

Class - 7

Taylor's and Maclaurin's expansion for a function of two variables

1. Find the Taylor's expansion of  $e^{xy}$  in terms of  $(x-1)$  and  $(y-1)$ .

Ans:  $e \left[ 1 + (x-1) + (y-1) + \frac{(x-1)^2}{2!} + (x-1)(y-1) + \frac{(y-1)^2}{2!} + \dots \right]$

2. Expand  $e^x \ln(1+y)$  about origin up to 3<sup>rd</sup> degree terms.

Ans:  $y + xy - \frac{y^2}{2} + \frac{(x^2y - xy^2)}{2} + \frac{y^3}{3} + \dots$

3. Find Taylor's expansion of  $\sqrt{1+x+y^2}$  in powers of  $(x-1)$  and  $(y-0)$ .

Ans:  $\sqrt{2} \left[ 1 + \frac{x-1}{4} - \frac{(x-1)^2}{32} + \frac{y^2}{4} + \dots \right]$