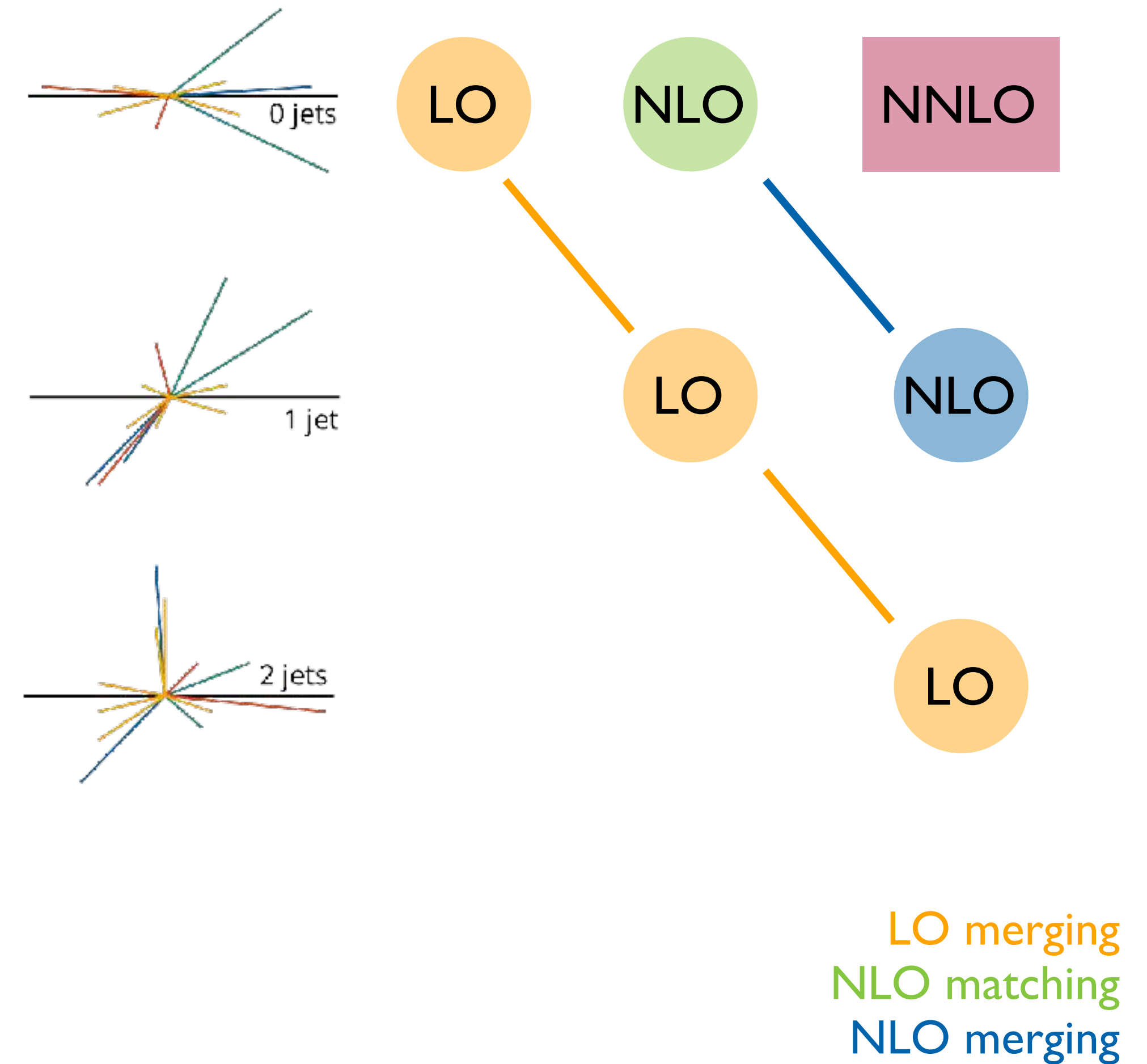


Matching & Merging

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At the
CTEQ/MCnet School 2021
Dresden/Online | 8 September 2021



Part I

Fixed Order Basics
NLO Matching

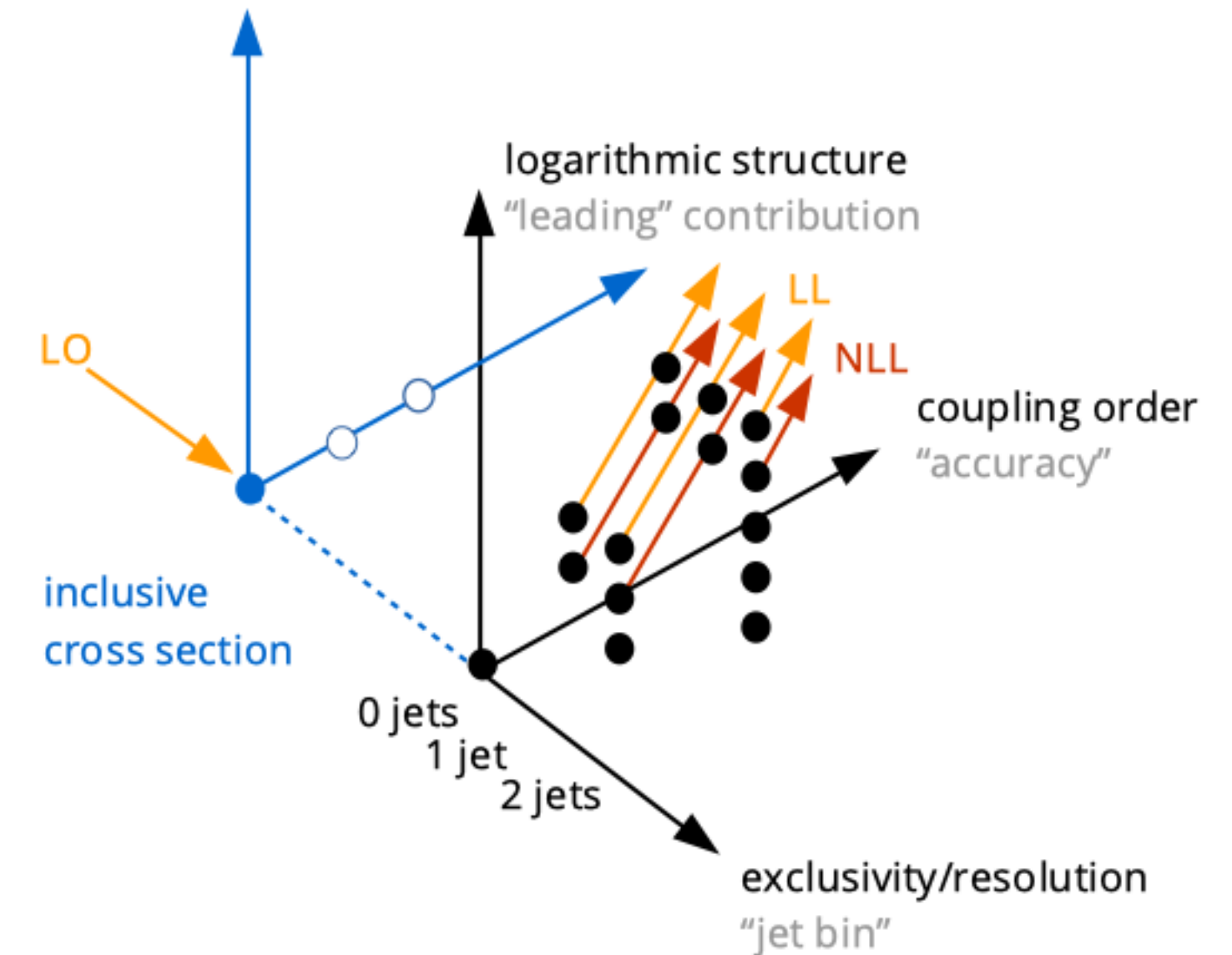
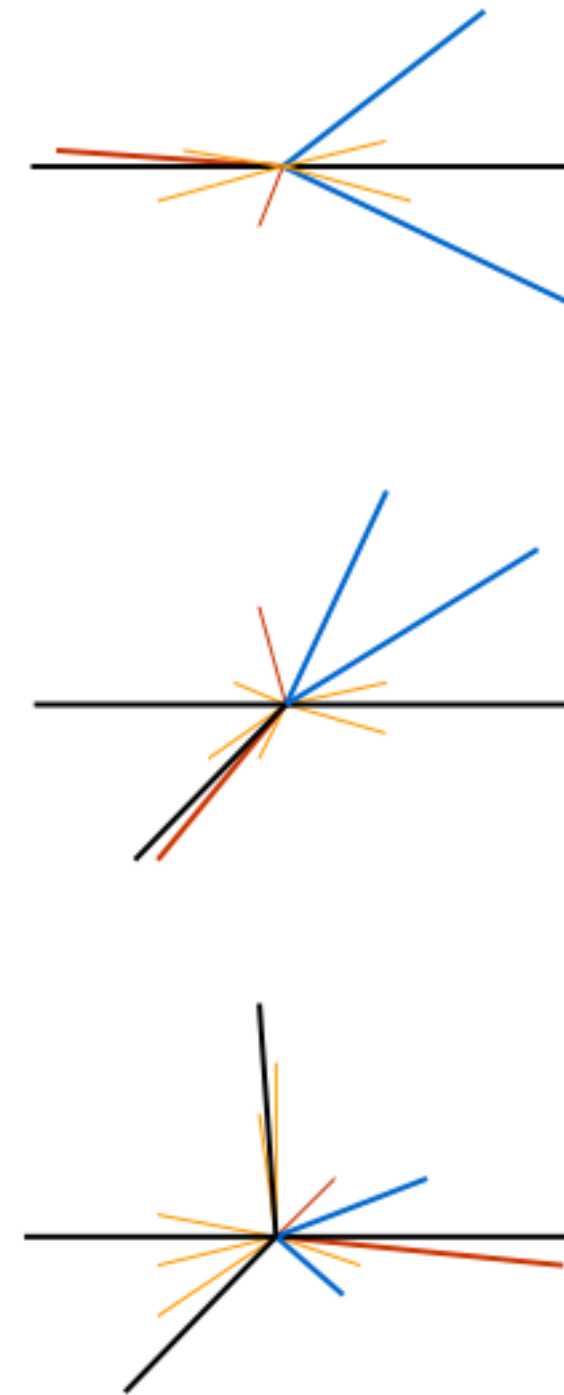
Part II

(N)LO Multijet Merging
Combination with NNLO
~~Outlook on shower development~~

Generalize matrix element corrections to higher multiplicities.

