

# Robot Navigation and Obstacle Avoidance

Robotics Y5 – Graduate Course Project

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## Goal:

**Program a robot's movement in a simulation environment**



**Program the robot's movement in a real environment**

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# The Robot:

- **Jackal** by Clearpath Robotics
- Mobile - Differential Drive
- Equipped with LiDAR



# Software:

- **ROS 1 Noetic** on Ubuntu 20.04 Focal Fossa
  - **Gazebo**
  - **rViz**
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# Problem Description:

- Workspace: 6 x 4.5 m
- Set randomly chosen **Start** and **Goal** configurations within the workspace
- Set 3 **cubic** obstacles at random points within the workspace

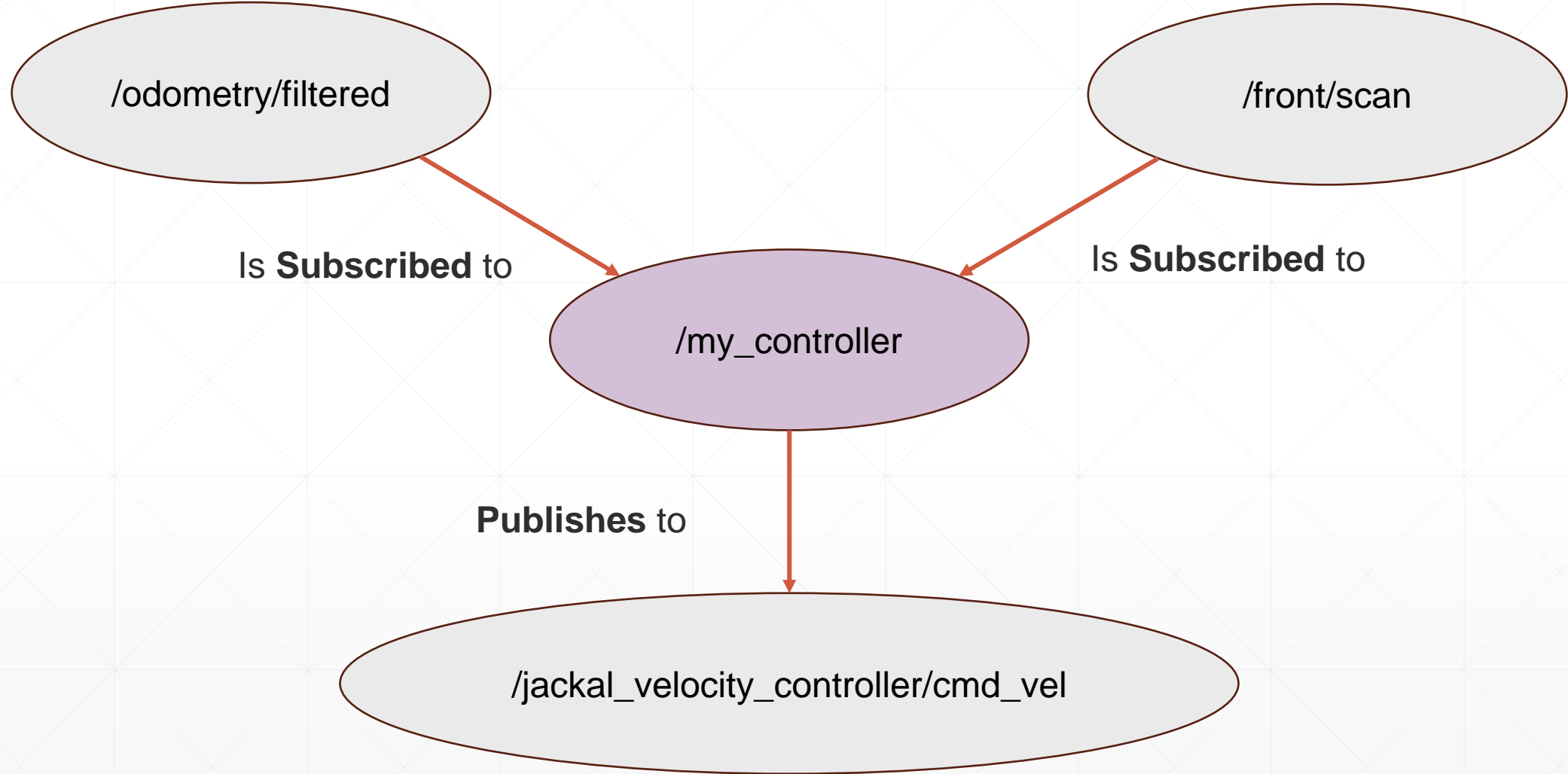
Configuration Representation:

