$$\frac{dy}{dx} = -1 - \frac{x^3}{(x+y+1)^2}$$
Let  $u = x+y+1$ 

$$\frac{du}{dx} = 1 + \frac{dy}{dx}$$

$$= 1 - 1 - \frac{x^3}{(x+y+1)^2}$$

$$\frac{dy}{dx} = -\frac{x^3}{(x+y+1)^2}$$

$$\frac{dy}{dx} = -\frac{x^3}{(x+y+1)^2}$$

$$\frac{dy}{dx} = -\frac{x^3}{(x+y+1)^2}$$

$$\int u^2 du = -\int x^3 dx$$

$$\frac{1}{3} u^3 = -\frac{1}{4} x^4 + C$$

$$y = 3 - \frac{3}{4} x^4 + C'$$

$$x+y+1 = 3 - \frac{3}{4} x^4 + C'$$

$$y = -x-1 + 3 - \frac{3}{4} x^4 + C'$$

Ber noulli DE with 
$$n=5$$
 ok but without this knowledge, is that  $change of variable logical??$ 

$$\frac{d^2}{dx} = \frac{dy}{dx} \left( -4y^{-5} \right)$$

$$= \left( y + xy^5 \right) \left( -4y^{-5} \right)$$

$$= -4x - 4y - 4$$

$$= -4x - 4x - 4x$$

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$$= -4x - 4x - 4x - 4x - 4x$$

$$= -4x -$$

you can also use cos.cos+sin.sin=...to just have a cos(...) here

Bernoulli DE when 
$$n=1$$
  
Let  $z=y^{-1}$   

$$\frac{dz}{dx} = \frac{dy}{dx}(-y^{-2})$$

$$= (y^2(\cos x - \sin x) - y)(-y^{-2})$$

= 
$$cosx-sinx+y^{-1}$$
  
=  $cosx-sinx+z$ 

$$\frac{dz}{dx} - z = \cos x - \sin x \quad p(x) = -1$$

integrating factor:  $M(x) = e^{\int p(x)dx} = e^{-\int dx} = e^{-x}$ 

$$e^{-x}\left(\frac{dz}{dx}-z\right)=e^{-x}\left(\cos x-\sin x\right)$$

$$\frac{d}{dx}(ze^{-x}) = e^{-x}(\cos x - \sin x)$$

$$ze^{-x} = \int e^{-x}(\cos x - \sin x) dx$$

$$\lim_{x \to \infty} |x| = -\sin(x) dx$$

u'= sinx-cosx V'=e-x

 $= -e^{-x}(\cos x - \sin x) + \int e^{-x}(\sin x - \cos x) dx$ 

= -e-x (cosx-sinx) - ze-x+C

 $2ze^{-x} = -e^{-x} \left( \cos x - \sin x \right) + C$   $z = \frac{\sin x - \cos x + Ce^{x}}{2}$ 

 $y = \frac{1}{2}$   $\Rightarrow$   $y = \frac{2}{\sin x - \cos x + Ce^x}$ 

1/[C\*exp(x)-sin (x)]

check this again

$$\frac{7.}{\sqrt{y-x}}\frac{dy}{dx} + (2x+3y) = 0$$

$$\frac{dy}{dx} = \frac{2x+3y}{x-y}$$

Multiplying & and y by a des not change the equation.

· Homogeneous

$$\frac{dy}{dx} = u + x \frac{du}{dx} = \frac{2x + 3ux}{x - ux}$$

$$u + x \frac{dy}{dx} = \frac{2+3y}{1-y}$$

$$x \frac{du}{dx} = \frac{2+3y}{1-y} - y$$

$$x \frac{du}{dx} = \frac{2+3u-u+u^2}{1-u}$$

$$\int \frac{1-u}{u^2+2u+2} du = \int \frac{1}{x} dx$$

$$\ln|x| = \int \frac{u-1}{u^2+2u+2} du$$

$$= -\frac{1}{2} \int \frac{2y-2}{y^2+2y+2} dy$$

$$= -\frac{1}{2} \left( \int \frac{2\alpha + 2}{\alpha^2 + 2\alpha + 2} d\alpha - \int \frac{4}{\alpha^2 + 2\alpha + 2} d\alpha \right)$$

$$=2\int \frac{1}{u^2+2u+2} du - \frac{1}{2} \int \frac{2u+2}{u^2+2u+2} du$$

$$|n|x|=2\int \frac{1}{1+(n+1)^{2}} du - \frac{1}{2} \int \frac{2u+2}{u^{2}+2u+2} du \quad \text{Let } v=u+1 \\ dv=du$$

$$=2\int \frac{1}{1+v^{2}} dv - \frac{1}{2} \int \frac{dw}{vv} \qquad \text{Let } w=u^{2}+2u+2 \\ =2tan^{-1} (v) - \frac{1}{2} |n|w|+c$$

$$=2tan^{-1} (u+1) - \frac{1}{2} |n|u^{2}+2u+2 + c$$

$$U = \frac{4}{x}$$

$$\therefore 2tan^{-1} (\frac{4}{x}+1) - \frac{1}{2} |n| (\frac{4^{2}}{x^{2}} + \frac{24}{x} + 2) = |n|x+c^{1}$$

ok...try regrouping the 'In' together to simplify a bit