As for matrix element corrections, we cannot guarantee anything about the inclusive cross section.

Using pure matrix elements for the first hand full of hard emissions is generally problematic: efficiency, resonances, ...



$$d\sigma_{n+1}(\phi_{n+1}) \simeq d\sigma_n(\Phi_n(\phi_{n+1})) \times V(q,z,\phi_n) \left| \frac{\partial \Phi_{n+1}(q,z,\phi_n)}{\partial (q,z,\phi_n)} \right| dq dz$$

$$V \sim \frac{|M_{n+1}|^2}{|M_n|^2}$$

Starting Point: Multiple Shower Emissions

Distinguish between shower domain and matrix element domain for each parton multiplicity.

If phase space reachable by shower in matrix element domain, replace by exact cross section.

Otherwise keep shower.

$$d\mathcal{S}(\phi_n) PS_{q_0}[u(\phi_n)]$$

$$= d\mathcal{S}(\phi_n) \Delta_n(p/q_0) + d\mathcal{S}(\phi_n) P(\phi_n, q_1) \frac{d\phi_{n+1}}{d\phi_n} \Delta_n(q_1/q_0) PS[u(\phi_{n+1})]$$

$$= d\mathcal{S}(\phi_n) \Delta_n(p/q_0)$$

$$+ d\mathcal{S}(\phi_n) P(\phi_n, q_1) \frac{d\phi_{n+1}}{d\phi_n} \Delta_{n+1}(p/q_1) \Delta_n(q_1/q_0)$$

$$+ d\mathcal{S}(\phi_n) P(\phi_{n+1}, q_2) P(\phi_n, q_1) \frac{d\phi_{n+2}}{d\phi_n} \Delta_{n+1}(q_2/q_1) \Delta_n(q_1/q_0) PS[u(\phi_{n+2})]$$



$$d\mathcal{S}(\phi_n) P(\phi_n, q_1) \frac{d\phi_{n+1}}{d\phi_n} \longrightarrow d\sigma_{n+1}$$

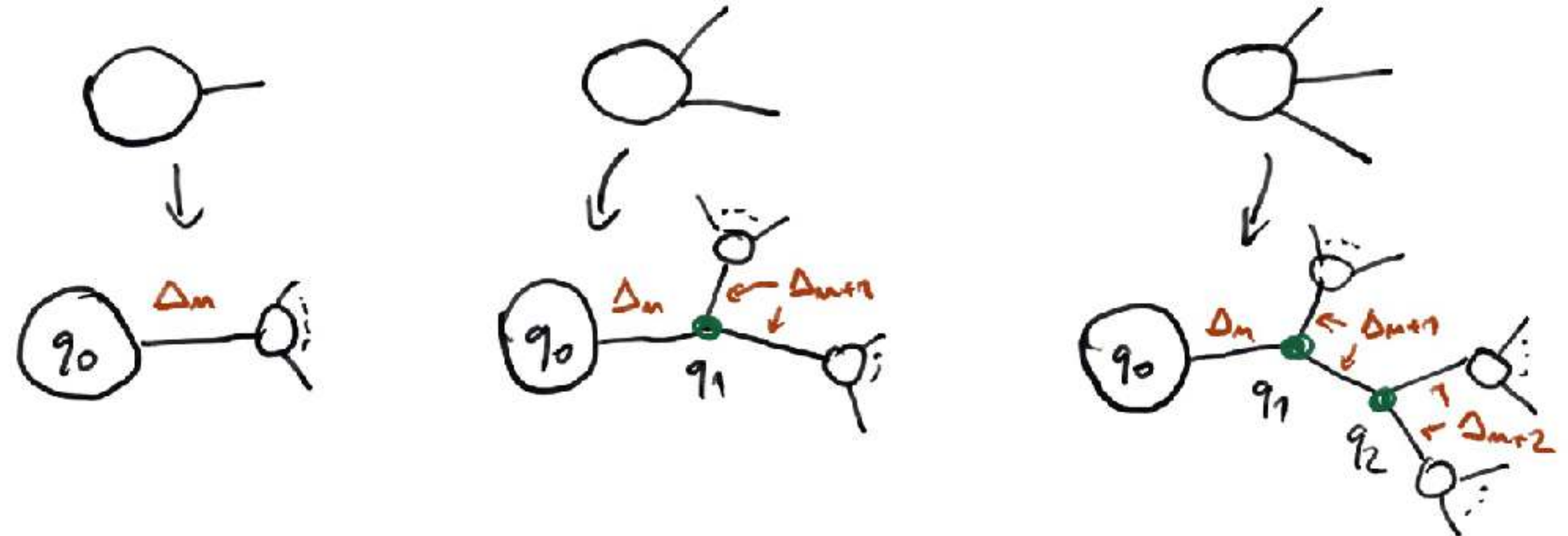
if $q_1 > \rho$

$$d\mathcal{S}(\phi_n) P(\phi_{n+1}, q_2) P(\phi_n, q_1) \frac{d\phi_{n+2}}{d\phi_n} \longrightarrow d\sigma_{n+2}$$

if $q_2 > \rho$

Reinterpret hard matrix elements in shower histories.

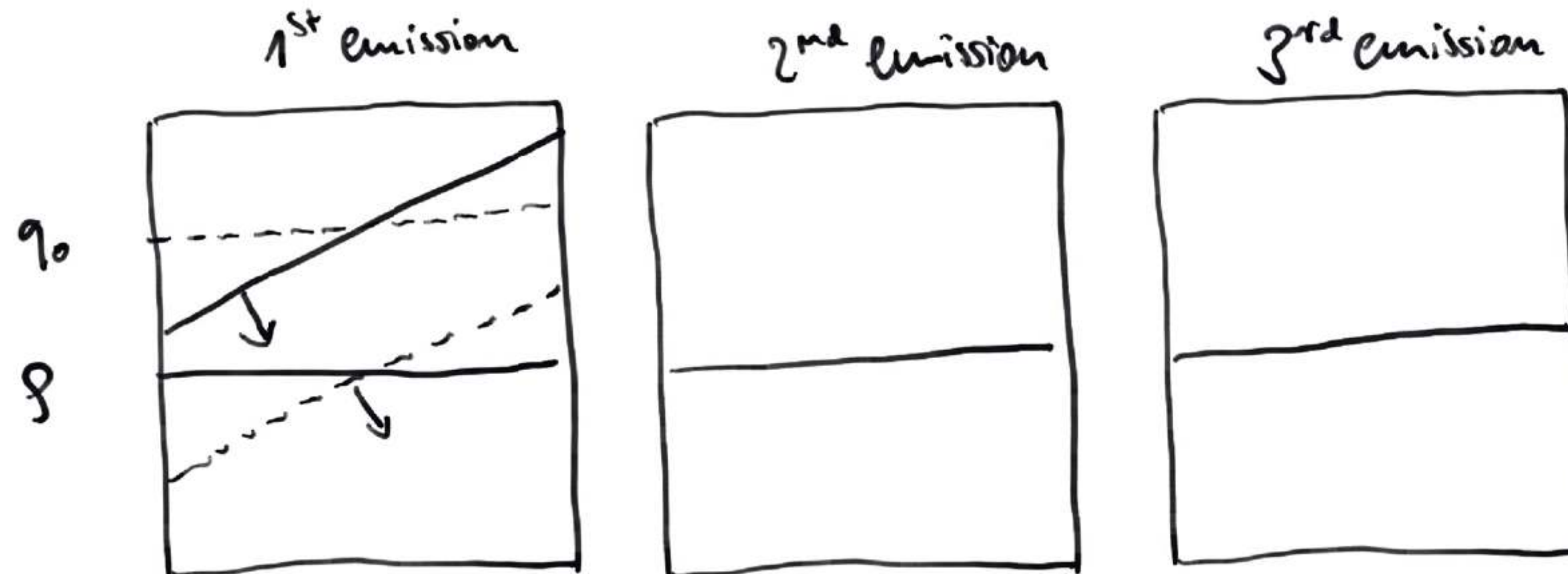
- Among the available histories select one with a particular weight.
- Reweight to account for the running coupling, and PDF in backward evolution.



The final step is to reweight by the Sudakov factors for each clustered line, and each hard parton down to the scale which separates matrix element from shower domain.

The first algorithms achieved this by numerical weights, newer versions do this by vetoed showers which automatically exponentiate the wanted contributions.