$$q = \begin{bmatrix} x \\ y \\ \theta \end{bmatrix} \quad \begin{array}{l} \text{position} \\ \text{orientation} \end{array}$$

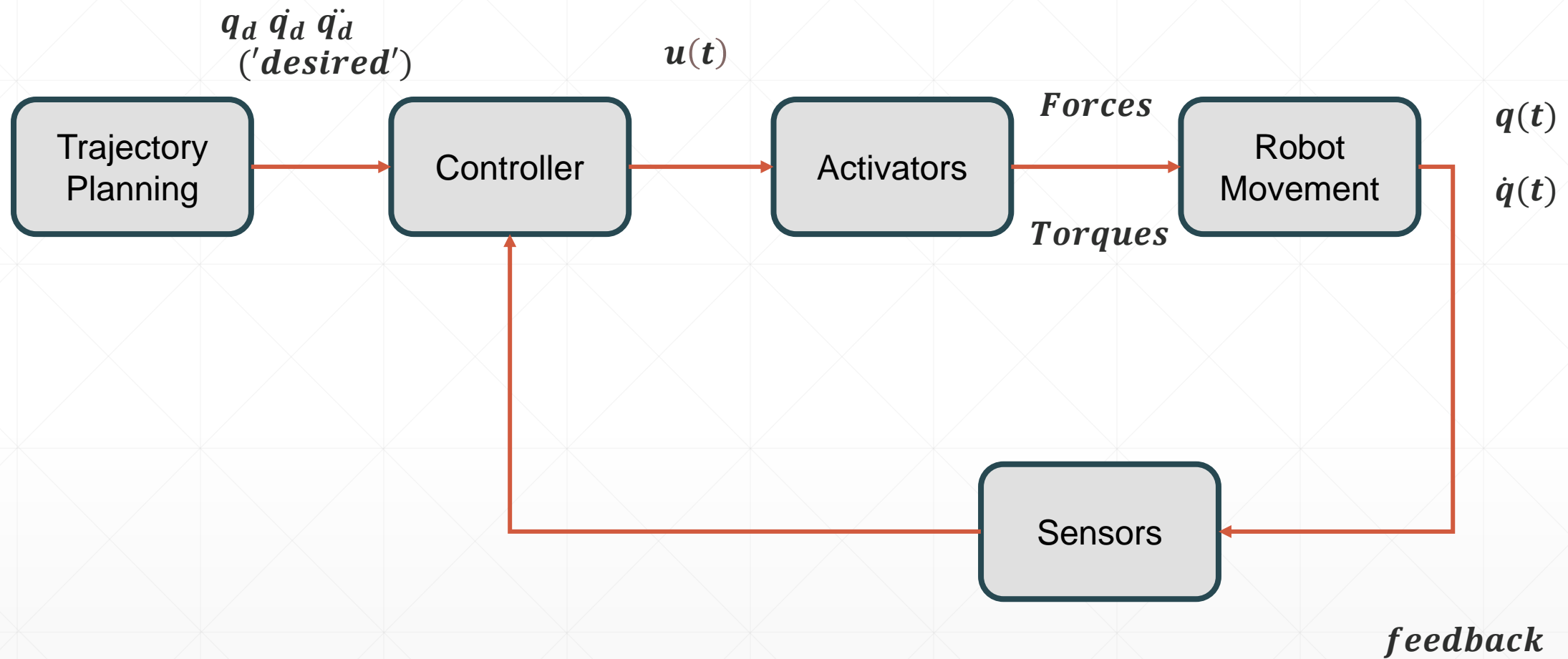
# Methodology:

