

Class 3 - Particular Integral of Standard Functions- Type-1

Solve the following Linear Differential Equations :

$$1. (D^2 - 5D + 6) y = e^{4x}$$

$$\text{Answer : } y = ae^{2x} + be^{3x} + \frac{e^{4x}}{2}$$

$$2. (D^2 + 4D + 5) y = -2 \cosh x. \text{ Also find } y \text{ when } y = 0, \frac{dy}{dx} = 1 \text{ at } x = 0.$$

$$\text{Answer : } y = \frac{3}{5} e^{-2x} (\cos x + 3 \sin x) - \frac{e^x}{10} - \frac{e^{-x}}{2}$$

$$3. (D^3 + 2D^2 + D) y = e^{-x}$$

$$\text{Answer : } y = c_1 + (c_2 + c_3 x) e^{-x} - \frac{x^2 e^{-x}}{2}$$

$$4. (D^2 + 4D + 13) y = 2 e^{-x} \text{ given } y(0) = 0 \text{ and } y'(0) = -1.$$

$$\text{Answer : } y = \frac{-1}{5} e^{-2x} (\cos 3x + 2 \sin 3x) + \frac{e^{-x}}{5}$$

$$5. (D^2 - 7D + 10) y = (1 + e^x)^2$$

$$\text{Answer : } y = ae^{2x} + be^{-5x} + \frac{1}{10} + \frac{1}{2}e^x - \frac{x}{3}e^{2x}$$