Ordering & Phase Space

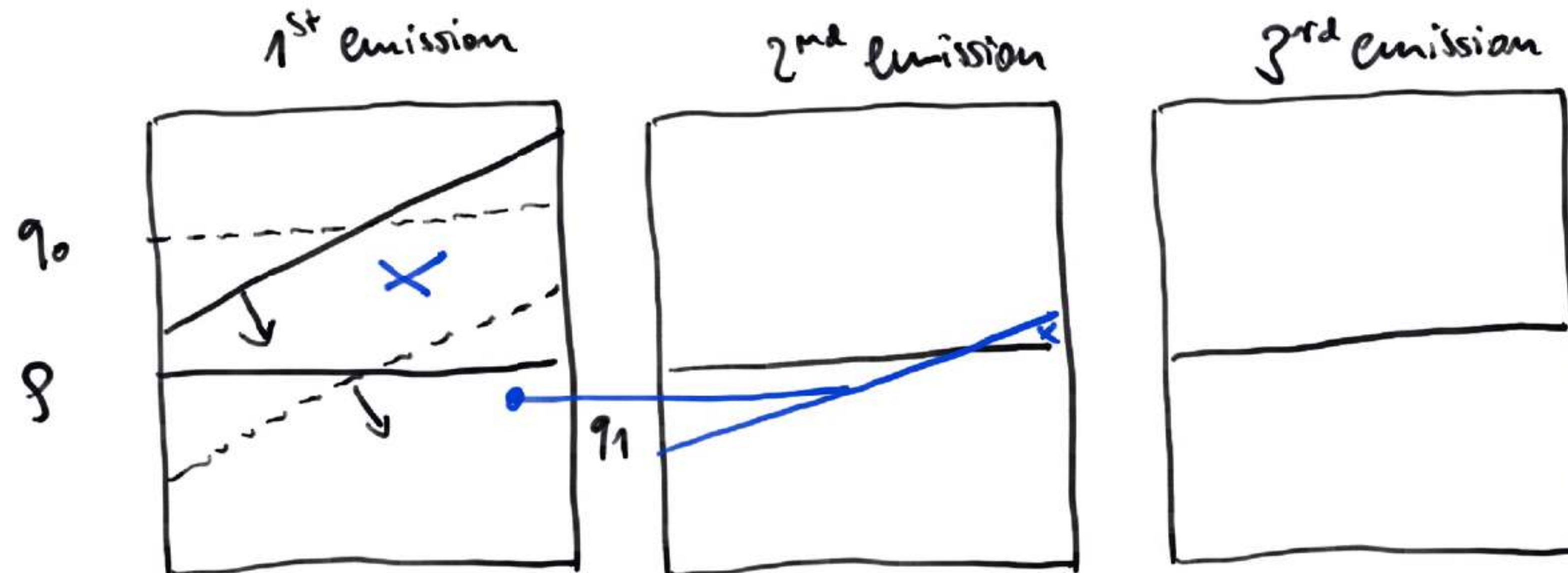


Mind differences in phase space boundaries.

Diagonal: Shower evolution boundary — horizontal: Matrix element boundary.

Not all phase space might be available to shower: add extra hard process.

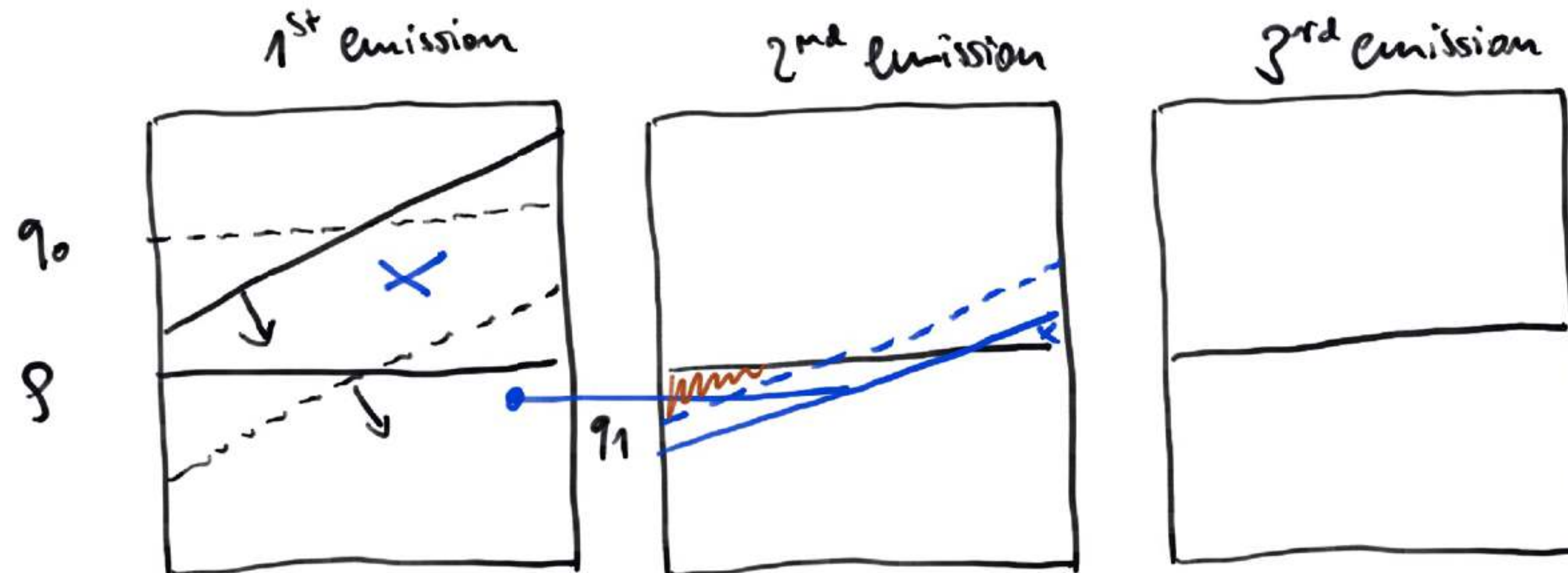
Ordering & Phase Space



Veto shower in matrix element region.

Naively starting at merging scale might leave out phase space.

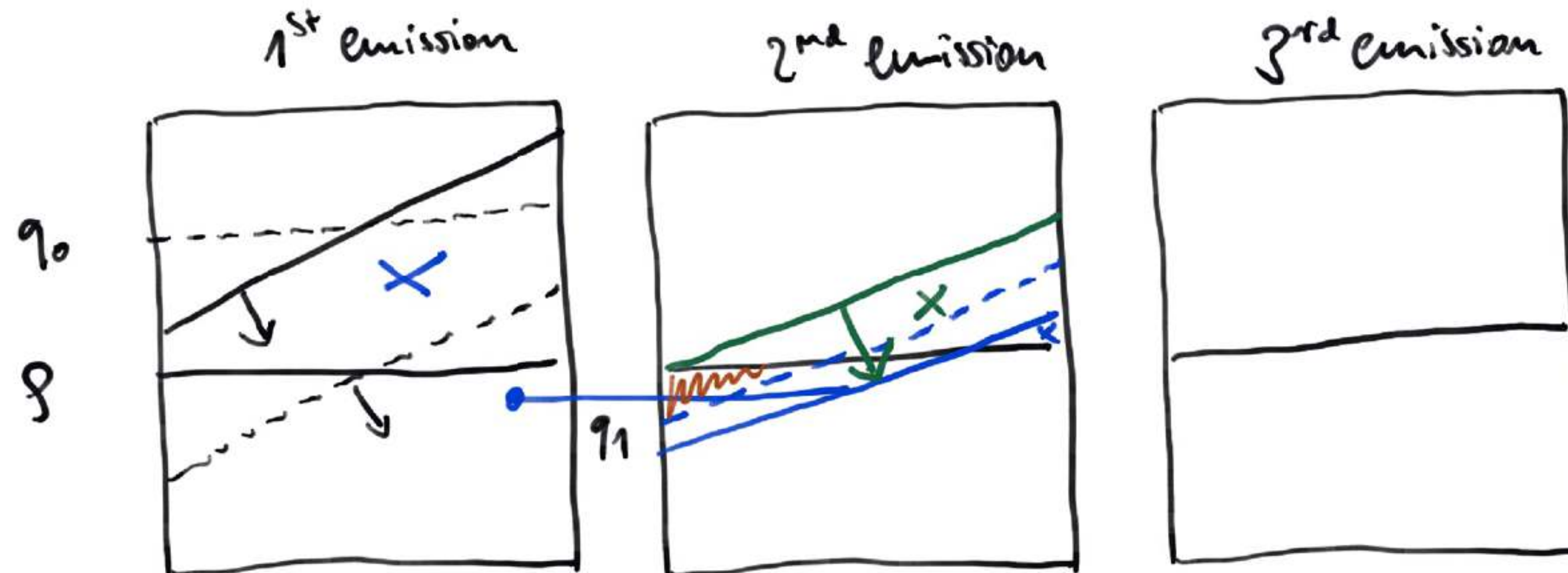
Ordering & Phase Space



Veto for secondary emissions.

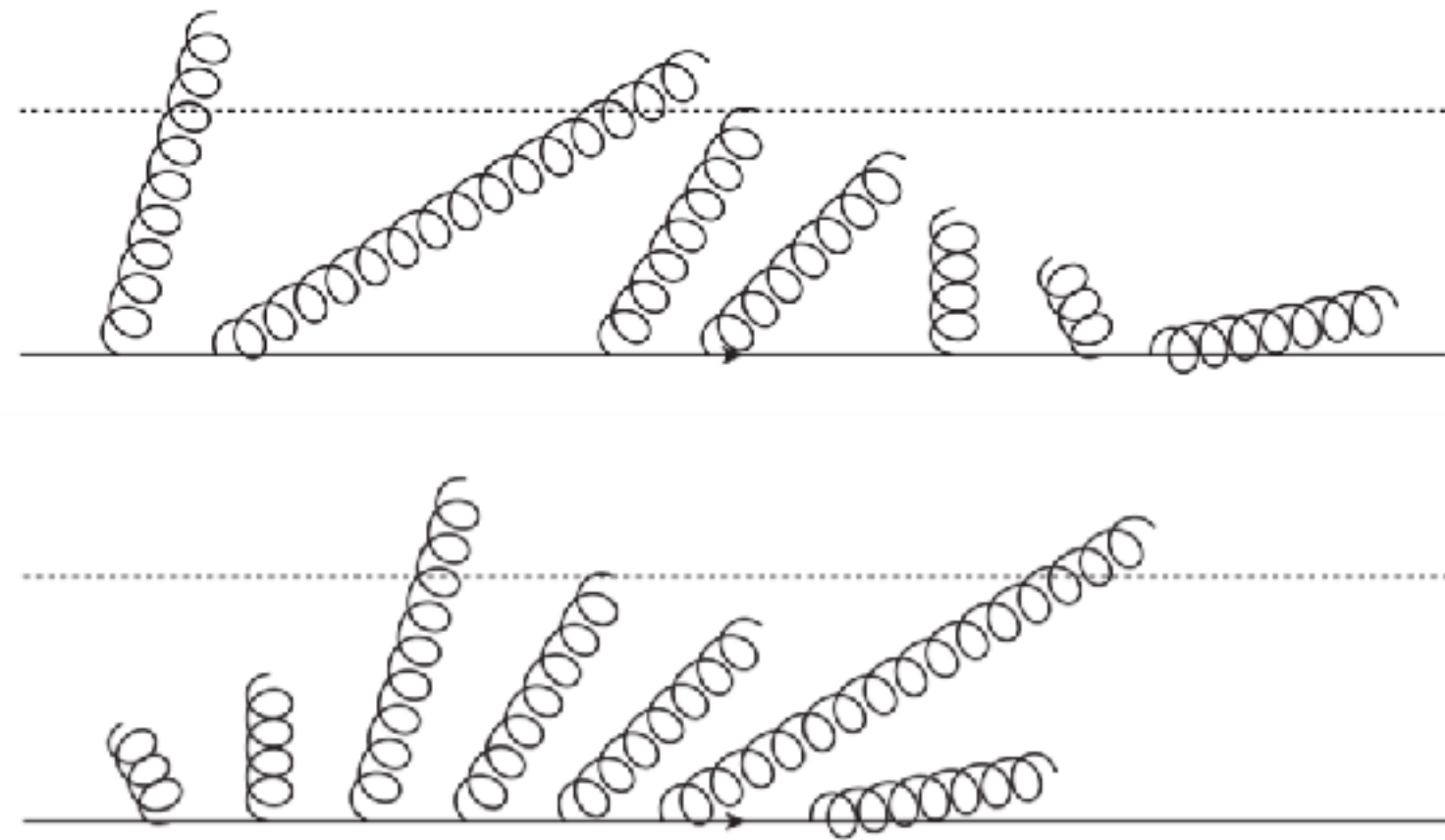
Incompatibility of resolutions might leave further holes in phase space.