- **New topic/s for a Controller**
  - **Artificial Potential Fields : Navigation Functions**
  - **Program scripts**
  - **Gazebo-rViz simulation and collect data**
  - **Run on real robot and collect data**
  - **Compare results**
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# Topics:



# Closed Loop Controller:





# Velocity Control:

In the Navigation Function methodology, the velocity command is

$$\dot{q} = u = -K_v \nabla \phi(q)$$

Where,  $\nabla \phi(q)$  is the gradient of the Navigation Function and  $K_v$  is a *gain* parameter

- The gradient has a magnitude and an orientation
  - The robot is a mobile, therefore it only has a linear velocity on axis x and an angular velocity on axis z (yaw)
  - The linear velocity must be proportional to the magnitude of the gradient
  - The angular velocity must be adjusted according to the gradient's orientation
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# Navigation Functions:

Distance of obstacles

$$\beta_i(q) = \begin{cases} -d^2(q, q_0) + r_0^2 \\ d^2(q, q_i) - r_i^2 \end{cases}$$

Repulsive Potential

$$\beta(q) = \prod_{i=0}^n \beta_i(q)$$

Attractive Potential

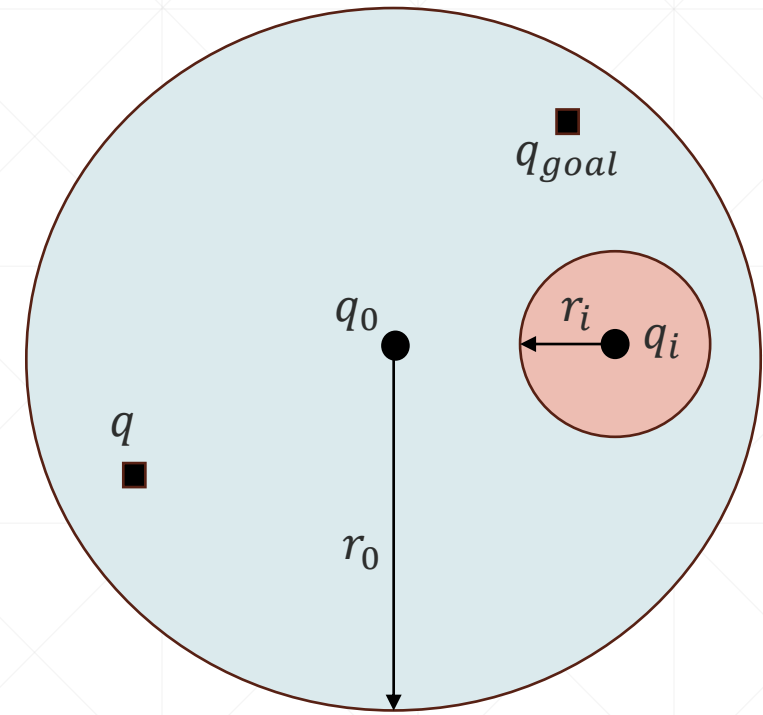
$$\gamma_k(q) = \left(d(q, q_{goal})\right)^{2k}$$

Navigation Function (NF)

$$\phi = \frac{\gamma_k(q)}{\beta(q) + \gamma_k(q)}$$

$$\phi_{morse} = \frac{d(q, q_{goal})^2}{(d(q, q_{goal})^{2k} + \beta(q))^{\frac{1}{k}}}$$

**For 2d vectors :**  $d(x, y) = ||x - y|| = \sqrt{(x_2 - x_1)^2 + (x_2 - y_1)^2}$



# Navigation Functions:

Gradient  $\nabla\phi(q) = \gamma(q) = \frac{2d(q, q_{goal})\nabla d(q, q_{goal})(d(q, q_{goal})^{2k} + \beta(q))^{\frac{1}{k}} - d(q, q_{goal})^2 \nabla(d(q, q_{goal})^{2k} + \beta(q))^{\frac{1}{k}}}{(d(q, q_{goal})^{2k} + \beta(q))^{\frac{2}{k}}}$

