

2019-20

## İSTANBUL OKAN ÜNİVERSİTESI MÜHENDİSLİK FAKÜLTESI MÜHENDİSLİK TEMEL BİLİMLERİ BÖLÜMÜ

MATH216 Mathematics IV - Exercise Sheet 8

N. Course

Exercise 30 (Systems of Linear Equations). Find the general solutions to the following systems of ODEs:

(a) 
$$\mathbf{x}' = \begin{bmatrix} 1 & 2 \\ 2 & 1 \end{bmatrix} \mathbf{x}$$

(b) 
$$\mathbf{x}' = \begin{bmatrix} -3 & 2 \\ -3 & 4 \end{bmatrix} \mathbf{x}$$

(c) 
$$\mathbf{x}' = \begin{bmatrix} 3 & -1 \\ 5 & -3 \end{bmatrix} \mathbf{x}$$
.

(d) 
$$\begin{cases} x' = 4x - y \\ y' = x + 2y \end{cases}$$

(e) 
$$\begin{cases} x' = 3x - y \\ y' = 4x - y \end{cases}$$

(f) 
$$\begin{cases} x' = 5x + 4y \\ y' = -x + y \end{cases}$$

(g) 
$$\begin{cases} x' = 3x + 2y \\ y' = -5x + y \end{cases}$$

(h) 
$$\begin{cases} x' = x - 4y \\ y' = x + y \end{cases}$$

(i) 
$$\begin{cases} x' = x - 3y \\ y' = 3x + y \end{cases}$$

(j) 
$$\begin{cases} x' = 4x - 2y \\ y' = 5x + 2y \end{cases}$$

(k) 
$$\begin{cases} x' = x + y - z \\ y' = 2x + 3y - 4z \\ z' = 4x + y - 4z \end{cases}$$

(1) 
$$\begin{cases} x' = x - y - z \\ y' = x + 3y + z \\ z' = -3x + y - z \end{cases}$$

$$(x') = -3x + y - z$$

$$(m) \begin{cases} x' = 3x + y + z \\ y' = 3y + z \\ z' = 6z \end{cases}$$

(n) 
$$\begin{cases} x' = 2x + y - z \\ y' = -4x - 3y - z \\ z' = 4x + 4y + 2z \end{cases}$$

Exercise 31 (Initial Value Problems). Solve the following IVPs:

(a) 
$$\begin{cases} \mathbf{x}' = \begin{bmatrix} 3 & 4 \\ 3 & 2 \end{bmatrix} \mathbf{x} \\ \mathbf{x}(0) = \begin{bmatrix} 1 \\ 1 \end{bmatrix} \end{cases}$$

(b) 
$$\begin{cases} \mathbf{x}' = \begin{bmatrix} 4 & -3 \\ 6 & -7 \end{bmatrix} \mathbf{x} \\ \mathbf{x}(0) = \begin{bmatrix} 8 \\ 0 \end{bmatrix} \end{cases}$$

(c) 
$$\begin{cases} x' = 3x + z \\ y' = 9x - y + 2z \\ z' = -9x + 4y - z \\ x(0) = 0 \\ y(0) = 0 \\ z(0) = 17 \end{cases}$$