Ordering & Phase Space

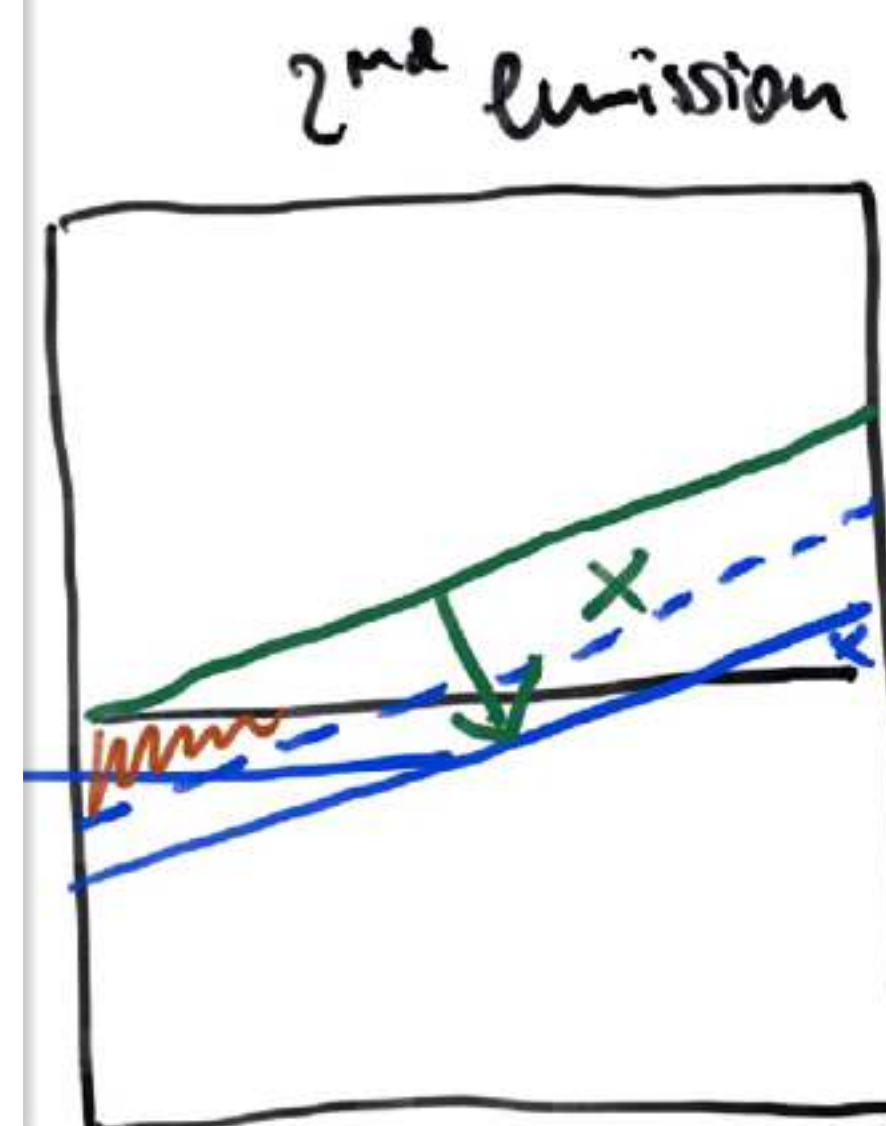


Add a truncated vetoed shower to account for mismatch.

Ordering & Phase Space

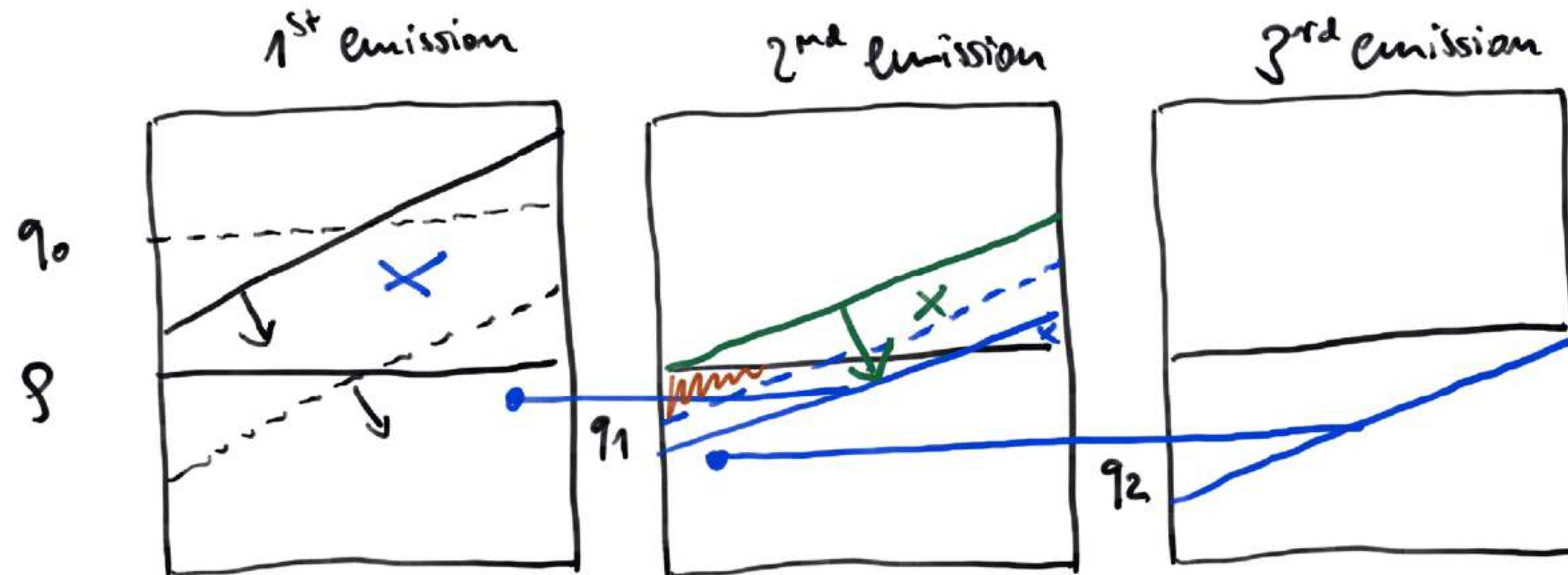


in the context of merging:
[Richardson, Hamilton, Tully]
[Höche, Krauss, Schumann, Siegert]



Add a truncated vetoed shower to account for mismatch.

Ordering & Phase Space



Continue normal showering if no further complications can happen.


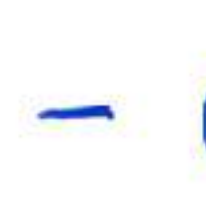
Inclusive & Exclusive Cross Sections

Cross sections generated by the shower:

