

# Modelling the effects of phylogeny and body size on within-host pathogen replication and immune response

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## Abstract

Understanding how quickly pathogens replicate and how quickly the immune system responds is important for predicting the epidemic spread of emerging pathogens. Host body size, through its correlation with metabolic rates, is theoretically predicted to impact pathogen replication rates and immune system response rates. Here, we use mathematical models of viral time courses from multiple species of birds infected by a generalist pathogen (West Nile Virus) to test more thoroughly how disease progression and immune response depend on mass and host phylogeny. We use hierarchical Bayesian models coupled with non-linear dynamical models of disease dynamics to incorporate the hierarchical nature of host phylogeny.

Our analysis suggests an important role for both host phylogeny and species mass in determining factors important for viral spread such as the basic reproductive number, WNV production rate, peak viremia in blood and competency of a host to infect mosquitoes. Our model is based on a principled analysis and gives a quantitative prediction for key epidemiological determinants and how they vary with species mass and phylogeny. This leads to new hypotheses about the mechanisms that cause certain taxonomic groups to have higher viremia. For example, our models suggest that higher viral burst sizes cause corvids to have higher levels of viremia and that the cellular rate of virus production is lower in larger species. We derive a metric of competency of a host to infect disease vectors and thereby sustain the disease between hosts. This suggests that smaller passerine species are highly competent at spreading the disease compared to larger non-passerine species. Our models lend mechanistic insight into why some species (smaller passerine species) are pathogen reservoirs and some (larger non-passerine species) are potentially dead-end hosts for WNV. Our techniques give insights into the role of body mass and host phylogeny in the spread of WNV and potentially other zoonotic diseases.

The major contribution of this work is a computational framework for infectious disease modelling at the within-host level that leverages data from multiple species. This is likely to be of interest to modellers of infectious diseases that jump species barriers and infect multiple species. Our method can be used to computationally determine the competency of a host to infect mosquitoes that will sustain WNV and other zoonotic diseases. We find that smaller passerine species are more competent in spreading the disease than larger non-passerine species. This suggests the role of host phylogeny as an important determinant of within-host pathogen replication. Ultimately we view our work as an important step in linking within-host viral dynamics models to between-host models that determine spread of infectious disease between different hosts.

## Introduction

Zoonotic diseases that jump the species barrier from animals to humans cause 2.5 billion cases of human illness and 2.7 million human deaths per year [1]. Many emerging diseases are zoonotic in origin and infect multiple host species [2]. Multi-host pathogens may have very different dynamics in different species [3].

Understanding how quickly pathogens replicate and how quickly the immune system responds is important for predicting the epidemic spread of emerging pathogens. While host-pathogen interactions have been studied qualitatively using mathematical models, it is not known how the parameters characterizing

the immune response and pathogen replication rates change from species to species. Emerging zoonotic diseases originate from species that differ in body size, e.g. birds in avian influenza and cattle in bovine spongiform encephalopathy. Thus it is important to understand how body size affects immune response and pathogenesis.

Body size can affect pathogenesis in two ways:

1. Host metabolism constrains energy delivery to cells [4–8] and could influence rates of pathogen replication and immune response rates [9]. The metabolic rate of each cell is constrained by the rate at which nutrients and oxygen are supplied by the cardio-vascular network. The rate at which this network supplies nutrients to each cell ( $R_{cell}$ ) scales as the body mass ( $M$ ) raised to an exponent of  $-1/4$ :  $R_{cell} \propto M^{-1/4}$  such that individual cellular metabolic rates decrease as the body mass increases [4–8]. This relationship holds over an incredible diversity of body sizes, from  $10^{-13}$  g (microbes) to  $10^8$  g (whales). Many biological rates, such as heart rates and reproductive rates, also scale as  $M^{-1/4}$ , while many characteristic times such as blood circulation times and life times, scale as  $M^{1/4}$  [7].

Cellular metabolic rate dictates the pace of many biological processes [8]. Cellular metabolism could affect immune system search times by reducing movement and proliferation of immune cells [9]. Rates of DNA and protein synthesis also depend on the cellular metabolic rate and could influence the rate at which pathogens replicate inside infected cells [3]. Pathogens are expected to replicate slower in larger species [3, 10]. The possibilities that cells of the immune system and pathogens may move and proliferate at speeds independent of host body mass  $M$  ( $\propto M^0$ ) or proportional to cellular metabolic rate ( $\propto M^{-1/4}$ ) lead to four hypotheses, as originally proposed by Wiegand and Perelson [9]. Here we use mathematical models and experimental data to test whether viral production rates and immune response rates and times vary with species body mass. We use West Nile virus (WNV) as a model pathogen for our studies because it is a generalist pathogen that infects many species in different taxonomic groups and with a range of body sizes.

2. An effective immune response requires efficient detection of pathogens that may be initially localized. The detection of small amounts of pathogen may be harder in larger animals due to larger physical spaces. We hypothesize that the immune system is capable of nearly scale-invariant detection and response, i.e. rates of immune response and time taken by the immune system to detect and respond to pathogens do not scale appreciably with host body size [11]. Previous work has suggested how: a) the physical architecture of the immune system, comprised of anatomical structures called lymph nodes (that facilitate recognition of pathogen by immune system cells), and b) chemical signalling within the immune system, guiding immune system cells to sites of infection, enable efficient and nearly scale-invariant detection and response [11, 12].

WNV pathogenesis also depends on host phylogeny, e.g. passerine species (like sparrows) sustain more viremia than non-passerine species (like geese) [13]. Corvid species (like crows) are particularly susceptible to WNV infection [13]. Hence host phylogeny is expected to affect immune response and pathogen replication rates. Viral dynamics may be similar in related species. Modeling techniques that take advantage of relatedness of infected species may produce more accurate results. This work incorporates host phylogenetic hierarchy to estimate biologically relevant quantities for WNV infection.

Hierarchical Bayesian models enable modelers to encapsulate knowledge about the underlying biology as priors. Hierarchical models also pool information across disparate individuals from different groups and are well suited for cases where there are a limited number of observations from several individuals. Suitable priors in a hierarchical Bayesian framework can help reduce variance of parameter estimates [14, 15]. A model that incorporates the hierarchical nature of host phylogeny and encodes this information as priors in a hierarchical Bayesian model may enable more accurate estimates of parameters characterizing WNV infection.

Hierarchical Bayesian models have been used in image processing [16], ecological modeling [17] and climate modeling [18]. Bayesian non-linear mixed effects models with a single level of hierarchy have been applied to modeling of the within-host response to HIV [19–21] and influenza [22]. Multilevel data fitting approaches and Bayesian frameworks are expected to be helpful in modeling within-host viral dynamics. However to the best of our knowledge, Bayesian non-linear mixed effects models with multiple levels of hierarchy have not been applied to within-host modeling.

Here, we use mathematical models of viral time courses from multiple species of birds infected by WNV to test more thoroughly how disease progression and immune response depend on mass and host phylogeny. Mathematical models that combine within-host experimental data from multiple species, such as the ones presented here, may also be useful in studying other zoonotic diseases and help increase our understanding of these diseases.

The role of host phylogeny in determining WNV infection outcome is known qualitatively [13]. We provide a quantitative prediction for viral competency for Passerines and corvids in particular. Further, the fits to experimental data using our mathematical models enable us to form hypotheses as to why WNV viremia is higher in these groups.

We also calculate a reservoir competence index that indicates the relative number of infectious mosquitoes that would be derived from feeding on these hosts. This could be helpful in coupling within-host dynamics of WNV or other zoonotic diseases to dynamics of spread between different hosts enabling multi-scale models of disease spread.

## 1 Background on West Nile Virus

We use WNV as a model pathogen for our studies because it is a generalist pathogen that infects many species in different taxonomic groups and with a range of body sizes. WNV has emerged globally as a major cause of viral encephalitis and is maintained in an enzootic cycle between mosquitoes and birds [23] but can also infect and cause disease in many other vertebrates including humans. Following its introduction into the United States in 1999, WNV spread rapidly across the North American continent in only four years and more recently has been reported in Mexico, South America, and the Caribbean [24–26]. Although vaccines are available for animal use, no vaccines or specific therapies for WNV are currently approved for humans [27].

WNV is an enveloped flavivirus with a single-stranded, positive sense, 11-kb RNA genome [27]. WNV is cytopathic and initially infects epidermal Langerhans cells, which then migrate to the draining lymph node and infect macrophages [27]. From the draining lymph node, WNV spreads to the spleen, kidney, and spinal cord and ultimately breaches the blood-brain barrier to infect neurons [27]. The standard pattern of WNV infection in birds is characterized by an initial exponential growth of virus that peaks around 3 to 4 days post infection (DPI), followed by an exponential decline until that leads to undetectable levels of virus by 6 to 8 DPI.

WNV infects a large number of species across different taxonomic groups. This allows us to test the effects of animal body size on pathogen replication and immune response. We focus on data from a study in which birds were experimentally infected with the same strain of WNV (WNV NY99-6480). Komar et al. [13] experimentally infected 25 species of birds (ranging from 3 gm sparrows to 3 kg geese) with WNV NY99-6480 and took daily measurements of the concentration of infectious virions in blood (viremia) over the course of infection. The initial inoculum size was not monitored as the infection was initiated by bites from infected mosquitoes.

## Materials and Methods

### 1.1 Overview of Methods

We use a Bayesian inference approach to estimate model parameters. Assume that a model (in our case a differential equation model describing how virus concentration changes over time in serum) contains parameters  $\Theta$ . The Bayesian approach allows us to include prior knowledge about model parameters in a systematic fashion. If we have information about  $\Theta$  (e.g., from experimental evidence) which needs to be incorporated in our analysis, this is represented as a prior probability distribution  $P(\Theta)$ . Bayes Rule allows us to incorporate the prior knowledge about parameters,  $P(\Theta)$ , and experimental data,  $D$ , to derive a posterior distribution of parameters:

$$P(\Theta|D) = \frac{P(D|\Theta) \cdot P(\Theta)}{P(D)} \quad (1)$$

The multi-level hierarchical Bayesian model mimics the hierarchical nature of host phylogeny. There are three levels in the hierarchical tree representation: individual, species and genus (Fig. 1). Each level of the tree has an equation describing the distribution of model parameters (differential equation models, Eqs. 2 - 5 and Eqs. 2 - 4, 6 - 7). The differential equation and hierarchical Bayesian models are explained in greater detail in the next section.

