Data Mining (Δ 02): Exercise Set 2: 2.2 - 5Gaussians Dataset

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```
In [1]: #general
    import pandas as pd
    import numpy as np
    import matplotlib.pyplot as plt

#data preprocessing

#classifiers
    from sklearn.cluster import KMeans
    from sklearn.cluster import AgglomerativeClustering
    from sklearn.cluster import SpectralClustering

#to ignore warnings
    import warnings
    warnings.filterwarnings('ignore')
```

Load Data

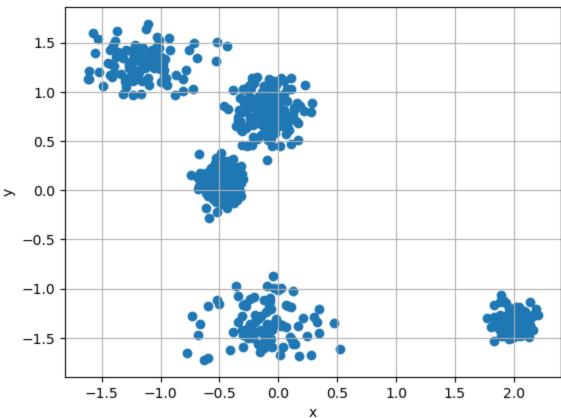
```
In [2]: data = []
# read the file line by line
with open(r'C:\Users\Nefeli\Desktop\dm_msc\DM_Homework2_2024\clustering\5Gaussians.txt',
    for line in file:
        # Strip whitespace, split (by space)
        clean_line = line.strip().split()
        data.append((float(clean_line[0]), float(clean_line[1])))

# Create DataFrame from the list
main_df = pd.DataFrame(data, columns=['x', 'y'])
#rings3
```

Plot data

```
In [3]: plt.scatter(main_df['x'], main_df['y'])
    plt.xlabel('x')
    plt.ylabel('y')
    plt.title('5Gaussians Dataset')
    plt.grid(True)
    plt.show()
```

5Gaussians Dataset



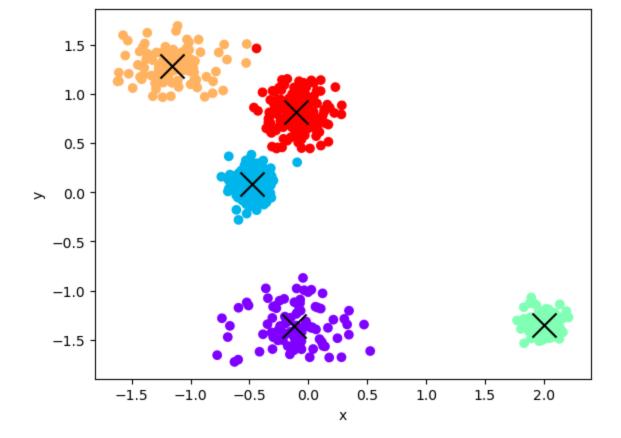
Expected number of clusters: 5

k-means

```
In [4]: #init and fit
   kmeans = KMeans(n_clusters=5)
   kmeans.fit(main_df)

# get centroids and labels
   centroids = kmeans.cluster_centers_
   labels = kmeans.labels_

plt.scatter(main_df['x'], main_df['y'], c=labels, cmap='rainbow')
   plt.scatter(centroids[:, 0], centroids[:, 1], s=300, c='black', marker='x')
   plt.xlabel('x')
   plt.ylabel('y')
   plt.show()
```

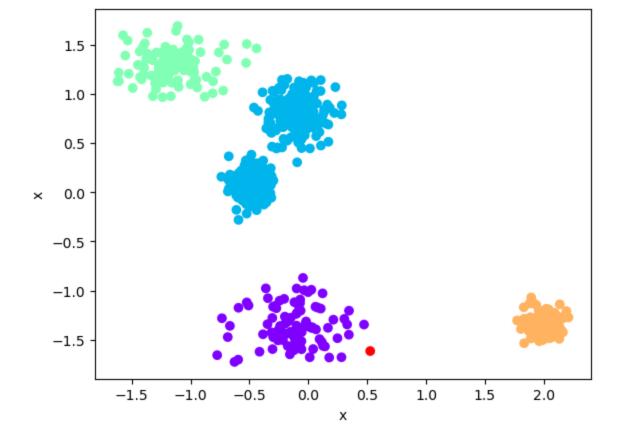


Agglomerative Clustering : single link