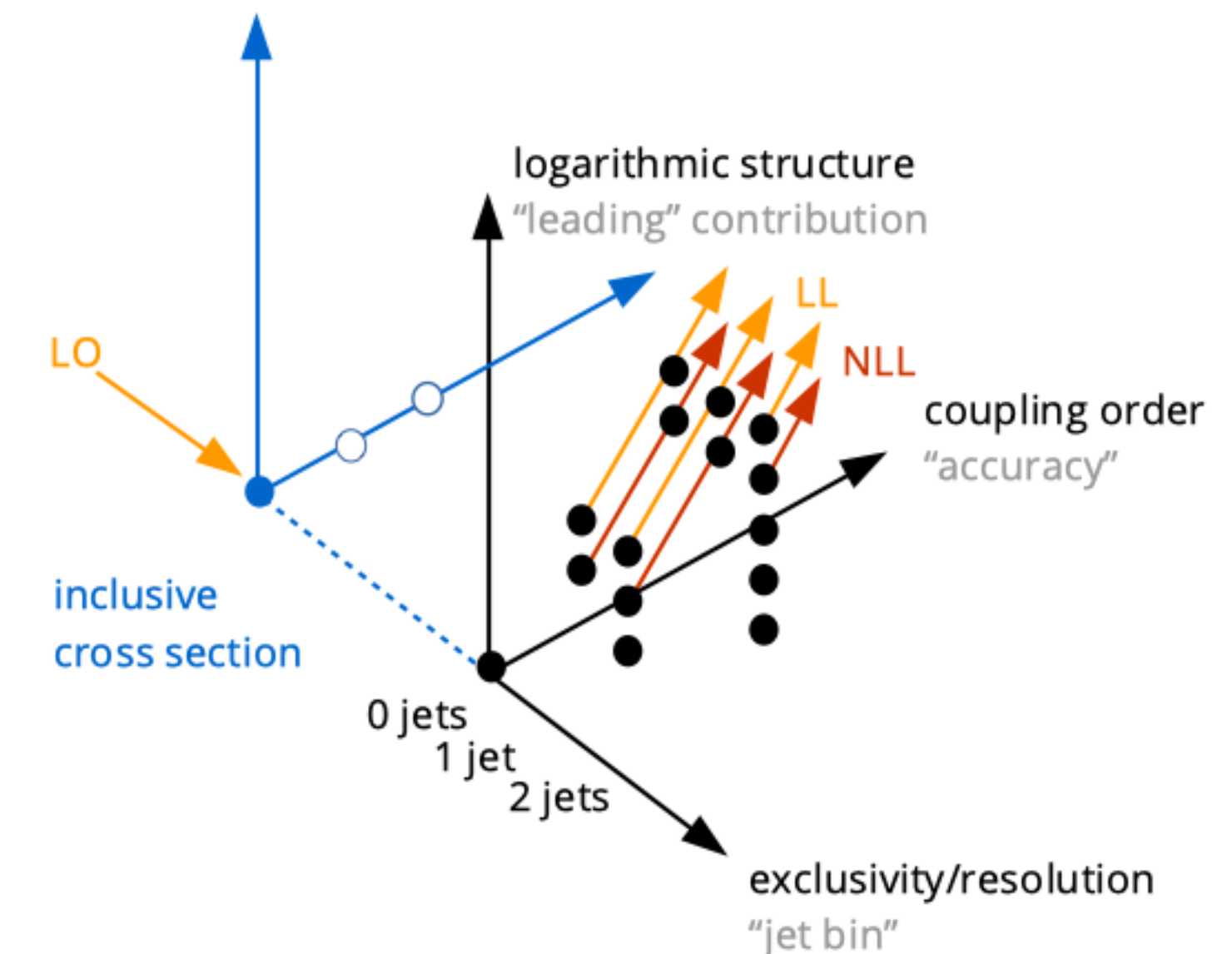
$$\begin{aligned} = n \text{ jets: } & d\sigma(\phi_0) \frac{d\phi_m}{d\phi_0} P(\phi_0, q_0) \dots P(\phi_m, q_m) \Delta_n(g|q_{m+1} \dots | q_0) \\ \geq n \text{ jets: } & d\sigma(\phi_0) \frac{d\phi_m}{d\phi_0} P(\phi_0, q_0) \dots P(\phi_m, q_m) \Delta_{n+1}(q_{m+1} \dots | q_0) \end{aligned}$$

Cross sections after merging:

$$\begin{aligned} = n : & d\sigma_n(\phi_n) \Delta_n(g|q_{n+1} \dots | q_0) \\ \geq n : & d\sigma_n(\phi_n) \Delta_{n+1}(q_{n+1} \dots | q_0) \\ & + \int_0^{q_m} dq_{m+1} \left(\frac{d\sigma(\phi_{m+1})}{dq_{m+1}} - \frac{d\phi_{m+1}}{d\phi_m dq_{m+1}} P(\phi_m, q_{m+1}) d\sigma(\phi_m) \right) \\ & \quad \times \Delta_n(q_{m+1} \dots | q_0) \end{aligned}$$

( - )

At tree level this is not logarithmically enhanced.



NLO matching condition:

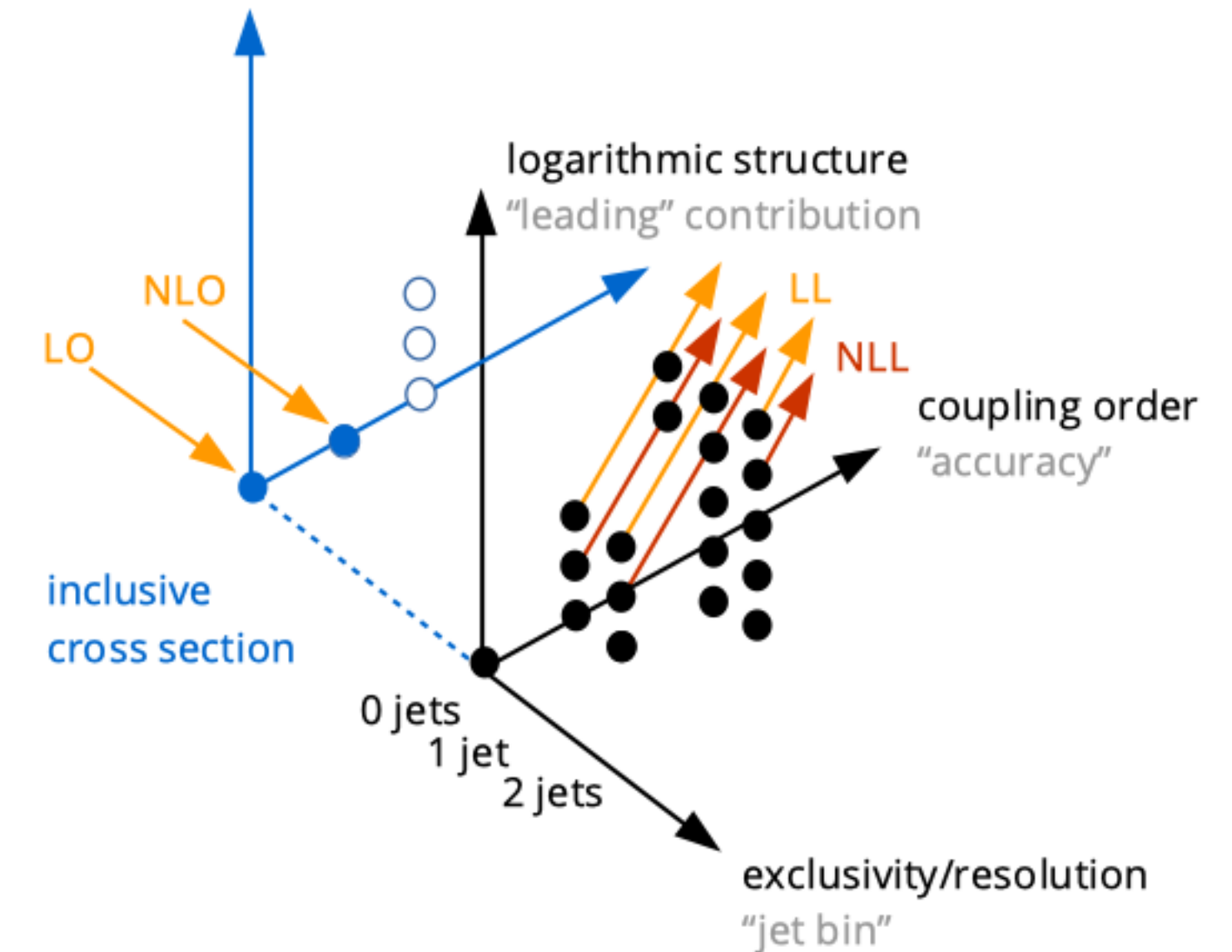
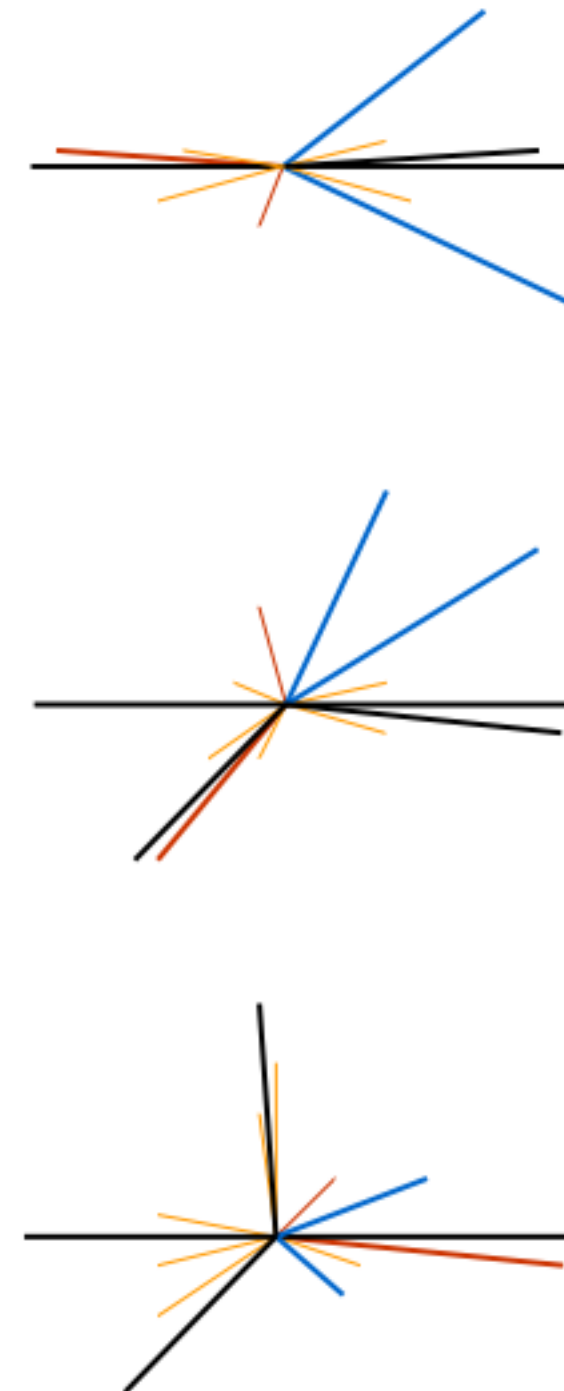
$$PS[d\sigma_{NLO}^{matched}] = d\sigma_{NLO} + \mathcal{O}(\alpha_s^{n+2})$$

$$\int PS[d\sigma_{NLO}^{matched}] = \sigma_{NLO}$$

$$d\sigma_{NLO}^{matched} = d\sigma_{NLO} - PS[d\sigma_{LO}]|_{\mathcal{O}(\alpha_s)}$$

Merging condition: Preserve exclusive cross sections in ME region

$$d\sigma_n(\phi_n) \Delta_n(g|q_{n1}, \dots, q_n)$$



Can we combine the two?