Our goal is to compare two different hierarchical Bayesian models: a multi-level model that has three levels of hierarchy (individual, species and genus) (Fig. 1) and an aggregated model with two levels of hierarchy (all individuals of all species pooled together under a single genus) (Fig. 2). We compare the accuracy of parameter estimates with respect to ground truth at the individual, species and genus level. We also experiment with different degrees of variation of parameters between species and within species.

### 1.2 Differential Equation Models of Viral Dynamics and Immune Response

We use two different viral dynamic models to account for the observed plasma viremia. The first model assumes that infection is target-cell limited in birds, i.e. the concentration of virus reaches a peak and then declines when few susceptible target cells remain. Models of target cell limited acute infection have been developed for HIV [28], influenza A virus [29], hepatitis C virus [30], simian immunodeficiency virus [31], dengue virus [32] and Zika virus [33, 34]. Here we use a target cell limited model with an eclipse phase, given by the following differential equations:

$$\frac{dT}{dt} = -\beta TV \quad (2)$$

$$\frac{dI_1}{dt} = \beta TV - kI_1 \quad (3)$$

$$\frac{dI_2}{dt} = kI_1 - \delta I_2 \quad (4)$$

$$\frac{dV}{dt} = pI_2 - \gamma V - \beta TV \quad (5)$$

where  $T$  is the density of uninfected target cells, and  $V$  is the viral titer in serum. Target cells become infected by virus at rate  $\beta TV$ , where  $\beta$  is the rate constant characterizing infection. The initial viral titer and the initial number of target cells are denoted  $V_0$  and  $T_0$ , respectively. The initial density of infected cells is assumed to be zero. The separation of infected cells into two classes,  $I_1$  cells that are infected but not yet producing virus and  $I_2$  cells that produce virus, is similar to that in a model proposed earlier for influenza infection [29]. This separation increases the realism of the model, since delays in the production of virus after the time of initial infection are part of the viral life cycle (the eclipse phase). The parameter

$1/k$  is the average transition time from  $I_1$  to  $I_2$ . Productively infected cells ( $I_2$ ) release virus at an average rate  $p$  per cell and die at rate  $\delta$  per cell, where  $1/\delta$  is the average life span of a productively infected cell. Free infectious virus is cleared at rate  $\gamma$  per infectious unit per day, for example by phagocytosis or loss of infectivity and is lost by entering cells during the infection process at rate  $\beta TV$ .

The Bayesian model infers  $(V_0, \beta, p, \delta)$  from the viral titer data.

We also use a more sophisticated model that assumes viral decline is due to an adaptive antibody (induced IgM) response. Humoral immunity is an essential component of the immune response to WNV, as neutralizing antibodies limit dissemination of infection [35, 36]. Diamond et al. [36] infected wild type mice subcutaneously with WNV and measured titers of neutralizing antibody (analyzed in [37]). The data can be described by the following piecewise linear function:

$$A(t) = \begin{cases} 0 & , \quad t < t_i \\ \eta(t - t_i) & , \quad t \geq t_i \end{cases} \quad (6)$$

The level of neutralizing antibody at time  $t$ ,  $A(t)$ , measured by the plaque reduction neutralization test (PRNT) is 0 before time  $t_i$  and increases linearly with time after that with rate  $\eta$ . We assume that neutralizing antibody,  $A$ , binds virus,  $V$ , and neutralizes it with rate constant  $\rho$ , so that infectious virus is lost at rate  $\rho A(t)V$ . The model including neutralizing antibody consists of Eqs. 2-4 and Eq. 6 with Eq. 5 replaced by:

$$\frac{dV}{dt} = pI_2 - \gamma V - \beta TV - \rho A(t)V \quad (7)$$

The Bayesian model infers  $(V_0, \beta, p, \delta, \rho, t_i)$  from the viral titer data.

The ordinary differential equations describing our viral kinetic models were solved numerically in Matlab [38]. The Runge-Kutta 4 method of integration was employed. All model parameters and virus concentration are logged (base 10) in order to stabilize variance and ensure positive estimates from the Bayesian inference. A sample plot of the target limited model prediction of virus concentration over time (compared to observed virus concentration data) using one representative set of parameters inferred from the Bayesian model is shown in Fig. 3. Additional fits are shown in Fig. 12, 13 and 14.

### 1.3 Constraints on Model Parameters

The parameter constraints are summarized in Table 1. The initial density of uninfected target cells,  $T_0$ , is fixed to  $2.3 \times 10^5$  /mL (mean of the estimated range in mice, [37]). The rate of clearance of free infectious virus,  $\gamma$ , is set to 44.4 /day (upper bound of estimate in mice, [37]) for all species except three corvids (Fish crows, Blue jays and American crows) for which we could get good fits only with a lower value (1 /day).

The eclipse phase length,  $1/k$ , is fixed to the lower bound of a range from wildtype mice (6 hours, [37]). Similarly, based on calculations in wildtype mice [37], the lifetime of productively infected cells,  $1/\delta$ , is constrained to be greater than 1 hour while obeying the relationship  $1/\delta + 1/k = 24$  hours. The rate at which neutralizing antibody,  $A(t)$ , increases linearly after time  $t_i$  ( $\eta$ ) is fixed to 54.7/day based on fit to antibody titer data in wildtype mice [36, 37]. Finally, the time of initiation of antibody,  $t_i$ , is bounded between 2 and 4 days [37] based on experimental data and model fits to experimental data in wildtype mice.

The infectious virion burst size,  $p/\delta$ , is constrained to not exceed  $10^{12}$  plaque forming units (PFU) based on fits of the target cell limited model to birds. Similarly, the efficacy of antibody neutralization,  $\rho$ , is bounded between 0.05 and  $1000 \text{ PRNT}_{50}^{-1} \text{ day}^{-1}$  based on model fits to experimental infection data on birds (where the amount of antibody is measured in units of plaque reduction neutralization titre for 50% inhibition of plaques,  $\text{PRNT}_{50}$ ). The initial viral titer,  $V_0$ , is constrained to be within 0.1 and  $10^{12}$  PFU/mL and the rate of production of virus,  $p$ , is constrained to lie within 0.5 and  $10^{12}$  /day based on fits in birds.

## 1.4 Experimental data

WNV infects bird species ranging from 3 gm sparrows to 3 kg geese. This wide range of species mass allows us to test the effects of animal body size on pathogen replication and immune response. We focus on data from a study which experimentally infected animals with the same strain of WNV (WNV NY99-6480). Komar et al. [13] experimentally infected 25 species of birds with WNV NY99-6480 and took daily measurements of the concentration of infectious virions in blood (viremia) over the course of infection (sample plot shown in Fig. 3, data points in red). Viremia was reported in plaque forming units (PFU, a measure of the number of infectious virions) over a span of at most 7 days post infection.

The order Passeriforme includes more than half of all bird species. The experimental infection study infected 10 passerine species and 15 non-passerine species. The passerine species were house finches, house sparrows, red winged blackbirds, blue jays, American robins, European starlings, common grackles, black-billed magpies, fish crows and American crows. WNV is exceptionally viremic in corvid species (a family within the order Passeriforme). The corvid species in the study were blue jays, black-billed magpies, fish crows and American crows. The number of individuals infected per species ranged from 1 (American cots) to 8 (American crows).

The experimental infection study included data on 87 individual birds belonging to 25 distinct species. Of the 87 individuals infected, 26 succumbed to infection. With the exception of one individual (a non-passerine ring billed gull), all mortality was in passerine species, primarily corvids.

From this experimental dataset we excluded data on 2 species (Japanese quail and ring-necked pheasant). The virus kinetics in Japanese quail were erratic and viremia levels in the ring-necked pheasant were approximately constant over time; as such the viral dynamics in these species could not be simulated by our model.

The experimental study also reported the level of detection (LOD) of their viral assay as  $10^{1.7}$  PFU. The raw experimental data had reports of consecutive viral measurements at LOD in the declining phase of viremia for some species. In these cases we only considered the first data point below the LOD in the time series and discarded the remaining. Considering all LOD data points would have led our models to an underestimate of the slope of the declining phase due to the flat trajectory induced by multiple consecutive viremia measurements at the same level. We note that there are alternate approaches for fitting measurements under the LOD as done for dengue virus [39].

## 1.5 Hierarchical Bayesian Model

### 1.5.1 Aggregated model

Given a population of individuals, the aggregated model assumes that the dynamics of infection of each individual is characterized by parameters  $(\theta_i, i = 1, \dots, n$  for  $n$  individuals) where  $\theta_i$  is a parameter vector that represents the differential equation model parameters  $(V_0, \beta, p, \delta)$  for a particular individual. Each  $\theta_i$  is drawn from a common top-level distribution  $(\mu)$ . In contrast to the multi-level Bayesian model (presented in the next section), the aggregated model has no species level and aggregates all individuals of all species together.

The aggregated model has 87 individuals. The individuals are aggregated to form a tree of height 2. The model is shown graphically in Fig. 2 (Left panel). There are two levels in the hierarchical tree representation: individual and all individuals of all species combined. Each level of the tree has a distribution of ODE model parameters (Eqs. 2 - 5 for the target cell limited model and Eqs. 2 - 4, 6 - 7 for the model with an antibody response). The  $i$ th individual has a parameter vector  $\theta_i$  that represents  $(V_0, \beta, p, \delta)$  for a particular individual. This parameter  $\theta_i$  is then drawn from a higher distribution with mean  $\mu$ . The details of the model are given in Supplementary Information.



### 1.5.2 Multi-level hierarchical model

We also devised a multi-level hierarchical Bayesian model that mimics the hierarchical nature of host phylogeny. There are three levels in the hierarchical tree representation: individual, species and order (Fig. 1). There are 23 groups (species) with a total of 87 individuals. The groups are arranged hierarchically to form a tree of height 3. The model is shown graphically in Fig. 1 (Left panel).

Each level of the tree has a distribution of ODE model parameters (Eqs. 2 - 5 for the target cell limited model and Eqs. 2 - 4, 6 - 7 for the model with an antibody response). The  $i$ th individual has a parameter vector  $\theta_i$  that represents  $(V_0, \beta, p, \delta)$  for a particular individual. This parameter vector  $\theta_i$  is then drawn from a species-level distribution with mean  $\mu$ . Finally, the species-level estimate is itself drawn from an order-level distribution centered around  $\eta$ . The details of the model are given in Supplementary Information.

