

Assignment - 6

Q:1

Given a decision tree you have the option of (a) Converting the decision tree to rules and then pruning the resulting rules, or (b) pruning the decision tree then converting pruned tree to rules. What advantage does (a) have over (b)?

=> With method (b) we would prune subtree of decision tree by removing the subtree completely.

=> However, with method (a) pruning a rule may remove any precondition of it which is less restrictive than method (b).

Q:2

Elaborate the steps of ID₃ algorithm for generating decision trees.

=> ID₃ stands for 'Iterative Dichotomiser 3'.

=> ID₃ uses a top-down greedy approach to build a decision tree.

=> Most generally ID₃ is only used for classification problems with nominal features only.

=> ID₃ uses information gain as its attribute selection measure.

=> Let Node N represent or hold the tuples of partition D .

=> The attribute with the highest information gain is

choose as the splitting attribute for node N .

\Rightarrow This attribute minimizes the information needed to classify the tuples in the resulting partitions and reflects the least randomness or impurity in these partitions.

\Rightarrow The expected information needed to classify a tuple in D is given by

$$\text{Info}(D) = - \sum_{i=1}^m p_i \log_2(p_i)$$

where p_i is the probability that an arbitrary tuple D belongs to class C_i and is estimated

$$p_i = |C_i \cap D| / |D|$$

\Rightarrow A log function to the base 2 is used, because the information is encoded in bits.

\Rightarrow $\text{Info}(D)$ is just the average amount of information needed to identify the class label of a tuple in D .

\Rightarrow $\text{Info}(D)$ is also known as the entropy of D .

*ID3 steps -

step 1: Calculate the information Gain of each feature.

Step 2 : Considering that all rows don't belong to the same class, split the dataset S into subsets using the feature for which the Information Gain is maximum.

Step 3 : Make a decision tree node using the feature with the maximum information gain.

Step 4 : If all rows belongs to the same class, make the current node as a leaf node with the class as its label.

Step 5 : Repeat for the remaining features until we run out of all features, or the decision tree has all leaf nodes.

Q:04 Why naive Bayesian classification is called "naive"?

- Apply Naive Bayesian classification on following dataset to classify given tuple.

$x = (\text{age} \leq 30, \text{Income} = \text{medium}, \text{student} = \text{yes}, \text{credit rating} = \text{fair})$

Age	income	student	credit-rating	buys-Computer
≤ 30	high	no	fair	no
≤ 30	high	no	excellent	no
31...40	high	no	fair	yes
> 40	medium	no	fair	yes
> 40	low	yes	fair	yes
> 40	low	yes	excellent	no
31...40	low	yes	excellent	yes
≤ 30	medium	no	fair	no
≤ 30	low	yes	fair	yes
> 40	medium	yes	fair	yes
≤ 30	medium	yes	excellent	yes
31...40	medium	no	excellent	yes
31...40	high	yes	fair	yes
> 40	medium	no	excellent	no

\Rightarrow The given tuple have attribute like,

Age ≤ 30

Income = medium

student = yes

credit-rating = fair

	class (9/14)		class (5/14)	
	Yes		No	
Attribute	Age			
≤ 30	2/9		3/5	
31...40	4/9		0	
> 40	3/9		2/5	

	Income			
Attribute				
Low	3/9		1/5	
medium	4/9		2/5	
high	2/9		2/5	

	Student			
Attribute				
No	3/9		4/5	
Yes	6/9		1/5	

	Credit-rating			
Attribute				
Fair	6/9		2/5	
Excellent	3/9		3/5	

$$\Rightarrow P(c_i) : P(\text{buys_computer} = \text{"yes"}) = 9/14 = 0.643$$

$$P(\text{buys_computer} = \text{"no"}) = 5/14 = 0.357$$

\rightarrow Compute $P(x/c_i)$ for each class

class
yes

$$\begin{aligned} 0) & P(\text{age} \leq 30 \mid \text{buys_computer} = \text{"yes"}) = 2/9 = 0.222 \\ & P(\text{income} = \text{"medium"} \mid \text{buys_computer} = \text{"yes"}) = 4/9 = 0.444 \\ & P(\text{student} = \text{"yes"} \mid \text{buys_computer} = \text{"yes"}) = 6/9 = 0.667 \\ & P(\text{credit_rating} = \text{"fair"} \mid \text{buys_computer} = \text{"yes"}) = 6/9 = 0.667 \end{aligned}$$

class
no

$$\begin{aligned} 0) & P(\text{age} \leq 30 \mid \text{buys_computer} = \text{"no"}) = 3/5 = 0.6 \\ & P(\text{income} = \text{"medium"} \mid \text{buys_computer} = \text{"no"}) = 2/5 = 0.4 \\ & P(\text{student} = \text{"yes"} \mid \text{buys_computer} = \text{"no"}) = 1/5 = 0.2 \\ & P(\text{credit_rating} = \text{"fair"} \mid \text{buys_computer} = \text{"no"}) = 2/5 = 0.4 \end{aligned}$$

