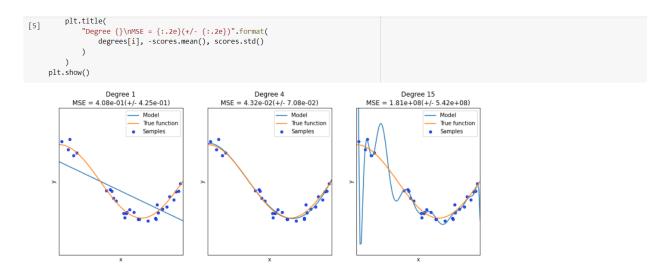
Task 2: Explain your analysis of the code. Make a detailed analysis that can also cover the following questions: (Submit the PDF of the Report)

Code Analysis:

1. Program for understanding Overfitting and Underfitting

Firstly, we import all the libraries needed. A true_fun is defined which is a cosine function. Then a random sample is taken and sorted and passed through the true_fun function. Then apply polynomial features and linear regression model to the data. Then pipeline the polynomial features and linear regression. Finally, evaluate the model using cross-validation. Plot the graphs for degree 1, degree 4, and degree 15 using MSE. The function is not sufficient to fit the training samples for degree 1, this is called underfitting. Degree 4 polynomial fits perfectly without underfitting or overfitting. When the degree increases, the model will overfit the training data by learning the noise of the training data. This is called overfitting.

```
/ [2] import numpy as np
        import matplotlib.pyplot as plt
       from sklearn.pipeline import Pipeline
       from sklearn.preprocessing import PolynomialFeatures
       from \ sklearn.linear\_model \ import \ LinearRegression
      from sklearn.model selection import cross val score
[3] def true_fun(X):
   return np.cos(1.5 * np.pi * X)
[4] np.random.seed(0)
       n samples = 30
       degrees = [1, 4, 15]
       X = np.sort(np.random.rand(n_samples))
    y = true_fun(X) + np.random.randn(n_samples) * 0.1
[5] plt.figure(figsize=(14, 5))
       for i in range(len(degrees)):
          ax = plt.subplot(1, len(degrees), i + 1)
          plt.setp(ax, xticks=(), yticks=())
          polynomial_features = PolynomialFeatures(degree=degrees[i], include_bias=False)
          linear_regression = LinearRegression()
          pipeline = Pipeline(
              [
                   ("polynomial_features", polynomial_features),
                   ("linear_regression", linear_regression),
          pipeline.fit(X[:, np.newaxis], y)
           # Evaluate the models using crossvalidation
          scores = cross_val_score(
             pipeline, X[:, np.newaxis], y, scoring="neg_mean_squared_error", cv=10
          X test = np.linspace(0, 1, 100)
          plt.plot(X_test, pipeline.predict(X_test[:, np.newaxis]), label="Model")
          plt.plot(X_test, true_fun(X_test), label="True function")
plt.scatter(X, y, edgecolor="b", s=20, label="Samples")
          plt.xlabel("x")
          plt.ylabel("y")
          plt.xlim((0, 1))
          plt.ylim((-2, 2))
          plt.legend(loc="best")
```



