

6.

1. The random variable X has a Poisson distribution. If $P(X = 1) = 0.01487$, $P(X = 2) = 0.04461$, then find $P(X = 3)$.

$$A. \quad P(X=1) = \frac{e^{-\lambda} \lambda}{1!} = 0.01487$$

$$P(X=2) = \frac{e^{-\lambda} \lambda^2}{2!} = 0.04461$$

$$\frac{P(X=2)}{P(X=1)} = \frac{\lambda^2}{2! \lambda} = \frac{\lambda}{2}$$

$$\frac{\lambda}{2} = \frac{0.04461}{0.01487} \Rightarrow \lambda = 6$$

$$P(X=3) = \frac{e^{-\lambda} \cdot \lambda^3}{3!} = \frac{e^{-6} \cdot (6)^3}{3!} = 0.0892$$

2. Wireless sets are manufactured with 25 soldered joints each. On the average, 1 joint in 500 is defective. How many sets can be expected to be free from defective joints in a consignment of 10000 sets?

A.

$$p = \frac{1}{500} \quad n = 10000 \quad \lambda = np = 20$$

$$P(X=25) = \frac{e^{-\lambda} \cdot \lambda^x}{x!} = \frac{e^{-20} \cdot (20)^{25}}{25!} = 0.04458$$

$$\text{In } 10000, \quad \text{No. of defective joints} = 10000 \times 0.04458 \\ = 445.8 \approx 446$$

$$\text{No. of sets free from defective joints in } 10000 = 10000 - 446 \\ = 9554$$

3. Suppose the number of telephone calls on an operator received from 9.00 to 9.25 follow a Poisson distribution with mean 3. Find the probability that

- The operator will receive no calls in that time interval tomorrow.
- In the next three days, the operator will receive a total of 1 call in that time interval.

$$A. \quad \lambda = 3$$

$$i) \quad x = 0$$

$$P(X=0) = \frac{e^{-\lambda} \cdot \lambda^x}{x!} = \frac{e^{-3} \cdot 3^0}{0!} = 0.0497$$

$$ii) \quad P(X=1) \quad \text{where} \quad \lambda = 3 \times 3$$

$$P(X=1) = \frac{e^{-9} \times 9^1}{1!} = 0.0011$$