

# Analysis of Animal Movements in R: the `adehabitatLT` Package

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Oct 2008

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# 1 History of the package `adehabitatLT`

The package `adehabitatLT` contains functions dealing with the analysis of animal movements that were originally available in the package `adehabitat` (Calenge, 2006). The data used for such analysis are generally relocation data collected on animals monitored using VHF or GPS collars.

I developed the package `adehabitat` during my PhD (Calenge, 2005) to make easier the analysis of habitat selection by animals. The package `adehabitat` was designed to extend the capabilities of the package `ade4` concerning studies of habitat selection by wildlife.

Since its first submission to CRAN in September 2004, a lot of work has been done on the management and analysis of spatial data in R, and especially with the release of the package `sp` (Pebesma and Bivand, 2005). The package `sp` provides classes of data that are really useful to deal with spatial data...

In addition, with the increase of both the number (more than 250 functions in Oct. 2008) and the diversity of the functions in the package `adehabitat`, it soon became apparent that a reshaping of the package was needed, to make its content clearer to the users. I decided to “split” the package `adehabitat` into four packages:

- `adehabitatHR` package provides classes and methods for dealing with home range analysis in R.
- `adehabitatHS` package provides classes and methods for dealing with habitat selection analysis in R.
- `adehabitatLT` package provides classes and methods for dealing with animals trajectory analysis in R.
- `adehabitatMA` package provides classes and methods for dealing with maps in R.

We consider in this document the use of the package `adehabitatLT` to deal with the analysis of animal movements. All the methods available in `adehabitat` are also available in `adehabitatLT`. Contrary to the other brother packages, the classes of data returned by the functions of `adehabitatLT` are the same as

those implemented in the original package `adehabitat`. Indeed, the structure of these classes were described in a paper (Calenge et al. 2009).

Package `adehabitatLT` is loaded by

```
> library(adehabitatLT)
```

## 2 The class `ltraj`

## 3 What is a trajectory?

### 3.1 Two types of trajectories

We designed the class `ltraj` to store the movements of animals monitored using radio-tracking, GPS, etc. The rationale underlying the structure of this class is described precisely in Calenge et al. (2009). We summarize this rationale in this vignette.

Basically, the trajectory of an animal is the curve described by the animal when it moves. The sampling of the trajectory implies a step of discretization, i.e., the division of this continuous curve into a number of discrete “steps” connecting successive relocations of the animal (Turchin, 1998). Two main classes of trajectories can be distinguished:

- **Trajectories of type I** are characterized by the fact that the time is not precisely known or not taken into account for the relocations of the trajectory;
- **the trajectories of type II** are characterized by the fact that the time is known for each relocation. This type of trajectory may in turn be divided into two subtypes:
  - **regular trajectories**: these trajectories are characterized by a constant time lag between successive relocations;
  - **irregular trajectories**: these trajectories are characterized by a variable time lag between successive relocations;

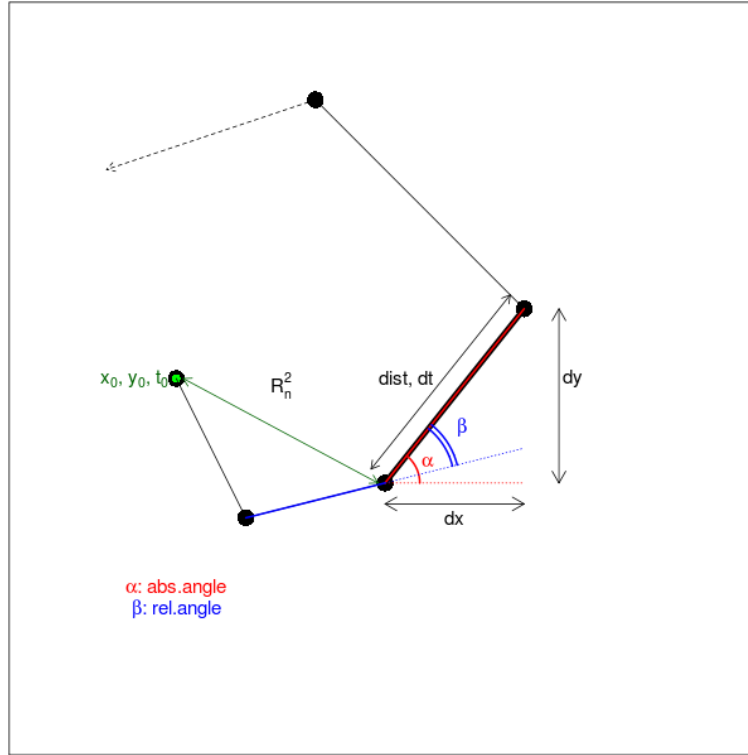
Note that the functions of `adehabitatLT` are mainly designed to deal with type I or type II regular trajectories. Irregular trajectories are harder to analyze, as the descriptive parameters of these trajectories (see below) may not be compared when computed on different time lags.

### 3.2 Descriptive parameters of the trajectory

Marsh and Jones (1988) noted that a good description of the trajectory is achieved when the following criteria are fulfilled:

- the description is achieved with a minimum set of relatively easily measured parameters;
- the relationships between these parameters are defined precisely (e.g., with the help of a model);
- the parameters and the relationships between them are sufficient to reconstruct characteristic tracks without losing any of their significant properties.

Based on a literature review (see Calenge et al. 2009), we have chosen to characterize all the trajectories by the following parameters:



- $dx$ ,  $dy$ ,  $dt$ : these parameters measured at relocation  $i$  describe the increments of the x and y directions and time between the relocations  $i$  and

$i + 1$ . Such parameters are often used in the framework of stochastic differential equation modelling (e.g. Brillinger et al. 2004, Wiktorsson et al. 2004);

- **dist**: the distance between successive relocations is often used in animal movement analysis (e.g. Root and Kareiva 1984, Marsh and Jones 1988);
- **abs.angle**: the absolute angle  $\alpha_i$  between the  $x$  direction and the step built by relocations  $i$  and  $i + 1$  is sometimes used together with the parameter **dist** to fit movement models (e.g. Marsh and Jones 1988);
- **rel.angle**: the relative angle  $\beta_i$  measures the change of direction between the step built by relocations  $i - 1$  and  $i$  and the step built by relocations  $i$  and  $i + 1$  (often called “turning angle”). It is often used together with the parameter **dist** to fit movement models (e.g. Root and Kareiva 1984, Marsh and Jones 1988);
- **R2n**: the squared distance between the first relocation of the trajectory and the current relocation is often used to test some movements models (e.g. the correlated random walk, see the seminal paper of Kareiva and Shigesada, 1983).

### 3.3 Several bursts of relocations

Very often, animal monitoring leads to several “bursts” of relocations for each monitored animal. For example, a GPS collar may be programmed to return one relocation every ten minutes during the night and no relocation during the day. Each night corresponds to a burst of relocations for each animal. We designed the class `ltraj` to take into account this burst structure.

### 3.4 Understanding the class `ltraj`

An object of class `ltraj` is created with the function `as.ltraj` (see the help page of this function). We will take an example to illustrate the creation of an object of class `ltraj`. First load the dataset `puechabonsp` from the package `adehabitatMA`:

```
> data(puechabonsp)
> locs <- puechabonsp$relocs
> locs <- as.data.frame(locs)
> head(locs)
```

	Name	Age	Sex	Date	X	Y
1	Brock	2	1	930701	699889	3161559
2	Brock	2	1	930703	700046	3161541
3	Brock	2	1	930706	698840	3161033
4	Brock	2	1	930707	699809	3161496
5	Brock	2	1	930708	698627	3160941
6	Brock	2	1	930709	698719	3160989

The data frame `locs` contains the relocations of 4 wild boar monitored using radio-tracking at Puechabon (Near Montpellier, South of France). First the date needs to be transformed into an object of the class `POSIXct`.

*Remark:* The class `POSIXt` is designed to store time data in R (see the very clear help page of `POSIXt`). This class extends two sub-classes:

- **the class `POSIXlt`:** This class stores a date in a list containing several elements related to this date (day of the month, day of the week, day of the year, month, year, time zone, hour, minute, second).
- **the class `POSIXct`:** This class stores a date in a vector, as the number of seconds passed since January, 1st, 1970 at 1AM. This class is more convenient for storing dates into a data frame.

We will use the function `strptime` (see the help page of this function) to convert the date in `locs` into a `POSIXlt` object, as then `as.POSIXct` to convert it into the class `POSIXct`:

```
> da <- as.character(locs$Date)
> head(da)

[1] "930701" "930703" "930706" "930707" "930708" "930709"

> da <- as.POSIXct(strptime(as.character(locs$Date), "%y%m%d"))
```

We can then create an object of class `ltraj` to store the wild boar movements:

```
> puech <- as.ltraj(xy = locs[, c("X", "Y")], date = da, id = locs$Name)
> puech
```

```
***** List of class ltraj *****
```

```
Type of the trajectory: Type II (time recorded)
Irregular trajectory. Variable time lag between two locs
```

Characteristics of the bursts:

	id	burst	nb.reloc	NAs	date.begin	date.end
1	Brock	Brock	30	0	1993-07-01	1993-08-31
2	Calou	Calou	19	0	1993-07-03	1993-08-31
3	Chou	Chou	40	0	1992-07-29	1993-08-30
4	Jean	Jean	30	0	1993-07-01	1993-08-31

The result is a list of class `ltraj` containing four bursts of relocations corresponding to four animals. The trajectory is of type II and is irregular. There are no missing values.

