The Stater: Ittigh, low for Actions: I beareh, waith Recharge for p(s'= high | s= high, a = beareh): \alpha

p(s'= low | s= high, a= beareh): I-d

p(s'= low | s= high, a= beareh): I-d

p(s'= high | s= low, a= beareh): I-B.

The table can be filled as.

5	a_	s	Υ	p(s',rls,a)
high	Search	high	Meareh	d
Ligh	seaseh	low	rsearch	l-d
low	bearch	high	- 3	1-p.
Low	Search	low	Vsearch	B
high	wait	high	rwait	1
high	wait	low	-	0
Low	wait	high	_	O
low	wait	Low	Tues	st 1
low	recharg	je Rie	jn o	1
low	recharg	e l	ew -	- 0

(3)

Egn (3.8)

Where r is a farameter, 0 \le r \le 1 called the discount rate.

,
$$\mathbb{E}\left[\frac{C}{1-r}\right]$$

E[constant]
. constant

Ct+K+1 2 C

... V° does not affect the relative values of any states.

Exercise 3.16.

Epirodie task: Gt. & NK-1-1 RK.

The reneards, we will sum over all the reneards to find the best action to be ficked.

When adding a constant,

The remark obtained on the expandic task is very important. Adding a constant can affect the remark obtained in a state, and affect the action to be ficked in the state.

eg: 7 Ro-5 & C=2.

The remard at a state s: -5+2

the severed value Excreased, and chances of ficking a non-bust own is high.

$$= \mathbb{E}\left[\frac{1}{K_{*}t+1} \frac{\gamma K_{-}t-1}{(R_{K+c})} \right]$$

. The action value function will also charge.

(5) Optimal state value function V+

A policy To is eligined to be better than or equal to a poliny Tif it expected return is greater than or equal to that of T for all state. To 7, T' if and only if VT(8) = VT(9). The optional proling is that proling which is better than or equal to all other policies. denoted by 17.4. They share a some state value function denoted by v*.

V*(s) 2 max VICs) +SES.

Optimal action value function 9, * gires the expected return for taking action a in states and there after following an optimal jobling.

q x (s,a) = max q (s,a) (1+4) 2 max 97x (s,a) a EALS)

It is taking the best action by taking best policy TX is to amount and giving the bost expected return.

(8) Yer, we ear express R+12 is terms of StR At. That means Rt72 is dependent on St & At. This happens when the frences state of St+2 ie St+1 doesit produce any revealed or didn't take any action.

This happen when the previous state of Rt +2 ie St+1 doer not kappen.

(10) The State value functions
$$V_{TT}(s) = \mathbb{E} \Big[G_{1}t \, \big| \, St-S \Big]$$

As use know, Gtz Rt+1 + r Gt+1.

Reward to go function.

If r21, the agent is far-signted of the future.

$$= \sum_{s} E[R+1|s_{1-s}] + \sum_{n} [C_{n+1}|s_{1+1}]$$

$$= \sum_{s} \sum_{r} r + \sum_{n} [C_{n+1}|s_{1+1},s_{1}]$$

Summing over all actom, to get the state value femetion.

=
$$= = = \pi(a|s) = p(s|s|s,a) [r+rv\pi(s)] + s \in s$$
.

This is the sam of all values of three variables a, s', v.

For each value of a, s', &v, we compute the probability
in The The Transfer of the probability

ie The Transfer of a, s', &v, we compute the probability

eurorest revealed a revealed to go term.

Then we sum over all possibilities to get an expected value.

(II) An agent receives a sequence of rewards $R_{1}=2, R_{2}=1, R_{3}=10 & R_{4}=-3.$

n. 0.5

The infinite horizon discounted return is

Al- Gt= Rt+1 + MRt+2+M2R1+3+...
Cot= Rt+1 + MB1+1

The or dis counted reveald/ tetam for each time step.