We also compare the two different hierarchical Bayesian models: a multi-level model that has three levels of hierarchy (for individual, species and order) and an aggregated model with two levels of hierarchy (all individuals of all species pooled together under a single top level entity) (Fig. 2). Each of these Bayesian models is run on 3 different kinds of experimental data: all passerine and non-passerine species combined, passerine and non-passerine species separately and finally only corvid species (a subset of passerines).

### 1.5.3 Markov Chain Monte Carlo implementation

We are interested in inferring the posterior distribution of the ODE parameters given the data  $(P(\Theta|D)$ , Eq. 1). However the distribution does not have an analytic form. Markov Chain Monte Carlo (MCMC) techniques enable us to sample from a target distribution; the approximation gets better as more samples are drawn. We combine the Metropolis-Hastings algorithm and the Gibbs sampler. The Gibbs sampler is a type of MCMC algorithm that divides the parameters into a number of components and at each iteration sequentially updates each of them by conditioning on the others. The Metropolis-Hastings (M-H) algorithm updates  $\Theta$ , and the Gibbs sampler updates all the remaining variables. We use a blockwise update scheme where proposed new values of parameters from the M-H algorithm are either all updated simultaneously or all reverted to their previous values. The M-H algorithm draws a subsequent sample from the target distribution centered around a proposal distribution. Our proposal distribution is a multi-variate normal distribution centered around the current value of  $\theta_i$ .

The choice of dispersion of the proposal distribution is important. If the dispersion is high, many MCMC moves will be rejected and the procedure will take longer to converge. If the dispersion is low, the chain may not explore the parameter space thoroughly [40, 41]. The standard deviation of the proposal distribution is chosen to be 0.01 on the log scale (base 10) for all the parameters. If a value returned by the proposal distribution is outside of the imposed bounds for ODE parameters, we reflect the value back into range. Convergence is checked informally based on graphical techniques [42].

All models were run for 10,000 iterations. This constitutes a single “run” of the Bayesian model. The initial 1000 iterations were discarded (burn-in phase). Of the remaining 9,000 samples we retained every fifth sample.

### 1.5.4 Calculation of averages for ODE parameters at different levels of hierarchy

We use the posterior samples of ODE parameters to generate the averages in the following way: for each individual, species or order we have 10,000 samples originally (as described in the previous section) at that level of the hierarchy. After burn-in this is reduced to 9000 samples and thinning of the samples leads to a total of 1800 samples. The average of these samples (henceforth referred to as individual-level, species-level or genus-level averages) for each ODE parameter  $(V_0, \beta, p, \delta)$  is used in the Results section.

## 1.6 Calculation of reservoir competencies

We calculate a reservoir competence index that indicates the relative number of infectious mosquitoes that would be derived from feeding on each host species and is calculated from the viremia that develops in the hosts after infection. We extend a competence index developed by Komar et al. [13] to account for time-varying viremia and species relatedness. Species that sustain WNV viremia above  $10^5$  PFU/mL are considered infectious for mosquito vectors [13]. The reservoir competence index ( $C_i$ ) is a function of susceptibility ( $s$ ), the proportion of birds that become infected as a result of daily exposure; mean daily infectiousness ( $i$ ), the proportion of exposed mosquito vectors that become infected per day; and the duration of infectious viremia above a threshold ( $d$ ) [13]. Komar et al. [13] calculate the competence as  $C_i = s \times i \times d$  where  $i = \frac{\log_{10}(V_p)-5}{10} + 0.02$  and  $V_p$  is the peak viremia attained in a host; this assumes that hosts sustain a fixed viremia (at the level of peak viremia) throughout the duration of infectivity.

Our competency index for each species is calculated as follows:

$$C_i = s \times \int_0^{t_d} i(t) dt \quad (8)$$

$$i(t) = \begin{cases} \frac{\log_{10}V(t)-5}{10} + 0.02 & , \log_{10}V(t) \geq 5 \\ 0 & , \log_{10}V(t) < 5 \end{cases} \quad (9)$$

where  $t_d$  is the time until viremia is measured experimentally,  $i(t)$  is the infectivity at time  $t$  and  $V(t)$  is the ODE model predicted viremia at time  $t$ . We note that our competency calculations also implicitly account for species relatedness via the hierarchical Bayesian model. Following bird mortality calculations made in Komar et al. [13], we set the susceptibility ( $s$ ) to be 0.7 for Budgerigars and 1 for all other species.

## 1.7 Estimate of accuracy in viremia prediction

We estimated the accuracy of viremia prediction by calculating three different estimates of a sum of squared residuals (SSR) between the data and the ODE model prediction (for both the multi-level and aggregated Bayesian models):

1. Individual-level SSR. We calculated individual-level averages of ODE parameters for each species as described in Section 1.5.4. For each individual, we used these individual-level parameter estimates to generate a SSR between data and model prediction in the following way: for each individual in a species, we gave the ODE solver the individual-level parameter estimates and calculated the SSR between model prediction and individual-level data. The SSR was then summed up for all individuals of all species and then divided by the number of individuals. We call this the individual-level SSR.
2. Species-level SSR. We calculated species-level averages of ODE parameters for each species as described in Section 1.5.4. For each species, we used these species-level parameter estimates to generate a SSR between data and model prediction in the following way: for each individual in a species, we gave the ODE solver the species-level parameter estimates and calculated the SSR between model prediction and individual-level data. The SSR was then summed up for all individuals within a species and then for all species and then divided by the number of individuals. We call this the species-level SSR.
3. Order-level SSR. We calculated order-level averages of ODE parameters for each species as described in Section 1.5.4. For each individual, we used these order-level parameter estimates to generate a SSR between data and model prediction in the following way: for each individual in a species, we gave the ODE solver the genus-level parameter estimates and calculated the SSR between model



prediction and individual-level data. The SSR was then summed up for all individuals of all species and then divided by the number of individuals. We call this the genus-level SSR.

## 2 Results

### 2.1 Effect of host phylogeny on parameter estimates

We investigated the effect of host phylogeny on two biologically relevant quantities - the basic reproductive number ( $R_0$ ) and the infectious virion burst size ( $p/\delta$ ). Estimates of the mean values of  $R_0$  from the multi-level model are higher for passerine species ( $R_0 = 23.8$ ) compared to non-passerines ( $R_0 = 4.7$ ) (Fig. 4, top panel). Within passerines, corvid species (fish crows, blue jays, American crows and black-billed magpies) have the highest value of  $R_0$  (93.2) (Fig. 4, top panel). Infectious virion burst sizes in passerine species (8690 PFU) are much higher than those in non-passerines (340 PFU) (Fig. 4, top panel).

Finally, estimates of  $R_0$  in the aggregated model (Fig. 8) are orders of magnitude higher than in the multi-level model (Fig. 4). We hypothesize that since the aggregated model aggregates all species (including corvids) under a single hierarchy, non-corvid species are significantly influenced by parameter estimates from corvid species (which have high  $R_0$ ). The multi-level model hierarchically separates corvid species from non-passerines and hence may moderate the influence of parameter estimates from corvid species on other non-corvid individuals.

### 2.2 Estimates of reservoir competence

We calculated a reservoir competence index that indicates the relative number of infectious mosquitoes that would be derived from feeding on these hosts (Section 1.6). The reservoir competency indices we calculate are correlated with and approximately half of the estimates in Komar et al. [13] (Fig. 5,  $r^2 = 0.94$ , slope = 0.54, p-value = 0). Passerine species have a higher mean reservoir competency (0.8) than non-passerine species (0.2),

Komar et al. [13] assume that virus is constant over time (at a level equal to peak viremia) and hence they overestimate the total amount of virus produced over the duration of infectivity. In reality, viremia changes over time and is actual highest at the time of peak viremia. Our estimates of competency account for this and hence are lower than that of Komar et al. [13]. Area under the curve in a simple model where virus increases linearly (on a log scale) and then declines linearly after some time forms a triangle. The triangle has approximately half the total area of the rectangle formed by assuming viremia is maintained at peak levels throughout the duration of infection. Hence our model has approximately half the area (and half the value) compared to the estimates of Komar et al. [13].

### 2.3 Scaling of biologically relevant quantities

A scaling relationship between a parameter  $\eta$  in our model and host body mass,  $M$ , is written as  $\eta \propto M^\alpha$  where  $\alpha$  is the scaling exponent. Taking the logarithm of both sides of this relationship, we notice

$$\log \eta \propto \alpha \log M \quad (10)$$

Thus the scaling exponent can be derived as the slope of a log-log plot of  $\eta$  vs.  $M$ .

In order to derive scaling relations with host body size, we used the slope of the correlation between individual-level averages of ODE parameters and species mass, assuming the correlation was statistically significant (Fig. 6, multi-level model). The scaling relationships and statistics are summarized in Table 2. We observed that the production rate of infectious virions ( $p$ , PFU /day) is correlated and declines with species body mass (all species combined: p-value = 0.002,  $r^2 = 0.11$ , slope = -1.1; only passerines: p-value = 0.04,  $r^2 = 0.1$ , slope = -1). We note that although the 95% confidence interval (CI) for the

slope  $([-1.5, 0.03])$  includes the theoretically predicted exponent of -0.25, the confidence interval is too large to provide a meaningful estimate of the scaling exponent.

The basic reproductive number represents the average number of second generation infections produced by a single infected cell placed in a population of susceptible cells. If  $R_0$  is greater than 1, then an infection can be established, whereas an infection rapidly dies out if  $R_0$  is less than 1. For the target cell limited model (Eqs. 2 - 5),  $R_0$  is given by [43]:

$$R_0 = \frac{p\beta T_0}{\delta(\gamma + \beta \cdot T_0)} \quad (11)$$

The basic reproductive number,  $R_0$ , had a significant overall decreasing correlation with mass (all species combined: p-value = 0.006,  $r^2 = 0.09$ , slope = -1.3; only passerines: p-value =  $7 \times 10^{-5}$ ,  $r^2 = 0.33$ , slope = -3.7). Peak viremia ( $P_v$ , the maximum viremia attained by an individual over the time course of infection) had a marginally significant correlation with species mass (all species combined: p-value = 0.06,  $r^2 = 0.04$ , slope = -0.82).

