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**Unit-3 Digital Electronics** 

**Basic Theorem and Properties of Boolean Algebra** 

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## **Basic Theorem and Properties of Boolean Algebra**



- ❖ Boolean Laws and Theorems are used to simplify the Boolean expressions. Hence reduce the number of logic gates.
- ★ Commutative Laws:

  (i) A+ B = B+ A
  (ii) A.B = B.A

$$A \longrightarrow A \text{ OR B} \equiv A \longrightarrow B \text{ OR A} \longrightarrow B \text{ OR A} \longrightarrow B \text{ AND B} \equiv A \longrightarrow B \text{ AND B} \longrightarrow B \text{ AND A}$$

A	В	(A+B)	(B+A)	(A.B)	(B.A)
0	0	0	0	0	0
0	1	1	1	0	0
1	0	1	1	0	0
1	1	1	1	1	1

**Proof: Truth Table** 

## **Basic Theorems and Properties of Boolean Algebra**



$$(A+B)+C=A+(B+C)$$

**Boolean addition** 

Proof

A	В	C	A + B	(A+B)+C	B + C	A + (B + C)
0	0	0	0	0	0	0
0	0	1	0	1	1	1
. 0	1	0	1	1	1	1
0	1	1	1	1	1	1
1	0	0	1	1	0	1
1	0	1	1	1	1	1
1	1	0	1	1	1	1
1	1	1	1	1	1	1

From principle of duality: (A.B).C = A.(B.C) Boolean Multiplication



## **Basic Theorem and Properties of Boolean Algebra**



## **❖** Distributive Law:

$$A + B.C = (A+B) . (A+C)$$

Proof: Truth Table

Α	В	С	BC	A+BC	(A+B)	(A+C)	(A+B)(A+C)
0	0	0	0	0	0	0	0
0	0	1	0	0	0	1	0
0	1	0	0	0	1	0	0
0	1	1	1	1	1	1	1
1	0	0	0	1	1	1	1
1	0	1	0	1	1	1	1
1	1	0	0	1	1	1	1
1	1	1	1	1	1	1	1

#### **Dual of distributive law:**

$$A. (B+C) = A.B + A.C$$

Proof: Truth Table

A	В	C	B+C	A(B+C)	AB	AC	AB+AC
0	0	0	0	0	0	0	0
0	0	1	1	0	0	0	0
0	1	0	1	0	0	0	0
0	1	1	1	0	0	0	0
1	0	0	0	0	0	0	0
1	0	1	1	1	0	1	1
1	1	0	1	1	1	0	1
1	1	1	1	1	1	1	1

#### **Basic Theorem and Properties of Boolean Algebra**



## De Morgan's Theorem :

(i) The complement of the sum of 2 variables is equal to the product of the complements of individual variables:  $\overline{A+B} = \overline{A} \cdot \overline{B}$ 

(ii) The complement of the product of 2 variables is equal to the sum of the complements of individual variables:  $\overline{A.B} = \overline{A} + \overline{B}$ 

Α	В	$\overline{A}$	$\overline{B}$	A+B	A.B	A+B	$\overline{A}$ . $\overline{B}$	<u>A</u> . <u>B</u>	$\overline{A} + \overline{B}$
0	0	1	1	0	0	1	1	1	1
0	1	1	0	1	0	0	0	1	1
1	0	0	1	1	0	0	0	1	1
1	1	0	0	1	1	0	0	0	0

## **Basic Theorem and Properties of Boolean Algebra**



# **Absorption Theorem:**

(i) 
$$A+AB=A$$

LHS: = A + AB  
= A.1 + AB 
$$\rightarrow$$
 since A.1 = A  
= A(1+B)  $\rightarrow$  since 1 + B = 1  
= A.1  
= A = RHS

(ii) 
$$A(A+B) = A$$

LHS = A (A + B)  
= A.A + A.B  
= A+AB 
$$\rightarrow$$
 since A . A = A  
= A (1 + B)  
= A.1  
= A = RHS

(iii) 
$$A+\bar{A}B = A+B$$

LHS = A + 
$$\bar{A}B$$
  
= (A +  $\bar{A}$ ) (A + B)  $\rightarrow$  since A+BC = (A+B)(A+C)  
= (1) . (A + B)  $\rightarrow$  since A +  $\bar{A}$  = 1  
= A + B = RHS

(iv) 
$$A.(\bar{A}+B) = AB$$

LHS = A.
$$(\bar{A} + B)$$
  
= A. $\bar{A} + A.B \rightarrow (A \bar{A} = 0)$   
= AB = RHS

Redundancy Laws

## **Basic Theorem and Properties of Boolean Algebra**



## Consensus Theorem:

$$AB + \bar{A}C + BC = AB + \bar{A}C$$

 $= AB + \bar{A}C = RHS$ 

LHS = AB+
$$\bar{A}$$
C+BC  
= AB +  $\bar{A}$ C + BC.1  
= AB +  $\bar{A}$ C + BC (A +  $\bar{A}$ )  $\rightarrow$  since A +  $\bar{A}$  = 1  
= AB +  $\bar{A}$ C + ABC +  $\bar{A}$ BC  
= AB (1 + C) +  $\bar{A}$ C (1 + B)  
1 + B = 1 + C = 1

## **Dual of consensus theorem:**

$$(A+B)(\bar{A}+C)(B+C) = (A+B)(\bar{A}+C)$$

**BC** is redundant term



# **THANK YOU**

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