2. Overfitting (Printing accuracy at different steps)

Here make_classification function is used for problems with 10000 samples and 20 features. Dataset is split into training and testing data. A decision tree is used as a classifier, tree depth is adjusted. Test and training data are evaluated, and accuracies are printed at different depths. As the tree depth increases the performance increases, and the shallow trees have low performance. That is the reason the shallow trees do not overfit and extremely deeper trees overfit. As shown below, until depth 5 the accuracy of the test set increases, and later it decreases but the accuracy of the training sets increases until the maximum depth, this is called overfitting. This can be solved by decreasing the depth of the tree.

```
[6] # evaluate decision tree performance on train and test sets with different tree depths
       from \ sklearn. datasets \ import \ make\_classification
       from sklearn.model selection import train test split
        from sklearn.metrics import accuracy_score
       from sklearn.tree import DecisionTreeClassifier
       from matplotlib import pyplot
✓ [65] # define dataset
       X, y = make_classification(n_samples=10000, n_features=20, n_informative=5, n_redundant=15, random_state=1)
       # summarize the dataset
       print(X.shape, y.shape)
       (10000, 20) (10000,)
                                                                                                                          ↑ ↓ © 目 ‡ 🗓 🔋 :
   # split into train test sets
       X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.3)
       # summarize the shape of the train and test sets
       print(X_train.shape, X_test.shape, y_train.shape, y_test.shape)
       (7000, 20) (3000, 20) (7000,) (3000,)
[43] train_scores, test_scores = list(), list()
       # define the tree depths to evaluate
       values = [i for i in range(1, 31)]
```

```
↑ ↓ ⊖ 目 ‡ 🖟 🗎 :
# evaluate a decision tree for each depth
      for i in values:
          # configure the model
          model = DecisionTreeClassifier(max_depth=i)
           # fit model on the training dataset
           model.fit(X_train, y_train)
           # evaluate on the train dataset
           train_yhat = model.predict(X_train)
           train_acc = accuracy_score(y_train, train_yhat)
           train scores.append(train acc)
           # evaluate on the test dataset
           test_yhat = model.predict(X_test)
           test_acc = accuracy_score(y_test, test_yhat)
           test_scores.append(test_acc)
           # summarize progress
           print('>%d, train: %.3f, test: %.3f' % (i, train_acc, test_acc))
      >1, train: 0.970, test: 0.970
     >2, train: 0.974, test: 0.971
>3, train: 0.975, test: 0.972
      >4, train: 0.976, test: 0.969
>5, train: 0.978, test: 0.970
      >6, train: 0.980, test: 0.969
     >7, train: 0.982, test: 0.967
>8, train: 0.983, test: 0.966
      >9, train: 0.986, test: 0.965
     >10, train: 0.987, test: 0.963
>11, train: 0.990, test: 0.962
>12, train: 0.992, test: 0.960
>13, train: 0.993, test: 0.962
      >14, train: 0.994, test: 0.960
   >14, train: 0.994, test: 0.902
>14, train: 0.994, test: 0.960
>15, train: 0.995, test: 0.959
>16, train: 0.997, test: 0.959
    >17, train: 0.997, test: 0.959
>18, train: 0.998, test: 0.957
    >19, train: 0.999, test: 0.957
    >20, train: 0.999, test: 0.956
>21, train: 1.000, test: 0.956
    >22, train: 1.000, test: 0.956
    >23, train: 1.000, test: 0.955
>24, train: 1.000, test: 0.955
    >25, train: 1.000, test: 0.956
    >26, train: 1.000, test: 0.957
    >27, train: 1.000, test: 0.957
    >28, train: 1.000, test: 0.956
    >29, train: 1.000, test: 0.955
    >30, train: 1.000, test: 0.955
```

3. Cross Validation

Here, we are using dataset load_iris. We use cross-validation to evaluate overfitting and underfitting.

```
[45] import numpy as np
    from sklearn.model_selection import train_test_split
    from sklearn import datasets
    from sklearn import svm

X, y = datasets.load_iris(return_X_y=True)
    X.shape, y.shape

((150, 4), (150,))
```

Firstly, we use the basic method to compute the score using svm.

▼ Basic method to compute score

Here, the accuracy is estimated by splitting the data, fitting the model, and evaluating the score 5 times. The score is calculated at each iteration.

Estimate the accuracy by splitting the data, computing the score 5 consecutive times (with different splits each time)

Here, cross_val_score is used to cross-validate the score.

Using the different scoring parameter

Here, the cross-validate iterator is used to calculate the score.

▼ Calculate cross validation score by passing a cross validation iterator

▼ Use an iterable yielding (train, test) splits as arrays of indices

4. Different types of Cross validations: Below are a few cross-validation types.

K-fold divides all the samples into k groups of samples(folds) of equal sizes. The prediction function is learned using k-1 folds, and the fold left out is used for testing.

Repeated K-fold repeats K-Fold n times. It can be used when one requires to run kfold, n times, producing different splits in each iteration.