The burst size ( $p/\delta$ , PFU), representing the number of infectious virions released by an infected cell over its productively infected lifespan, had a significant decreasing relationship with species body mass (all species combined: p-value = 0.001,  $r^2 = 0.12$ , slope = -1.1; only passerines: p-value = 0.03,  $r^2 = 0.12$ , slope = -1.1). Also the viremia at day 1 ( $V(1)$ ) was correlated with mass (all species combined, p-value = 0.003,  $r^2 = 0.1$ , slope = -1.1).

The density of inoculated virions ( $V_0$ ) and the infectivity of WNV ( $\beta$ ) had no significant relationship with species mass (all species combined: p-value = 0.35,  $r^2 = 0.1$  and p-value = 0.64,  $r^2 = 0.003$ , respectively). Finally, the death rate of productively infected cells ( $\delta$ , /day) had no relationship with mass (all species combined, p-value = 0.6).

We also used the adaptive immune response model (Eqs. 2 - 4, 6 - 7) to investigate how parameters related to the immune response scale with host body mass (multi-level model, Fig. 7 and Table 2). The rate of adaptive immune system mediated neutralization of virus ( $\rho$ , PRNT<sub>50</sub><sup>-1</sup>day<sup>-1</sup>) did not have a significant relationship with body mass (all species combined: p-value = 0.11,  $r^2 = 0.03$ , slope = -0.19), although we observed that in passerines it declined significantly with mass (p-value = 0.04,  $r^2 = 0.1$ , slope = -0.51). The time of initiation of IgM response ( $t_i$ ) also did not have a significant relationship with species mass (all species combined: slope = 0.002, p-value = 0.56,  $r^2 = 0.004$ ; only passerines: slope = 0.01, p-value = 0.07,  $r^2 = 0.08$ ).

The model parameter estimates and confidence intervals for all species are summarized in Tables 3 and 4. The ODE model predictions for viremia (for the parameters shown in Table 3 and 4) for all species are shown in Fig. 12, 13 and 14.

We also show the posterior distributions of parameters for two selected species to highlight the differences in model parameters between these species in Fig. 10 (target cell limited model parameters  $V_0$ ,  $\beta$ ,  $p$ ,  $\delta$  for two species: American crows and Canadian geese). This underscores the variation in parameters between different species. Similar variation was seen between other species.

Finally, we show the trace plots of samples from the posterior distribution (the Monte Carlo Markov chain after burn-in and thinning) in Fig. 11. These show that the inference procedure converges around a particular value with variation around it. There is variation around a mean consistent with what would be observed when parameters have been identified. Similar behaviour was seen for posterior distributions of other species (data not shown).

## 2.4 Accuracy in viremia prediction

We estimated the accuracy of viremia prediction by calculating three different estimates of a sum of squared residuals (SSR) between the data and the ODE model prediction (for both the multi-level and aggregated Bayesian models) as described in Materials and Methods (Subsection Estimate of accuracy in viremia prediction).

We observed that the multi-level model produced more accurate estimates at the individual-level and species-level (Fig. 9, top panel). A representative viremia prediction for both the multi-level and aggregated model is also shown (Fig. 9, bottom panel). The performance of both the models at the order-level were similar.

We note that in some cases our hierarchical Bayesian models produce parameter estimates that appear to be biologically unreasonable, e.g. the production rate of WNV from infected cells ( $p$ ) for some corvid species is predicted to be approximately  $10^8$  PFU day<sup>-1</sup>, which is unreasonably high. This could be due to the fact that the empirically measured viremia goes up to  $10^{15}$  PFU / mL in some of these species and the initial susceptible cell population density ( $T_0$  in our models) is much higher in corvids. This may suggest that other cell types are also available for infection in these species. Further experimental data on the susceptible cell population in corvid species may lead to more realistic estimates of the production rate (since these two parameters are correlated in our models).

### 3 Discussion

#### 3.1 Summary

Understanding how quickly pathogens replicate and how quickly the immune system responds is important for predicting the epidemic spread of emerging pathogens. Host body size, through its correlation with metabolic rates, is theoretically predicted to impact pathogen replication and immune system response [9]. Prior work suggests that body mass affects pathogen replication [3, 11, 44], but immune response times are either independent of mass or increase only very slowly as mass increases [11, 45]. Here, we use mathematical models of viral time courses from multiple species of birds infected by WNV to test more thoroughly how disease progression and immune response depend on host phylogeny and mass. The mathematical framework presented here is an approach to uncover systematic differences in disease progression and immune response in animals that differ in body mass and phylogeny.

Host phylogeny is an important determinant of the pathogenesis of WNV. Passerine species sustain more viremia than non-passerine species, and corvid species are particularly susceptible to WNV infection [13]. Therefore, any analysis of disease dynamics in multi-host pathogens like WNV should take host phylogeny into account. We accomplish this using hierarchical Bayesian models that incorporate the hierarchical nature of phylogeny. We observe that the multi-level model produces more accurate predictions of viremia at the individual and species level when compared to hierarchical models that have fewer levels of hierarchy (Fig. 9). Additionally, multi-level models with passerines and non-passerines or just passerines (Fig. 4, top and middle panels) produced more realistic and more strongly peaked distributions of  $R_0$  and burst size, than a multi-level model with only corvids (Fig. 4, bottom panel) and the aggregated model (Fig. 8). This appears to be due to the ability of multi-level models to pool information at the species level from different related species.

A major contribution of this work is a computational framework for infectious within-host disease modelling that leverages data from multiple species. This is particularly important given recent analysis of the many zoonotic diseases that have, or have potential to, cross species boundaries to infect humans [46]. Our models estimate a competency for infected hosts to infect mosquito vectors that can then sustain the disease between hosts. This link between within- and between-host disease models is an important step toward understanding the threat from emerging zoonotic diseases and identifying likely candidate species for biosurveillance.

#### 3.2 Effect of host phylogeny on within-host pathogen replication

We quantified the basic reproductive number ( $R_0$ ), which represents the average number of infections produced by a single infected cell. The mean values of  $R_0$  from the multi-level model are higher for

passerine species ( $R_0 = 23.8$ ) compared to non-passerines ( $R_0 = 4.7$ ) (Fig. 4, top panel). Within Passerines, corvid species have the highest mean value of  $R_0 = 93.2$ .

Burst sizes of passerine species (8690 PFU) are also much higher than those in non-passerines (340 PFU) (Fig. 4, top panel). This is consistent with experimental studies that found passerines and corvids have higher reservoir competency (ability to transmit infection to mosquitoes) than non-passerines [13]. Overall, host phylogeny emerges as a key determinant of biologically relevant quantities like the basic reproductive number and burst size. The mean passerines values for  $R_0$  (23.8) and burst size (8690 PFU) are also higher than the corresponding model predicted values in mice (mean  $R_0 = 2.5$  and burst size = 3 PFU [37]).

We also calculated a reservoir competence index that indicates the relative number of infectious mosquitoes that would be derived from feeding on these hosts (Section 1.6) and accounts for time-varying viremia and species relatedness (via the multi-level Bayesian model). The mean reservoir competence for passerine species (0.8) is higher than that of non-passerines (0.2). This lends mechanistic insight into why some species (smaller passerine species) are pathogen reservoirs and some (larger non-passerine species) are potentially dead-end hosts for WNV.

### 3.3 Effect of host body size on virion production rate and immune response

Individual cellular metabolic rates and biological times, if constrained by host metabolism, are expected to scale with host body mass as  $M^{-1/4}$  and  $M^{1/4}$ , respectively [4-9]. We observe that the production rate of infectious virions ( $p$ , /day) declined significantly with host body mass. While the 95% confidence interval for the slope (CI = [-1.5, 0.03]) includes the theoretically predicted exponent of -0.25 (Fig. 6), the confidence interval is too large to provide a meaningful estimate of the scaling exponent.

The death rate of productively infected cells ( $\delta$ , /day), also theoretically predicted to decrease with mass, had no relationship with species mass. The basic reproductive number ( $R_0$ ), declined significantly with body mass (Fig. 6) and the relationship is even more significant within passerine species. This is most likely due to the fact that the production rate of virions ( $p$ ), a component of the  $R_0$  (Eq. 11), declined with mass.

We found that the mean of peak viral concentration in serum (peak viremia) declines with species body mass (Fig. 6) although the correlation was only marginally significant. Additionally, most passerine species had higher peak viremia than non-passerines. This is likely due to the fact that most of the passerine species had a higher value of the viral production rate ( $p$ ) than the non-passerines. Overall, we observed modest trends in the direction predicted by scaling theory, but host phylogeny is a more important predictor of WNV dynamics.

The density of inoculated virions ( $V_0$ ) has no significant relationship with species mass (Fig. 6). This is surprising since if mosquitoes inoculated a fixed dose directly into the host bloodstream, the density of virions ( $V_0$ ) would be expected to decline with host mass since the dilution would be higher in the larger blood volume of a larger species. Mosquito inoculated WNV, that is initially localized at the site of infection [47], is taken up by immune cells to nearby lymph nodes and thereby trafficks to different organs via the bloodstream. However, for computational efficiency we use differential equation models that assume all components are well-mixed. Our results point to the importance of accounting for spatial patterns of viral spread, especially in the initial stages of an infection when virus is localized, and this should be considered in future work.

The target-cell limited and adaptive immune response models both produce similar scaling predictions when coupled to the multi-level hierarchical model (Table 2).

We used the adaptive immune response model (Eqs. 2 - 4, 6 - 7) to investigate how parameters related to the immune response scale with host body mass (multi-level model, Fig. 7). The rate at which the adaptive (antibody) immune response neutralizes virus ( $\rho$ ) did not have a significant relationship with body mass, although we observed that in passerine species it declined significantly with mass. The time

of initiation of the adaptive (antibody) immune response ( $t_i$ ) also did not have a significant relationship with species mass.

Hence in sharp contrast to the vast majority of biological rates that slow systematically as body size increases [7,8], the rate at which the adaptive (antibody) immune response clears WNV and the time at which it is initiated do not vary systematically with mass (Fig. 7). Previous work has suggested two plausible mechanisms that both enable this scale-invariant search and response. A sub-modular architecture of lymph nodes, that balances local pathogen detection and global antibody production, may lead to nearly scale-invariant search and response times [11]. Chemical signals released from infected sites also help guide immune system cells towards infected regions, reducing the time for the immune system to search for infection [12].

