



## Class 10: Bessel's Integral formula and Orthogonality of Bessel functions

- **1.** If  $\alpha$  and  $\beta$  are distinct roots of the equation  $AJ_n(x) + BxJ_n'(x) = 0$  where  $\alpha$  and  $\beta$ are constants, show that  $\int\limits_0^1 x J_n(\alpha) J_n(\beta x) dx = 0$
- **2.** Prove that  $y = J_n(3x)$  is a solution of the equation  $x^2y'' + xy' + (9x^2 n^2)y = 0$