Where

$$\nabla d(q, q_{goal}) = \frac{q - q_{goal}}{d(q, q_{goal})}$$

$$\nabla(d(q, q_{goal})^{2k} + \beta(q))^{\frac{1}{k}} = \frac{1}{k}(d(q, q_{goal})^{2k} + \beta(q))^{\frac{1}{k}-1}(2k d(q, q_{goal})^{2k-1} \nabla d(q, q_{goal}) + \nabla \beta(q))$$

$$\nabla \beta(q) = \sum_{i=0}^n \nabla \beta_i(q) \prod_{j=0, j \neq i}^n \beta_j(q) \quad \text{where} \quad \nabla \beta_i(q) = \begin{cases} -2(q - q_0) \\ 2(q - q_i) \end{cases}$$

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# Programming NFs

- Partition LiDAR data considering objects every  $n$  samples ->  $m$  obstacles
- Keep min reading from each of the  $m$  obstacles
- Combine with angle increment information to find the distances between the robot and the obstacles ( $\beta(q)$ )
- Obstacle buffer zone = Robot Length + Virtual Obstacle Radius = 0.2+0.5
- Linear Velocity:

- If the obstacle is within the robot's "safe zone":

$$linear.x = K_v * ||\nabla\phi(q)||$$

$$angular.z = K_a * \left( \arctan \left( \frac{-\frac{d\nabla\phi(q)}{dq_y}}{-\frac{d\nabla\phi(q)}{dq_x}} \right) - yaw \right)$$

- If there are no objects in the "safe zone":

$$linear.x = K_v * ||\nabla\gamma_k(q)||$$

$$angular.z = K_a * \left( \arctan \left( \frac{-\frac{d\nabla\gamma_k(q)}{dq_y}}{-\frac{d\nabla\gamma_k(q)}{dq_x}} \right) - yaw \right)$$

$K_v, K_a$  : gains ( $> 0$ )

**Attractive Potential Only**

# Simulation Scenario

- We place a cylindrical obstacle at random (could be any shape)
- We set the goal configuration as:

$$\mathbf{q}_{goal} = \begin{bmatrix} 6.5 \\ 4.0 \\ 0.0 \end{bmatrix}$$

- $K_v, K_a = 0.5$
  - $k = 1$
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File

Edit

Camera

View

Window

Help

World

Insert

Layers

GUI

Scene

Spherical Coordinates

Physics

Atmosphere

Wind

Models

ground\_plane

LINKS

link

jackal

unit\_cylinder

Lights

Property	Value
name	ground_plane
is_static	<input checked="" type="checkbox"/> True
self_collide	<input type="checkbox"/> False
enable_wind	<input type="checkbox"/> False
▶ pose	
▶ link	ground_plane::link