▼ Repeated K-Fold

```
[78] import numpy as np
         from sklearn.model_selection import RepeatedKFold
        random_state = 12883823
        rkf = RepeatedKFold(n_splits=2, n_repeats=2, random_state=random_state)
        for train, test in rkf.split(X):
            print("%s %s" % (train, test))
        [ 2 4 5 7 8 9 12 13 14 15 16 18 19 20 27 28 29 30 31 33 34 36 37 38 40 42 45 46 49 50 51 53 56 59 60 62
          63 68 69 73 74 75 78 80 84 86 87 88 89 91 95 96 97 98 99 100 102 103 104 105 112 115 116 120 126 129 135 138 139 141 142 143
         144 145 147] [ 0 1 3 6 10 11 17 21 22 23 24 25 26 32 35 39 41 43 44 47 48 52 54 55 57 58 61 64 65 66 67 70 71 72 76 77 79 81 82 83 85 90 92 93 94 101 106 107 108 109 110 111 113 114
         117\ 118\ 119\ 121\ 122\ 123\ 124\ 125\ 127\ 128\ 130\ 131\ 132\ 133\ 134\ 136\ 137\ 140
         146 148 149]
        [ 0 1 3 6 10 11 17 21 22 23 24 25 26 32 35 39 41 43 44 47 48 52 54 55 57 58 61 64 65 66 67 70 71 72 76 77
           79 81 82 83 85 90 92 93 94 101 106 107 108 109 110 111 113 114
         99 100 102 103 104 105 112 115 116 120 126 129 135 138 139 141 142 143
          144 145 147]
```

In LOO, learning sets are created by taking all the samples leaving only one, which is the test set.

LPO creates all the possible training/test sets by removing p samples from the complete set. For n samples, this produces (np) train-test pairs.

```
▼ Leave P Out (LPO)

                                                                                                                                                        ↑ ↓ ⊖ 目 ‡ 🗓 📋 :
   from sklearn.model_selection import LeavePOut
         lpo = LeavePOut(p=2)
         for train, test in lpo.split(X):
          print("%s %s" % (train, test))
   146 147 148 149] [133 136]
        [ 0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48 49 50 51 52 53 54 55 56 57 58 59 60 61 62 63 64 65 66 67 68 69 70 71
           108 109 110 111 112 113 114 115 116 117 118 119 120 121 122 123 124 125
          126 127 128 129 130 131 132 134 135 136 138 139 140 141 142 143 144 145
          146 147 148 149] [133 137]
           0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34 35
           36 37 38 39 40 41 42 43 44 45 46 47 48 49 50 51 52 53 54 55 55 56 57 58 59 60 61 62 63 64 65 66 67 68 69 70 71 72 73 74 75 76 77 78 79 80 81 82 83 84 85 86 87 88 89
          90 91 92 93 94 95 96 97 98 99 100 101 102 103 104 105 106 107 108 109 110 111 112 113 114 115 116 117 118 119 120 121 122 123 124 125
          126 127 128 129 130 131 132 134 135 136 137 139 140 141 142 143 144 145
          146 147 148 149] [133 138]
         [ 0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34 15 16
            36 37 38 39 40 41 42 43 44 45 46 47 48 49 50 51 52 53
```

Stratified k-fold is a variation of k-fold which returns stratified folds, each set contains approximately the same percentage of samples of each target class as the complete set.

Stratified Shuffle Split is a variation of Shuffle Split, which returns stratified splits i.e., which creates splits by preserving the same percentage for each target class as in the complete set