### 3.4 Implications for spread of WNV and other zoonotic diseases

Our modeling suggests that rates of WNV production decline with species mass whereas rates and times related to the adaptive immune response do not vary systematically with mass. Taken together, these results provide an understanding of how epidemiological determinants vary with species body mass. The probability of infecting an uninfected mosquito increases with viremia above a certain threshold for WNV [13]. This has also been observed for other flaviviruses such as dengue virus [48,49]). Above a threshold of viremia of  $10^5$  PFU/mL of blood, a host is capable of infecting an uninfected mosquito and maintaining WNV in an enzootic cycle [13]. Hence hosts that can sustain high viremia above this threshold and for a longer duration are pathogen reservoirs [13]. The dependence of viremia on host mass and phylogeny may give important insights into the role of mass and phylogeny on the spread of WNV. For example, larger non-passerine species, predicted to have lower viremia, may be less competent as pathogen reservoirs.

Incorporating our within-host viral dynamics model into a between-host model that incorporates interactions between vectors and hosts, mosquito biting preferences [50–52] and bird abundance would be a fruitful avenue for future work. This analysis should consider the multiple ways in which host body size and phylogeny effect mosquito biting rates. Larger animals might have a greater probability of receiving an infective bite due to their larger surface area. However, the relationship between body size and the frequency of mosquito bites is complicated by several factors. For example, mosquitoes also have distinct biting preferences across species [50,51] and the ecological niche occupied by the species may influence biting rates. The effect of total body surface area may be limited given that the footpads, neck and the face are the only exposed regions in birds that do not have feathers and are most accessible for biting. Finally, body size affects population density which is approximately inversely proportional to host metabolism [53], and relative abundance of a species is another important factor in determining the spread of WNV. There are many unknowns and we speculate that models that combine species body size and other ecological factors with within-host modelling will be important in predicting outcomes of emerging diseases and formulating outbreak control strategies, as has been proposed for vector-borne diseases [54], Dengue virus [48], Zika virus [55] and Ebola virus [56].

Our analysis suggests an important role for both species mass and host phylogeny in dictating epidemiological determinants like basic reproductive number, WNV production rate, peak viremia in blood and host competency to infect mosquitoes. Our model is based on a principled analysis and gives a quantitative prediction for key epidemiological determinants and how they vary with species mass and phylogeny. The WNV production rate ( $p$ ) and the basic reproductive number ( $R_0$ ) decline with host body mass (Fig. 6). The relationship is even more significant within passerine species (Fig. 6).

We calculated a reservoir competence index that indicates the relative number of infectious mosquitoes that would be derived from feeding on these hosts (Section 1.6). Our reservoir competency index is a refinement on previously published indices [13] since they take time-varying viremia and species relatedness (via the multi-level Bayesian model) into account. The reservoir competency indices we calculate are correlated with and approximately half of the estimates in Komar et al. [13] (Fig. 5). The mean

reservoir competence for passerine species (0.8) is higher than that of non-passerines (0.2). Thus, our models provide insight into why some species (smaller passerine species) are pathogen reservoirs and some (larger non-passerine species) are potentially dead-end hosts for WNV.

WNV infection progresses along multiple scales: infection within hosts is related to dynamics of WNV spread between hosts by mosquito vectors. Coupling two different processes over multiple scales, from individual cells to epidemic spread in bird populations, is challenging and could yield valuable insights. Our predictions of host competency to infect mosquitoes (Eq. 8 and Fig. 5) can be coupled to models of WNV spread between multiple species. Such an approach would help link within-host WNV dynamics to dynamics between hosts and may help produce accurate estimates of spread of WNV.

Hierarchical Bayesian models coupled with within-host viral dynamics models can leverage data from multiple species to infer how body size and host phylogeny affect viral dynamics. This approach can be applied to model other zoonotic diseases and multi-host pathogens [37], particularly other emerging viruses such as dengue [32, 48], Ebola [56] and Zika virus [33, 55].

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## Supplementary Information

### Bayesian Aggregated Model

The aggregated model has individuals of different species. The individuals are aggregated to form a tree of height 2. The model is shown graphically in Fig. 2 (Left panel).

We denote the number of individuals by  $n$  and the number of experimental measurements of virus concentration on the  $i$ th individual by  $m_i$ .  $y_{ij}(t_j)$  represents the experimental measurements of logarithmic virus concentration in serum for the  $i$ th individual at times  $t_j$  ( $j = 1, 2, 3, \dots, m_i$ ). For notational convenience, let  $\mu = (\log_{10} V_0, \log_{10} \beta, \log_{10} p, \log_{10} \delta)^T$ ,  $\theta_i = (\log_{10} V_{0i}, \log_{10} \beta_i, \log_{10} p_i, \log_{10} \delta_i)^T$ ,  $\Theta = \{\theta_i, i = 1..n\}$ ,  $Y = \{y_{ij}, i = 1..n, j = 1..m_i\}$  and  $f_{ij}(\theta_i, t_j) = \log_{10} V_{ij}(\theta_i, t_j)$  where  $V_{ij}(\theta_i, t_j)$  denotes the numerical solution for  $V(t)$  in Eq. 5 for the  $i$ th individual at time  $t_j$ .

The Bayesian non-linear mixed effects aggregated model can be written as the following three stages [19, 20, 57]:

1. Within-individual variation

$$[y_i | \theta_i, \sigma^2] \sim \text{Normal}(f_i(\theta_i), \sigma^2) \quad (12)$$

2. Between-individual variation

$$[\theta_i | \mu, \Sigma] \sim \text{Normal}(\mu, \Sigma) \quad (13)$$

3. Prior distributions

$$\sigma^{-2} \sim \text{Gamma}(a, b), \Sigma^{-1} \sim \text{Wishart}(\Omega, \nu), \mu \sim \text{Normal}(\eta, \Lambda) \quad (14)$$

The Normal, Wishart and Gamma distributions are chosen to simplify calculations [57, 58].

The full conditional distributions for  $\theta_i$ ,  $\sigma^{-2}$ ,  $\mu$  and  $\Sigma^{-1}$  can be written as [57, 58]:

$$[\theta_i | \sigma^{-2}, \mu, \Sigma, \eta, \Theta, Y] \propto \exp \left( -\frac{\sigma^{-2}}{2} \sum_{j=1}^{m_i} [y_{ij} - f_{ij}(\theta_i, t_j)]^2 - \frac{1}{2} (\theta_i - \mu)^T \Sigma^{-1} (\theta_i - \mu) \right) \quad (15)$$

$$[\sigma^{-2} | \mu, \Sigma, \Theta, Y] \sim \text{Gamma} \left( a + \frac{\sum_{i=1}^n m_i}{2}, A^{-1} \right) \quad (16)$$

$$[\mu | \sigma^{-2}, \Sigma, \Theta, Y] \sim \text{Normal} (B^{-1}C, B^{-1}) \quad (17)$$

$$[\Sigma^{-1} | \sigma^{-2}, \mu, \Theta, Y] \sim \text{Wishart} (D^{-1}, n + \nu) \quad (18)$$

where  $A = b^{-1} + \frac{1}{2} \sum_{i=1}^n \sum_{j=1}^{m_i} [y_{ij} - f_{ij}(\theta_i, t_j)]^2$ ,  $B = n\Sigma^{-1} + \Lambda^{-1}$ ,  $C = \Sigma^{-1} \sum_{i=1}^n \theta_i + \Lambda^{-1}\eta$  and  $D = \Omega^{-1} + \sum_{i=1}^n (\theta_i - \mu) \cdot (\theta_i - \mu)^T$ .

The parameters  $\sigma^{-2}$ ,  $\mu$  and  $\Sigma^{-1}$  are sampled using a Gibbs sampler and a Metropolis-Hastings algorithm is used to sample  $\theta_i$  (both algorithms are described later).

## Bayesian Multi-level Model

The multi-level hierarchical model has groups (species) with individuals in each group. The groups are arranged hierarchically to form a tree of height 3. The model is shown graphically in Fig. 1 (Left panel). Let there be  $m$  distinct species indexed by  $k$  and the number of individuals in the  $k$ th group is represented by  $n_k$ . Let us represent the number of experimental measurements on the  $i$ th individual of the  $k$ th species by  $m_{ik}$ .  $y_{ijk}(t_j)$  represents the experimental measurements of logarithmic virus concentration in serum for the  $i$ th individual belonging to the  $k$ th species at times  $t_j (j = 1, 2, 3, \dots, m_{ik})$ .

For notational convenience, we define the individual level distribution ( $i$ th individual belonging to the  $k$ th species) by  $\theta_{ik} = (\log_{10}V_{0ik}, \log_{10}\beta_{ik}, \log_{10}p_{ik}, \log_{10}\delta_{ik})^T$ . We define the  $k$ th species level distribution by  $\mu_k = (\log_{10}V_{0,k}, \log_{10}\beta_k, \log_{10}p_k, \log_{10}\delta_k)^T$  and the genus level distribution by  $\eta = (\log_{10}V_0, \log_{10}\beta, \log_{10}p, \log_{10}\delta)^T$ .

Let  $\Theta = \{\theta_{ik}, i = 1..n_k, k = 1..m\}$ ,  $Y = \{y_{ijk}, i = 1..n_k, j = 1..m_{ik}, k = 1..m\}$  and  $f_{ijk}(\theta_{ik}, t_j) = \log_{10}V_{ijk}(\theta_{ik}, t_j)$  where  $V_{ijk}(\theta_{ik}, t_j)$  denotes the numerical solution for  $V(t)$  in Eq. 5 for the  $i$ th individual (belonging to the  $k$ th species) at time  $t_j$ .

We write this Bayesian non-linear mixed effects multi-level model as the following four stages:

1. Within-individual variation

$$[y_{ik}|\theta_{ik}, \sigma_k^2] \sim \text{Normal}(f_{ik}(\theta_{ik}), \sigma_k^2) \quad (19)$$

for the  $i$ th individual belonging to the  $k$ th species.