This object is actually a list containing 4 elements (the four bursts). Each element is a data frame. Have a look, for example, at the first rows of the first data frame:

```
> head(puech[[1]])
```

	x	y	date	dx	dy	dist	dt	R2n	abs.angle
1	699889	3161559	1993-07-01	157	-18	158.0285	172800	0	-0.11415127
2	700046	3161541	1993-07-03	-1206	-508	1308.6252	259200	24973	-2.74292194
3	698840	3161033	1993-07-06	969	463	1073.9320	86400	1377077	0.44574032
4	699809	3161496	1993-07-07	-1182	-555	1305.8135	86400	10369	-2.70260603
5	698627	3160941	1993-07-08	92	48	103.7690	86400	1974568	0.48088728
6	698719	3160989	1993-07-09	272	26	273.2398	345600	1693800	0.09529869

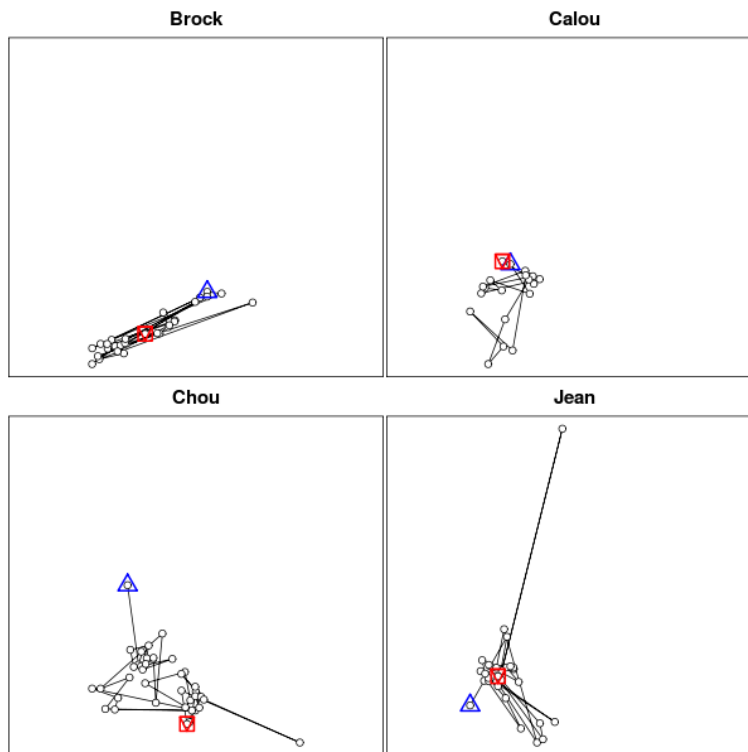
  

	rel.angle
1	NA
2	-2.6287707
3	-3.0945230
4	3.1348390
5	-3.0996920
6	-0.3855886

The function `as.ltraj` has automatically computed the descriptive parameters described in section 3.2 from the `x` and `y` coordinates, and from the date. Note that `dx`, `dy`, `dist` are expressed in the units of the coordinates `x`, `y` (here, metres) and `abs.angle`, `rel.angle` are expressed in radians.

A graphical display of the bursts can be obtained simply by:

```
> plot(puech)
```



## 4 Managing objects of class `ltraj`

### 4.1 Cutting a burst into several segments

Now, let us analyse the object `puech` created in the previous section. We noted that the object `puech` was not regular:

```
> is.regular(puech)
```

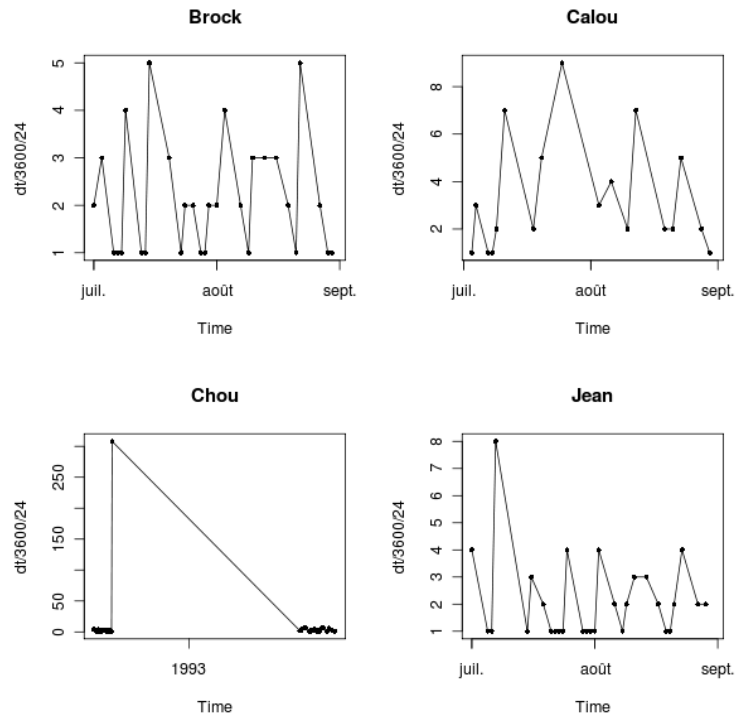
```
[1] FALSE
```

The function `is.regular` returns a Boolean... such a result can be obtained from a regular trajectory where just one relocation is missing, or from a completely irregular trajectory... we need more precision!

Have a look at the value of `dt` according to the date, using the function `plotltr`. Because `dt` is measured in seconds and that no more than one relocation is collected every day, we convert this time lag into days by dividing it by 24 (hours/day)  $\times$  3600 (seconds / hour):

```
> plotltr(puech, "dt/3600/24")
```





The wild boar Chou was monitored during two successive summers (1992 and 1993). We need to “cut” this burst into two “sub-burst”. We will use the function `cutltraj` to proceed. We first define a function `foo` that returns `TRUE` when the time lag between two successive relocations is greater than 100 days:

```
> foo <- function(dt) {
+   return(dt > (100 * 3600 * 24))
+ }
```

Then, we use the function `cutltraj` to cut any burst relocations with a value of `dt` such that `foo(dt)` is true, into several bursts for which no value of `dt` fulfills this criterion:

```
> puech2 <- cutltraj(puech, "foo(dt)", nexttr = TRUE)
> puech2
```

```
***** List of class ltraj *****
```

```
Type of the trajet: Type II (time recorded)
Irregular trajet. Variable time lag between two locs
```

```
Characteristics of the bursts:
```

	id	burst	nb.reloc	NAs	date.begin	date.end
1	Brock	Brock.1	30	0	1993-07-01	1993-08-31
2	Calou	Calou.1	19	0	1993-07-03	1993-08-31
3	Chou	Chou.1	16	0	1992-07-29	1992-08-28
4	Chou	Chou.2	24	0	1993-07-02	1993-08-30
5	Jean	Jean.1	30	0	1993-07-01	1993-08-31

Now, note that the burst of Chou has been splitted into two bursts: the first burst corresponds to the monitoring of Chou during 1992, and the second burst corresponds to the monitoring of Chou during 1993. We can give more explicit names to these bursts:

```
> burst(puech2)[3:4] <- c("Chou.1992", "Chou.1993")
> puech2
```

```
***** List of class ltraj *****
```

```
Type of the trajet: Type II (time recorded)
Irregular trajet. Variable time lag between two locs
```

```
Characteristics of the bursts:
```

	id	burst	nb.reloc	NAs	date.begin	date.end
1	Brock	Brock.1	30	0	1993-07-01	1993-08-31
2	Calou	Calou.1	19	0	1993-07-03	1993-08-31
3	Chou	Chou.1992	16	0	1992-07-29	1992-08-28
4	Chou	Chou.1993	24	0	1993-07-02	1993-08-30
5	Jean	Jean.1	30	0	1993-07-01	1993-08-31

Note that the function `id()` can be used similarly to replace the IDs of the animals.

## 4.2 Playing with bursts

The bursts in an object `ltraj` can be easily managed. For example, consider te object `puech2` created previously:

```
> puech2
```

```
***** List of class ltraj *****
```

```
Type of the trajet: Type II (time recorded)
Irregular trajet. Variable time lag between two locs
```

```
Characteristics of the bursts:
```

	id	burst	nb.reloc	NAs	date.begin	date.end
1	Brock	Brock.1	30	0	1993-07-01	1993-08-31

2	Calou	Calou.1	19	0	1993-07-03	1993-08-31
3	Chou	Chou.1992	16	0	1992-07-29	1992-08-28
4	Chou	Chou.1993	24	0	1993-07-02	1993-08-30
5	Jean	Jean.1	30	0	1993-07-01	1993-08-31

Imagine that we want to work only on the males (Brock, Calou and Jean). We can subset this object using a classical extraction function:

```
> puech2b <- puech2[c(1, 2, 5)]
> puech2b
```

```
***** List of class ltraj *****
```

```
Type of the trajet: Type II (time recorded)
Irregular trajet. Variable time lag between two locs
```

```
Characteristics of the bursts:
```

	id	burst	nb.reloc	NAs	date.begin	date.end
1	Brock	Brock.1	30	0	1993-07-01	1993-08-31
2	Calou	Calou.1	19	0	1993-07-03	1993-08-31
3	Jean	Jean.1	30	0	1993-07-01	1993-08-31

Or, if we want to study the animals monitored in 1993, we may combine this object with the monitoring of Chou in 1993:

```
> puech2c <- c(puech2b, puech2[4])
> puech2c
```

```
***** List of class ltraj *****
```

```
Type of the trajet: Type II (time recorded)
Irregular trajet. Variable time lag between two locs
```

```
Characteristics of the bursts:
```

	id	burst	nb.reloc	NAs	date.begin	date.end
1	Brock	Brock.1	30	0	1993-07-01	1993-08-31
2	Calou	Calou.1	19	0	1993-07-03	1993-08-31
3	Jean	Jean.1	30	0	1993-07-01	1993-08-31
4	Chou	Chou.1993	24	0	1993-07-02	1993-08-30

It is also possible to select the bursts according to their id of their burst id (see the help page of `Extract.ltraj` for additional information, and in particular the example section).