- Preserve exclusive cross sections in ME region up to NLO
- Possibly preserve cross sections in shower region up to NLO

Exclusive cross sections are now NLO accurate by virtue of the merging condition.

The mismatch in inclusive cross section is now disturbing: Logarithmic enhancement of difference is same parametric size as the NLO corrections for lowest jet multiplicity.

NLO cross section for n jets.

$$= n : d\sigma_n(\phi_n) \Delta_n(q_{n1} \dots q_n)$$

$$\geq n : d\sigma_n(\phi_n) \Delta_{n+1}(q_{n1} \dots q_n) + \int_0^{q_n} dq_{n+1} \left(\frac{d\sigma(\phi_{n+1})}{dq_{n+1}} - \frac{d\phi_{n+1}}{d\phi_n dq_{n+1}} P(\phi_n, q_{n+1}) d\sigma(\phi_n) \right) \times \Delta_n(q_{n+1} \dots q_n)$$

NLO cross section for n+1 jets.

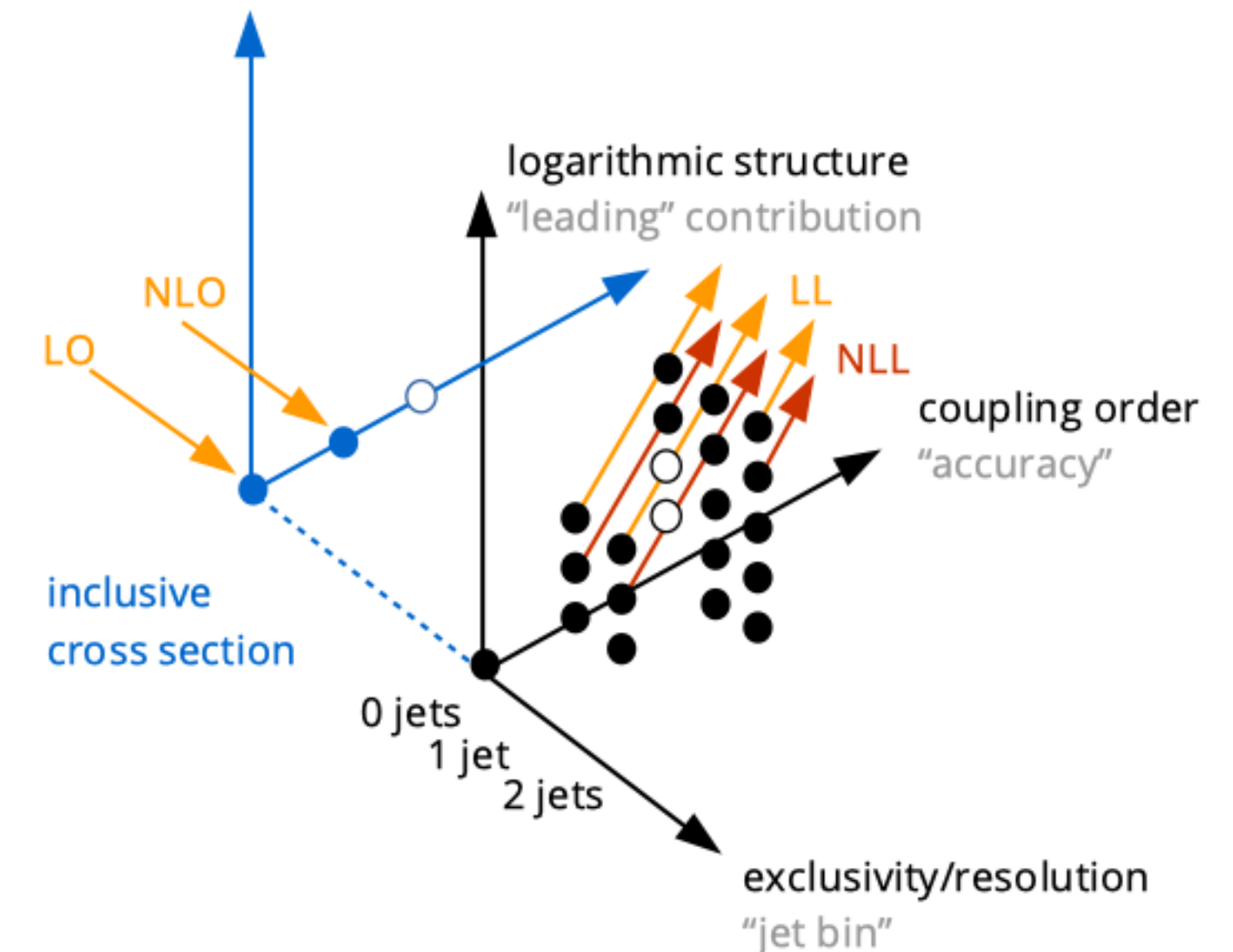
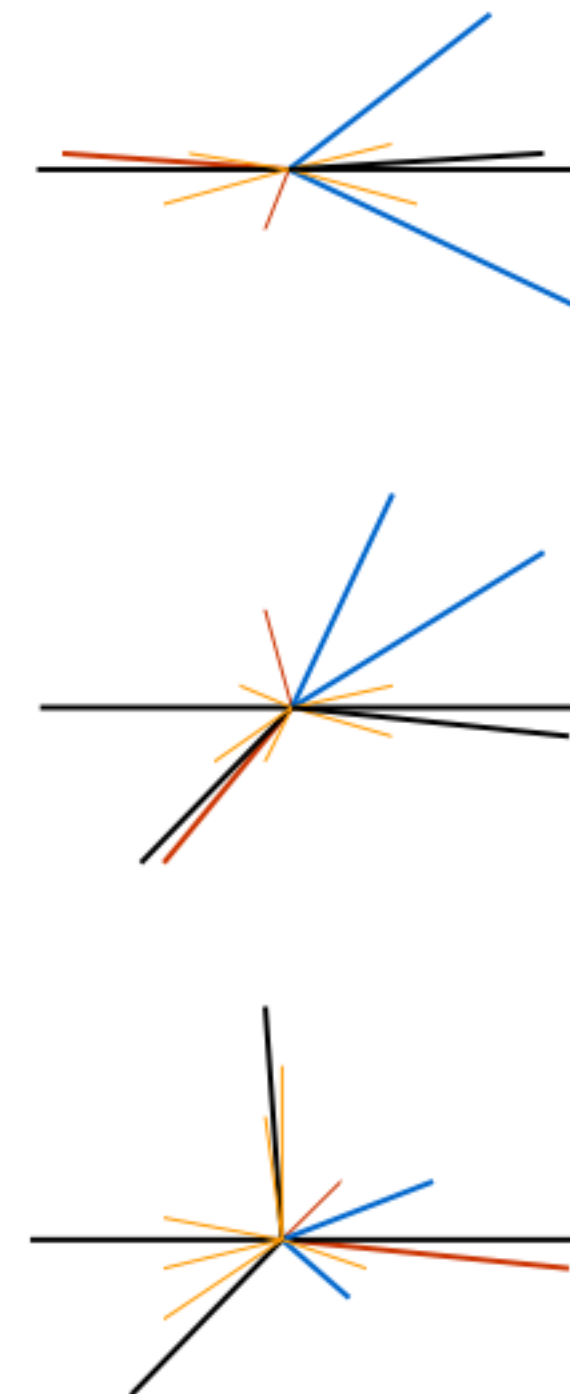
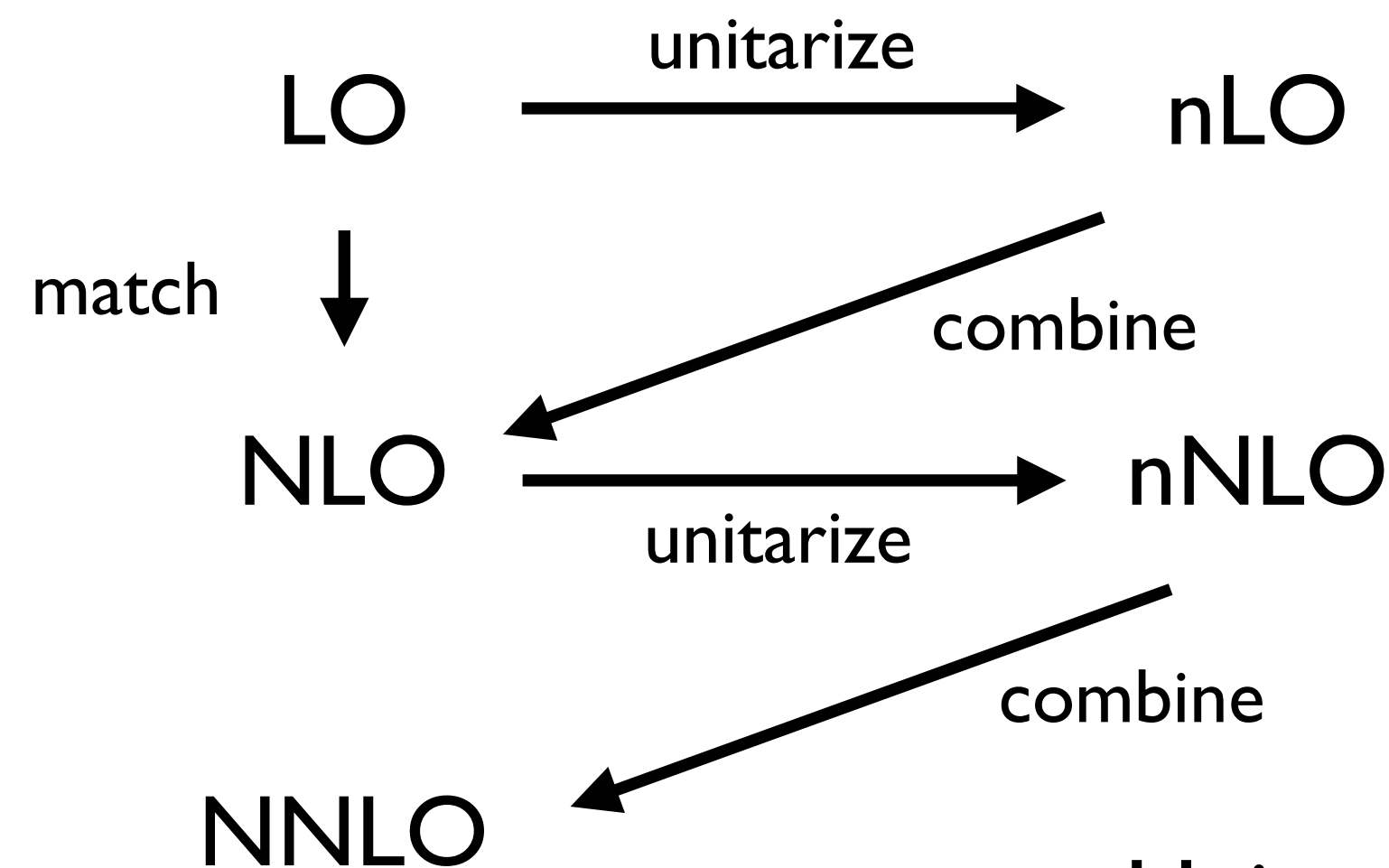
NLO cross section for n jets times tree level splitting function.