2. Between-individual variation

$$[\theta_{ik}|\mu_k, \Sigma_k] \sim \text{Normal}(\mu_k, \Sigma_k) \quad (20)$$

3. Between species variation

$$\sigma_k^{-2} \sim \text{Gamma}(a, b), \Sigma_k^{-1} \sim \text{Wishart}(\Omega, \nu), \mu_k \sim \text{Normal}(\eta, \Lambda) \quad (21)$$

for the  $k$ th species. The Normal, Wishart and Gamma distributions are chosen to simplify calculations.

4. Genus level prior distributions

$$\eta \sim \text{Normal}(x, y), \Lambda^{-1} \sim \text{Wishart}(p, q) \quad (22)$$

Fig. 1 (right panel) represents these equations graphically in a plate diagram. In a graphical model like Fig. 1 (right panel), for any node  $u$ , we can represent the remaining nodes by  $U_{-u}$  and the full conditional distribution  $P(u, U_{-u})$  is  $\propto P(u|\text{parents}[u]) \cdot \prod_{w \in \text{children}[u]} P(w|\text{parents}[w])$  [41]. The full conditional distribution for  $u$  contains a prior component (from the parents of  $u$ ) and a likelihood component (from each child of  $u$ ).

Following the principle above and simplifying, we derived the full conditional distributions for  $\theta_{ik}$ ,  $\sigma_k^{-2}$ ,  $\mu_k$ ,  $\Sigma_k^{-1}$ ,  $\eta$  and  $\Lambda^{-1}$ :

$$[\theta_{ik}|\sigma_k^{-2}, \mu_k, \Sigma_k, \eta, \Lambda^{-1}, \Theta, Y] \propto \exp \left( -\frac{\sigma_k^{-2}}{2} \sum_{j=1}^{m_{ik}} [y_{ijk} - f_{ijk}(\theta_{ik}, t_j)]^2 - \frac{1}{2} (\theta_{ik} - \mu_k)^T \Sigma_k^{-1} (\theta_{ik} - \mu_k) \right) \quad (23)$$

$$[\sigma_k^{-2} | \mu_k, \Sigma_k, \eta, \Lambda^{-1}, \Theta, Y] \sim \text{Gamma} \left( a + \frac{\sum_{i=1}^n m_{ik}}{2}, A_k^{-1} \right) \quad (24)$$

$$[\mu_k | \sigma_k^{-2}, \Sigma_k, \eta, \Lambda^{-1}, \Theta, Y] \sim \text{Normal} (B_k^{-1} C_k, B_k^{-1}) \quad (25)$$

$$[\Sigma_k^{-1} | \sigma_k^{-2}, \mu_k, \eta, \Lambda^{-1}, \Theta, Y] \sim \text{Wishart} (D_k^{-1}, n_k + \nu) \quad (26)$$

$$[\eta | \sigma_k^{-2}, \mu_k, \Sigma_k^{-1}, \Lambda^{-1}, \Theta, Y] \sim \text{Normal} (z, Z) \quad (27)$$

$$[\Lambda^{-1} | \sigma_k^{-2}, \mu_k, \Sigma_k^{-1}, \eta, \Theta, Y] \sim \text{Wishart} (E, q + m) \quad (28)$$

where  $A_k = b^{-1} + \frac{1}{2} \sum_{i=1}^{n_k} \sum_{j=1}^{m_{ik}} [y_{ijk} - f_{ijk}(\theta_{ik}, t_j)]^2$ ,  $B_k = n_k \Sigma_k^{-1} + \Lambda^{-1}$ ,  $C_k = \Sigma_k^{-1} \sum_{i=1}^{n_k} \theta_{ik} + \Lambda^{-1} \eta$ ,  $D_k = \Omega^{-1} + \sum_{i=1}^{n_k} (\theta_{ik} - \mu_k) \cdot (\theta_{ik} - \mu_k)^T$ ,  $Z = (U^{-1} + y^{-1})^{-1}$ ,  $z = Z (U^{-1} u + y^{-1} x)$  and  $E^{-1} = p^{-1} + \sum_{k=1}^m (\mu_k - \eta) \cdot (\mu_k - \eta)^T$ .

The parameters  $\sigma_k^{-2}$ ,  $\mu_k$ ,  $\Sigma_k^{-1}$ ,  $\eta$  and  $\Lambda^{-1}$  are sampled using a Gibbs sampler and a Metropolis-Hastings algorithm is used to sample  $\theta_{ik}$  (both algorithms are described later).

## Metropolis-Hastings Sampler

We use two popular MCMC algorithms known as the Metropolis-Hastings sampler and the Gibbs sampler. We use these algorithms to sample from the posterior distribution  $P(\Theta|D)$ . Let  $\Theta^{(t)}$  represent the state of the Markov chain at iteration  $t$  of the algorithm. The Metropolis-Hastings sampler uses a proposal distribution  $q(\Theta|\Theta^{(t-1)})$  to generate a candidate point,  $\Theta^*$ , that is conditioned on the previous state of the sampler,  $\Theta^{(t-1)}$ . In the next step, the algorithm either accepts or rejects the candidate point based on an acceptance probability:

$$\alpha = \min(1, \frac{P(\Theta^*)}{P(\Theta^{(t-1)})} \cdot \frac{q(\Theta^{(t-1)}|\Theta^*)}{q(\Theta^*|\Theta^{(t-1)})}) \quad (29)$$

The Metropolis-Hastings algorithm is as follows:

1. Set  $t = 1$
2. Generate an initial value  $u$ , and set  $\Theta^{(t)} = u$
3. Repeat
  - $t = t + 1$
  - Generate a candidate  $\Theta^*$  from the proposal distribution  $q(\Theta|\Theta^{(t-1)})$
  - Evaluate the probability of acceptance,  $\alpha = \min(1, \frac{P(\Theta^*)}{P(\Theta^{(t-1)})} \cdot \frac{q(\Theta^{(t-1)}|\Theta^*)}{q(\Theta^*|\Theta^{(t-1)})})$
  - Generate a  $x$  from a Uniform(0,1) distribution
  - If  $x \leq \alpha$ , accept the candidate solution and set  $\Theta^t = \Theta^*$ , else set  $\Theta^t = \Theta^{(t-1)}$
4. Until  $t =$  required number of iterations

The Metropolis-Hastings sampler has the advantage of not requiring knowledge of the normalizing constant,  $P(D)$ . In our case the parameter  $\Theta$  is multi-variate and has different components corresponding to the different ODE model parameters. We accept or reject the candidate solution involving all components as a block simultaneously. This is known as a block-wise updating scheme. A component-wise updating scheme updates each component in turn and independently of each other.

We use the Metropolis-Hastings sampler to sample the ordinary differential equation model parameters  $\theta_i$  (Bayesian aggregated model) and  $\theta_{ik}$  (Bayesian multi-level model).

## Gibbs Sampler

The Gibbs sampler is an algorithm in which all samples are accepted and hence is computationally more efficient than the Metropolis-Hastings sampler. However, the Gibbs sampler can only be applied in the case when we know the full conditional distribution of each component of the parameter  $\Theta$  conditioned on all other components.

As an illustrative example, we show the workings of the Gibbs sampler for the joint two-component distribution  $g(\theta_1, \theta_2)$ . The Gibbs sampler can be used if we can derive the distribution of each component conditioned on the other, i.e. in this case the conditional distributions  $g(\theta_1|\theta_2 = \theta_2^{(t)})$  and  $g(\theta_2|\theta_1 = \theta_1^{(t)})$ . The Gibbs sampler for the case of two-components is as follows:

1. Set  $t = 1$
2. Generate an initial value  $u = (u_1, u_2)$ , and set  $\Theta^{(t)} = u$
3. Repeat
  - $t = t + 1$
  - Sample  $\theta_1^{(t)}$  from the conditional distribution  $g(\theta_1|\theta_2 = \theta_2^{(t-1)})$
  - Sample  $\theta_2^{(t)}$  from the conditional distribution  $g(\theta_2|\theta_1 = \theta_1^{(t)})$
4. Until  $t =$  required number of iterations

We update each component sequentially in turn (systematic-scan Gibbs sampler). In the Bayesian aggregated model, the parameters  $\sigma^{-2}$ ,  $\mu$  and  $\Sigma^{-1}$  are sampled using a Gibbs sampler. In the Bayesian multi-level model, the Gibbs sampler is used to sample the parameters  $\sigma_k^{-2}$ ,  $\mu_k$ ,  $\Sigma_k^{-1}$ ,  $\eta$  and  $\Lambda^{-1}$ .

Our approach is to use the Metropolis-Hastings sampler within the Gibbs sampler; this involves using the computationally efficient Gibbs update steps whenever the full posterior conditional distributions are known and using Metropolis-Hastings acceptance steps when the full conditional distribution is not available.

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## Tables

**Table 1.** Parameter constraints for the target cell limited and adaptive immune response models in birds

Parameters	Description	Estimated Ranges	Source
$\gamma$	WNV clearance rate	44.4/day for non-corvids and 1/day for corvids	Value for non-corvids estimated from fit to viral decay study in wildtype mice [59] ( [37])
$\eta$	Rate of IgM production	54.7/day	Fit to antibody titer study in wildtype mice [36] ( [37])
$T_0$	Initial target cell density	$2.3 \times 10^5$ /mL	Average of estimated range in mice from [60] ( [37])
$k$	Rate of transition from $I_1$ to $I_2$	4/day	Upper bound of estimate in mice from [61,62] ( [37])
$1/\delta$	Lifetime of productively infected cells	$\leq 24 - 1/k$ days	Calculations in mice ( [37])
$t_i$	Time of initiation of IgM response (days post infection)	2 - 4 days	Estimates in mice [36] ( [37])
$V_0$	Initial viral titer	0.1 - $10^{12}$ PFU/mL	Model constraint in birds
$p$	Rate of WNV production	0.5 - $10^{12}$ PFU/day	Model constraint in birds
$p/\delta$	Infectious virion burst size	$\leq 10^{12}$ PFU	Model constraint in birds
$\rho$	Efficacy of antibody neutralization	0.05 - $1000 \text{ PRNT}_{50}^{-1} \text{ day}^{-1}$	Model constraint in birds

**Table 2.** Statistics of scaling relationships with species mass (all species combined) from multi-level model with target cell limitation (TCL) or an adaptive immune response (AIR)

Parameters	Combined slope	p-value	$r^2$
$p$ (TCL): WNV production rate	-1.1	0.002	0.11
$p$ (AIR): WNV production rate	-0.84	0.04	0.05
$R_0$ (TCL): Basic reproductive number	-1.3	0.006	0.09
$R_0$ (AIR): Basic reproductive number	-0.57	0.08	0.04
$p/\delta$ (TCL): Burst size	-1.1	0.001	0.12
$p/\delta$ (AIR): Burst size	-0.86	0.03	0.06
$V_p$ (TCL): Peak viremia	-0.82	0.06	0.04
$V_p$ (AIR): Peak viremia	-	0.54	0.005
$V_0$ (TCL): Inoculated WNV density	-	0.35	0.1
$V_0$ (AIR): Inoculated WNV density	-	0.1	0.03
$\beta$ (TCL): WNV infectivity	-	0.64	0.003
$\beta$ (AIR): WNV infectivity	-	0.39	0.009
$\delta$ (TCL): Death rate of productively infected cells	-	0.6	0.003
$\delta$ (AIR): Death rate of productively infected cells	-	0.51	0.005
$\rho$ (AIR): Rate of adaptive immune system mediated virus neutralization	-	0.11	0.03
$t_i$ (AIR): Time of initiation of IgM response	-	0.56	0.004

**Table 3.** Estimated parameters (mean and 95% confidence interval) for all species from the multi-level model with target cell limitation (TCL).  $V_0$  - inoculated virus density (PFU/mL),  $\beta$  - rate constant of infection [ $\text{mL day}^{-1}$ ],  $p$  - infectious virus production rate (PFU  $\text{day}^{-1}$ ),  $\delta$  - death rate of productively infected cells ( $\text{day}^{-1}$ ).