The function `which.ltraj` can also be used to identify the bursts satisfying a condition. For example, imagine that we want to identify the bursts where the distance between successive relocations was greater than 2000 metres at least once:

```
> bu <- which.ltraj(puech2, "dist>2000")
> bu
```

```
      id  burst results
1 Jean Jean.1      18
2 Jean Jean.1      19
```

This data frame contains the ID, burst ID and relocation numbers satisfying the specified criterion. We can then extract the bursts satisfying this criterion:

```
> puech2[burst(puech2) %in% bu$burst]
```

```
***** List of class ltraj *****
```

```
Type of the trajet: Type II (time recorded)
Irregular trajet. Variable time lag between two locs
```

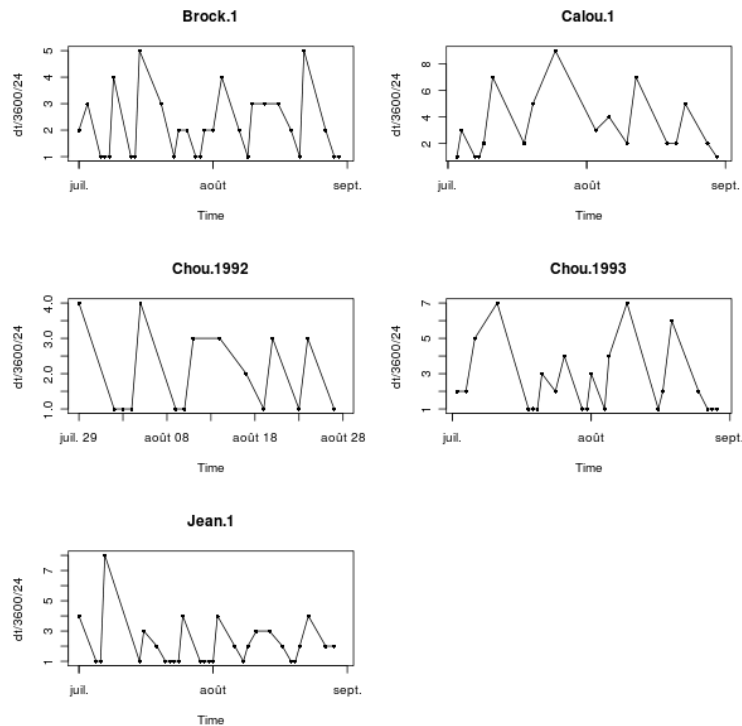
```
Characteristics of the bursts:
```

```
      id  burst nb.reloc NAs date.begin  date.end
1 Jean Jean.1      30   0 1993-07-01 1993-08-31
```

### 4.3 Placing the missing values in the trajectory

Now, look again at the time lag between successive relocations:

```
> plotltr(puech2, "dt/3600/24")
```



The relocations have been collected daily, but there are many days during which this relocation was not possible (storm, lack of field workers, etc.). We need to add missing values to define a regular trajectory. To proceed, we will use the function `setNA`. We have to define a reference date:

```
> refda <- strptime("00:00", "%H:%M")
> refda

[1] "2010-04-17"
```

This reference date will be used to check that each date in the object of class `ltraj` is separated from this reference by an integer multiple of the theoretical `dt` (here, one day), and place the missing values at the times when relocations should theoretically have been collected. We use the function `setNA`:

```
> puech3 <- setNA(puech2, refda, 1, units = "day")
> puech3
```

```
***** List of class ltraj *****
```

```
Type of the trajet: Type II (time recorded)
Regular trajet. Time lag between two locs: 86400 seconds
```

Characteristics of the bursts:

	id	burst	nb.reloc	NAs	date.begin	date.end
1	Brock	Brock.1	62	32	1993-07-01	1993-08-31
2	Calou	Calou.1	60	41	1993-07-03	1993-08-31
3	Chou	Chou.1992	31	15	1992-07-29	1992-08-28
4	Chou	Chou.1993	60	36	1993-07-02	1993-08-30
5	Jean	Jean.1	62	32	1993-07-01	1993-08-31

The trajectories are now regular, but there are now a lot of missing values!

#### 4.4 Rounding the timing of the trajectories to define a regular trajectory

In some cases, despite the fact that the relocations were expected to be collected to return a regular trajectory, a minor delay is sometimes observed in this timing. For example, consider the monitoring of four ibex in the Belledonne Mountains (French Alps):

```
> data(ibexraw)
> ibexraw
```

```
***** List of class ltraj *****
```

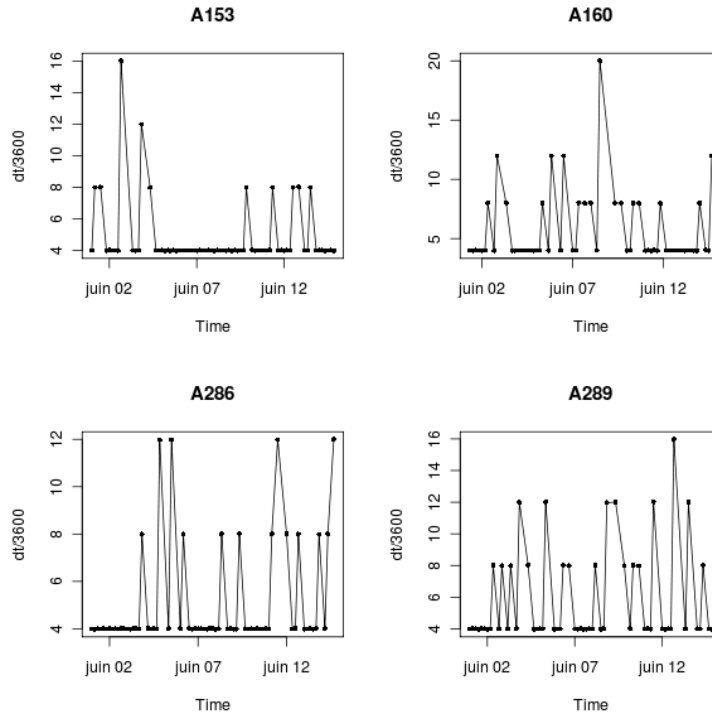
```
Type of the trajct: Type II (time recorded)
Irregular trajct. Variable time lag between two locs
```

Characteristics of the bursts:

	id	burst	nb.reloc	NAs	date.begin	date.end
1	A153	A153	71	0	2003-06-01 00:00:56	2003-06-14 20:01:33
2	A160	A160	59	0	2003-06-01 08:01:35	2003-06-14 16:02:20
3	A286	A286	68	0	2003-06-01 00:02:45	2003-06-14 16:01:41
4	A289	A289	58	0	2003-06-01 00:01:31	2003-06-14 20:02:32

There is a variable time lag between successive relocations. Look at the time lag between successive relocations:

```
> plotltr(ibexraw, "dt/3600")
```



The relocations should have been collected every 4 hours, but there are some missing values. Use the function `setNA` to place the missing values, as in the section 4.3. We define a reference date and place the missing values:

```
> refda <- strptime("00:00", "%H:%M")
> ib2 <- setNA(ibexraw, refda, 4, units = "hour")
> ib2
```

\*\*\*\*\* List of class ltraj \*\*\*\*\*

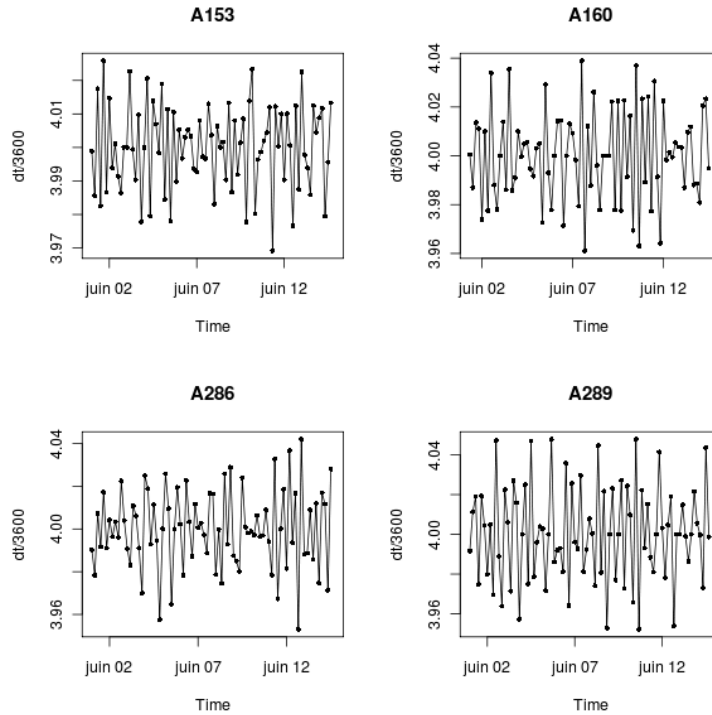
Type of the trajet: Type II (time recorded)  
Irregular trajet. Variable time lag between two locs

Characteristics of the bursts:

	id	burst	nb.reloc	NAs	date.begin	date.end
1	A153	A153	84	13	2003-06-01 00:00:56	2003-06-14 20:01:33
2	A160	A160	81	22	2003-06-01 08:01:35	2003-06-14 16:02:20
3	A286	A286	83	15	2003-06-01 00:02:45	2003-06-14 16:01:41
4	A289	A289	84	26	2003-06-01 00:01:31	2003-06-14 20:02:32

Even when filling the gaps with NAs, the trajectory is still not regular. Now, look again at the time lag between successive relocations:

```
> plotltr(ib2, "dt/3600")
```



We can see that the time lag is only slightly different from 4 hour. The function `sett0` can be used to “round” the timing of the coordinates:

```
> ib3 <- sett0(ib2, refda, 4, units = "hour")
> ib3
```

```
***** List of class ltraj *****
```

```
Type of the trajet: Type II (time recorded)
Regular trajet. Time lag between two locs: 14400 seconds
```

```
Characteristics of the bursts:
```

	id	burst	nb.reloc	NAs	date.begin	date.end
1	A153	A153	84	13	2003-06-01 00:00:00	2003-06-14 20:00:00
2	A160	A160	81	22	2003-06-01 08:00:00	2003-06-14 16:00:00
3	A286	A286	83	15	2003-06-01 00:00:00	2003-06-14 16:00:00
4	A289	A289	84	26	2003-06-01 00:00:00	2003-06-14 20:00:00

The trajectory is now regular.



