Assignment 1

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Download all python codes from

https://github.com/neharani289/ee14014/ Assignment1/codes

and latex-tikz codes from

https://github.com/neharani289/ee14014/ Assignment1

Q no. 46. what are the points on the y-axis whose distance from the line $(4 \ 3)x = 12$ is 4 units.

Solution:

Here the slope of the line is -4/3, thus the direction vectors of the lines are $\begin{pmatrix} 3 \\ -4 \end{pmatrix}$ finding the normal vector n,

$$n = \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix} \begin{pmatrix} 3 \\ -4 \end{pmatrix} \tag{0.0.1}$$

$$\implies n = \begin{pmatrix} 4 \\ 3 \end{pmatrix} \tag{0.0.2}$$

now distance between a given line which meet y-axis at point P1(0,4) and desired point P2(0,b) and P3(0,a) is at 4 units distance from the line is given by

$$d = \frac{(P1 - P2)^T n}{\|n\|} \tag{0.0.3}$$

$$\implies 4 = \frac{\binom{0}{(4-a)}^T \binom{4}{3}}{5} \implies 20 = 12 - 3a$$

$$(0.0.4)$$

$$a = -8/3 \tag{0.0.5}$$

similarly distance between given line and the desired point P3 can be calculated as:

$$d = \frac{(P3 - P1)^T n}{\|n\|} \tag{0.0.6}$$

$$\implies 4 = \frac{\binom{0}{(b-4)}^T \binom{4}{3}}{5} \tag{0.0.7}$$

$$20 = 3b - 12 \tag{0.0.8}$$

$$b = 32/3 \tag{0.0.9}$$

therefore points on y-axis at 4 units distance from line are (0,-8) and (0,32/3).