Species	$V_0$	$\beta$	$p$	$\delta$
Fishcrow	$5 \cdot 10^3$ [ $4.3 \cdot 10^3$ , $5.8 \cdot 10^3$ ]	$3.7 \cdot 10^{-9}$ [ $2.8 \cdot 10^{-9}$ , $4.8 \cdot 10^{-9}$ ]	$2.1 \cdot 10^4$ [ $1.8 \cdot 10^4$ , $2.4 \cdot 10^4$ ]	4.8 [4.5, 5]
Bluejay	$2.9 \cdot 10^3$ [ $2.5 \cdot 10^3$ , $3.3 \cdot 10^3$ ]	$3.9 \cdot 10^{-8}$ [ $3.3 \cdot 10^{-8}$ , $4.6 \cdot 10^{-8}$ ]	$4.9 \cdot 10^4$ [ $4.4 \cdot 10^4$ , $5.5 \cdot 10^4$ ]	5.3 [4.9, 5.6]
American crow	740 [650.4, 842.2]	$1.6 \cdot 10^{-9}$ [ $1.4 \cdot 10^{-9}$ , $1.9 \cdot 10^{-9}$ ]	$1.4 \cdot 10^4$ [ $1.3 \cdot 10^4$ , $1.6 \cdot 10^4$ ]	6.2 [5.9, 6.4]
Common grackle	185.1 [163.1, 210]	$4.4 \cdot 10^{-8}$ [ $3.8 \cdot 10^{-8}$ , $5 \cdot 10^{-8}$ ]	$2.5 \cdot 10^5$ [ $2.2 \cdot 10^5$ , $2.8 \cdot 10^5$ ]	6.8 [6.6, 7]
American robin	$1.1 \cdot 10^3$ [ $0.9 \cdot 10^3$ , $1.3 \cdot 10^3$ ]	$4.8 \cdot 10^{-8}$ [ $4.2 \cdot 10^{-8}$ , $5.4 \cdot 10^{-8}$ ]	$1.5 \cdot 10^5$ [ $1.3 \cdot 10^5$ , $1.7 \cdot 10^5$ ]	7.4 [7.1, 7.6]
Redwinged black-bird	731.4 [648.7, 824.6]	$8 \cdot 10^{-7}$ [ $7.2 \cdot 10^{-7}$ , $8.7 \cdot 10^{-7}$ ]	$1.5 \cdot 10^4$ [ $1.4 \cdot 10^4$ , $1.6 \cdot 10^4$ ]	6.4 [6.2, 6.6]
Blackbilled magpie	$1.4 \cdot 10^3$ [ $1.2 \cdot 10^3$ , $1.5 \cdot 10^3$ ]	$1 \cdot 10^{-7}$ [ $0.9 \cdot 10^{-7}$ , $1.1 \cdot 10^{-7}$ ]	$5.2 \cdot 10^4$ [ $4.8 \cdot 10^4$ , $5.7 \cdot 10^4$ ]	5.3 [5.1, 5.5]
House finch	305.9 [269.2, 347.8]	$1.3 \cdot 10^{-7}$ [ $1.1 \cdot 10^{-7}$ , $1.5 \cdot 10^{-7}$ ]	$3.5 \cdot 10^4$ [ $3.1 \cdot 10^4$ , $3.8 \cdot 10^4$ ]	3.1 [2.9, 3.3]
House sparrow	$3.4 \cdot 10^3$ [ $3 \cdot 10^3$ , $3.9 \cdot 10^3$ ]	$2.2 \cdot 10^{-7}$ [ $1.9 \cdot 10^{-7}$ , $2.5 \cdot 10^{-7}$ ]	$7.4 \cdot 10^4$ [ $6.6 \cdot 10^4$ , $8.2 \cdot 10^4$ ]	4.6 [4.5, 4.7]
Mallard	164.2 [146.4, 184.1]	$2.5 \cdot 10^{-6}$ [ $2.3 \cdot 10^{-6}$ , $2.9 \cdot 10^{-6}$ ]	$3.3 \cdot 10^3$ [ $3 \cdot 10^3$ , $3.7 \cdot 10^3$ ]	5.4 [5.2, 5.7]

**Table 4.** Estimated parameters (mean and 95% confidence interval) for all species from multi-level model with target cell limitation (TCL) (continued from Table 3).  $V_0$  - inoculated virus density (PFU/mL),  $\beta$  - rate constant of infection [mL day<sup>-1</sup>],  $p$  - infectious virus production rate (PFU day<sup>-1</sup>),  $\delta$  - death rate of productively infected cells (day<sup>-1</sup>).

Species	$V_0$	$\beta$	$p$	$\delta$
Mourning dove	867.9 [750, 1000.4]	$5.3 \cdot 10^{-6}$ [ $4.8 \cdot 10^{-6}$ , $5.9 \cdot 10^{-6}$ ]	$1.1 \cdot 10^3$ [ $1 \cdot 10^3$ , $1.2 \cdot 10^3$ ]	5.3 [5.1, 5.6]
Ringbilled gull	$3.2 \cdot 10^3$ [ $2.8 \cdot 10^3$ , $3.7 \cdot 10^3$ ]	$1.8 \cdot 10^{-7}$ [ $1.6 \cdot 10^{-7}$ , $2.1 \cdot 10^{-7}$ ]	$2.8 \cdot 10^4$ [ $2.5 \cdot 10^4$ , $3.1 \cdot 10^4$ ]	3.5 [3.4, 3.6]
Great-horned owl	$1 \cdot 10^3$ [ $0.9 \cdot 10^3$ , $1.1 \cdot 10^3$ ]	$3.4 \cdot 10^{-7}$ [ $3.1 \cdot 10^{-7}$ , $3.7 \cdot 10^{-7}$ ]	$1.5 \cdot 10^4$ [ $1.4 \cdot 10^4$ , $1.7 \cdot 10^4$ ]	4.6 [4.5, 4.9]
American kestrel	$2.1 \cdot 10^3$ [ $1.8 \cdot 10^3$ , $2.4 \cdot 10^3$ ]	$2.5 \cdot 10^{-7}$ [ $2.2 \cdot 10^{-7}$ , $2.9 \cdot 10^{-7}$ ]	$3.3 \cdot 10^4$ [ $3 \cdot 10^4$ , $3.8 \cdot 10^4$ ]	5.5 [5.3, 5.7]
Killdeer	871.7 [769.5, 987.3]	$5.9 \cdot 10^{-7}$ [ $5.3 \cdot 10^{-7}$ , $6.7 \cdot 10^{-7}$ ]	$1.9 \cdot 10^4$ [ $1.8 \cdot 10^4$ , $2.1 \cdot 10^4$ ]	5.2 [4.9, 5.4]
Northern bobwhite	$4.7 \cdot 10^3$ [ $3.9 \cdot 10^3$ , $5.6 \cdot 10^3$ ]	$2.6 \cdot 10^{-6}$ [ $2.1 \cdot 10^{-6}$ , $3.1 \cdot 10^{-6}$ ]	$1.1 \cdot 10^3$ [ $0.9 \cdot 10^3$ , $1.3 \cdot 10^3$ ]	2.7 [2.5, 2.9]
Northern flicker	250.3 [223.6, 280.2]	$7.2 \cdot 10^{-6}$ [ $6.6 \cdot 10^{-6}$ , $8 \cdot 10^{-6}$ ]	884.3 [811.6, 963.5]	5.9 [5.7, 6.3]
Rockdove	228.4 [200.7, 259.9]	$8.5 \cdot 10^{-5}$ [ $7.9 \cdot 10^{-5}$ , $9 \cdot 10^{-5}$ ]	95.7 [90.8, 100.9]	5.5 [5.3, 5.7]
American coot	208.7 [182.4, 238.7]	$2.1 \cdot 10^{-5}$ [ $1.8 \cdot 10^{-5}$ , $2.3 \cdot 10^{-5}$ ]	207.4 [187.9, 228.8]	5.3 [5, 5.6]
Monk parakeet	$2.3 \cdot 10^3$ [ $1.9 \cdot 10^3$ , $2.7 \cdot 10^3$ ]	$1.3 \cdot 10^{-5}$ [ $1.1 \cdot 10^{-5}$ , $1.5 \cdot 10^{-5}$ ]	296.3 [264.9, 331.5]	6.1 [5.7, 6.5]
Budgerigar	674.7 [599.4, 759.4]	$2.9 \cdot 10^{-6}$ [ $2.5 \cdot 10^{-6}$ , $3.4 \cdot 10^{-6}$ ]	860.8 [757.2, 978.6]	4.8 [4.5, 5.1]
Canada goose	647.3 [553.2, 757.3]	$4.1 \cdot 10^{-5}$ [ $3.7 \cdot 10^{-5}$ , $4.6 \cdot 10^{-5}$ ]	144.5 [131, 159.4]	4.8 [4.5, 5.2]



## Figure Legends

**Figure 1.** Left Panel: Multi-level hierarchical model with two groups. Each group has three individuals. Also shown are the genus, species and individual levels. Right Panel: Plate diagram for the multi-level hierarchical model. The plate denotes iteration of parameters and the number enclosed in the plate shows the number of iterations.