**Important note:** The functions `setNA` and `sett0` are to be used to set a theoretically regular trajectory into a practically regular trajectory. **It is NOT intended to transform an irregular trajectory into a regular one** (many users of `adehabitat` asked this question).

## 4.5 A special type of trajectories: same duration

In some cases, an object of class `ltraj` contains several regular bursts of the same duration characterized by relocations collected at the same time (same time lags between successive relocations, same number of relocations). We can check whether an object of class “`ltraj`” is of this type with the function `is.sd`. For example, consider again the movement of 4 ibexes monitored using GPS, stored in an object of class `ltraj` created in the previous section:

```
> is.sd(ib3)
```

```
[1] FALSE
```

This object is not of the type `sd` (same duration). However, theoretically, all the trajectories should have been sampled at the same time points. It is regular, but there are mismatches between the time of the relocations:

```
> ib3
```

```
***** List of class ltraj *****
```

```
Type of the traject: Type II (time recorded)
```

```
Regular traject. Time lag between two locs: 14400 seconds
```

```
Characteristics of the bursts:
```

	id	burst	nb.reloc	NAs	date.begin	date.end
1	A153	A153	84	13	2003-06-01 00:00:00	2003-06-14 20:00:00
2	A160	A160	81	22	2003-06-01 08:00:00	2003-06-14 16:00:00
3	A286	A286	83	15	2003-06-01 00:00:00	2003-06-14 16:00:00
4	A289	A289	84	26	2003-06-01 00:00:00	2003-06-14 20:00:00

This is caused by the fact that there are missing relocations at the beginning and/or end of the monitoring for several animals (A160 and A286). We can use the function `set.limits` to define the time of beginning and ending of the trajectories. This function adds NAs to the beginning and ending of the monitoring when required:

```
> ib4 <- set.limits(ib3, begin = "2003-06-01 00:00", dur = 14,
+   units = "day", pattern = "%Y-%m-%d %H:%M")
> ib4
```

```
***** List of class ltraj *****
```

Type of the trajct: Type II (time recorded)  
Regular trajct. Time lag between two locs: 14400 seconds

Characteristics of the bursts:

	id	burst	nb.reloc	NAs	date.begin	date.end
1	A153	A153	85	14	2003-06-01	2003-06-15
2	A160	A160	85	26	2003-06-01	2003-06-15
3	A286	A286	85	17	2003-06-01	2003-06-15
4	A289	A289	85	27	2003-06-01	2003-06-15

All the trajectory are now covering the same time period:

```
> is.sd(ib4)
```

```
[1] TRUE
```

**Remark:** in our example, all the bursts are covering exactly the same time period (all begin at the same time and date and all stop at the same time and date). However, the function `set.limits` is much more flexible. Imagine for example that we are studying the movement of an animal during the night, from 00:00 to 06:00. If we have one burst per night, then it is possible to define an object of class `ltraj`, type `sd`, containing several nights of monitoring, even if the nights of monitoring do not correspond to the same date. If we consider that all the bursts cover the same period, then it is still possible to use the function `set.limits` to define an object of type `sd` (this is explained deeply on the help page of `set.limits`).

It is then possible to store some parameters of `sd` objects into a data frame (with one relocation per row and one burst per column), using the function `sd2df`. For example, considering the distance between successive relocations:

```
> di <- sd2df(ib4, "dist")
> head(di)
```

	A153	A160	A286	A289
1	41.04875	NA	214.2008	15.65248
2	NA	NA	428.8508	293.60007
3	NA	517.4882	606.9802	837.70401
4	NA	1533.7881	637.1538	1108.75065
5	NA	608.6912	216.0000	72.61543
6	244.66303	2264.8366	216.8156	383.65870

This data frame can then be used to study the interactions or similarities between the bursts.

## 4.6 Metadata on the trajectories (Precision of the relocations, etc.)

Sometimes, additional information is available for each relocation, and we may wish to store this information in the object of class `ltraj`, to allow the analysis of the relationships between these additional variables and the parameters of the trajectory.

This meta information can be stored in the attribute `infolocs` of each burst. This should be defined when creating the object `ltraj`. For example, load the dataset `capreochiz`:

```
> data(capreochiz)
> head(capreochiz)
```

	x	y	date	Dop	Status	Temp	Act	Conv
1	967.3994	1137.488	2004-02-13 17:02:18	5.7	3DDif	10	0	0
2	961.9346	1141.413	2004-02-14 00:31:23	3.6	3DDif	3	0	0
3	961.9340	1141.401	2004-02-14 12:02:17	6.9	3DDif	8	0	0
4	961.9426	1141.409	2004-02-15 00:00:47	5.0	3DDif	3	0	0
5	961.9472	1141.405	2004-02-15 00:30:13	4.1	3DDif	2	0	0
6	961.9430	1141.409	2004-02-15 12:01:11	8.1	3DDif	5	0	0

This dataset contains the relocations of one roe deer monitored using a GPS collar in the Chize forest (Deux-Sevres, France). This dataset contains the x and y coordinates (in kilometres), the date, and several variables characterizing the precision of the relocations. Note that the date is already of class `POSIXct`. We now define the object of class `ltraj`, storing the variables `Dop`, `Status`, `Temp`, `Act`, `Conv` in the attribute `infolocs` of the object:

```
> capreo <- as.ltraj(xy = capreochiz[, c("x", "y")], date = capreochiz$date,
+   id = "Roe.Deer", infolocs = capreochiz[, 4:8])
> capreo
```

```
***** List of class ltraj *****
```

```
Type of the trajet: Type II (time recorded)
Irregular trajet. Variable time lag between two locs
```

```
Characteristics of the bursts:
```

	id	burst	nb.reloc	NAs	date.begin	date.end
1	Roe.Deer	Roe.Deer	2355	0	2004-02-13 17:02:18	2004-08-31 06:00:47

```
infolocs provided. The following variables are available:
[1] "Dop" "Status" "Temp" "Act" "Conv"
```

The object `capreo` can be managed as usual. The function `infolocs()` can be used to retrieve the attributes `infolocs` of the bursts building up a trajectory:

```
> inf <- infolocs(capreo)
> head(inf[[1]])
```

	Dop	Status	Temp	Act	Conv
1	5.7	3DDif	10	0	0
2	3.6	3DDif	3	0	0
3	6.9	3DDif	8	0	0
4	5.0	3DDif	3	0	0
5	4.1	3DDif	2	0	0
6	8.1	3DDif	5	0	0

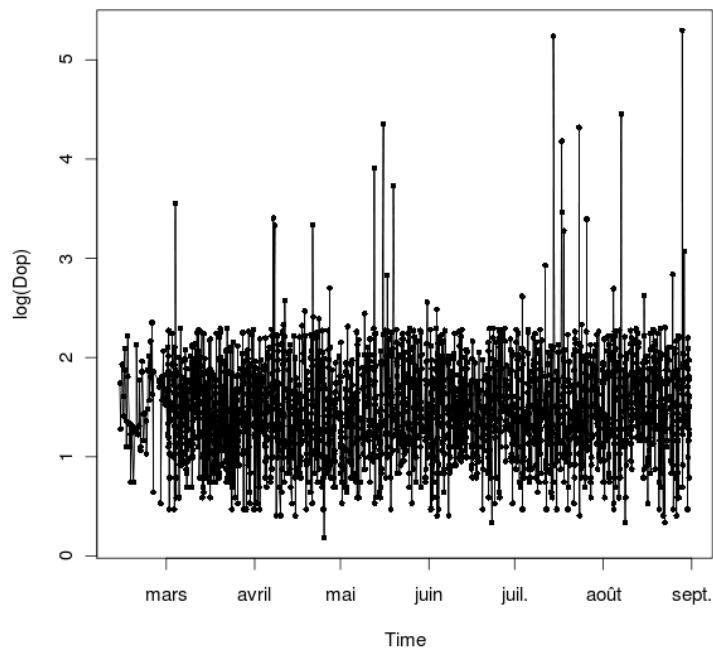
The function `removeinfo` can be used to set the attribute `infolocs` of all bursts to `NULL`.

Note that it is required that:

- all the burst are characterized by the same variables in the attribute `infolocs`. For example, it is not possible to store only the variable `Dop` for one burst and only the variable `Status` for another burst into the same object;
- each row of the data frame stored as attributes `infolocs` correspond to one relocation (that is, the number of rows of the attribute should be the same as the number of relocations in the corresponding burst).

Most functions of the package `adehabitatLT` do manage this attribute. For example, the functions `cutltraj` and `plotltr` can be used by calling variables stored in this attribute (as well as many other functions). For example:

```
> plotltr(capreo, "log(Dop)")
```



## 5 Analyzing the trajectories

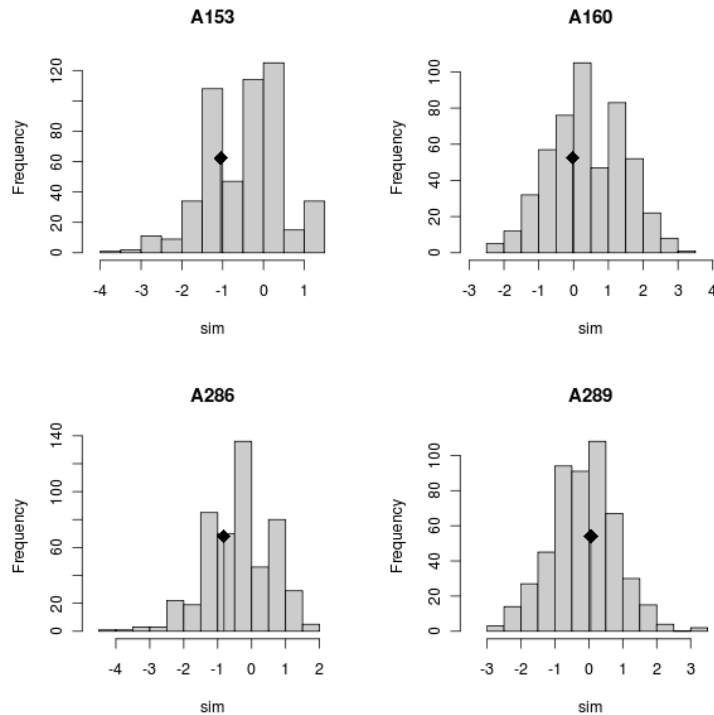
In this section, we will describe several tools available in `adehabitatLT` to analyse a trajectory.

