt.pcolormesh
 - Plot your data points --> plt.scatter
 - Plot the centroids --> plt.scatter
 - Set titles, x and y ranges
 - plt.show()

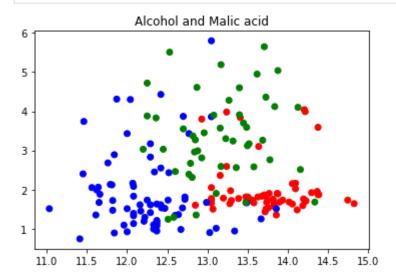
```
from sklearn.cluster import KMeans
    from sklearn.metrics.cluster import completeness_score
    from sklearn.metrics.cluster import homogeneity_score

Xwine_full , ywine = load_wine(return_X_y = True)

Xc = Xwine_full [:, :2]

colormap = np.array(['r' , 'b' , 'g'])
    plt.scatter(Xc[:,0],Xc[:,1] , c = colormap[ywine])
```

```
plt.title("Alcohol and Malic acid")
plt.show()
```



```
# Your code here
cmap_light = ListedColormap(['#FBBBB9', '#82CAFF', '#5EFB6E'])
cmap_bold = ListedColormap(['#CA226B', '#2B65EC', '#387C44'])
cmap_test = ListedColormap(['#8E35EF', '#659EC7', '#FFFF00'])
cmap_predict1 = ListedColormap(['#8105ED', '#ED05CA', '#FA0505'])

# Run k-means, Number of clusters = 2
y1_predict = KMeans(n_clusters = 3, random_state = 170).fit_predict(Xc)

#plot
print("Completness Score: ",completeness_score(ywine, y1_predict))
print("Homogeneity Score: ",homogeneity_score(ywine, y1_predict))
```

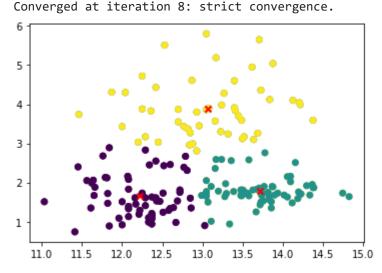
Completness Score: 0.4080524820388842 Homogeneity Score: 0.4103507797096971

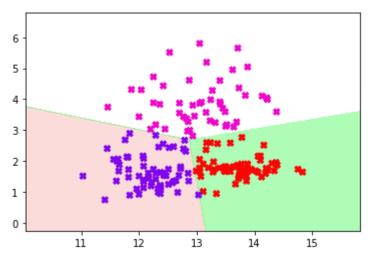
```
In [105...
          kmeans = KMeans(n_clusters = 3, init ='random', random_state = 200, verbose=True).fit(X
          plt.scatter(Xc[:,0], Xc[:,1], c =y1_predict)
          plt.scatter(Xc[:,0], Xc[:,1], c= kmeans.labels_)
          plt.scatter(kmeans.cluster_centers_[:,0],kmeans.cluster_centers_[:,1],c = 'r',marker ='
          plt.show()
          xx5, yy5 = meshGrid(Xc[:,0], Xc[:,1], 0.01)
          Z5 = kmeans.predict(np.c_[xx5.ravel(), yy5.ravel()])
          Z5 = Z5.reshape(xx4.shape)
          plt.figure()
          plt.contourf(xx5, yy5, Z5, cmap=cmap_light ,levels=[-1, 0, 1] ,alpha = 0.5)
          # For plotting all data use the following line
          #plt.scatter(Xs[:, 0], Xs[:, 1], c=ys, cmap=cmap_bold, edgecolor='k', s=50)
          # For plotting train and test and prediction separatley
          plt.scatter(Xc[:, 0], Xc[:, 1], alpha=1.0,c = y1 predict, cmap=cmap predict1 ,linewidth
          plt.xlim(xx5.min(), xx5.max())
          plt.ylim(yy5.min(), yy5.max())
```

plt.show()

