CSCE 5150 – Analysis of Computer Algorithms

Programming Assignment 1 – Divide and Conquer

Neha Goud Baddam

11519516

A computer program to implement the Strassen' algorithm for matrix multiplication.

```
In [1]: import numpy as np
        #below is the function defined for strassens algorithm
        # we are passing x and y matrices as parameters
        def strassen(matrix_A, matrix_B):
            #if the size of the matrix is 1, then just multiply the matrices
            if matrix A.size == 1 or matrix B.size == 1:
                return matrix_A * matrix_B
            #firstly we get the size of the matrix
            sizeOfMatrix = matrix_A.shape[0]
            #if the size of the matrix is odd, we pad the matrix with zeros to get a ever
            if sizeOfMatrix % 2 == 1:
                matrix_A = np.pad(matrix_A, (0, 1), mode='constant')
                matrix_B = np.pad(matrix_B, (0, 1), mode='constant')
            #now we divide the matrix A and matrix B into half and store it in the below
            #get the nearsest interger of size of the matrix / 2
            halfOfSize= int(np.ceil(sizeOfMatrix / 2))
            #partitioning into sub matrices
            A11 = matrix_A[: halfOfSize, : halfOfSize]
            A12 = matrix_A[: halfOfSize, halfOfSize:]
            A21 = matrix A[halfOfSize:, : halfOfSize]
            A22 = matrix A[halfOfSize:, halfOfSize:]
            B11 = matrix B[: halfOfSize, : halfOfSize]
            B12 = matrix B[: halfOfSize, halfOfSize:]
            B21 = matrix B[halfOfSize:, : halfOfSize]
            B22 = matrix_B[halfOfSize:, halfOfSize:]
            #finding the sum and differences of the matrices based on the below formulas
            s1 = B12 - B22
            s2 = A11 + A12
            s3 = A21 + A22
            s4 = B21 - B11
            s5 = A11 + A22
            s6 = B11 + B22
            s7 = A12 - A22
            s8 = B21 + B22
            s9 = A11 - A21
            s10 = B11 + B12
            #finding the product of the matrices using the below formula
            #recurssively call the function strassen to divide the matrix until it cannow
            #any submatrix
            p1 = strassen(A11, s1)
            p2 = strassen(s2, B22)
            p3 = strassen(s3, B11)
            p4 = strassen(A22, s4)
            p5 = strassen(s5, s6)
            p6 = strassen(s7, s8)
            p7 = strassen(s9, s10)
```

```
#now finally create a result matrix of original size of mtraix A and B and st
matrix_C = np.zeros((2 * halfOfSize, 2 * halfOfSize), dtype=np.int32)

matrix_C[: halfOfSize, : halfOfSize] = p5 + p4 - p2 + p6
matrix_C[: halfOfSize, halfOfSize:] = p1 + p2
matrix_C[halfOfSize:, : halfOfSize] = p3 + p4
matrix_C[halfOfSize:, halfOfSize:] = p1 + p5 - p3 - p7

#now we return the matrix_c value that has the result
return matrix_C[: sizeOfMatrix, : sizeOfMatrix]
```

```
In [2]:
        #take the size of matrix as input
        matrixSize = int(input("Enter matrix size for matrix A and matrix B : "))
        #create two arrays of size given above
        arr1 = np.zeros(shape = (matrixSize, matrixSize))
        arr2 = np.zeros(shape = (matrixSize, matrixSize))
        #take matrix A and matrix B as input for matrix multiplication
        for i in range(0,matrixSize):
            for j in range(0,matrixSize):
                arr1[i][j] = input("Enter numbers in the first matrix A, one after the ot
        for i in range(0,matrixSize):
            for j in range(0,matrixSize):
                arr2[i][j] = input("Enter numbers in the second matrix B, one after the 
        print("Below is the matrix_A",arr1)
        print("Below is the matrix B",arr2)
        matrix_A = np.array(arr1)
        matrix B = np.array(arr2)
        print('Strassens Matrix multiplication result for above matrix_A and matrix_B is
        print(strassen(matrix A, matrix B))
```

```
Enter matrix size for matrix A and matrix B : 2
Enter numbers in the first matrix A, one after the other: 1
Enter numbers in the first matrix A, one after the other: 3
Enter numbers in the first matrix A, one after the other: 7
Enter numbers in the first matrix A, one after the other: 5
Enter numbers in the second matrix B, one after the other: 6
Enter numbers in the second matrix B, one after the other: 8
Enter numbers in the second matrix B, one after the other: 4
Enter numbers in the second matrix B, one after the other: 2
Below is the matrix A [[1. 3.]
 [7. 5.]]
Below is the matrix_B [[6. 8.]
 [4. 2.]]
Strassens Matrix multiplication result for above matrix_A and matrix_B is :
[[18 14]
 [62 66]]
```

```
In [3]: #take the size of matrix as input
        matrixSize = int(input("Enter matrix size for matrix A and matrix B : "))
        #create two arrays of size given above
        arr1 = np.zeros(shape = (matrixSize, matrixSize))
        arr2 = np.zeros(shape = (matrixSize, matrixSize))
        #take matrix A and matrix B as input for matrix multiplication
        for i in range(0,matrixSize):
            for j in range(0,matrixSize):
                arr1[i][j] = input("Enter numbers in the first matrix A, one after the ot
        for i in range(0,matrixSize):
            for j in range(0,matrixSize):
                arr2[i][j] = input("Enter numbers in the second matrix B, one after the (