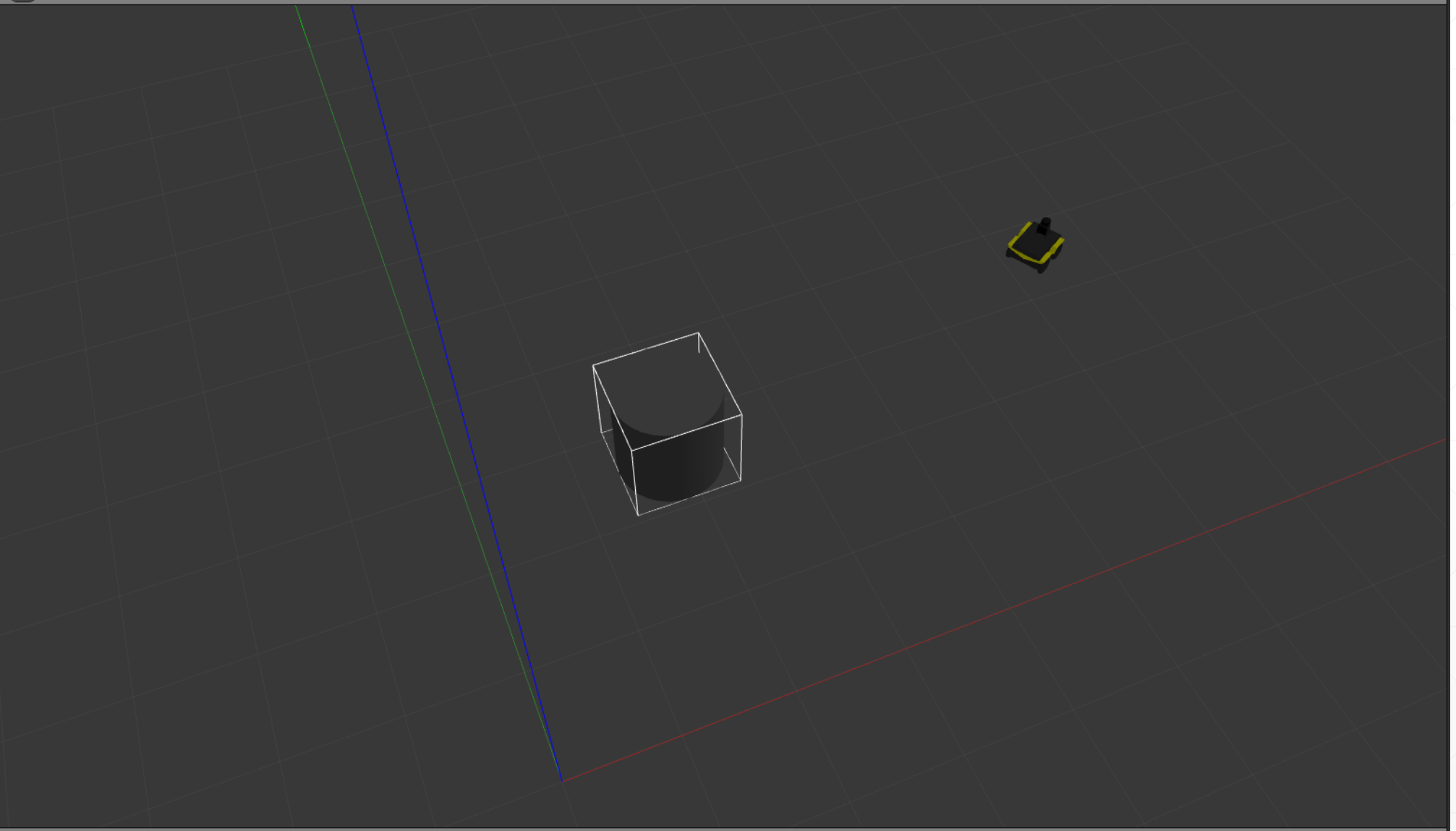


File Edit Camera View Window Help

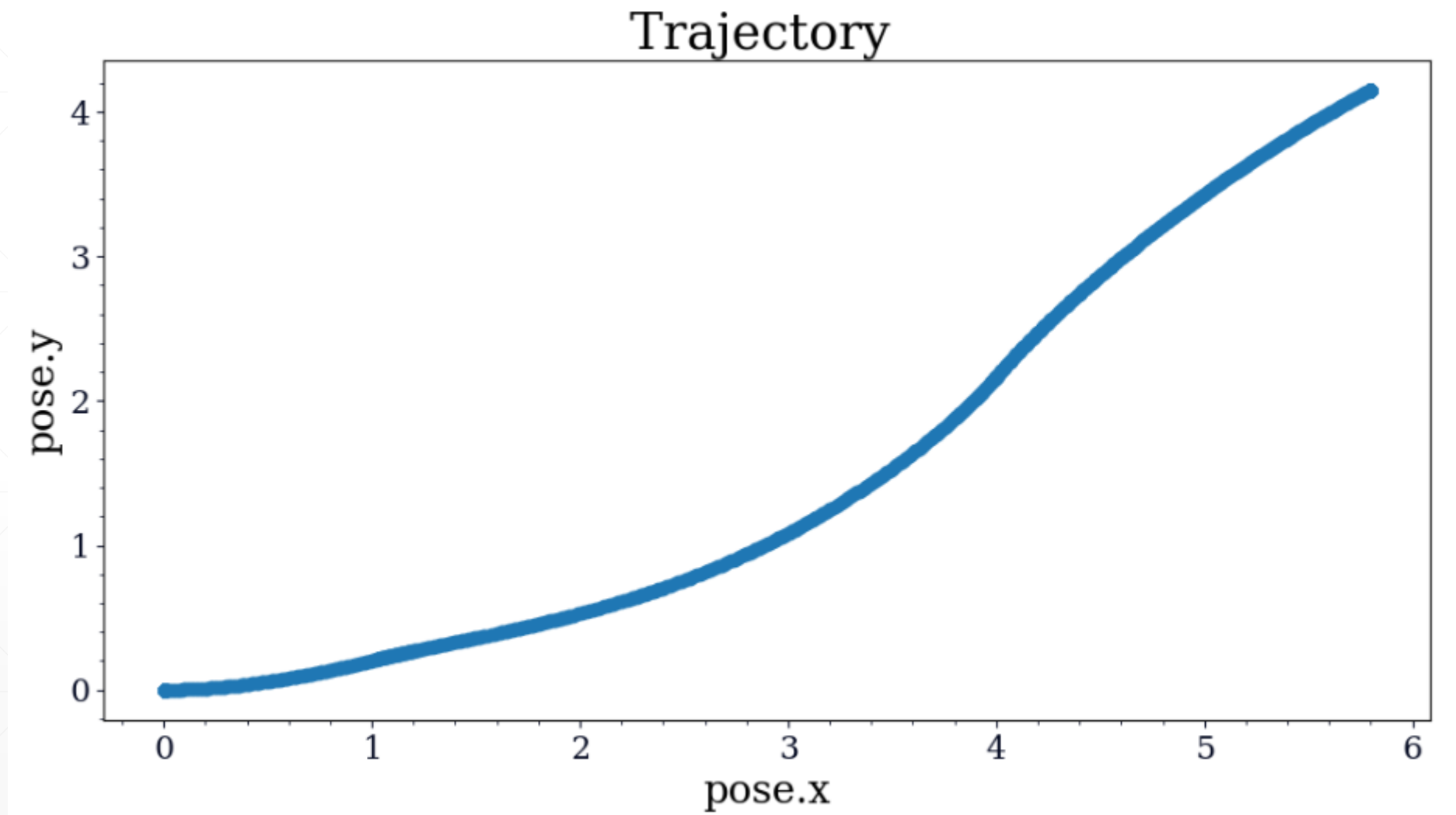
World Insert Layers

- GUI
- Scene
- Spherical Coordinates
- Physics
- Atmosphere
- Wind
- Models
  - ground\_plane
    - LINKS
    - link
  - jackal
  - unit\_cylinder
    - LINKS
    - link
- Lights

Property	Value
name	unit_cylinder
is_static	<input type="checkbox"/> False
self_collide	<input type="checkbox"/> False
enable_wind	<input type="checkbox"/> False
pose	
x	1.888312
y	2.586358
z	0.499997
roll	0.000004
pitch	0.000004
yaw	0.00
link	unit_cylinder::link