Initialization complete Iteration 0, inertia 151.7837000000001 Iteration 1, inertia 99.30364833650812 Iteration 2, inertia 96.21666479021775 Iteration 3, inertia 95.60041513507419 Iteration 4, inertia 95.55394205616612 Converged at iteration 4: strict convergence. Initialization complete Iteration 0, inertia 549.3189000000003 Iteration 1, inertia 189.82676406927294 Iteration 2, inertia 108.35491426116245 Iteration 3, inertia 98.55081215657327 Iteration 4, inertia 96.2556072332222 Iteration 5, inertia 96.03746916956139 Iteration 6, inertia 95.63063596469088 Iteration 7, inertia 95.57183751367191 Iteration 8, inertia 95.55394205616612 Converged at iteration 8: strict convergence. Initialization complete Iteration 0, inertia 226.13800000000003 Iteration 1, inertia 123.8032406649898 Iteration 2, inertia 101.2007092408733 Iteration 3, inertia 96.12908247185473 Iteration 4, inertia 95.55989885435001 Converged at iteration 4: strict convergence. Initialization complete Iteration 0, inertia 300.068899999998 Iteration 1, inertia 134.91766665736398 Iteration 2, inertia 109.23193825270297 Iteration 3, inertia 97.32424214615946 Iteration 4, inertia 95.87981960678495 Iteration 5, inertia 95.55989885435001 Converged at iteration 5: strict convergence. Initialization complete Iteration 0, inertia 361.35339999999985 Iteration 1, inertia 191.87547238636702 Iteration 2, inertia 159.2018810445558 Iteration 3, inertia 111.37486848019257 Iteration 4, inertia 97.19406178248845 Iteration 5, inertia 96.08770320254003 Iteration 6, inertia 95.63063596469088 Iteration 7, inertia 95.57183751367191 Iteration 8, inertia 95.55394205616612 Converged at iteration 8: strict convergence. Initialization complete Iteration 0, inertia 164.90930000000003 Iteration 1, inertia 99.34740054621203 Iteration 2, inertia 96.55853931708775 Iteration 3, inertia 96.16699229731377 Iteration 4, inertia 95.79042113653588 Iteration 5, inertia 95.57183751367191 Iteration 6, inertia 95.55394205616612 Converged at iteration 6: strict convergence. Initialization complete Iteration 0, inertia 502.4055999999999 Iteration 1, inertia 164.17815920538158 Iteration 2, inertia 153.29269456209832

Iteration 3, inertia 148.8612646005445 Iteration 4, inertia 146.72308116227103 Iteration 5, inertia 146.1975250439638 Iteration 6, inertia 145.4802019123721 Iteration 7, inertia 140.6861804860087 Iteration 8, inertia 136.85367487414223 Iteration 9, inertia 133.5144659668164 Iteration 10, inertia 126.48860322654284 Iteration 11, inertia 116.26765870918304 Iteration 12, inertia 102.8478692868655 Iteration 13, inertia 96.12908247185473 Iteration 14, inertia 95.55989885435001 Converged at iteration 14: strict convergence. Initialization complete Iteration 0, inertia 146.70680000000002 Iteration 1, inertia 99.50908220820313 Iteration 2, inertia 95.95970345518677 Iteration 3, inertia 95.60660697105247 Iteration 4, inertia 95.55394205616612 Converged at iteration 4: strict convergence. Initialization complete Iteration 0, inertia 126.47810000000007 Iteration 1, inertia 99.16788129617385 Iteration 2, inertia 96.47641962235046 Iteration 3, inertia 95.68708159216268 Iteration 4, inertia 95.55394205616612 Converged at iteration 4: strict convergence. Initialization complete Iteration 0, inertia 336.5507999999987 Iteration 1, inertia 196.2055058589258 Iteration 2, inertia 164.5474488010176 Iteration 3, inertia 117.09913739579174 Iteration 4, inertia 98.50947900158808 Iteration 5, inertia 95.96815455205041 Iteration 6, inertia 95.63063596469088 Iteration 7, inertia 95.57183751367191 Iteration 8, inertia 95.55394205616612





