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Abstract—This manual is an introduction to control systems based on GATE problems.Links to sample Python codes are available in the text.

Download python codes using

1 STABILITY

2 ROUTH HURWITZ CRITERION

- 3 Compensators
- 4 NYQUIST PLOT
- 5 FEEDBACK SYSTEMS
- 5.0.1. The non-inverting op-amp configuration shown in fig.5.0.1 provides direct implementation of feedback loop. Assuming operational amplifier has infinite input resistance and zero output resitance. Find the expression for feedback factor. **Solution:** Let the gain of the operational

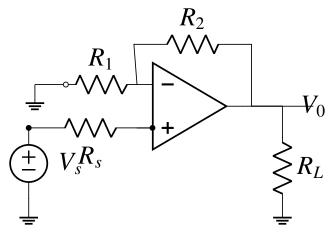


Fig. 5.0.1

amplifier be G. The equivalent circuit of the amplifier is in fig.5.0.1 From the equivalent circuit, Applying Ohms law,

$$V_0 = G(V_i) (5.0.1.1)$$

and,
$$V_i = V_+ - V_-$$
 (5.0.1.2)

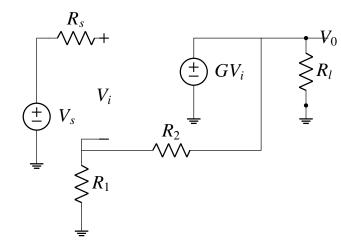


Fig. 5.0.1

Now, Applying voltage dividing rule

$$V_{-} = \left[\frac{R_1}{R_1 + R_2} \right] V_0 \tag{5.0.1.3}$$

Substituting in equ.5.0.1.1

$$V_0 = G(V_+ - \left[\frac{R_1}{R_1 + R_2}\right] V_0) \quad (5.0.1.4)$$

$$\implies V_0 = GV_+ - G\left[\frac{R_1}{R_1 + R_2}\right] V_0 \quad (5.0.1.5)$$

$$G(V_{+}) = V_{0} + G \left[\frac{R_{1}}{R_{1} + R_{2}} \right] V_{0}$$
 (5.0.1.6)

But.

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$$V_{\rm s} = V_{+}$$
 (5.0.1.7)

because, no current flows through resistor,Rs Since,input resistance is given infinite in fig.5.0.1 The equation can be written as...,

$$V_0 = G \left[\frac{1}{1 + \frac{GR_1}{R_1 + R_2}} \right] V_s \qquad (5.0.1.8)$$

Gain =
$$\frac{V_0}{V_s} = \left[\frac{G}{1 + \frac{GR_1}{R_1 + R_2}} \right]$$
 (5.0.1.9)

For a negative feedback system,

$$\frac{V_0}{V_i} = \frac{G}{1 + GH} \quad (5.0.1.10)$$

where.,
$$H = \frac{R_1}{R_1 + R_2}$$
 (5.0.1.11)

The equation.5.0.1.1 looks exactly similar to the Gain of a negative feedback system with

• Open loop gain = G

- Loop gain = P
- Amount of feedback = F
- Feedback factor = f
- closed loop gain = T

where

$$G = G (5.0.1.12)$$

$$P = GH = G\frac{R_1}{R_1 + R_2} \tag{5.0.1.13}$$

$$P = GH = G\frac{R_1}{R_1 + R_2}$$
 (5.0.1.13)
$$F = 1 + GH = 1 + \frac{GR_1}{R_1 + R_2}$$
 (5.0.1.14)

$$f = H = \frac{R_1}{R_1 + R_2} \tag{5.0.1.15}$$

Therefore, This operational amplifier can be modelled as a negative feedback system shown in the fig.5.0.1 So, the feedback factor f..,

