## MAT1320 LINEAR ALGEBRA EXERCISES VII

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- 1. If  $A = \begin{bmatrix} 2 & 323 & -1 \\ 1 & 466 & 1 \\ 2 & 889 & 1 \end{bmatrix}$  and det(A) = -480, then which of the followings is the solution of  $x_2$  for the linear system of equations  $A\begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} 1 \\ 0 \\ 1 \end{bmatrix}$ ?

  a) 0 b) 480 + c c) -1 d) -480 + c 240

  Since M(A) = -460 + C, the system has a solution by Garer's method. Then,

by Carer's weethed Ther,

 $x_2 = \frac{\begin{vmatrix} 2 & 1 & -1 \\ 1 & 0 & 1 \end{vmatrix}}{\begin{vmatrix} 1 & 1 & 1 \\ 2 & 1 & 1 \end{vmatrix}} = \frac{-2}{-480} = \frac{1}{240}$ 

2)  $A^{T} \times b \Rightarrow (A^{T})^{-1} A^{T} \times c (A^{T})^{-1} b \Rightarrow (A^{-1})^{T} b$ 

- 2. (A points) Let A be an invertible matrix and  $A^{-1}$  $\begin{bmatrix} 0 & 1 \\ 1 & -4 \end{bmatrix}$ . If  $b = \begin{bmatrix} 1 \\ -2 \end{bmatrix}$ , then which of the followings is the solution of the linear system of equation  $A^T x = b$ ?
  - (a)  $x = \begin{bmatrix} 3 \\ -3 \end{bmatrix}$  b)  $x = \begin{bmatrix} 3 \\ -1 \end{bmatrix}$  c)  $x = \begin{bmatrix} 3 \\ 1 \end{bmatrix}$
- d)  $x = \begin{bmatrix} -3 \\ 1 \end{bmatrix}$  e)  $x = \begin{bmatrix} -3 \\ -1 \end{bmatrix}$

- 3. (B points) Let  $A = \begin{bmatrix} \clubsuit & \diamondsuit & \heartsuit \\ \spadesuit & \bigstar & \Box \\ \triangle & \bullet & \blacksquare \end{bmatrix}$  with  $det(A) \neq 0$ . Which of the followings is the value  $x_1 + x_2 + x_3$  for the solution of the linear system of equations  $A \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} \diamondsuit \\ \bigstar \end{bmatrix}$ ?

- $A^{T} \times 1 = b = 1 \qquad (A^{T})^{-1} \cdot A^{T} \cdot \lambda = (A^{T})^{-1} \cdot b$   $\Rightarrow \quad \lambda = (A^{-1})^{T} \cdot b$  $= \left(\begin{array}{cc} 4 & -5 \\ -3 & 4 \end{array}\right) \cdot \left(\begin{array}{c} 3 \\ 2 \end{array}\right)$  $=\begin{pmatrix} 2 \\ 5 \end{pmatrix}$
- 4. (C points) Let A be an invertible matrix and  $A^{-1} = \begin{bmatrix} 4 & -3 \\ -5 & 4 \end{bmatrix}$ . If  $b = \begin{bmatrix} 3 \\ 2 \end{bmatrix}$ , then which of the followings

a) 
$$x = \begin{bmatrix} 7 \\ -6 \end{bmatrix}$$
 b)  $x = \begin{bmatrix} 6 \\ -7 \end{bmatrix}$  c)  $x = \begin{bmatrix} 2 \\ -1 \end{bmatrix}$ 

$$x = \begin{bmatrix} 6 \\ -7 \end{bmatrix}$$

$$\begin{array}{c}
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\text{c)} x = \begin{bmatrix} 2 \\ -1 \end{bmatrix}$$

d) 
$$x = \begin{bmatrix} 22\\17 \end{bmatrix}$$
 e)  $x = \begin{bmatrix} 18\\23 \end{bmatrix}$