▼ Stratified Shuffle split

```
[87] from sklearn.model_selection import StratifiedShuffleSplit
       sss = StratifiedShuffleSplit(n_splits=5, test_size=0.5, random_state=0)
       sss.get n splits(X, y)
       StratifiedShuffleSplit(n_splits=5, random_state=0)
       for train_index, test_index in sss.split(X, y):
    print("TRAIN:", train_index, "TEST:", test_index)
    X_train, X_test = X[train_index], X[test_index]
        y_train, y_test = y[train_index], y[test_index]
       StratifiedShuffleSplit(n_splits=5, random_state=0, test_size=0.5,
                  train size=None)
       TRAIN: [ 16 69 15 4 78 138 111 10 93 45 74 58 106 22 56 28 107 27 94 72 66 33 143 87 96 115 73 84 26 126 11 91 128 105 79 48 7 148 31 119 59 124 38 57 95 101 83 137 112 52 92 30 63 42
         14 108 125 122 141 32 140 35 76 41 2 18 146 135 127 116 80 29
        104 82 34] TEST: [139 65 145 6 129 25 85 23 118 64 17 121 71 39 67 36 131 149 24 0 89 8 136 110 132 147 117 9 130 75 134 144 97 114 19 43 49 21 50 86 37 20 61 81 5 123 44 99 77 102 98 31 42 40 88 60 12 103 53 109 90 133 70 100 13 47 54 1 51 68 113 62
TRAIN: [ 7 10 141 6 94 31 113 140 108 11 128 96 149 110 98 4 101 44
           5 2 144 102 112 86 41 20 59 118 148 115 99 132 88 57 105 103
           83 45 138 62 74 81 52 13 114 67 40 47 82 33 106 38 18 135
           63 \quad 75 \quad 79 \quad 37 \quad 55 \quad 72 \quad 70 \quad 111 \quad 95 \quad 142 \quad 15 \quad 64 \quad 121 \quad 19 \quad 91 \quad 42 \quad 26 \quad 126
           12  1 69] TEST: [120 78 29 46 58 134 125 25 53 48 51 104 146 123 54 131 9 68
           35 139 50 43 147 145 73 130 32 3 77 127 24 109 16 87 71 56
           36 30 39 60 122 65 129 28 97 85 119 21 92 117 80 90 49 143
          84 107 61]
         TRAIN: [131 76 116 145 114 18 4 95 52 61 94 87 29 103 142 9 0 65
           45 46 81 121 88 44 24 32 28 56 122 89 71 90 77 72 115 60
           78 85 49 58 41 129 91 117 127 69 107 99 113 11 33 74 119 34
          105 147 102 3 101 30 111 100 106 109 2 19 23 51 40 143 15 97
          20 38 123] TEST: [130 17 125 124 53 43 62 86 79 80 31 137 55 36 42 64 141 8
           5 82 98 84 10 134 83 7 135 27 50 48 12 132 35 16 133 139
          59 140 136 63 93 73 148 108 1 138 110 66 68 21 128 96 70 13
          26 92 126 39 54 22 75 37 149 67 6 118 25 57 104 144 120 47
         112 146 14]
         TRAIN: [138 137 136 139 82 64 27 21 3 99 9 33 30 149 100 72 47 145
          50 40 96 79 97 140 109 134 7 142 92 133 112 58 45 42 131 32
           4 66 60 118 110 95 10 13 75 12 38 57 44 77 41 20 83 51
          81 130 73 101 117 18 28 91 89 62 125 68 106 148 143 78 36 34
          120 108 2] TEST: [ 23 123 26 1 37 102 15 113 25 90 31 124 147 22 111 105 71 86
          146 56 128 24 69 88 126 121 122 61 0 43 87 141 144 119 19 127
          49 \quad 17 \quad 65 \quad 5 \quad 46 \quad 85 \quad 135 \quad 76 \quad 16 \quad 67 \quad 52 \quad 14 \quad 103 \quad 11 \quad \quad 6 \quad 55 \quad 93 \quad 94
         116 53 74 70 84 104 115 39 132 129 54 63 35 48 114 80 29
          98 107 59]
         TRAIN: [ 65 30 56 92 131 37 149 49 57 38 99 125 19 24 134 55
         115 109 81 36 146 108 35 132 128 6 48 54 59 14 43 88 114 22
          26 73 84 3 85 121 47 72 100 138 82 130 39 106 141 140 76 113
          139 \quad 78 \ 111 \quad 93 \ 101 \quad 10 \quad 21 \quad 44 \quad 41 \ 148 \quad 58 \quad 15 \quad 89 \ 133 \quad 80 \quad 61 \ 137 \quad 75
            2 18 97] TEST: [ 31 126 33 71 145 102 7 29 60 40 45 74 123 51 50 136 96 144
```

5. Validation Curve

The influence of a single hyperparameter on the training score and the validation score is used to find out if the estimator is overfitting or underfitting for some hyperparameter values. If the training score and the validation score are both low, the estimator will be underfitting. If the training score is high and the validation score is low, the estimator is overfitting.

Here, the train and test data CSV files are trained using a random forest classifier and data is fit, then used to draw a validation curve.

