$$\begin{array}{ll}
8. & \left(p + \frac{q}{\sqrt{2}}\right) \left(V - b\right) = RT \\
p V - p b + a V^{-1} - b V^{-2} = RT \\
no need to develop...you can straight use deterposesion) = ...dV+...dP+...dT than pick up what you need

$$\left(\frac{\partial p}{\partial V}\right)_{T} V + p - k\left(\frac{\partial p}{\partial V}\right)_{T} - a V^{-2} + 2b V^{-3} = 0$$

$$\left(\frac{\partial p}{\partial V}\right)_{T} - \frac{a V^{-2} - 2b V^{-3} - p}{V - b}$$

$$\left(\frac{\partial V}{\partial T}\right)_{p} - a \left(\frac{\partial V}{\partial T}\right)_{p} V^{-2} + 2b \left(\frac{\partial V}{\partial T}\right)_{p} V^{-3} = R$$

$$\left(\frac{\partial V}{\partial T}\right)_{p} = \frac{R}{p - a V^{-2} + 2b V^{-3}} = -\frac{R}{a V^{-2} - 2b V^{-3} - p}$$

$$V - b = R\left(\frac{\partial T}{\partial p}\right)_{V} \Rightarrow \left(\frac{\partial T}{\partial p}\right)_{V} = \frac{V - b}{R}$$

$$\left(\frac{\partial P}{\partial V}\right)_{T} \left(\frac{\partial V}{\partial T}\right)_{p} \left(\frac{\partial T}{\partial p}\right)_{V} = \left(\frac{a V^{-2} - b V^{-3} - p}{A V^{-2} - b V^{-3} - p}\right)_{V} \left(\frac{\partial V}{\partial V}\right)_{T} \left(\frac{\partial V}{\partial T}\right)_{p} \left(\frac{\partial T}{\partial p}\right)_{V} = \left(\frac{a V^{-2} - b V^{-3} - p}{A V^{-2} - b V^{-3} - p}\right)_{V} \left(\frac{\partial V}{\partial V}\right)_{T} \left(\frac{\partial V}{\partial T}\right)_{p} \left(\frac{\partial T}{\partial p}\right)_{V} = \left(\frac{a V^{-2} - b V^{-3} - p}{A V^{-2} - b V^{-3} - p}\right)_{V} \left(\frac{\partial V}{\partial V}\right)_{T} \left(\frac{\partial V}{\partial T}\right)_{p} \left(\frac{\partial T}{\partial p}\right)_{V} = \left(\frac{a V^{-2} - b V^{-3} - p}{A V^{-2} - b V^{-3} - p}\right)_{V} \left(\frac{\partial V}{\partial V}\right)_{T} \left(\frac{\partial V}{\partial T}\right)_{p} \left(\frac{\partial T}{\partial p}\right)_{V} = \left(\frac{a V^{-2} - b V^{-3} - p}{A V^{-2} - b V^{-3} - p}\right)_{V} \left(\frac{\partial V}{\partial V}\right)_{T} \left(\frac{\partial V}{\partial T}\right)_{p} \left(\frac{\partial V}$$$$

$$\begin{pmatrix}
\cos \theta & -\sin \theta \\
\sin \theta & \cos \theta
\end{pmatrix}
\begin{pmatrix}
\chi \\
y
\end{pmatrix} = \begin{pmatrix}
u \\
V
\end{pmatrix}$$

ok but how to get this if you do not know matrices?

$$\begin{pmatrix} \chi \\ y \end{pmatrix} = \begin{pmatrix} \cos\theta & -\sin\theta \\ \sin\theta & \cos\theta \end{pmatrix} \begin{pmatrix} y \\ y \end{pmatrix}$$

Let
$$A = \begin{pmatrix} \cos\theta & -\sin\theta \\ \sin\theta & \cos\theta \end{pmatrix}$$

$$A^{-1} = \frac{adj(A)}{det(A)} = \begin{pmatrix} \cos\theta & \sin\theta \\ -\sin\theta & \cos\theta \end{pmatrix}$$

$$-: \begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} y \\ y \end{pmatrix}$$

$$\chi(u,v) = u\cos\theta + v\sin\theta$$

 $\gamma(u,v) = -u\sin\theta + v\cos\theta$

$$\frac{\partial x}{\partial u} = \cos\theta \qquad \frac{\partial x}{\partial v} = \sin\theta$$

$$\frac{\partial y}{\partial u} = -\sin\theta$$
 $\frac{\partial y}{\partial v} = \cos\theta$

$$\frac{\partial f}{\partial u} = \frac{\partial f}{\partial x} \frac{\partial x}{\partial u} + \frac{\partial f}{\partial y} \frac{\partial y}{\partial u}$$

$$= \frac{\partial f}{\partial x} \cos \theta - \frac{\partial f}{\partial y} \sin \theta$$

$$= \frac{\partial f}{\partial x} \cos \theta - \frac{\partial f}{\partial y} \sin \theta$$

$$= \cos \theta \frac{\partial^2 f}{\partial x^2} \frac{\partial x}{\partial u} - \sin \theta \frac{\partial^2 f}{\partial y^2} \frac{\partial y}{\partial u}$$

$$= \cos \theta \frac{\partial^2 f}{\partial x^2} + \sin^2 \theta \frac{\partial^2 f}{\partial y^2}$$

$$= \frac{\partial f}{\partial x} \sin \theta + \frac{\partial f}{\partial y} \cos \theta$$

$$= \frac{\partial f}{\partial x} \sin \theta + \frac{\partial f}{\partial y} \cos \theta$$

$$= \sin^2 \theta \frac{\partial^2 f}{\partial x^2} + \cos^2 \theta \frac{\partial^2 f}{\partial y^2} + \sin^2 \theta \frac{\partial^2 f}{\partial y^2} + \sin^2 \theta \frac{\partial^2 f}{\partial x^2} + \cos \theta \frac{\partial^2 f}{\partial x^2} + \cos^2 \theta \frac{\partial^2 f}{\partial x^2} + \cos^2 \theta \frac{\partial^2 f}{\partial x^2} + \sin^2 \theta \frac{\partial^2 f}{\partial x^2} + \sin^2 \theta \frac{\partial^2 f}{\partial x^2} + \cos^2 \theta \frac{\partial^2 f}{\partial x^2} + \cos^2 \theta \frac{\partial^2 f}{\partial x^2} + \cos^2 \theta \frac{\partial^2 f}{\partial x^2} + \sin^2 \theta \frac{\partial^2 f}{\partial x^2} + \cos^2 \theta \frac{\partial^2 f}{\partial x^2} + \cos^2$$