# Mathematics Knowledge Base

#### neilfvhv

November 5, 2016

### 1 Number Theory

#### 1.1 Fundamental theorem of arithmetic

Any integer a > 1 can be factored in a unique way as

$$a = p_1^{a_1} \times p_2^{a_2} \times \dots \times p_t^{a_t}$$

where  $p_1 < p_2 < \ldots < p_t$  are prime numbers and where each  $a_i$  is a positive integer.

#### 1.2 Euler's function

For any integer n > 1:

$$n = p_1^{a_1} \times p_2^{a_2} \times \dots \times p_t^{a_t}$$

$$\phi(n) = ((p_1 - 1) \times p_1^{a_1 - 1}) \times (p_1 - 1) \times ((p_2 - 1) \times p_2^{a_2 - 1}) \times \dots \times ((p_t - 1) \times p_t^{a_t - 1})$$

## 2 Complex Analysis

#### 2.1 Euler's formula

For any real number x:

$$e^{ix} = \cos x + i\sin x$$

where e is the base of the natural logarithm, i is the imaginary unit.