Exercise 4.5 (20 pts)

In the previous model you used the first two features: 'Alcohol' and 'Malic acid'. For this exercise, pick features 'Alcohol' and 'OD280/OD315 of diluted wines' (feature #1 and feature #12) as your two attributes and perform the tasks in Exercise 4.4. (cluster, report metrics, draw decision boundaries)

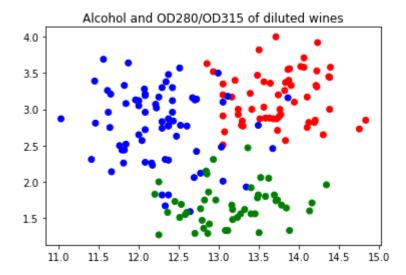
Which model performs better?

This model performance better because Completness Score: 0.7006853440435565 and Homogeneity Score: 0.7072039236692641 is way higher than compare to 4.4 model.

```
In [106...
# your code here
Xwine_full , ywine = load_wine(return_X_y = True)

Xc = Xwine_full[:, [0, 11]]

colormap = np.array(['r' , 'b' , 'g'])
plt.scatter(Xc[:,0],Xc[:,1] , c = colormap[ywine])
plt.title("Alcohol and OD280/OD315 of diluted wines")
plt.show()
```



```
In [107...
cmap_light = ListedColormap(['#FBBBB9', '#82CAFF', '#5EFB6E'])
```

```
cmap bold = ListedColormap(['#CA226B', '#2B65EC', '#387C44'])
          cmap_test = ListedColormap(['#8E35EF', '#659EC7', '#FFFF00'])
          cmap_predict1 = ListedColormap(['#8105ED', '#ED05CA', '#FA0505'])
          # Run k-means, Number of clusters = 2
          y1 predict = KMeans(n clusters = 3, random state = 200).fit predict(Xc)
          #plot
          print("Completness Score: ",completeness_score(ywine, y1_predict))
          print("Homogeneity Score: ",homogeneity score(ywine, y1 predict))
         Completness Score: 0.7006853440435565
         Homogeneity Score: 0.7072039236692641
In [108...
          Xc = Xwine full[:, [0, 11]]
          print(Xc)
          kmeans = KMeans(n clusters = 3, init = 'random', random state = 200, verbose=True).fit(X
          plt.scatter(Xc[:,0], Xc[:,1], c =y1_predict)
          plt.scatter(Xc[:,0], Xc[:,1], c= kmeans.labels_)
          plt.scatter(kmeans.cluster centers [:,0],kmeans.cluster centers [:,1],c = 'r',marker ='
          plt.show()
          xx6, yy6 = meshGrid(Xc[:,0], Xc[:,1], 0.01)
          Z6 = kmeans.predict(np.c [xx6.ravel(), yy6.ravel()])
          Z6 = Z6.reshape(xx6.shape)
          plt.figure()
          plt.contourf(xx6, yy6, Z6, cmap=cmap_light ,levels=[-1, 0, 1] ,alpha = 0.5)
          # For plotting all data use the following line
          #plt.scatter(Xs[:, 0], Xs[:, 1], c=ys, cmap=cmap_bold, edgecolor='k', s=50)
          # For plotting train and test and prediction separatley
          plt.scatter(Xc[:, 0], Xc[:, 1], alpha=1.0,c = y1 predict, cmap=cmap predict1 ,linewidth
          plt.xlim(xx6.min(), xx6.max())
          plt.ylim(yy6.min(), yy6.max())
          plt.show()
         [[14.23 3.92]
          [13.2 3.4]
          [13.16 3.17]
          [14.37 3.45]
          [13.24 2.93]
          [14.2
                 2.85]
          [14.39 3.58]
          [14.06 3.58]
          [14.83 2.85]
          [13.86 3.55]
          [14.1 3.17]
          [14.12 2.82]
          [13.75 2.9]
          [14.75 2.73]
          [14.38 3. ]
          [13.63 2.88]
          [14.3 2.65]
          [13.83 2.57]
```

