

Class 9: Problems on generating functions and Jacobi Series:

1. Prove the following recurrence relation using generating functions:

$$xJ_{n-1}(x) = nJ_n(x) + xJ'_n(x)$$

2. Using Jacobi Series prove the following results.

$$(i) \quad x \cos(x) = 2(J_1 - 3^2 J_3 + 5^2 J_5 - \dots)$$

$$(ii) \quad x \sin(x) = 2(2^2 J_2 - 4^2 J_4 + 6^2 J_6 - \dots)$$