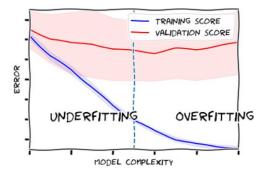
```
[58] import pandas as pd
        import numpy as np
        import matplotlib.pyplot as plt
        from \ sklearn.ensemble \ import \ Random Forest Classifier
        from \ sklearn.model\_selection \ import \ GridSearchCV
        from \ sklearn.model\_selection \ import \ cross\_val\_score, \ learning\_curve, \ validation\_curve
[59] df_train = pd.read_csv('train.csv')
        df_test = pd.read_csv('test.csv')
        df_comb = df_train.append(df_test)
        X = pd.DataFrame()
(50) def encode_sex(x):
            return 1 if x == 'female' else 0
        def family_size(x):
           size = x.SibSp + x.Parch
            return 4 if size > 3 else size
        X['Sex'] = df_comb.Sex.map(encode_sex)
        X['Pclass'] = df_comb.Pclass
X['FamilySize'] = df_comb.apply(family_size, axis=1)

  [61] fare_median = df_train.groupby(['Sex', 'Pclass']).Fare.median()

        fare_median.name = 'FareMedian'
        age_mean = df_train.groupby(['Sex', 'Pclass']).Age.mean()
        age_mean.name = 'AgeMean
        def join(df, stat):
           return pd.merge(df, stat.to_frame(), left_on=['Sex', 'Pclass'], right_index=True, how='left')
        X['Fare'] = df_comb.Fare.fillna(join(df_comb, fare_median).FareMedian)
        X['Age'] = df_comb.Age.fillna(join(df_comb, age_mean).AgeMean)
[62] def quantiles(series, num):
            return pd.qcut(series, num, retbins=True)[1]
        def discretize(series, bins):
            return pd.cut(series, bins, labels=range(len(bins)-1), include_lowest=True)
        X['Fare'] = discretize(X.Fare, quantiles(df_comb.Fare, 10))
X['Age'] = discretize(X.Age, quantiles(df_comb.Age, 10))
[31] X_train = X.iloc[:df_train.shape[0]]
        X_test = X.iloc[df_train.shape[0]:]
        y_train = df_train.Survived
(33] clf_1 = RandomForestClassifier(n_estimators=100, bootstrap=True, random_state=0)
        clf_1.fit(X_train, y_train)
        # Number of folds for cross validation
        num_folds = 7
```

```
[34] def plot_curve(ticks, train_scores, test_scores):
              train_scores_mean = -1 * np.mean(train_scores, axis=1)
train_scores_std = -1 * np.std(train_scores, axis=1)
test_scores_mean = -1 * np.mean(test_scores, axis=1)
               test_scores_std = -1 * np.std(test_scores, axis=1)
               plt.fill_between(ticks,
                                     train_scores_mean - train_scores_std,
                                    train_scores_mean + train_scores_std, alpha=0.1, color="b")
               plt.fill between(ticks,
                                   test_scores_mean - test_scores_std,
                                     test_scores_mean + test_scores_std, alpha=0.1, color="r")
              plt.plot(ticks, train_scores_mean, 'b-', label='Training score')
plt.plot(ticks, test_scores_mean, 'r-', label='Validation score')
plt.legend(fancybox=True, facecolor='w')
               return plt.gca()
[35] def plot_validation_curve(clf, X, y, param_name, param_range, scoring='roc_auc'):
               ax = plot_curve(param_range, *validation_curve(clf, X, y, cv=num_folds,
                                                                            scoring=scoring,
                                                                           param_name=param_name,
                                                                           param_range=param_range, n_jobs=-1))
               ax.set title('')
               ax.set_xticklabels([])
               ax.set_yticklabels([])
               ax.set_xlim(2,12)
              ax.set_ylim(-0.97, -0.83)
ax.set_ylabel('Error')
               ax.set_xlabel('Model complexity')
               ax.text(9, -0.94, 'Overfitting', fontsize=22)
ax.text(3, -0.94, 'Underfitting', fontsize=22)
ax.axvline(7, ls='--')
               plt.tight_layout()

// [36] plot_validation_curve(clf_1, X_train, y_train, param_name='max_depth', param_range=range(2,13))
```



6. ROC

The two main metrics of true positive rate and two negative rates are visualized using a ROC.