**Figure 2.** Left Panel: Aggregated model with two groups combined. Each group has three individuals. Also shown are the genus, species and individual levels. Right Panel: Plate diagram for the aggregated model. The plate denotes iteration of parameters and the number in the plate shows the number of iterations.

**Figure 3.** A sample prediction of the ODE model given by Eqs. 2-5 for plasma virus concentration (in  $\log_{10}$  PFU/mL) over time post infection (blue) and experimental data on virus concentration (red). Data show viremia of great-horned owls from [13].

**Figure 4.** Posterior distribution of  $\log_{10} R_0$  and burst size ( $\log_{10} p/\delta$ ) for the multi-level model (target cell limited model). Top panel: Multi-level model with all passerines (red), corvids (green) and non-Passerines (blue). Middle panel: Multi-level model with only passerines (red) and corvids (green). Bottom panel: Multi-level model with only corvids (green).

**Figure 5.** Correlation between multi-level model predicted competency and competency from Komar et al. [13] assuming static viremia ( $r^2 = 0.94$ , slope = 0.54, p-value = 0)

**Figure 6.** Scaling of biologically relevant quantities with host mass for the multi-level model: Passerines (black square and black regression line, non-passerines (red circle and red regression line) and all combined (blue regression line). Top left: Peak viremia ( $V_p$ ), slope = -0.82, p-value = 0.06,  $r^2 = 0.04$ . Top right: WNV production rate ( $p$ ), slope = -1.1, p-value = 0.002,  $r^2 = 0.11$ . Bottom left: Inoculated density of virions ( $V_0$ ), p-value = 0.35. Bottom right:  $R_0$ , slope = -1.3, p-value = 0.006,  $r^2 = 0.09$ .

**Figure 7.** Scaling of immune response parameters with host mass for the multi-level model with immune response: Passerines (black square) and non-passerines (red circle). Left panel: Rate of adaptive immune system mediated virus neutralization ( $\rho$ ,  $\text{PRNT}_{50}^{-1}\text{day}^{-1}$ ). Right panel: Time of initiation of IgM response ( $t_i$ , days) (combined and each group separately are non-significant).

**Figure 8.** Posterior distribution of  $\log_{10} R_0$  and burst size ( $\log_{10} p/\delta$ ) for the aggregated model (target cell limited model). Top panel: Aggregated model with all passerines (red), corvids (green) and non-passerines (blue). Middle panel: Aggregated model with only passerines (red) and corvids (green). Bottom panel: Aggregated model with only corvids (green).

**Figure 9.** Top panel: Accuracy in viremia prediction between multi-level model (blue) and aggregated model (red) for three different levels - individual, species and order. SSR - sum of squared residuals between model predicted viremia and data. Bottom panel: A sample viremia prediction from the multi-level (blue) and aggregated model (red).

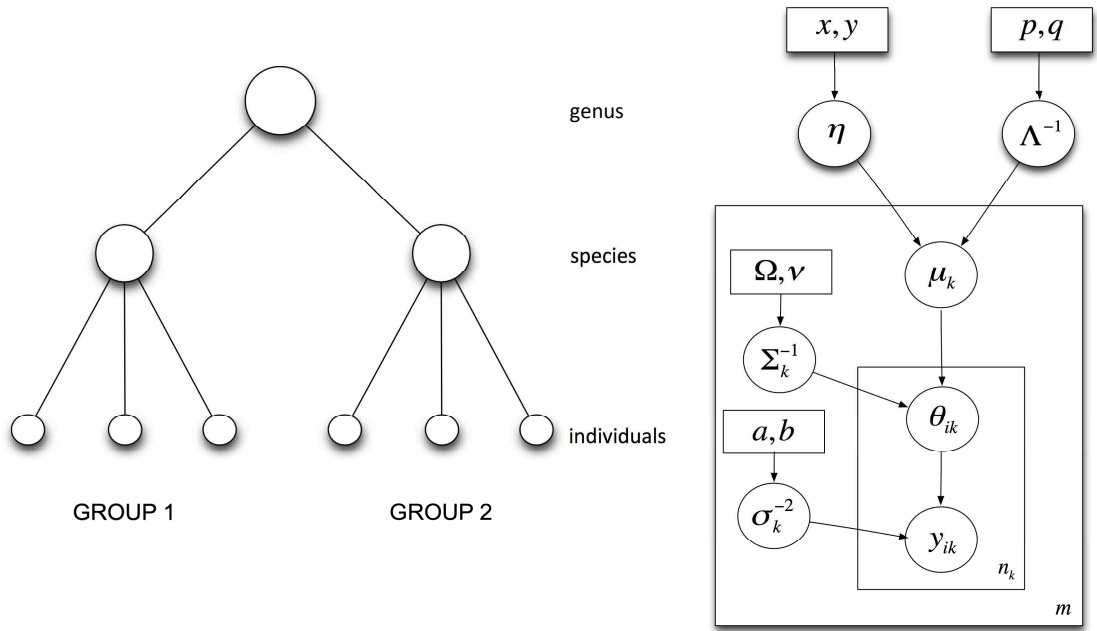
**Figure 10.** Top panel: Posterior distribution of target cell limited model parameters for American crows. Bottom panel: Posterior distribution of target cell limited model parameters for Canadian geese. Parameters shown are  $V_0$  - inoculated virus density (PFU/mL),  $\beta$  - rate constant of infection [ $\text{mL day}^{-1}$ ],  $p$  - infectious virus production rate (PFU  $\text{day}^{-1}$ ),  $\delta$  - death rate of productively infected cells ( $\text{day}^{-1}$ ).

**Figure 11.** Trace of samples from the Monte Carlo Markov Chain after burn-in and thinning (taking every 5th sample). Top panel: Trace of parameters of target cell limited model parameters for American crows. Bottom panel: Trace of parameters of target cell limited model parameters for Canadian geese. Parameters shown are  $V_0$  - inoculated virus density (PFU/mL),  $\beta$  - rate constant of infection [ $\text{mL day}^{-1}$ ],  $p$  - infectious virus production rate (PFU  $\text{day}^{-1}$ ),  $\delta$  - death rate of productively infected cells ( $\text{day}^{-1}$ ).

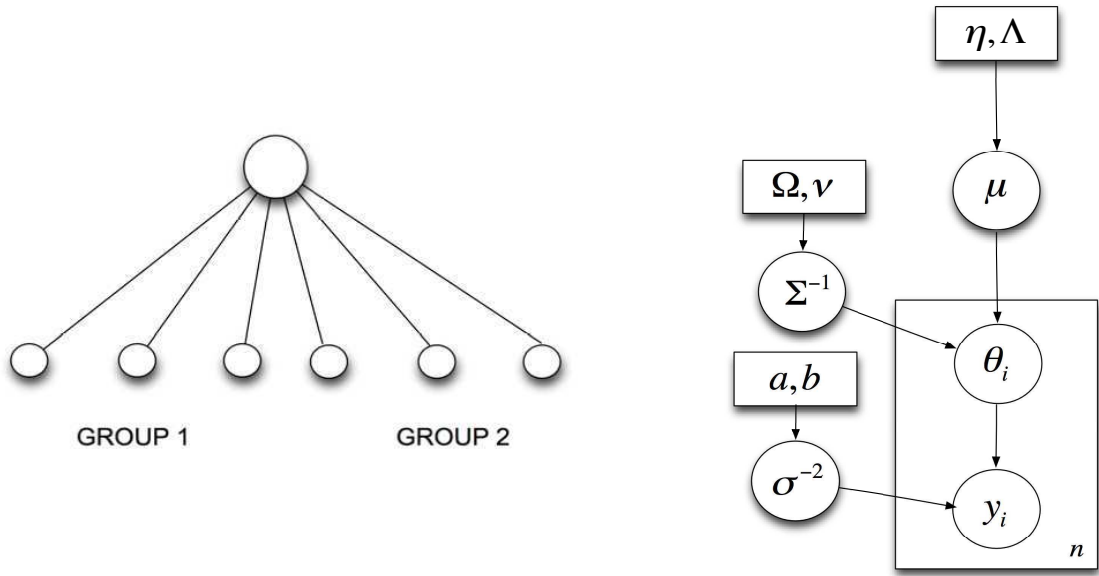
**Figure 12.** Predictions from the ODE model given by Eqs. 2-5 for plasma virus concentration (in  $\log_{10}$  PFU/mL) over time post infection (blue) and experimental data on virus concentration (black). Parameters used are the mean for each species from the multi-level model. Data shows the viremia of the following species from [13]: American crow, American robin, redwinged blackbird, blackbilled magpie, house finch, house sparrow, mallard and mourning dove, respectively from top left to bottom right.

**Figure 13.** Predictions from the ODE model given by Eqs. 2-5 for plasma virus concentration (in  $\log_{10}$  PFU/mL) over time post infection (blue) and experimental data on virus concentration (black). Parameters used are the mean for each species from the multi-level model. Data shows the viremia of the following species from [13]: Ring-billed gull, great-horned owl, American kestrel, Killdeer, Northern bobwhite, Northern flicker, Rockdove and American coot, respectively from top left to bottom right.

**Figure 14.** Predictions from the ODE model given by Eqs. 2-5 for plasma virus concentration (in  $\log_{10}$  PFU/mL) over time post infection (blue) and experimental data on virus concentration (black). Parameters used are the mean for each species from the multi-level model. Data shows the viremia of the following species from [13]: Monk parakeet, Canadian geese and common grackle, respectively from top left to bottom right.



**Figure 1.** Left Panel: Multi-level hierarchical model with two groups. Each group has three individuals. Also shown are the genus, species and individual levels. Right Panel: Plate diagram for the multi-level hierarchical model. The plate denotes iteration of parameters and the number enclosed in the plate shows the number of iterations.



**Figure 2.** Left Panel: Aggregated model with two groups combined. Each group has three individuals. Also shown are the genus, species and individual levels. Right Panel: Plate diagram for the aggregated model. The plate denotes iteration of parameters and the number in the plate shows the number of iterations.

