

CL14\_Q1. Using the Schrödinger's wave equation find the wave function associated with particle having energy 10 eV travelling along positive x-direction approach a potential step of height 7 eV.

CL14\_Q2. Define the terms reflection coefficient and transmission coefficient with respect to step potential.

CL14\_Q3 A stream of particles of mass  $m$  and total energy  $E$  moves towards a potential step of height  $V_0$ , if the energy of the electrons is lesser than the step potential ( $E > V_0$ ) then by applying continuity conditions obtain the expression for reflection coefficient.

CL14\_Q4. The probability of reflection from a potential step is given by  $\frac{(k_2-k_1)^2}{(k_2+k_1)^2}$ , where the  $k$ 's are the wavenumbers in the two regions. If a 5 eV electron encounters a 2 eV potential step, what is the probability that it will be reflected?

CL15\_Q1. A particle of mass  $m$  and total energy  $E$  moves from a region of constant potential  $V_1$  to a region of potential  $V_2$ . If  $E < V_2$  find the associated wave function and reflection coefficient for the particle experience a step potential.

CL15\_Q2. Explain the term penetration depth for a step potential.

CL15\_Q3. A proton of energy 3 eV approaches a potential step of height 4 eV. Evaluate the possible depth of penetration into the classically forbidden region.

CL15\_Q5. A spherical dust particle of radius  $10^{-5}m$  and density  $10^4 \text{ Kg/m}^3$ , moving at a speed of  $10^{-2} \text{ m/s}$  encounters a step potential of height equal to twice the K.E of the particle. Estimate the penetration depth of the particle inside the step.

**CL18\_Q1.** Obtain the energy Eigen values for a particle bound in an infinite potential well. Comment on why the particle cannot have zero energy?

**CL18\_Q2.** Show that the probability of locating the particle between the limits 0 to  $0.5L$  is the same in any quantum state. Here  $L$  is the width of the well.

**CL18\_Q3.** Plot the first two states Eigen functions for a particle in an infinite potential well.

**CL18\_Q4.** Plot the probability densities for the first three excited quantum states of an electron trapped in an infinite potential well of width  $L$ . Calculate the probability of locating the electron in the third excited state between the limits  $\frac{3}{8}L$  and  $\frac{5}{8}L$  where  $L$  is the width of the well?

**CL18\_Q5.** Show that the energy of an electron confined in a 1-D symmetric potential well of length ' $L$ ' and infinite depth is quantized. Is the electron trapped in a potential well allowed to take zero energy? If not, why?

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CL18\_Q1. Derive the expression of energy Eigen values for a particle in an infinite potential well using the admissible solutions.

CL18\_Q2. The wave function associated with a particle in a infinite potential box is  $\psi = \left(\frac{2}{L}\right)^{1/2} \sin\left(\frac{\pi x}{L}\right)$  for  $0 \leq x \leq L$ . What is the probability of finding the particle in the region (i)  $0 \leq x \leq L/2$  and (ii)  $0 \leq x \leq 3L/4$  ?

CL18\_Q3. Plot the probability densities for the first three excited quantum states of an electron trapped in an infinite potential well of width L.

CL18\_Q4. A particle is free to move in a one dimensional region of zero potential between the two rigid walls at  $x = -a$  and  $x = a$ . If  $E_n$  is the energy of the nth state and  $\Delta E_n$  is the energy separation between the  $(n + 1)^{th}$  and  $n^{th}$  state, then show that  $\frac{\Delta E_n}{E_n} = \frac{(2n+1)}{n^2}$

CL18\_Q5. The lowest energy level of a particle confined to a one-dimensional region of space with fixed dimension  $L$  is  $E_0$  (i.e., a "particle in a box"). If an identical particle is confined to a similar region with fixed distance  $\frac{1}{9}L$ , what is the energy of the lowest energy level that the particles have in common? Express your answer in terms of  $E_0$ .

**CL21\_Q1.** Compare the energy levels of the first three quantum states of identically sized finite and infinite potential wells.

**CL21\_Q2.** Why do finite square wells have only a finite number of bound energy values? What are the characteristics of bound energy values?

**CL21\_Q3.** A particle trapped in a finite potential well. Sketch the Eigen functions for first three energy states.

**CL21\_Q4.** Plot the first two states Eigen wave functions and the probability function for a particle in a finite potential well.

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CL21\_Q1. How are the energy values of a quantum mechanical oscillator fundamentally different from the energy values of a classical oscillator?

CL21\_Q2. The energy of a linear harmonic oscillator in the third excited state is 0.1 eV. Find the frequency of the oscillator.