(12) We know the optimal State value function

Y*(s) 2 \[\begin{array}{c} & \begin{array

By Bellman's optomality from eight, V +(s) = max q +(s,a)

As we have giren x*(s),

V*(s) = max q*(s,a) = max [R++1+MV*(s++1) | Stal, At=a]

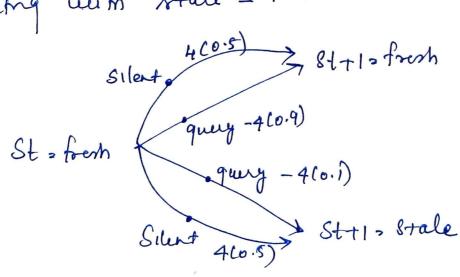
· · · * (s) = argmax E[R+++ + Y x (s++1) | s+-1, A+-a]

 $\pi \times (s) = \underset{a \in A(s)}{\operatorname{argmax}} \underbrace{\mathbb{E}}_{s', r} p(s', r|s, a) \left[r + v \times (s')\right]$

(3)

(i) MDP.

dis Starting with state = frosh.



Styl = fresh = -1.6.

St+12 Male 2 1.6.

Silent 410.5)

St+2. Fresh = -1.6

St+1. Fresh. query -410.9)

query -410.1)

Silent 410.7)

St+2. Stale. = 1.6.

guery -8(0.t) St+2 = from = -6.6

Step = 0.

Step = 0.

Step = 4

Step = 4

Guery = -8(0.2)

query 40.9) frenh = S++3 = -1.6 S++2 = bresh (31lent 40.5) query -40.1) Stent 40.0)

query -2(0.8) St+3: fresh = -6.9 Step = 0 Silent = 0 SHent = 4 query -2(0.8)

Bt= Rt+1+ MGttl St St+1 St+2 St+3 Frem(P) Frenh(F) Fran(F) Frenh (P) -1.6 +/2 (-1.6-1.6)+10 -1.6+ & (-1.6+1.6) F F F Stale (S) 2 8.4 -1.6+/2 (+1.6+2.4) = 10.4 -1.6+% (1.6 + 6.4) F FF 1.6+6 (-6.4-1.6)+10 F > 7-6 1.6+ /2 (2.4 + 6.4) +10 > 9.6 F S S F 1.6+ /2 (-6.4 + 1.6)+a = 9.2 F s s 1.6+/2 (2.4+2.4)-10

The optimal boling is that griesing maximum ruard

St = Fronh Str = Stale

St + 1 = Broth Str = Stale.

(4) Policy improvement step: is Either improves polity or leaves it uncharged. (11) If it leaves uncharged, the policy is optimal The operator Tmfcs) = #[R++1+rf(s++1)|st] THUTKLE) = VTKLE) SES. . T [VTK] ? Tret, VTK. ie Vnices) > Vnices) Pro of :-Tricti Varies) = Tuness > Tak Varies) = Varies? Trees VARCES) > VARCES) ·· Tricti (Tricti (Vincon)) > Vincon) TRK+1 VAK W) ZVARW) — (1) Applying limit MIN TAKTI VAK (S) = VAK+1(S) -3 From 1, @ can be writen as

N-100 TRKET YTES) > VTKG)

· Ynk+16) > Vnicks)

+ s∈S

7 VARC+160) = VARC 6).

... Tok+1 has a unique fixed foist Kork+1

... Tok+1 has a unique fixed foist Kork+1

York = Vork+1 YSES.

1) Heration \Rightarrow Remard $\rightarrow R_1$ $(-1 \times 0.5 + 1 \times 0.7) + 1(4 \times 0.5)$

= 2

(4 x 0.5+ 2x0.5) +1(2x0.5) = 4

So as we are intrearing the Pterations, or incurring the value of m, the Sterations increase proportional. It we are emidering in mem, there will be in iterations.

The optimal policy is quin by.

Step 2 -> step 1 -> Copround.