### 5.1 Randomness of the missing values

A first important point is the examination of the distribution of the missing values in the trajectory. Missing values are frequent in the trajectories of animals collected using telemetry (e.g., GPS collar may not receive the signal of the satellite at the time of relocation, due for example to the habitat structure obscuring the signal, etc.). As noted by Graves and Waller (2006), the analysis of the patterns of missing values should be part of trajectory analysis.

The package `adehabitatLT` provides several tools for this analysis. For example, consider the object `ib4` created in section 4.5, and containing 4 bursts describing the movements of 4 ibexes in the Belledonne mountain. We can first test whether the missing values occur at random in the monitoring using the function `runsNAltraj`:

```
> runsNAltraj(ib4)
```



In this case, no difference appears between the number of runs actually observed in our trajectories and the distribution of the number of runs under the hypothesis of a random distribution of the NAs. The hypothesis of a random distribution of the NAs seems reasonable here.

But now, consider the distribution of the missing values in the case of the monitoring of one brown bear using a GPS collar:

```
> data(bear)
> bear

***** List of class ltraj *****

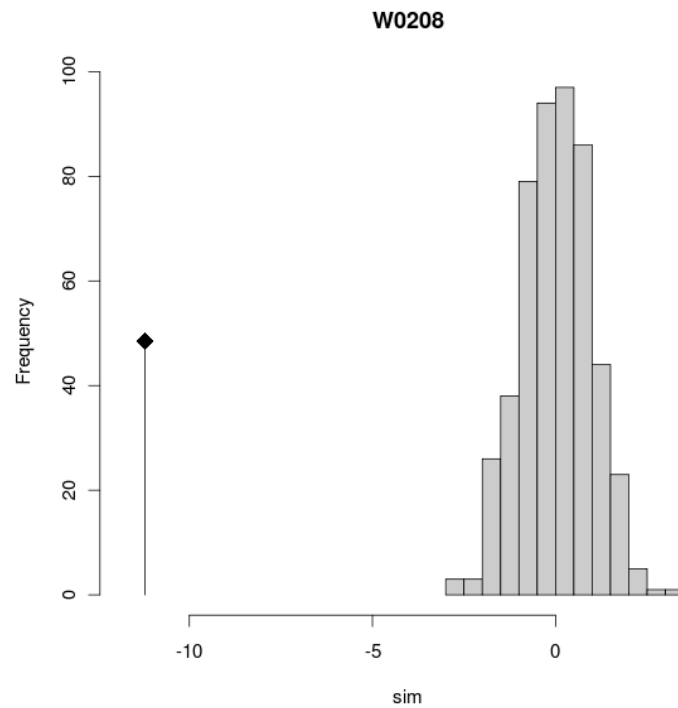
Type of the trajet: Type II (time recorded)
Regular trajet. Time lag between two locs: 1800 seconds

Characteristics of the bursts:
      id burst nb.reloc NAs      date.begin      date.end
1 W0208 W0208      1157 157 2004-04-19 16:30:00 2004-05-13 18:30:00
```

This trajectory is regular. The bear was monitored during one month, with

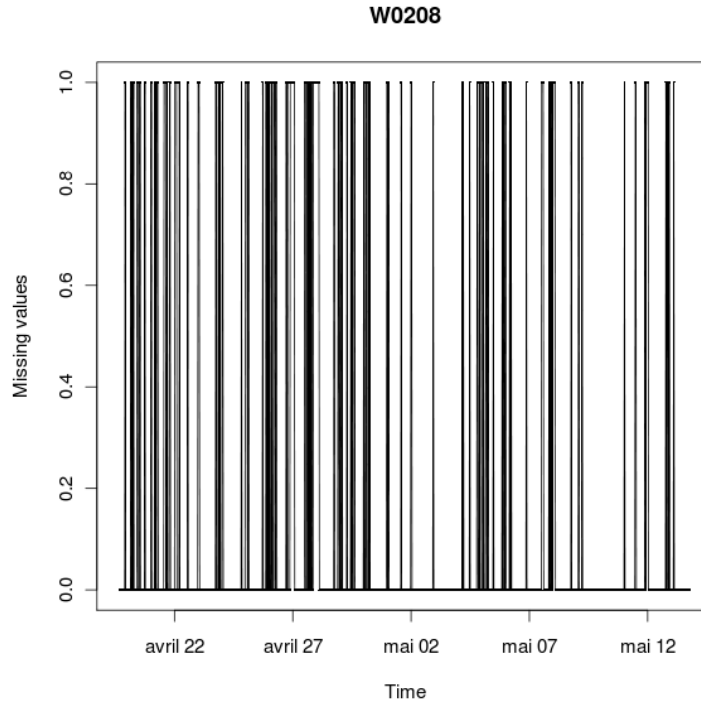
one relocation every 30 minutes. We now test for a random distribution of the missing values for this trajectory:

```
> runsNAltraj(bear)
```



In this case, the missing values are not distributed at random. Have a look at the distribution of the missing values:

```
> plotNAltraj(bear)
```



Because of the high number of relocations in this trajectory, this graph is not very clear. So a better way to study the distribution of the missing values is to work directly on the vector indicating whether the relocations are missing or not. That is:

```
> missval <- as.numeric(is.na(bear[[1]]$x))
> head(missval)

[1] 0 0 0 0 0 0
```

This vector can then be analyzed using classical time series methods (e.g. Diggle 1990). We do not pursue on this aspect, as this is not the aim of this vignette to describe time series methods.

## 5.2 Should we consider the time?

### 5.2.1 Type II or type I?

Until now, we have only considered trajectories of type II (time recorded). However, a common approach to the analysis of animal movements is to consider the movement as a discretized curve, and to study the geometrical properties of this curve (e.g., Turchin 1998; Benhamou 2004). That is, even if the data collection



implied the recording of the time, it is often more convenient to consider the monitored movement as a trajectory of type I. There are two ways to define a type I trajectory with the functions of `adehabitatLT`. The first is to set the argument `typeII=FALSE` when calling the function `as.ltraj`. The second is to use the function `typeII2typeI`. For example, considering the trajectory of the bear loaded in the previous section, we can transform it into a type I object by:

```
> bearI <- typeII2typeI(bear)
> bearI

***** List of class ltraj *****

Type of the trajectory: Type I (time not recorded)

Characteristics of the bursts:
      id burst Nb.reloc NAs
1 W0208 W0208    1157 157
```

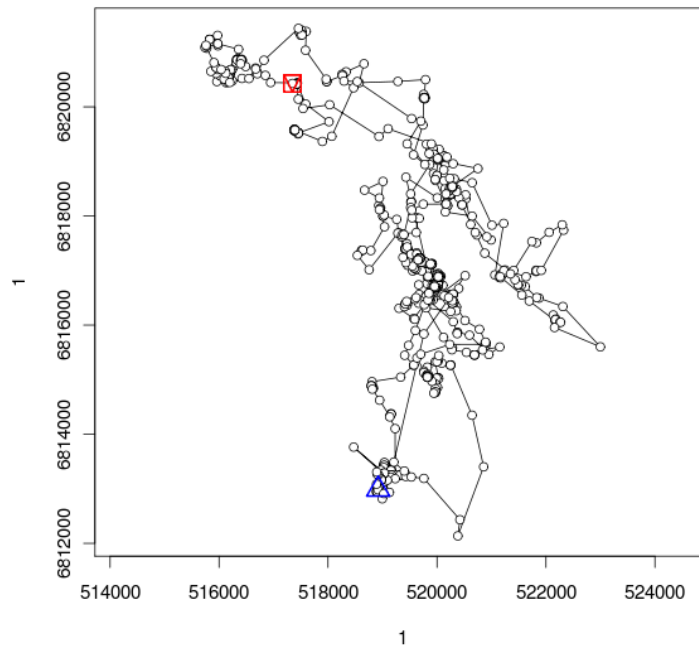
Nothing has changed, except that the time is replaced by an integer vector ordering the relocations in the trajectory.

### 5.2.2 Rediscretizing the trajectory

Several authors have advised to rediscretize type I trajectories so that they are built by steps with a constant length (e.g. Turchin 1998). This is a convenient approach to the analysis, as all the geometrical properties of the trajectory can be summarized by studying the variation of the relative angles.