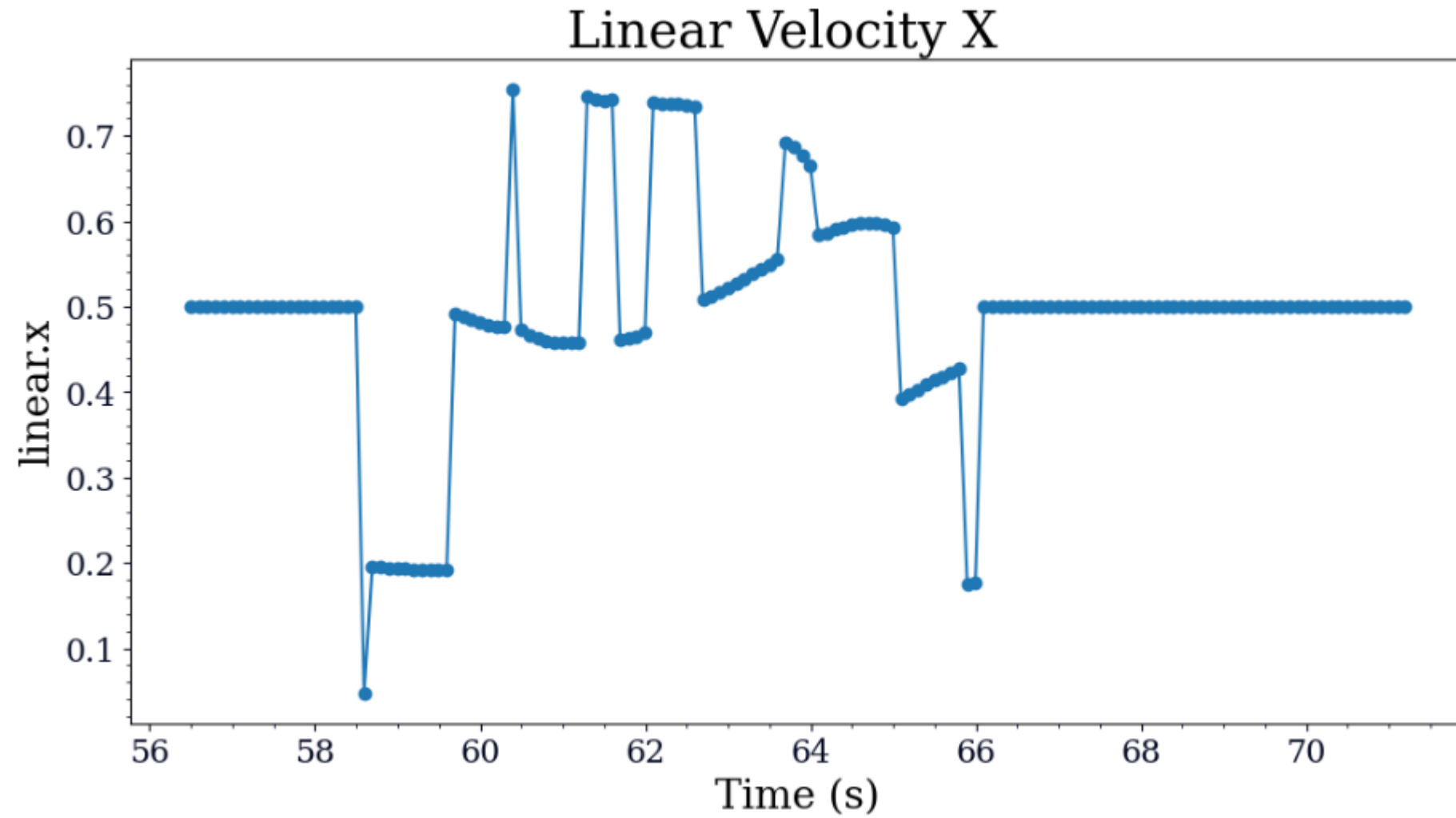


# Simulation: Odometry Results

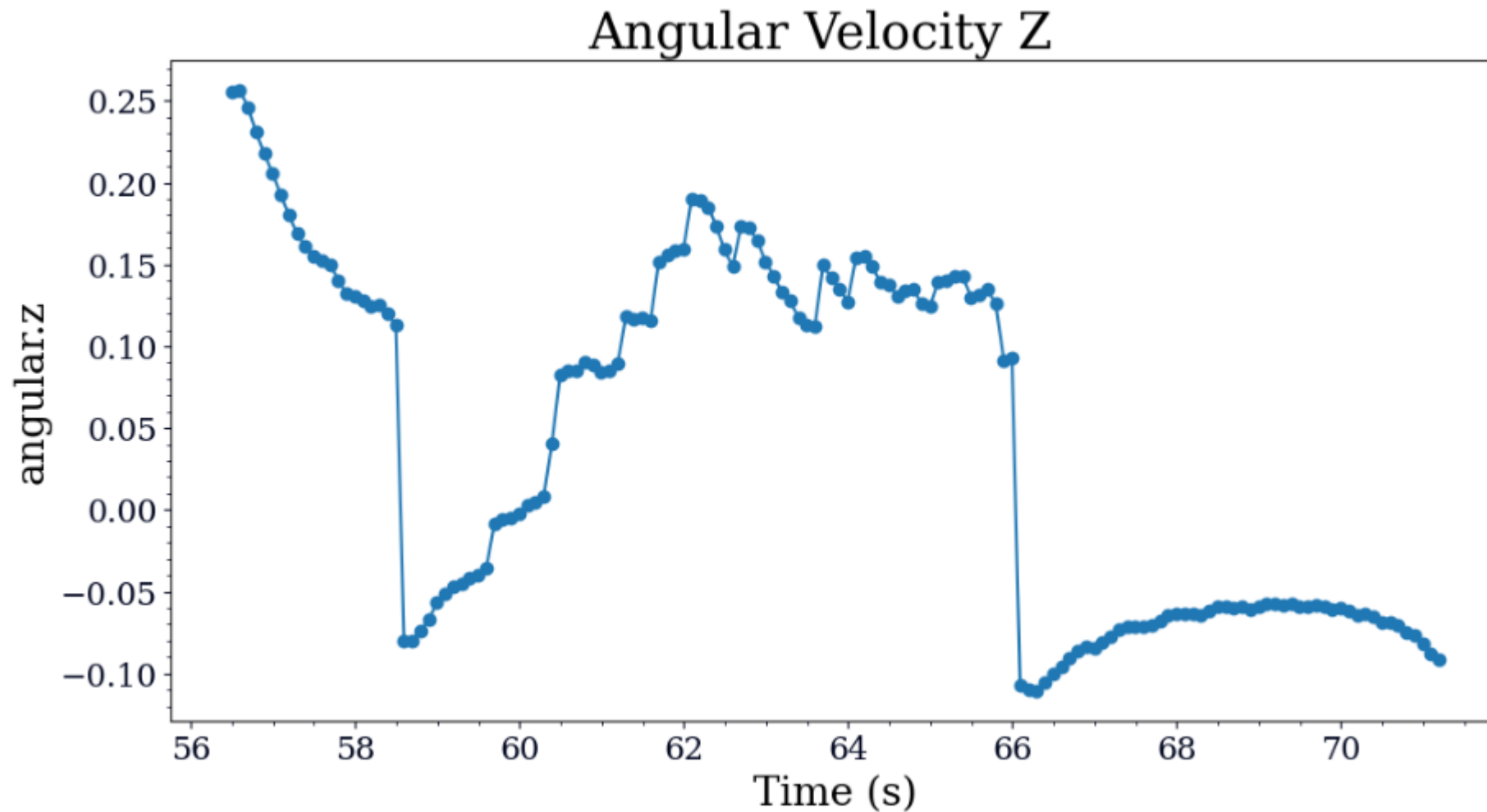




# Simulation: Velocity Results



# Simulation: Velocity Results



# Experiments in a Real Environment

- **Experiment 1 (Simulation to real world):**

- Goal Configuration:  $x = 6.5$   $y = 4$   $\theta = 0$ ,  $K_v, K_a = 0.5$ ,  $k = 1$
- It was stopped before attempting to go through the wall but the trajectory it was on was correct
- Link to video: [https://drive.google.com/file/d/1-aFstjbn\\_DAgrovlkNKFjyuxKuny7vDY/view?usp=drive\\_link](https://drive.google.com/file/d/1-aFstjbn_DAgrovlkNKFjyuxKuny7vDY/view?usp=drive_link)

- **Experiment 2 (Goal within available lab space):**

- Goal Configuration:  $x = 4$   $y = 4$   $\theta = 0$ ,  $K_v, K_a = 0.5$ ,  $k = 1$
- Successfully reaches the goal and stops
- Link to video: [https://drive.google.com/file/d/1rq3qUtUcCK7O-VWkYEEWPHHpCpDoiybM/view?usp=drive\\_link](https://drive.google.com/file/d/1rq3qUtUcCK7O-VWkYEEWPHHpCpDoiybM/view?usp=drive_link)

Note: Google Chrome works best with the links

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# Conclusion

- **The simulation and real results matched**
  - **The robot behaves as we expect it to based on the simulation**
  - **The robot both avoids the obstacle and reaches the goal**
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# Sources

Course Materials

For the Gradients:

- <https://www.sciencedirect.com/science/article/pii/019688589090017S>
  - [https://ecourse.uoi.gr/pluginfile.php/395920/mod\\_resource/content/17/robotics\\_project\\_grads\\_2024\\_B.pdf](https://ecourse.uoi.gr/pluginfile.php/395920/mod_resource/content/17/robotics_project_grads_2024_B.pdf)
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**Thank You!**

