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Given,

	Bad	Good
Battery	0.1	0.9

	Empty	Not empty
Fuel	0.2	0.8

Battery	Fuel	Gauge	
		Empty	Not empty
Bad	Empty	0.9	0.1
Bad	Not empty	0.2	0.8
Good	Empty	0.8	0.2
Good	Not empty	0.1	0.9

Battery	Fuel	Start	
		No	Yes
Bad	Empty	1	0
Bad	Not empty	0.9	0.1
Good	Empty	0.8	0.2
Good	Not empty	0.1	0.9

- (a) $P(B = \text{bad}, F = \text{empty}, G = \text{empty}, S = \text{no}) = 0.1 \times 0.2 \times 0.9 \times 1 = \mathbf{0.018}$
- (b) $P(S = \text{No} \mid F = \text{Not Empty}) = P(S = \text{No}, F = \text{Not Empty}) / P(F = \text{Not Empty})$
 $= (P(F = \text{Not empty}, B = \text{Bad}, S = \text{No}) + P(F = \text{Not empty}, B = \text{Good}, S = \text{No})) / P(F = \text{Not Empty})$
 $= ((0.8 \times 0.1 \times 0.9) + (0.8 \times 0.9 \times 0.1)) / 0.8$
 $= (0.072 + 0.072) / 0.8$
 $= 0.144 / 0.8$
 $= \mathbf{0.18}$
- (c) $P(G = \text{Empty} \mid \text{Battery} = \text{Bad}, \text{Start} = \text{No}) = P(B = \text{Bad}, S = \text{No}, G = \text{Empty}) / P(B = \text{Bad}, S = \text{No})$
 $= (P(B = \text{Bad}, F = \text{Empty}, S = \text{No}, G = \text{Empty}) + P(B = \text{Bad}, F = \text{Not Empty}, S = \text{No}, G = \text{Empty})) / (P(B = \text{Bad}, F = \text{Empty}, S = \text{No}) + P(B = \text{Bad}, F = \text{Not Empty}, S = \text{No}))$
 $= ((0.1 \times 0.2 \times 1 \times 0.9) + (0.1 \times 0.8 \times 0.9 \times 0.2)) / ((0.1 \times 0.2 \times 1) + (0.1 \times 0.8 \times 0.9))$
 $= (0.018 + 0.0144) / (0.02 + 0.072)$
 $= 0.0324 / 0.092$
 $= \mathbf{0.3522}$