The function `redisltraj` can be used for this rediscretization. For example, look at the trajectory of the brown bear stored in `bearI` (created in the previous section):

```
> plot(bearI)
```



Now, rediscrctize this trajectory with constant step length of 500 metres:

```
> bearIr <- redisltraj(bearI, 500)
> bearIr
```

```
***** List of class ltraj *****
```

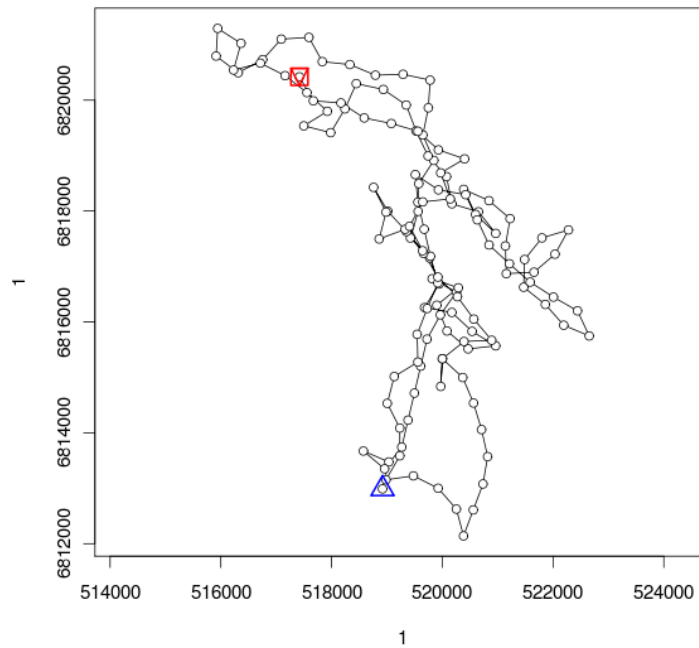
```
Type of the trajct: Type I (time not recorded)
```

```
Characteristics of the bursts:
```

	id	burst	Nb.reloc	NAs
1	W0208	W0208.R500	131	0

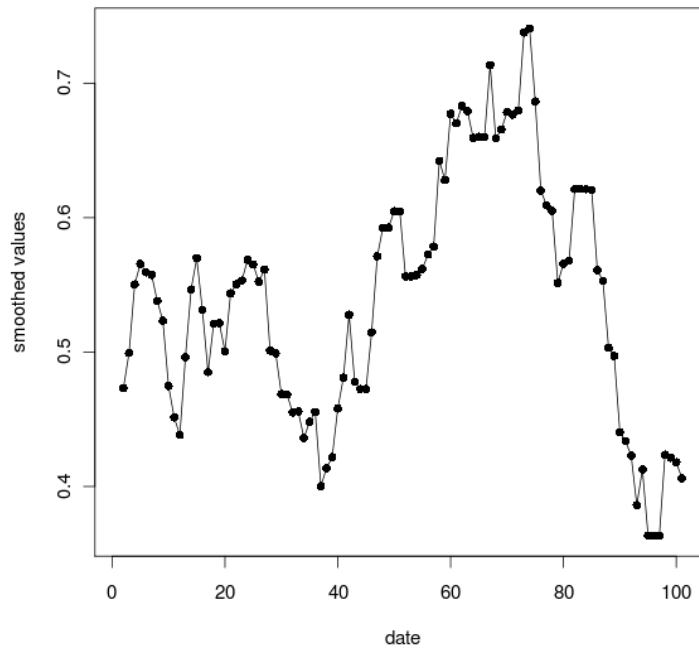
The number of relocations has increased. Have a look at the rediscrctized trajectory:

```
> plot(bearIr)
```



Then, the geometrical properties can be studied by examining the distribution of the relative angles. For example, the function `sliwinltr` can be used to smooth the cosine of relative angle using a sliding window method:

```
> sliwinltr(bearIr, function(x) mean(cos(x$rel.angle)), type = "locs",
+   step = 30)
```



The beginning of the trajectory is characterized by mean cosine close to 0.5 (tortuous trajectory). Then the movements of the animal is more linear (i.e., less tortuous). A finer analysis should now be done on these data. So that we need to get the relative angles from this rediscretized trajectory:

```
> cosrelangle <- cos(bearIr[[1]]$rel.angle)
> head(cosrelangle)

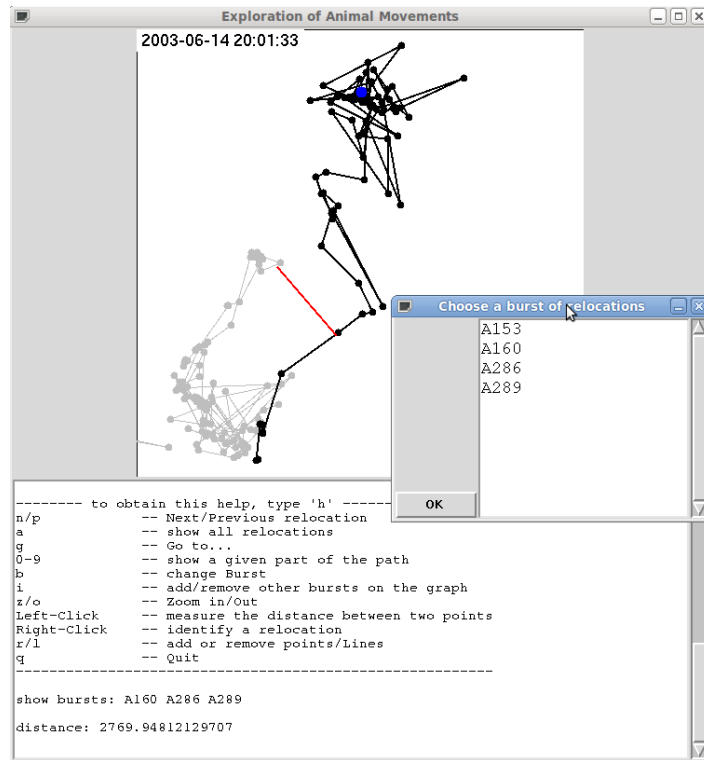
[1]      NA  0.17250586 -0.95704496 -0.02868423  0.90540260  1.00000000
```

This vector can now be analyzed using classical time series analysis methods. We do not pursue this analysis further, as this is beyond the scope of this vignette.

### 5.3 Dynamic exploration of a trajectory

The package `adehabitatLT` provides a function very useful for the dynamic exploration of animal movement: the function `trajdyn`. This function allows to dynamically zoom/unzoom, measure distance between several bursts or several relocations, explore the trajectory in space and time, etc. For example, the `ibex` data set is explored by typing:

```
> trajdyn(ib4)
```



Note that this function can draw a background defined by an object of class `SpatialPixelsDataFrame` or `SpatialPolygonsDataFrame`.

## 5.4 Analyzing autocorrelation

Dray et al. (2010) noted that the analysis of the sequential autocorrelation of the descriptive parameters presented in section 3.2 is essential to the understanding of the mechanisms driving these movements. The approach proposed by these authors is implemented in `adehabitatLT`. In this section, we describe the functions that can be used to carry out this kind of analysis.

A positive autocorrelation of a parameter means that values taken near to each other tend to be either more similar (positive autocorrelation) or less similar (negative autocorrelation) than would be expected from a random arrangement.

### 5.4.1 Testing for autocorrelation of the linear parameters

The independence test of Wald and Wolfowitz (1944) is implemented in the generic function `wawotest`. Basically, this function can be used to test the sequential autocorrelation in a vector. However, the method `wawotest.ltraj`

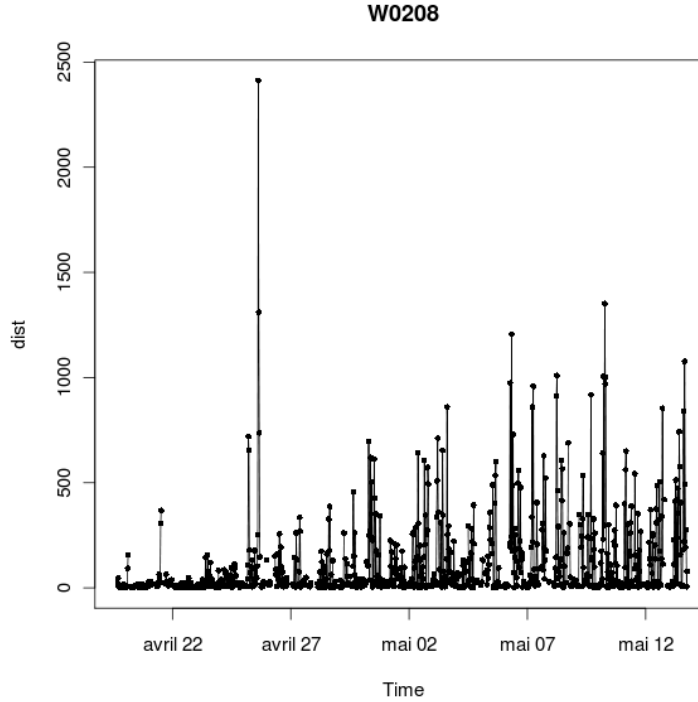
allows to test autocorrelation for the three *linear* parameters `dx`, `dy` and `dist` for each burst in an object of class `ltraj`. For example, consider again the monitoring of movements of the bear:

```
> wawotest(bear)

249 NA removed
249 NA removed
249 NA removed
[[1]]
      dx      dy      dist
a  1.180527e+02  2.089499e+02  405.90227
ea -1.000000e+00 -1.000000e+00  -1.00000
va  8.927603e+02  8.612297e+02  878.76704
za  3.984481e+00  7.154119e+00  13.72629
p   3.381395e-05  4.211076e-13  0.00000
```

Note that this function removes the missing values before the test. The row `p` indicates the P-value of the test. We can see that the three linear parameters are strongly positively autocorrelated. There are periods during which the animal is traveling at large speed and periods when the animals are walking at lower speed. Note that this was already apparent on the graph showing the changes with time of the distance between successive relocations:

```
> plotltr(bear, "dist")
```



This was even clearer on the graph showing the moving average of the distance (with a window of 5 days):

```
> sliwinltr(bear, function(x) mean(na.omit(x$dist)), 5 * 48, type = "locs")
```

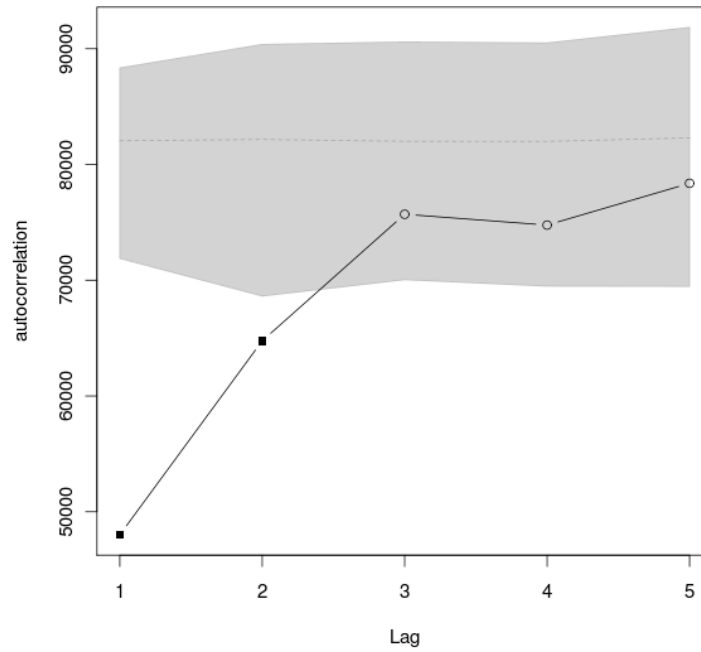
(not executed in this report).