At this level we could subtract this effect from the lower jet multiplicity and enforce to preserve *inclusive* cross sections.

Combination with NNLO

A higher order shower evolution would not have suffered from the problem above.

We could also have used such a shower to truly match to NNLO, which would have contained NLO for the zero and first jet bin.



Unitarization well suited for combination with NNLO.
Similar considerations underpin the MiNNLO method.

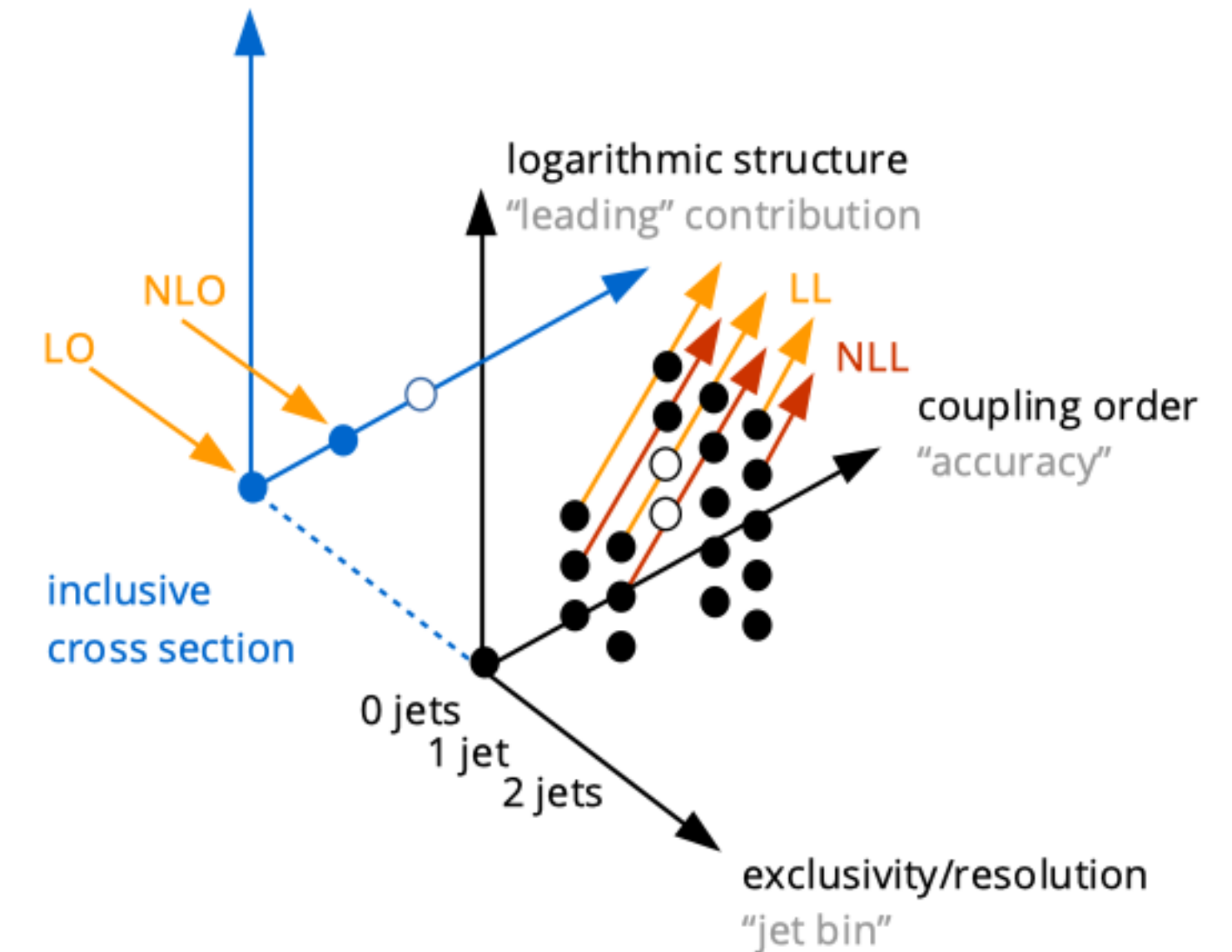
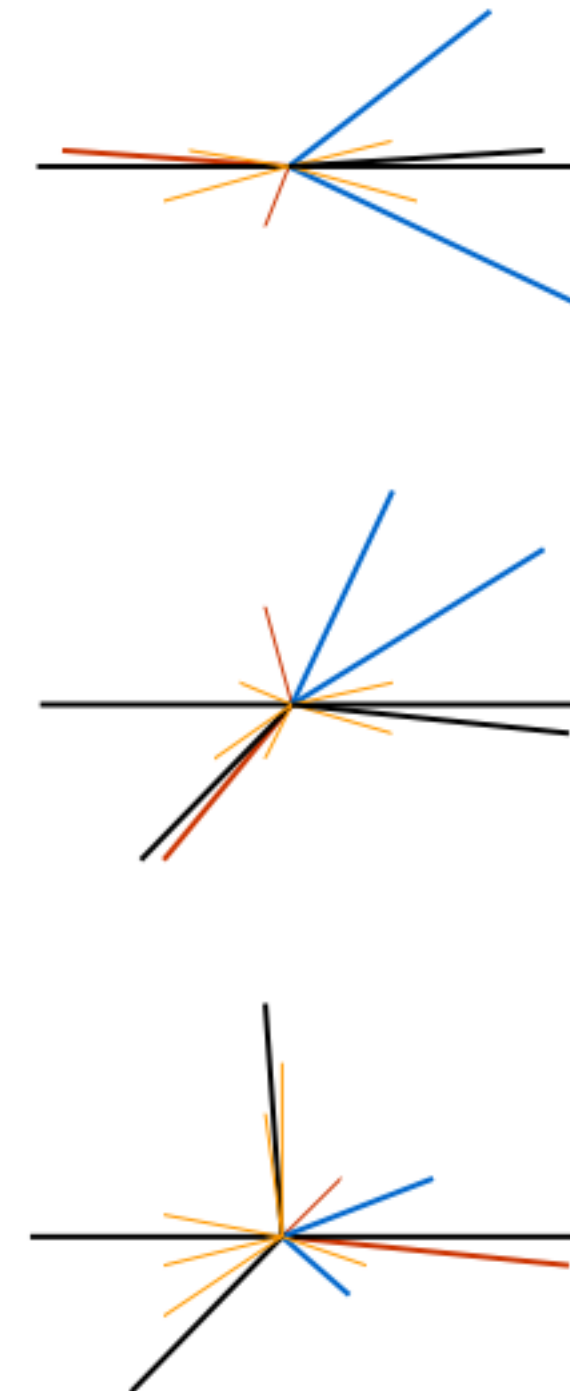
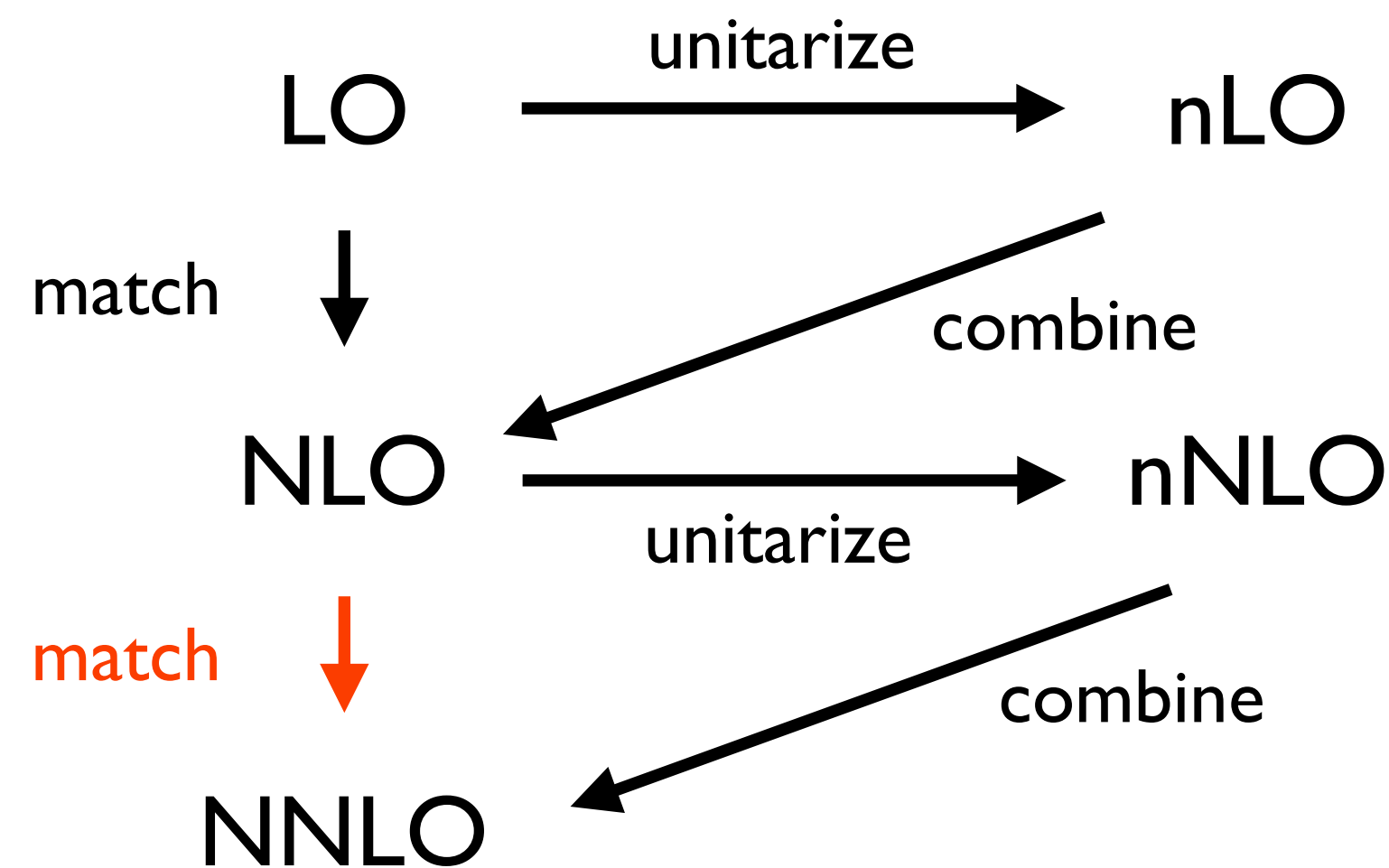
[Höche, Prestel]

[Hamilton, Nason, Zanderighi ...]