Data is fetched from the GitHub URL; a logical regression model is used, and data is fit. The metrics are defined, and the ROC curve is drawn. If the curve touches the top left corner of the plot, the model is considered better at classifying the data into categories.

```
[37] import pandas as pd
       import numpy as np
       from sklearn.model_selection import train_test_split
       from sklearn.linear_model import LogisticRegression
       from sklearn import metrics
       import matplotlib.pyplot as plt
[38] #import dataset from CSV file on Github
       url = "https://raw.githubusercontent.com/Statology/Python-Guides/main/default.csv"
       data = pd.read csv(url)
       #define the predictor variables and the response variable
       X = data[['student', 'balance', 'income']]
       y = data['default']
       \# split the dataset into training (70%) and testing (30%) sets
       X_train,X_test,y_train,y_test = train_test_split(X,y,test_size=0.3,random_state=0)
       #instantiate the model
       log_regression = LogisticRegression()
       #fit the model using the training data
       log_regression.fit(X_train,y_train)
       LogisticRegression()
(39) #define metrics
        y_pred_proba = log_regression.predict_proba(X_test)[::,1]
        fpr, tpr, _ = metrics.roc_curve(y_test, y_pred_proba)
        #create ROC curve
       plt.plot(fpr,tpr)
       plt.ylabel('True Positive Rate')
        plt.xlabel('False Positive Rate')
       plt.show()
           1.0
        RATE
8:0
        POSITIVE
FO 00
```

1) According to you, why do overfitting and underfitting occur, and how resolve them? What is the difference between them?

When the model tries to capture the relation between the input and target values very efficiently leading to the memorization of the data, the model does not perform well on the testing data but performs well on the training data.

When the model performs poorly on training data, it is called underfitting. This is because the model is unable to capture the relationship between the input examples and the target values.

There are a few common ways to control the overfitting of data i.e., by Adding more data, data augmentation, regularization, and removing features from the data. In the

code, we have regulated the depth of the decision tree to control overfitting. Or for the KNN classifier, we can change the neighbor number to control overfitting.

The underfitting problem can be solved by increasing the model complexity, reducing regularization, and adding features to training data.

A model that is under fitted will have high training and high testing error while an overfit model will have extremely low training error but a high testing error.

2) What kind of pattern did you analyze in the Train and Test score while running the code of overfitting?

Test and training data are evaluated, and accuracies are printed at different depths. As the tree depth increases the performance increases, and the shallow trees have low performance. That is the reason why the shallow trees do not overfit and extremely deeper trees overfit, until depth 5 the accuracy of the test set increases, and later it decreases but the accuracy of the training sets increases until the maximum depth, this is called overfitting. This can be solved by decreasing the depth of the tree.

3) What is cross-validation, and what did you analyze in a different type of validation that you performed?

To avoid overfitting, sometimes available data is divided into three parts training, testing, and validation data, as the size of the samples used for learning decreases, the results depend on a particular random pair of training and validation data, to solve this problem cross-validation is used.

- K-fold divides all the samples into k groups of samples(folds) of equal sizes. The prediction function is learned using k-1 folds, and the fold left out is used for testing.
- Repeated K-fold repeats K-Fold n times. It can be used when one requires to run kfold, n times, producing different splits in each iteration.
- In LOO, learning sets are created by taking all the samples leaving only one, which is the test set.
- LPO creates all the possible training/test sets by removing p samples from the complete set. For n samples, this produces (np) train-test pairs.
- Stratified k-fold is a variation of k-fold which returns stratified folds, each set contains the same percentage of samples of each target class as the complete set.
- Stratified Shuffle Split is a variation of Shuffle Split, which returns stratified splits i.e., which creates splits by preserving the same percentage for each target class as in the complete set.
- 4) Explain the analysis from generated ROC and validation curve and what they represent? Validation Curve:

To estimate the generalization accurately we must compute the score on another test set. If the training score and the validation score are both low, the estimator will be underfitting. If the training score is high and the validation score is low, the estimator is overfitting and otherwise, it is working very well. A low training score and a high validation score are usually not possible.

ROC Curve:

The two main metrics, true positive rate, and true negative rates are visualized using a ROC. If the curve touches the top left corner of the plot, the model is considered better at classifying the data into categories.