#### 5.4.2 Analyzing the autocorrelation of the parameters

The autocorrelation function (ACF)  $\rho(a)$  measures the correlation between a parameter measured at time  $t$  and the same parameter measured at time  $t - a$  in the same time series (Diggle, 1990). This allows to analyze the autocorrelation, and to identify the scales at which this autocorrelation occurs. Dray et al. (2010) noted that the autocorrelation function measured at lag 1 ( $\rho(1)$ ) is mathematically equivalent to the independence test of Wald and Wolfowitz (1944).

Dray et al. (2010) extended the mathematical bases underlying the ACF to handle the missing data occurring frequently in the trajectories. Their approach is implemented in the function `acfdist.ltraj` (the management of NAs is described in detail on the help page of this function). For example, consider again the monitoring of a brown bear:

```
> acfdist.ltraj(bear, lag = 5, which = "dist")
```



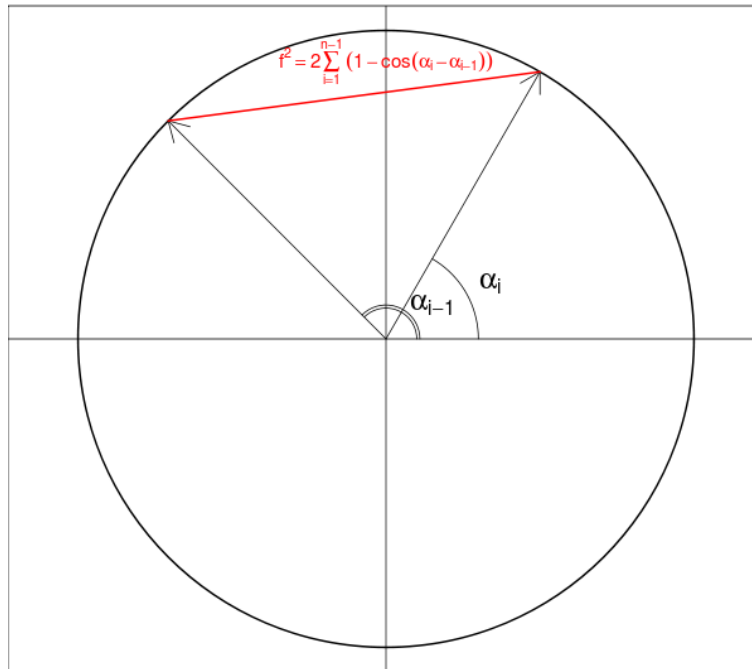
We have calculated here the ACF for the distance for a time lag up to 5 relocations. The interested reader can try to calculate the ACF for trajectories up to 100 relocations to see the cyclic patterns occurring in this trajectory.

#### 5.4.3 Testing autocorrelation of the angles

The test of the autocorrelation of the angular parameters (relative or absolute angles, see section 3.2) is based on the chord distance between successive angles (see Dray et al. 2010 for additional details):



**Criteria f for the measure of independence between successive angles at time i-1 and i**



For example, the function `testang.ltraj` is a randomization test using the mean squared chord distance as a criteria. For example, considering again the trajectory of the bear, we can test the autocorrelation of the relative angles between successive moves:

```
> testang.ltraj(bear, "relative")

[[1]]
Monte-Carlo test
Call: as.randtest(sim = res$sim[-1], obs = res$sim[1], alter = alter)

Observation: 1471.667

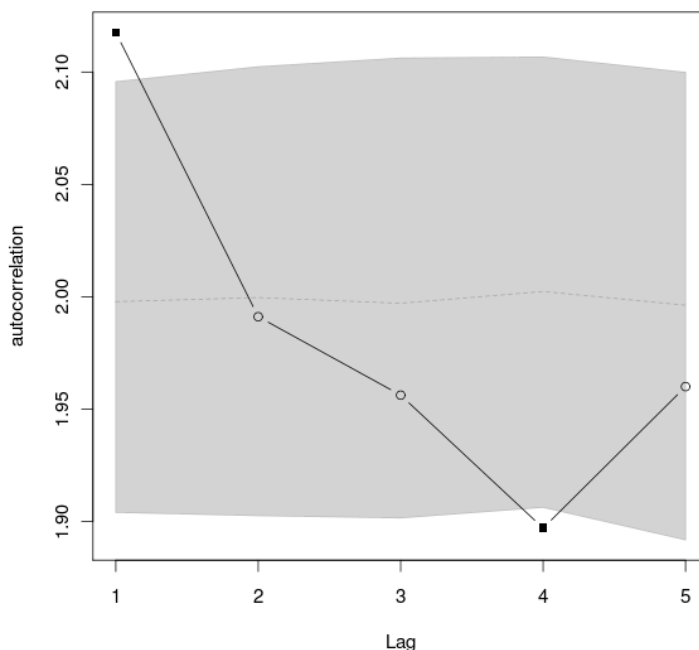
Based on 999 replicates
Simulated p-value: 0.081
Alternative hypothesis: two-sided

      Std.Obs Expectation  Variance
-1.745187 1542.343797 1640.102306
```

#### 5.4.4 Analyzing the autocorrelation of angular parameters

Dray et al. (2010) extended the ACF to angular parameters by considering the chord distance as a criteria to build the ACF. This approach is implemented in the function `acfang.ltraj`. Considering again the `bear` dataset:

```
> acfang.ltraj(bear, lag = 5)
```



We can see that the relative angle observed at time  $i$  is significantly correlated with the angle observed at time  $i - 1$ .

#### 5.5 Partitioning a trajectory into segments characterized by a homogenous behaviour

We implemented a new approach to the partitioning of movement data, relying on a Bayesian partitioning of a sequence. This approach was originally developed in molecular biology, to partition DNA sequences (Gueguen 2001). We describe this approach in this section.

Biologically, a positive autocorrelation in any of the descriptive parameters may mean that the animal behaviour is changing with time (there are periods during which the animal is feeding, other during which the animal is resting,

etc.). The idea is then to partition the trajectory of the animal into homogenous segments.

We will use the movements of a porpoise monitored using an Argos collar to illustrate this method. First we load the data:

```
> data(porpoise)
> gus <- porpoise[1]
> gus
```

```
***** List of class ltraj *****
```

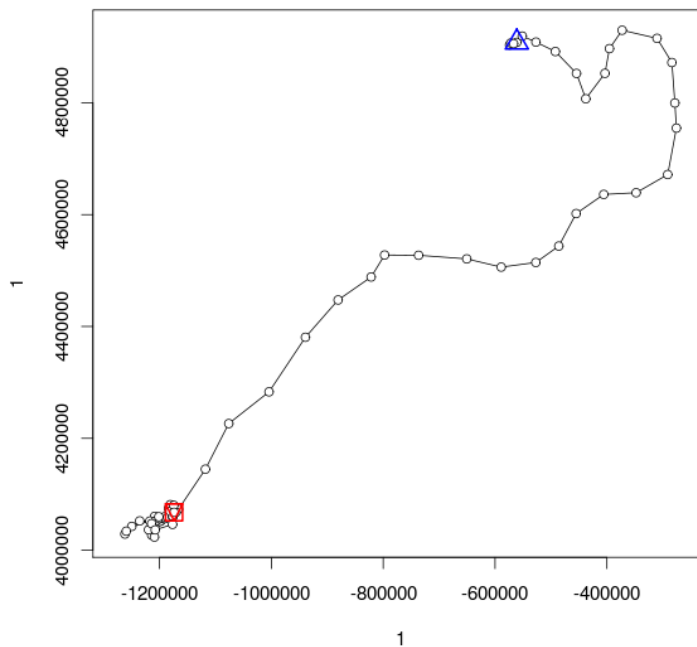
```
Type of the trajct: Type II (time recorded)
Regular trajct. Time lag between two locs: 86400 seconds
```

Characteristics of the bursts:

	id	burst	nb.reloc	NAs	date.begin	date.end
1	GUS	GUS	64	0	2004-01-20 11:00:00	2004-03-23 11:00:00

The trajectory is regular and is built by relocations collected every 24 hours during two months. Plot the data:

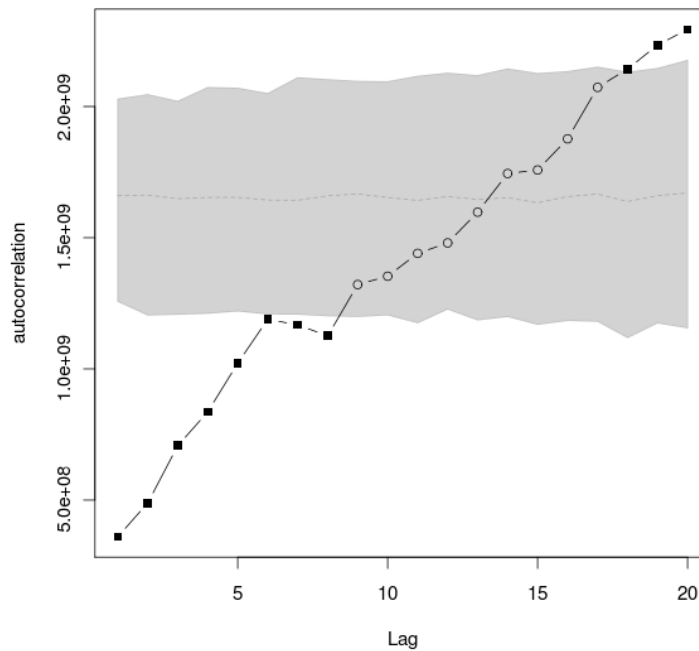
```
> plot(gus)
```



Visually, **the trajectory seems to be built by three segments**. At the very beginning of the trajectory, the animal is performing very short moves. Then, the animal is travelling faster toward the southwest, and finally, the animal is again performing very small moves.