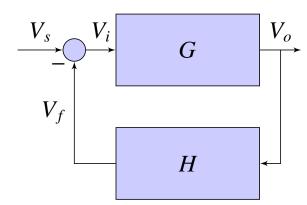


Fig. 5.0.1

$$f = H = \frac{R_1}{R_1 + R_2} \tag{5.0.1.16}$$

5.0.2. Find the condition under which closed loop gain T is almost entirely determined by the feedback network. Solution: For T to entirely 5.0.4. What is the amount of feedback in decibels? dependent on feedback network, it should be independent on G(open loop gain) T is given by...,

$$T = \frac{G}{1 + \frac{GR_1}{R_1 + R_2}} \tag{5.0.2.1}$$

(5.0.2.2)

For T to be independent on G.,

$$GH >> 1$$
 (5.0.2.3)

$$G\frac{R_1}{R_1 + R_2} >> 1 (5.0.2.4)$$

$$G >> 1 + \frac{R_2}{R_1} \tag{5.0.2.5}$$

Under such condition...

$$T = \frac{1}{H} \tag{5.0.2.6}$$

$$T = \frac{R_1 + R_2}{R_1} \tag{5.0.2.7}$$

$$T = 1 + \frac{R_2}{R_1} \tag{5.0.2.8}$$

so, the necessary condition for Af depend only on feedback network is

$$G >> T$$
 (5.0.2.9)

5.0.3. If the open loop voltage gain

$$G = 10^4 \tag{5.0.3.1}$$

Find the ratio of R2 and R1 to obtain a closed loop gain of 10. **Solution:** The closed loop gain gain T is given by

$$T = \frac{G}{1 + GH} = \frac{G}{1 + \frac{GR_1}{R_1 + R_2}} = 10$$

(5.0.3.2)

where..,
$$G = 10^4$$
 (5.0.3.3)

$$10 = \frac{10^4}{1 + \frac{10^4}{1 + \frac{R_2}{p_-^2}}} \tag{5.0.3.4}$$

$$\implies 1 + \frac{R_2}{R_1} = \frac{10^4}{\frac{10^4}{10} - 1} \tag{5.0.3.5}$$

$$1 + \frac{R_2}{R_1} = 10.010 \tag{5.0.3.6}$$

$$\frac{R_2}{R_1} = 9.010 \tag{5.0.3.7}$$

Solution: The value of F in decibals is given by

$$F(dB) = 20log(F) (5.0.4.1)$$

where...,
$$F = 1 + GH$$
 (5.0.4.2)

$$F = \frac{G}{T} \tag{5.0.4.3}$$

where..,
$$G = 10^4$$
 (5.0.4.4)

$$T = 10 (5.0.4.5)$$

$$F(dB) = 20log(\frac{10^4}{10}) = 20log(1000)$$
(5.0.4.6)

$$F(dB) = 60dB (5.0.4.7)$$

5.0.5. If G decreases by 20%, what is the corresponding decrease in T? Solution: Given

$$G = 10^4 \tag{5.0.5.1}$$

If G decrease by 20% then, the value of G is..,

$$G = (1 - 0.2)10^4 (5.0.5.2)$$

$$= 8000$$
 (5.0.5.3)

For this value of G and,

$$\frac{R_2}{R_1} = 9.010 \tag{5.0.5.4}$$

The value of T can be solved as follows,

$$T = \frac{G}{1 + \frac{G}{1 + \frac{R_2}{R_1}}}$$

$$T = \frac{8000}{1 + \frac{8000}{1 + 0.9010}}$$
(5.0.5.6)

$$T = \frac{8000}{1 + \frac{8000}{1 + 0.00010}} \tag{5.0.5.6}$$

$$T = 9.99749 \tag{5.0.5.7}$$

The percentage change in T is..,

$$fractional change = \frac{10 - 9.99749}{10} \quad (5.0.5.8)$$

$$= 2.51x10^{-4} (5.0.5.9)$$

$$%changeinT = 0.00251$$
 (5.0.5.10)

Therefore T decreases by 0.0025% when G decreases by 20%