CL21\_Q3. Sketch the wave functions and probability densities for the first two quantum states of quantum harmonic oscillators.

CL21\_Q4. A lithium atom, mass  $1.17 \times 10^{-26}$  kg, is vibrating with simple harmonic motion in a crystal lattice, where the force constant  $k$  is 64.0 N/m. (a) what is the ground state energy of this system in eV? (b) What would be the wavelength of the photon that could excite this system to the  $n = 1$  level?

CL21\_Q4. Establish Schrodinger's equation of a linear harmonic oscillator and write its solution.

CL22\_Q1. Write down the Schrodinger wave equation for the hydrogen atom in spherical polar co-ordinates and explain the significance of different quantum numbers

CL22\_Q2. Explain the stationary states of the hydrogen atom.

CL22\_Q3. Electrons in hydrogen are described by four numbers,  $n$ ,  $l$ ,  $m$  and  $ms$ . What restrictions (if any) are there on these four numbers?

CL22\_Q4. In the analysis of Schrodinger's equation for a hydrogen atom using spherical polar coordinates, elaborate the azimuthal and polar wave function. Also comment on the possible values of magnetic quantum number.

CL22\_Q2. Plot the ground-state eigen function of the hydrogen atom as a function of the distance  $r$ .

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CL19\_Q1. What is meant by degeneracy of energy states in quantum systems?

CL19\_Q2. Give examples for degenerate states for a particle in three dimensional box with infinite potential at the boundaries.

CL19\_Q3. Calculate the Eigen value of the electron in the lowest energy level, confined in a 2D potential box of side 0.1 nm.

CL19\_Q4. Using the appropriate boundary conditions obtain the energy eigen values and the corresponding eigenfunctions for a particle trapped in a three dimensional infinite potential box.

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CL25\_Q1. Discuss the variation of Fermi factor on temperature and consequent effect on probability of occupation of energy levels.

CL25\_Q2. Use the Fermi distribution function to obtain the value of  $F_d$  for  $E-E_F = 0.01 \text{ eV}$  at 200 K.

CL25\_Q3. Show that the probability of occupancy of an energy level  $\Delta E$  below the Fermi level is the same as that of the probability of non-occupancy of an energy level  $\Delta E$  above the Fermi level.

CL25\_Q4. At what temperature would the probability of occupancy of an energy state 0.01eV below the Fermi level be 0.95?

CL25\_Q5. Estimate the temperature at which there is 2% probability that a state with energy 0.4 eV above the Fermi energy level is occupied.

CL25\_Q6. Show that the density of states for conduction electron per unit volume of the metal is  $g(E)dE = \frac{\pi}{2} \left(\frac{8m}{h^2}\right)^{\frac{3}{2}} E^{\frac{1}{2}} dE$

CL25\_Q7. Calculate the number of states lying in an energy interval of 0.01 eV above the Fermi-level for a crystal of unit volume with energy  $E_F = 3.0 \text{ eV}$

CL24\_Q1. Give the basic ideas of quantum free electron theory of metals.

CL24\_Q2. Explain the (energy) distribution of free electrons at 0K based on the quantum free electron theory.

CL24\_Q3. Discuss the free electron theory of electronic conduction in metals. Comment on the effect of temperature and impurities on conductivity.

CL24\_Q4. State Mattheissen's rule and give an account of the nature of total resistivity both at high and low temperature.

CL24\_Q5. Describe how quantum free electron theory has been successful in overcoming the failures of classical free- electron theory.

CL24\_Q6. Elucidate the difference between classical free electro theory and quantum free electron theory.

CL27\_Q1. Explain the concept of Fermi energy.

CL27\_Q2. Obtain an expression for Fermi energy using the concept of density of states.

CL27\_Q3. Determine the Fermi temperature and Fermi velocity in a metal with  $18 \times 10^{28}$  free electrons per unit volume.

CL27\_Q4. Calculate the Fermi energy in eV for a metal at 0K, whose density is  $10500 \text{ kg/m}^3$ , atomic weight is 107.9, and it has one conduction electron per atom.

CL27\_Q5. Using the expression of density of states, show that average energy of electrons in a metal at 0K is  $\frac{3}{5} E_F$

CL27\_Q6. A current of 5A can easily be carried in a copper wire of length 3m and resistance 20 mΩ at room temperature. Given: Density of copper =  $8.95 \times 10^3 \text{ kg/m}^3$ , mobility of charge carriers =  $4.3 \times 10^{-3} \text{ m}^2/\text{Vs}$  and Fermi energy = 7eV. Estimate and compare the values of

- a. Drift velocity
- b. Thermal velocity
- c. Fermi velocity