        print("Below is the matrix A",arr1)
        print("Below is the matrix_B",arr2)
        matrix A = np.array(arr1)
        matrix_B = np.array(arr2)
        print('Strassens Matrix multiplication result for above matrix_A and matrix_B is
        print(strassen(matrix_A, matrix_B))
        Enter matrix size for matrix A and matrix B : 3
        Enter numbers in the first matrix A, one after the other: 2
        Enter numbers in the first matrix A, one after the other: 3
        Enter numbers in the first matrix A, one after the other: 4
        Enter numbers in the first matrix A, one after the other: 5
        Enter numbers in the first matrix A, one after the other: 6
        Enter numbers in the first matrix A, one after the other: 7
        Enter numbers in the first matrix A, one after the other: 8
```

```
Enter numbers in the first matrix A, one after the other: 9
Enter numbers in the first matrix A, one after the other: 0
Enter numbers in the second matrix B, one after the other: 12
Enter numbers in the second matrix B, one after the other: 45
Enter numbers in the second matrix B, one after the other: 76
Enter numbers in the second matrix B, one after the other: 8
Enter numbers in the second matrix B, one after the other: 9
Enter numbers in the second matrix B, one after the other: 3
Enter numbers in the second matrix B, one after the other: 4
Enter numbers in the second matrix B, one after the other: 5
Enter numbers in the second matrix B, one after the other: 6
Below is the matrix_A [[2. 3. 4.]
 [5. 6. 7.]
 [8. 9. 0.]]
Below is the matrix B [[12. 45. 76.]
 [8. 9. 3.]
 [ 4. 5. 6.]]
Strassens Matrix multiplication result for above matrix_A and matrix_B is :
[[ 64 137 185]
 [136 314 440]
 [168 441 635]]
```

```
In [4]: #take the size of matrix as input
        matrixSize = int(input("Enter matrix size for matrix A and matrix B : "))
        #create two arrays of size given above
        arr1 = np.zeros(shape = (matrixSize, matrixSize))
        arr2 = np.zeros(shape = (matrixSize, matrixSize))
        #take matrix A and matrix B as input for matrix multiplication
        for i in range(0,matrixSize):
            for j in range(0,matrixSize):
                arr1[i][j] = input("Enter numbers in the first matrix A, one after the ot
        for i in range(0,matrixSize):
            for j in range(0,matrixSize):
                arr2[i][j] = input("Enter numbers in the second matrix B, one after the (
        print("Below is the matrix A",arr1)
        print("Below is the matrix_B",arr2)
        matrix A = np.array(arr1)
        matrix_B = np.array(arr2)
        print('Strassens Matrix multiplication result for above matrix_A and matrix_B is
        print(strassen(matrix_A, matrix_B))
        Enter matrix size for matrix A and matrix B: 4
        Enter numbers in the first matrix A, one after the other: 1
        Enter numbers in the first matrix A, one after the other: 2
        Enter numbers in the first matrix A, one after the other: 3
        Enter numbers in the first matrix A, one after the other: 4
        Enter numbers in the first matrix A, one after the other: 5
        Enter numbers in the first matrix A, one after the other: 6
        Enter numbers in the first matrix A, one after the other: 7
        Enter numbers in the first matrix A, one after the other: 8
        Enter numbers in the first matrix A, one after the other: 9
        Enter numbers in the first matrix A, one after the other: 1
        Enter numbers in the first matrix A, one after the other: 2
        Enter numbers in the first matrix A, one after the other: 3
        Enter numbers in the first matrix A, one after the other: 4
        Enter numbers in the first matrix A, one after the other: 6
        Enter numbers in the first matrix A, one after the other: 7
        Enter numbers in the first matrix A, one after the other: 8
        Enter numbers in the second matrix B, one after the other: 6
        Enter numbers in the second matrix B, one after the other: 4
        Enter numbers in the second matrix B, one after the other: 3
        Enter numbers in the second matrix B, one after the other: 6
        Enter numbers in the second matrix B, one after the other: 8
        Enter numbers in the second matrix B, one after the other: 4
        Enter numbers in the second matrix B, one after the other: 2
        Enter numbers in the second matrix B, one after the other: 9
        Enter numbers in the second matrix B, one after the other: 5
        Enter numbers in the second matrix B, one after the other: 2
        Enter numbers in the second matrix B, one after the other: 1
        Enter numbers in the second matrix B, one after the other: 4
        Enter numbers in the second matrix B, one after the other: 3
```

```
Enter numbers in the second matrix B, one after the other: 6
Enter numbers in the second matrix B, one after the other: 8
Enter numbers in the second matrix B, one after the other: 9
Below is the matrix_A [[1. 2. 3. 4.]
 [5. 6. 7. 8.]
[9. 1. 2. 3.]
 [4. 6. 7. 8.]]
Below is the matrix_B [[6. 4. 3. 6.]
 [8. 4. 2. 9.]
 [5. 2. 1. 4.]
 [3. 6. 8. 9.]]
Strassens Matrix multiplication result for above matrix_A and matrix_B is :
[[ 49 42 42 72]
 [137 106 98 184]
 [ 81 62 55 98]
 [131 102 95 178]]
```

In []: