

CORE111 Logical Problem Solving

Homework 1

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1 Elections

- (a) $p \vee q$: The election is decided or the votes have been counted
- (b) $\neg p \wedge q$: The election is not decided and the votes have been counted
- (c) $\neg q \vee (\neg p \wedge q)$: The votes have not been counted or the election is not decided and the votes have been counted

2 Think and Drive

- (a) $p \rightarrow \neg q$
- (b) $q \rightarrow p$
- (c) $\neg p \rightarrow \neg q$

3 Arguments

- (a) Converse: Whenever it is a sunny summer day I go to the beach.
Inverse: I do not go to the beach whenever it is not a sunny summer day.
Contra-positive: Whenever it is not a sunny summer day I do not go to the beach.
- (b) Converse: It is necessary that I sleep until noon when I stay up late.
Inverse: When I don't stay up late, it is not necessary that I sleep until noon.
Contra-positive: It is not necessary that I sleep until noon when i do not stay up late.

4 Formulas

Here is the truth table for $p \rightarrow q$.

p	q	$p \rightarrow q$
F	F	T
F	T	T
T	F	F
T	T	T

a) Neither

p	q	$p \leftrightarrow q$
T	T	T
T	F	F
F	T	F
F	F	T

b) Neither

p	q	$\neg q$	$p \wedge \neg q$
F	F	T	F
F	T	F	F
T	F	T	F
T	T	F	T

c) Neither

$(p \rightarrow q) \rightarrow p$	$((p \rightarrow q) \rightarrow p) \rightarrow p$
T	F
T	F
F	T
T	T

d) Tautology

p	q	$\neg p$	$\neg q$	$p \rightarrow q$	$\neg q \rightarrow \neg p$	$(p \rightarrow q) \rightarrow (\neg q \rightarrow \neg p)$
F	F	T	T	T	T	T
F	T	T	F	T	T	T
T	F	F	T	F	F	T
T	T	F	F	T	T	T

e) Contradiction

p	q	$\neg p$	$p \rightarrow q$	$p \wedge (p \rightarrow q)$	$(p \wedge (p \rightarrow q)) \wedge \neg p$
F	F	T	T	F	F
F	T	T	T	F	F
T	F	F	F	F	F
T	T	F	T	T	F