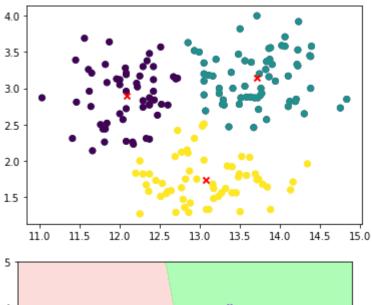
[14.19 2.82] [13.64 3.36] [14.06 3.71] [12.93 3.52] [13.71 4.] [12.85 3.63] [13.5 3.82] [13.05 3.2] [13.39 3.22] [13.3 2.77] [13.87 3.4] [14.02 3.59] [13.73 2.71] [13.58 2.88] [13.68 2.87] [13.76 3.] [13.51 2.87] [13.48 3.47] [13.28 2.78] [13.05 2.51] [13.07 2.69] [14.22 3.53] [13.56 3.38] [13.41 3.] [13.88 3.56] [13.24 3.] [13.05 3.35] [14.21 3.33] [14.38 3.44] [13.9 3.33] [14.1 2.75] [13.94 3.1] [13.05 2.91] [13.83 3.37] [13.82 3.26] [13.77 2.93] [13.74 3.2] [13.56 3.03] [14.22 3.31] [13.29 2.84] [13.72 2.87] [12.37 1.82] [12.33 1.67] [12.64 1.59] [13.67 2.46] [12.37 2.87] [12.17 2.23] [12.37 2.3] [13.11 3.18] [12.37 3.48] [13.34 1.93] [12.21 3.07] [12.29 1.82] [13.86 3.16] [13.49 2.78] [12.99 3.5] [11.96 3.13] [11.66 2.14] [13.03 2.48] [11.84 2.52]

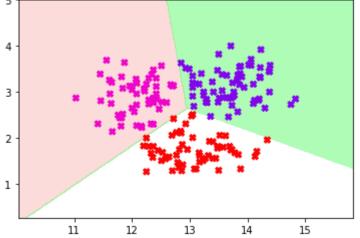
[12.33 2.31] [12.7 3.13] [12. 3.12] [12.72 3.14] [12.08 2.72] [13.05 2.01] [11.84 3.08] [12.67 3.16] [12.16 2.26] [11.65 3.21] [11.64 2.75] [12.08 3.21] [12.08 2.27] [12. 2.65] [12.69 2.06] [12.29 3.3] [11.62 2.96] [12.47 2.63] [11.81 2.26] [12.29 2.74] [12.37 2.77] [12.29 2.83] [12.08 2.96] [12.6 2.77] [12.34 3.38] [11.82 2.44] [12.51 3.57] [12.42 3.3] [12.25 3.17] [12.72 2.42] [12.22 3.02] [11.61 3.26] [11.46 2.81] [12.52 2.78] [11.76 2.5] [11.41 2.31] [12.08 3.19] [11.03 2.87] [11.82 3.33] [12.42 2.96] [12.77 2.12] [12. 3.05] [11.45 3.39] [11.56 3.69] [12.42 3.12] [13.05 3.1] [11.87 3.64] [12.07 3.28] [12.43 2.84] [11.79 2.44] [12.37 2.78] [12.04 2.57] [12.86 1.29] [12.88 1.42] [12.81 1.36] 1.29] [12.7 [12.51 1.51] [12.6 1.58] [12.25 1.27] [12.53 1.69]