$x = (\text{age} \leq 30, \text{income} = \text{medium}, \text{student} = \text{yes}, \text{credit_rating} = \text{fair})$

$$\begin{aligned} P(x|C_i): P(x \mid \text{buys_computer} = \text{"yes"}) \\ = 0.222 \times 0.444 \times 0.667 \times 0.667 = 0.044 \end{aligned}$$

$$\begin{aligned} & P(x \mid \text{buys_computer} = \text{"no"}) \\ & = 0.6 \times 0.4 \times 0.2 \times 0.4 = 0.019 \end{aligned}$$

$$\begin{aligned} P(x|C_i) \times P(C_i): P(x \mid \text{buys_computer} = \text{"yes"}) \times \\ P(\text{buys_computer} = \text{"yes"}) = 0.028 \\ : P(x \mid \text{buys_computer} = \text{"no"}) \times P(\text{buys_comp} = \text{"no"}) \\ = 0.007 \end{aligned}$$

\therefore Therefore, x belongs to class (computer-buys = yes)

Q:5 Calculate the weights using neural network single layer perceptron model. Three inputs are x_0, x_1, x_2 bias and weights are as follows:

$$W_1(0) = 30$$

$$W_2(0) = 300$$

$$b(a) = 50$$

$$\eta = 0.01, x_0 = +1$$

Activation function is

$$\text{sgn}(x) = +1 \quad ; \text{ if } x \geq 0$$

$$\text{sgn}(x) = -1 \quad ; \text{ if } x < 0$$

c1) Calculate the x_2 for $x_1 = 100$ and 200

$$\Rightarrow 30x_1 + 300x_2 + 50 = 0$$

$$\therefore x_2 = \frac{-50 - 30x_1}{300}$$

$$\text{For } x_1 = 100$$

$$= \frac{-500 - 3000}{300}$$

$$= -10.1667$$

$$\text{for } x_1 = 200$$

$$x_2 = \frac{-50 - 6000}{300}$$

$$= -20.1667$$

b) For bias $b(0) = -1230$ recalculate the weights w_1 and w_2 .

\Rightarrow For $b = -1230$, $w_1 = 30$, $w_2 = 300$

$$(100, -10.1667)$$

$$(200, -20.1667)$$

$$x(0) = [1, 100, -10.1667]^T$$

$$x(0) = [-1230, 30, 300]^T$$

$$y(0) = \text{sgn}(w^T(0) \cdot x(0))$$

$$= \text{sgn}(-1230 + 3000 - 3050.01)$$

$$= -1 \neq d(0)$$

we need to recalculate weights

$$x(1) = [+1, 200, -20.1667]^T$$

$$w(1) = [-1230, 30, 300]^T$$

$$y(1) = \text{sgn}(w^T(1) \cdot x(1))$$

$$= \text{sgn}(-1230 + 6000 - 6050.01)$$

$$= -1 \neq d(0)$$

we need to recalculate weights

$$w(n+1) = w(n) + \eta [d(n) - y(n)] \cdot x(n)$$

$$w(1) = [-1230, 30, 300]^T$$

$$x(1) = [+1, 200, -20.1667]^T$$

$$d(1) = +1, y(1) = -1, \eta = 0.01$$

$$\begin{aligned}
 W(1+1) &= W(2) = (-1230, 30, 300)^T + (0, 0.12, 11)^T \\
 &\quad [+1, 200, -20, 166]^T \\
 &= [-1230, 30, 300]^T + [0.02, 4, -0.4033]^T \\
 W(1) &= [-1229.98, 34, 299.59]^T
 \end{aligned}$$

hence $w_1 = 34$

$$w_2 = 299.59$$

Q:2

Define linear and nonlinear regression using figures. Calculate the value of y for $x=100$ based on linear regression prediction method.

x	y	$(x_i - \bar{x})$	$(y_i - \bar{y})$	$(x_i - \bar{x})(y_i - \bar{y})$	$(x_i - \bar{x})^2$
4	390	-4.75	-165	783.75	22.5625
9	580	0.25	25	6.25	0.0625
10	650	1.75	95	166.25	3.0625
14	730	5.25	175	918.75	27.5625
4	410	-4.75	-145	688.75	22.5625
7	530	-1.75	-25	43.75	3.0625
12	600	3.25	45	146.25	10.5625
22	790	13.25	235	3113.75	175.5625
1	350	-7.75	-205	1588.75	60.0625
3	400	-5.75	-155	891.25	33.0625
8	590	-0.75	35	-26.25	0.5625
11	640	2.25	85	191.25	5.0625

⇒ For linear regression

$$y = b_0 + b_1 x \quad \text{where} \quad b_1 = \frac{\sum [(x_i - \bar{x})(y_i - \bar{y})]}{\sum (x_i - \bar{x})^2} \quad b_0 = \bar{y} - b_1 \bar{x}$$

$$\bar{x} = \frac{\sum x}{n} = \frac{105}{12} = 8.75 \quad \bar{y} = \frac{\sum y}{n} = \frac{6660}{12} = 555$$

$$b_1 = \frac{[\sum (x_i - \bar{x})(y_i - \bar{y})]}{\sum (x_i - \bar{x})^2}$$

$$= \frac{8512.5}{363.75}$$

$$= 23.4020$$

$$b_0 = \bar{y} - b_1 \bar{x}$$

$$= 555 - 23.4020 \times 8.75$$

$$= 555 - 204.7675$$

$$= 350.2325$$

For $x = 100$

$$y = b_0 + b_1 x$$

$$= 350.2325 + (23.4020) \times 100$$

$$= 350.2325 + 2340.2$$

$$= 2690.4325$$

Simple linear regression relates two variables (x & y) with a straight line ($y = mx + b$), while non-linear regression relates the two variable (x & y) in a non-linear (curved) relationship.

Nonlinear equation is different for every curve.