Combination with NNLO

A higher order shower evolution would not have suffered from the problem above.

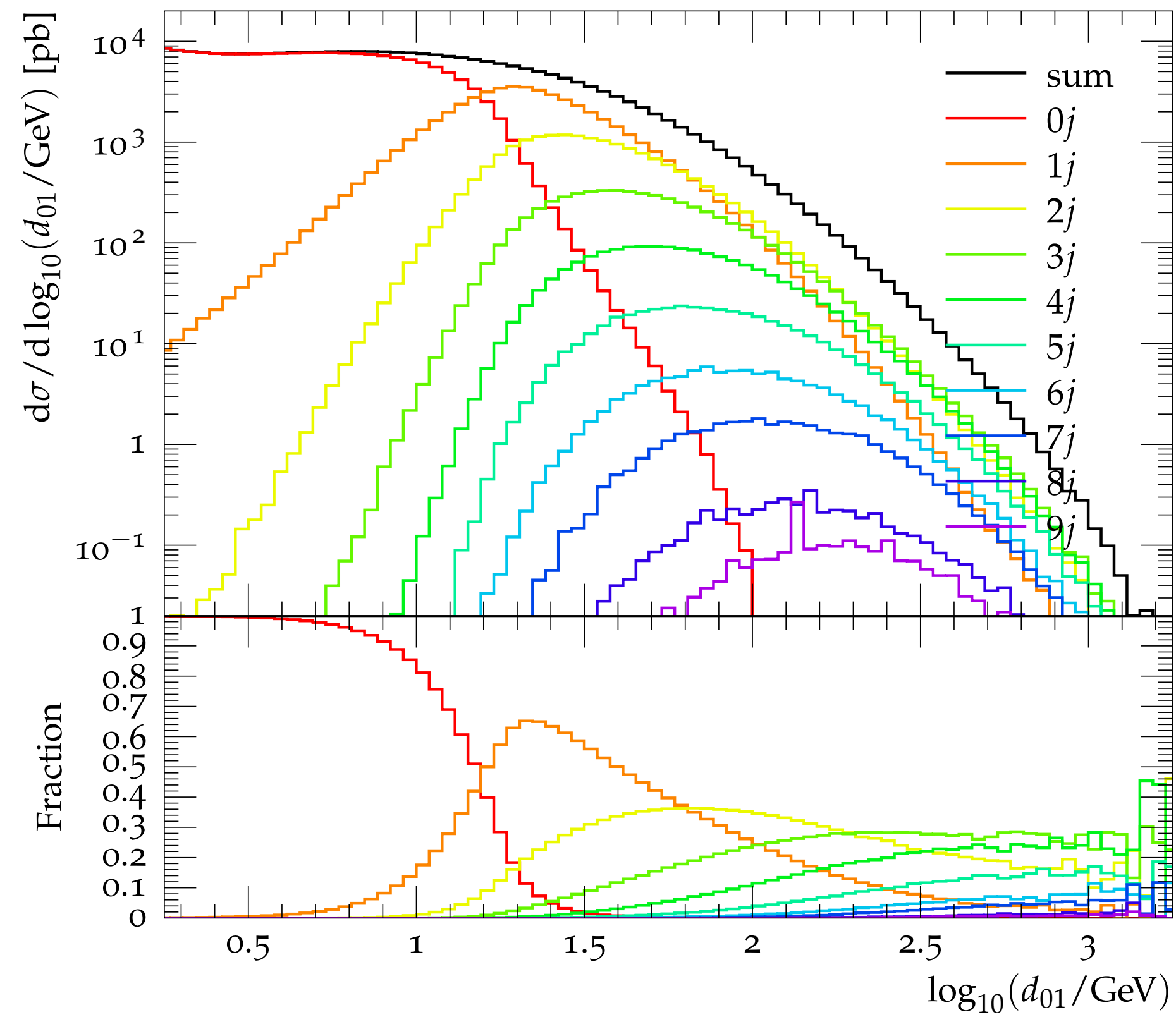
We could also have used such a shower to truly match to NNLO, which would have contained NLO for the zero and first jet bin.



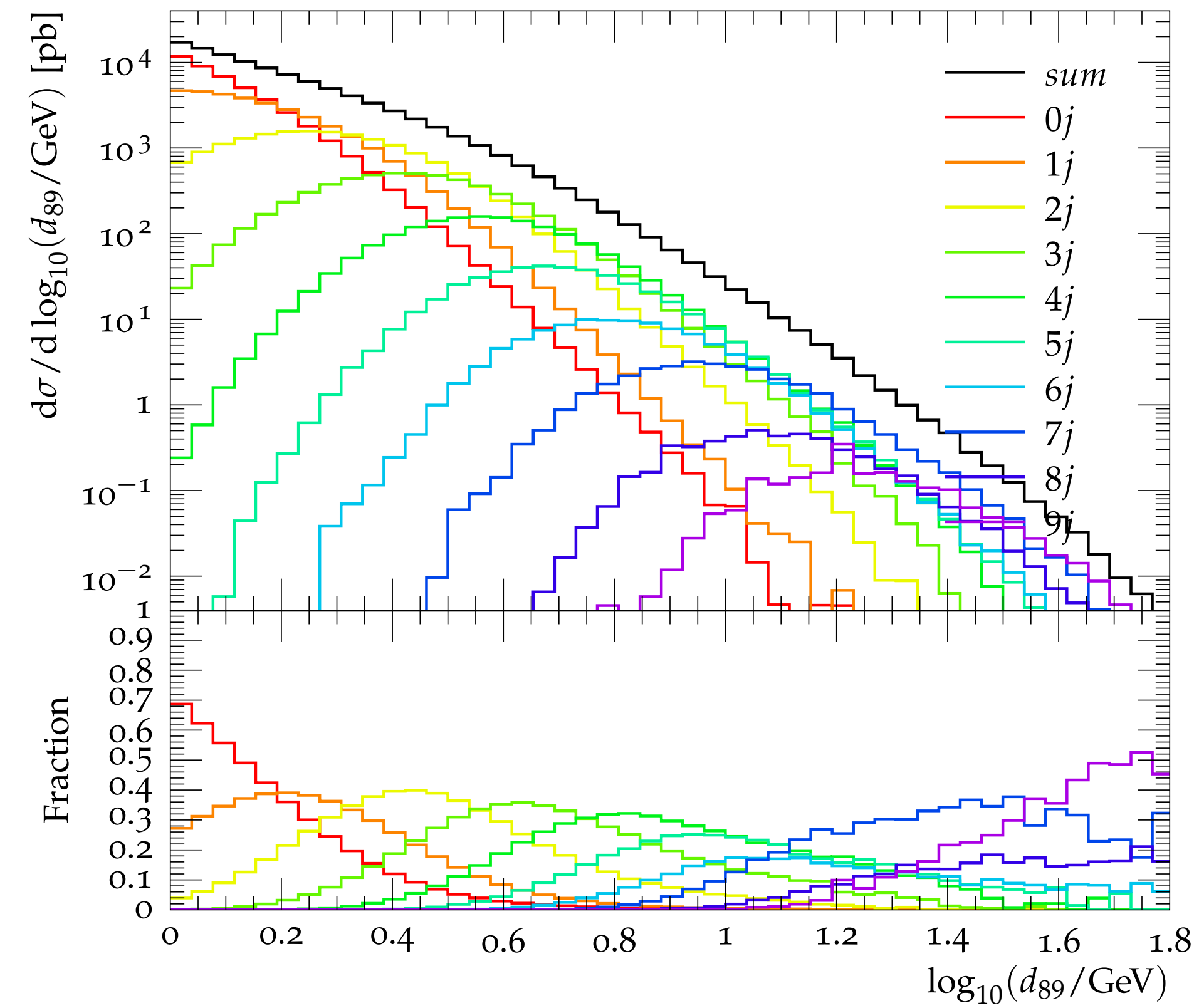
Matching to NNLO is more desirable, and requires **better parton showers**.

Examples

Differential 0 \rightarrow 1 jet resolution in W^+ +jets



Differential 8 \rightarrow 9 jet resolution in W^+ +jets



Multi-purpose Event Generators



Current release series	Hard matrix elements	Shower algorithms	NLO Matching	Multijet merging	MPI	Hadronization	Shower variations
Herwig 7	Internal, libraries, event files	QTilde, Dipoles	Internally automated	Internally automated	Eikonal	Clusters, (Strings)	Yes
Pythia 8	Internal, event files	Pt ordered, DIRE, VINCIA	External	Internal, ME via event files	Interleaved	Strings	Yes
Sherpa 2	Internal, libraries	CSShower, DIRE	Internally automated	Internally automated	Eikonal	Clusters, Strings	Yes



All now offer unitarized merging.

Thank you!

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