```
In [5]: #init and fit
    agg_cluster = AgglomerativeClustering(n_clusters=5, linkage='single')

#get labels
    labels = agg_cluster.fit_predict(main_df)

plt.scatter(main_df['x'], main_df['y'], c=labels, cmap='rainbow')
    plt.xlabel('x')
    plt.ylabel('x')
    plt.show()
```

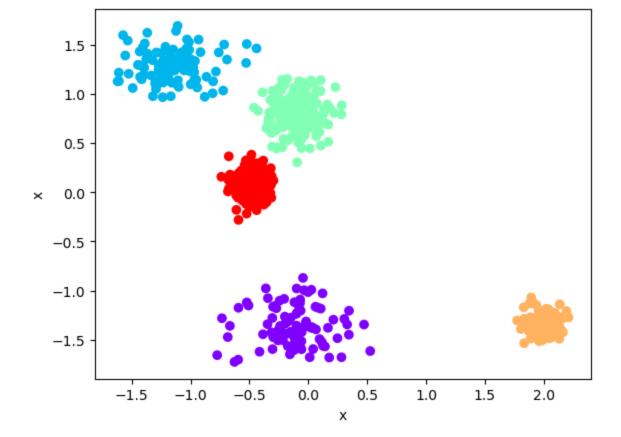


Agglomerative Clustering : average link

```
In [6]: #init and fit
    agg_cluster = AgglomerativeClustering(n_clusters=5, linkage='average')

#get labels
    labels = agg_cluster.fit_predict(main_df)

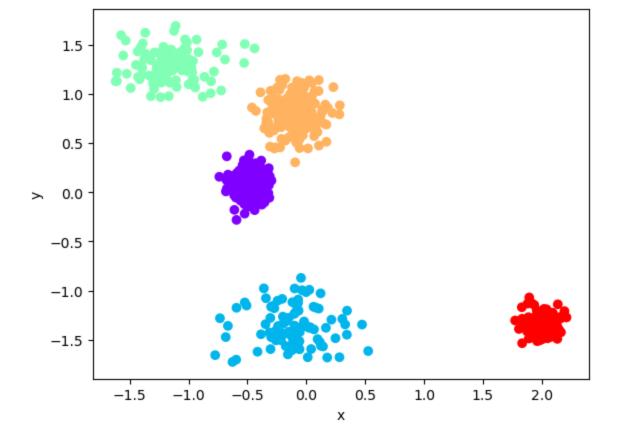
plt.scatter(main_df['x'], main_df['y'], c=labels, cmap='rainbow')
    plt.xlabel('x')
    plt.ylabel('x')
    plt.show()
```



Spectral Clustering

```
In [8]: # perform spectral clustering
sigma = 0.1 # tried 0.1, 0.5, 1
spectral_cluster = SpectralClustering(n_clusters=5, affinity='rbf', gamma = (1/(sigma**2 labels = spectral_cluster.fit_predict(main_df)

plt.scatter(main_df['x'], main_df['y'], c=labels, cmap='rainbow')
plt.xlabel('x')
plt.ylabel('y')
plt.show()
```



Remarks

K-means, Average Link Agglomerative Clustering and Spectral Clustering for *sigma=0.1* achieve the expected clustering. Agglomerative Clustering with a Single Link setting fails.

The first three classifiers succeed due to the data having desirable properties of similar shape, density, and variability, making the clusters well-separable, except for two clusters in the middle that are closer together.

Single Link Agglomerative Clustering fails due to the "chaining effect." This effect occurs because this method merges clusters based on the minimum distance between any two points in the clusters. In closely spaced points, this can result in long, chain-like clusters. In this dataset, the two middle clusters are incorrectly merged into one, and a single red point appears because the classifier attempts to "find" five clusters despite the chaining effect.