[13.49 1.82] [12.84 2.15] [12.93 2.31] [13.36 2.47] [13.52 2.06] [13.62 2.05] [12.25 2.] [13.16 1.68] [13.88 1.33] [12.87 1.86] [13.32 1.62] [13.08 1.33] [13.5 1.3] [12.79 1.47] [13.11 1.33] [13.23 1.51] [12.58 1.55] [13.17 1.48] [13.84 1.64] [12.45 1.73] [14.34 1.96] [13.48 1.78] [12.36 1.58] [13.69 1.82] [12.85 2.11] [12.96 1.75] [13.78 1.68] [13.73 1.75] [13.45 1.56] [12.82 1.75] [13.58 1.8] [13.4 1.92] [12.2 1.83] [12.77 1.63] [14.16 1.71] [13.71 1.74] [13.4 1.56] [13.27 1.56] [13.17 1.62] [14.13 1.6]] Initialization complete Iteration 0, inertia 132.754999999999 Iteration 1, inertia 62.55360383767907 Iteration 2, inertia 58.61901063358439 Iteration 3, inertia 58.382247645340385 Iteration 4, inertia 58.325945538943834 Converged at iteration 4: strict convergence. Initialization complete Iteration 0, inertia 284.798800000001 Iteration 1, inertia 99.42618673559507 Iteration 2, inertia 67.82120886410212 Iteration 3, inertia 61.80121390118983 Iteration 4, inertia 59.539565124863934 Iteration 5, inertia 58.497102132111955 Iteration 6, inertia 58.325945538943834 Converged at iteration 6: strict convergence. Initialization complete Iteration 0, inertia 152.9971000000002 Iteration 1, inertia 81.85833266900501 Iteration 2, inertia 65.34792635199175

Iteration 3, inertia 59.95221319907506 Iteration 4, inertia 58.54423198571707 Iteration 5, inertia 58.450151711010335 Iteration 6, inertia 58.382247645340385 Iteration 7, inertia 58.325945538943834 Converged at iteration 7: strict convergence. Initialization complete Iteration 0, inertia 294.46950000000015 Iteration 1, inertia 128.38851366806745 Iteration 2, inertia 94.13081578350302 Iteration 3, inertia 64.43612695395325 Iteration 4, inertia 58.481049153601376 Iteration 5, inertia 58.37116387090805 Iteration 6, inertia 58.34320751540833 Converged at iteration 6: strict convergence. Initialization complete Iteration 0, inertia 125.2024999999996 Iteration 1, inertia 60.62295509104096 Iteration 2, inertia 58.567803888001336 Iteration 3, inertia 58.34320751540833 Converged at iteration 3: strict convergence. Initialization complete Iteration 0, inertia 229.87070000000003 Iteration 1, inertia 72.47210205500825 Iteration 2, inertia 61.36077153758995 Iteration 3, inertia 58.54772661539147 Iteration 4, inertia 58.40472389803835 Iteration 5, inertia 58.347779588931495 Iteration 6, inertia 58.325945538943834 Converged at iteration 6: strict convergence. Initialization complete Iteration 0, inertia 251.40840000000006 Iteration 1, inertia 104.4259348097662 Iteration 2, inertia 89.30179104765773 Iteration 3, inertia 70.12392008416644 Iteration 4, inertia 60.542237960593475 Iteration 5, inertia 58.51829821590716 Iteration 6, inertia 58.38390589446463 Iteration 7, inertia 58.347779588931495 Iteration 8, inertia 58.325945538943834 Converged at iteration 8: strict convergence. Initialization complete Iteration 0, inertia 136.00200000000007 Iteration 1, inertia 63.392825041598414 Iteration 2, inertia 58.54352322979602 Iteration 3, inertia 58.38390589446463 Iteration 4, inertia 58.347779588931495 Iteration 5, inertia 58.325945538943834 Converged at iteration 5: strict convergence. Initialization complete Iteration 0, inertia 123.16800000000006 Iteration 1, inertia 61.188081596336424 Iteration 2, inertia 58.770385233423056 Iteration 3, inertia 58.399696396681904 Iteration 4, inertia 58.347779588931495 Iteration 5, inertia 58.325945538943834 Converged at iteration 5: strict convergence. Initialization complete Iteration 0, inertia 113.84550000000004 Iteration 1, inertia 59.57558783470234

Iteration 2, inertia 58.4556352519123
Iteration 3, inertia 58.347779588931495
Iteration 4, inertia 58.325945538943834
Converged at iteration 4: strict convergence.





End Of Lab