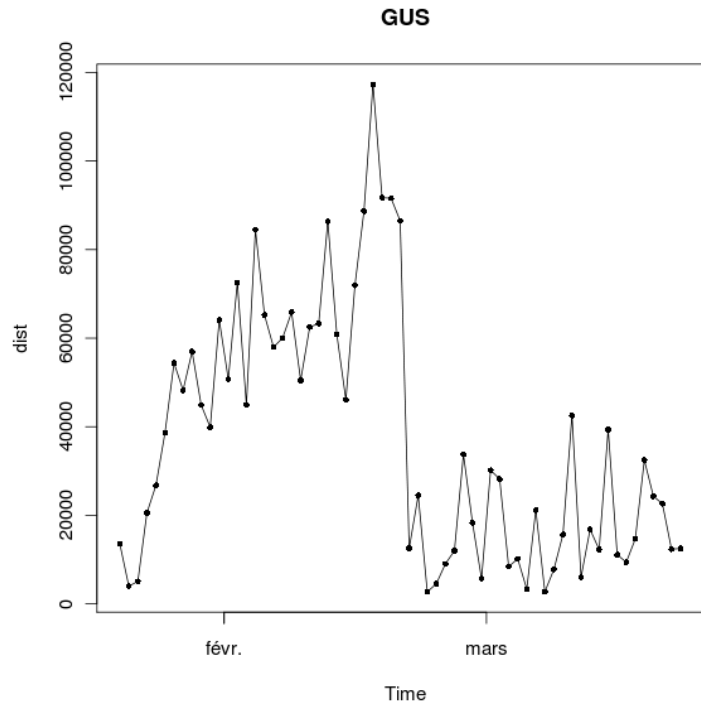
We can draw the ACF for the distance between successive relocations to illustrate the autocorrelation pattern from another point of view:

```
> acfdist.ltraj(gus, "dist", lag = 20)
```



There is a strong autocorrelation pattern present in the data, up to lag 8. We can plot the distances between successive relocations according to the date

```
> plotltr(gus, "dist")
```



Now, let us suppose that the distances between successive relocations have been generated by a normal distribution, with different means corresponding to different behaviours. Let us build 10 models corresponding to 10 values of the mean distance ranging from 0 to 130 km/day:

```
> (tested.means <- round(seq(0, 130000, length = 10), 0))

[1]      0  14444  28889  43333  57778  72222  86667 101111 115556 130000
```

Based on the visual exploration of the distribution of distance, we set the standard deviation of the distribution to 5 km. We can now define 10 models characterized by 10 different values of means and with a standard deviation of 5 km:

```
> (limod <- as.list(paste("dnorm(dist, mean =", tested.means, ", sd = 5000)"))))

[[1]]
[1] "dnorm(dist, mean = 0 , sd = 5000)"

[[2]]
[1] "dnorm(dist, mean = 14444 , sd = 5000)"
```

```

[[3]]
[1] "dnorm(dist, mean = 28889 , sd = 5000)"

[[4]]
[1] "dnorm(dist, mean = 43333 , sd = 5000)"

[[5]]
[1] "dnorm(dist, mean = 57778 , sd = 5000)"

[[6]]
[1] "dnorm(dist, mean = 72222 , sd = 5000)"

[[7]]
[1] "dnorm(dist, mean = 86667 , sd = 5000)"

[[8]]
[1] "dnorm(dist, mean = 101111 , sd = 5000)"

[[9]]
[1] "dnorm(dist, mean = 115556 , sd = 5000)"

[[10]]
[1] "dnorm(dist, mean = 130000 , sd = 5000)"

```

The approach of Gueguen (2001) allows, based on these *a priori* models, to find both the number and the limits of the segments building up the trajectory. Any model can be supposed for any parameter of the steps (the distance, relative angles, etc.), provided that the model is Markovian.

Given the set of *a priori* models, for a given step of the trajectory, it is possible to compute the probability density that the step has been generated by each model of the set. The function `modpartltraj` computes the matrix containing the probability densities associated to each step (rows), under each model of the set (columns):

```

> mod <- modpartltraj(gus, limod)
> mod

*****
* Probabilities computed for a traject
* with the following models:

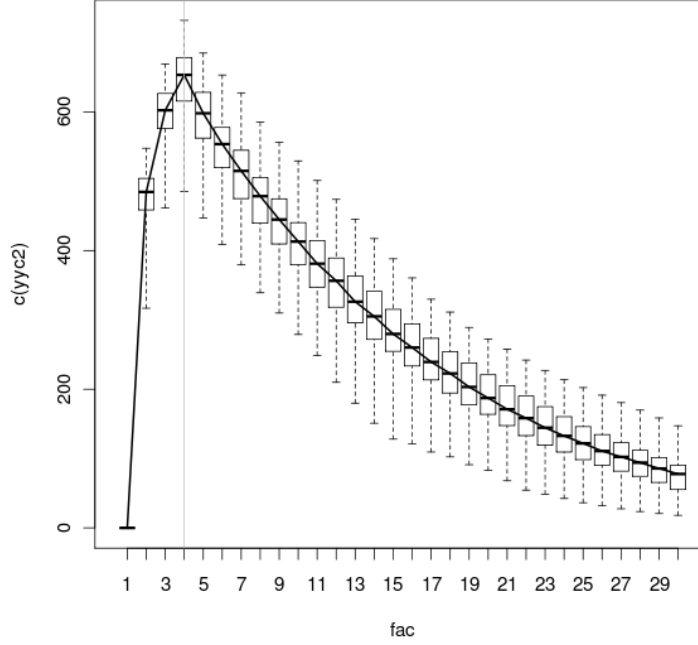
[1] "mod.1" "mod.2" "mod.3" "mod.4" "mod.5" "mod.6" "mod.7" "mod.8"
[9] "mod.9" "mod.10"

```

Then, we can estimate the optimal number of segments in the trajectory, given the set of *a priori* models, using the function `bestpartmod`, taking as argument the matrix `mod`:

```
> bestpartmod(mod)
```

Maximum likelihood for  $K = 4$



This graph presents the value of the log-likelihood (y) that the trajectory is actually made of  $K$  segments (x). Note that this log-likelihood is actually corrected using the method of Gueguen (2001) (which implies the Monte Carlo simulation of the independence of the steps in the trajectory – explaining the boxplots –, see the help page of `bestpartmod` for further details on this procedure). In this case, the method indicates that 4 segments are a reasonable choice for the partitioning. **This is a surprise for us, as we rather expected 3 segments** (actually, the number of segments returned by the function depend on the models supposed *a priori*).

Finally, the function `partmod.1traj` can be used to compute the partition. The mathematical rationale underlying these two functions is the following: given an optimal  $k$ -partition of the trajectory, if the  $i^{th}$  step of the trajectory belongs to the segment  $k$  predicted by the model  $d$ , then either the relocation  $i - 1$  belongs to the same segment, in which case the segment containing  $i - 1$  is predicted by  $d$ , or the relocation  $i - 1$  belongs to another segment, and the other  $(k - 1)$  segments together constitute an optimal  $(k - 1)$  partition of the trajectory  $[1-(i - 1)]$ . These two probabilities are computed recursively by the functions from the matrix `mod`, observing that the probability of a 1-partition

(partition built by one segment) of the trajectory from 1 to  $i$  described by the model  $m$  is simply the product of the probability densities of the steps from 1 to  $i$  under the model  $m$ .

**Remark:** this approach relies on the hypothesis of the independence of the steps within each segment.

Now, use the function `partmod.ltraj` to partition the trajectory of the porpoise into 4 segments:

```
> (pm <- partmod.ltraj(gus, 4, mod))
```

Number of partitions: 4

Partition structure:

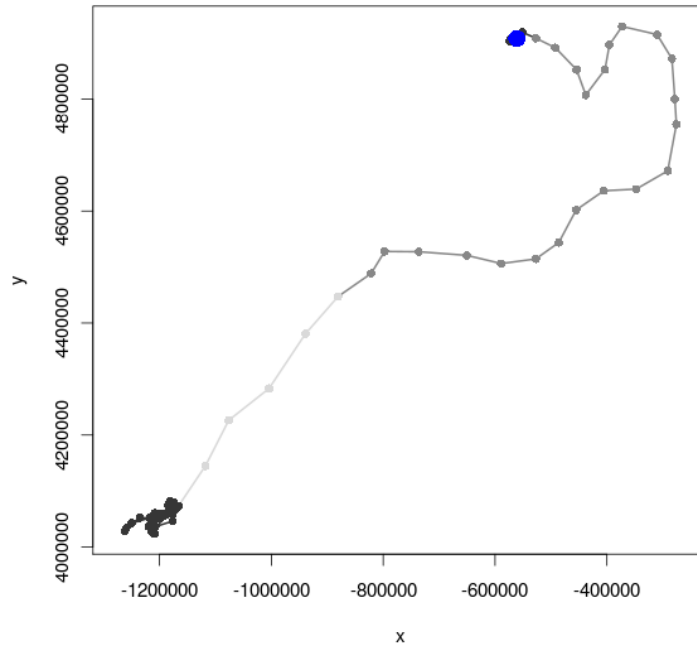
	relocation	Num	Model
1	1	---	-----
2		2	mod.2
3	6	---	-----
4		5	mod.5
5	28	---	-----
6		8	mod.8
7	33	---	-----
8		2	mod.2
9	64	---	-----

The segments are contained in the component `$ltraj` of the list

We can see that the models at the beginning of the trajectory and at the end of the trajectory are the same. Have a look at this partition:

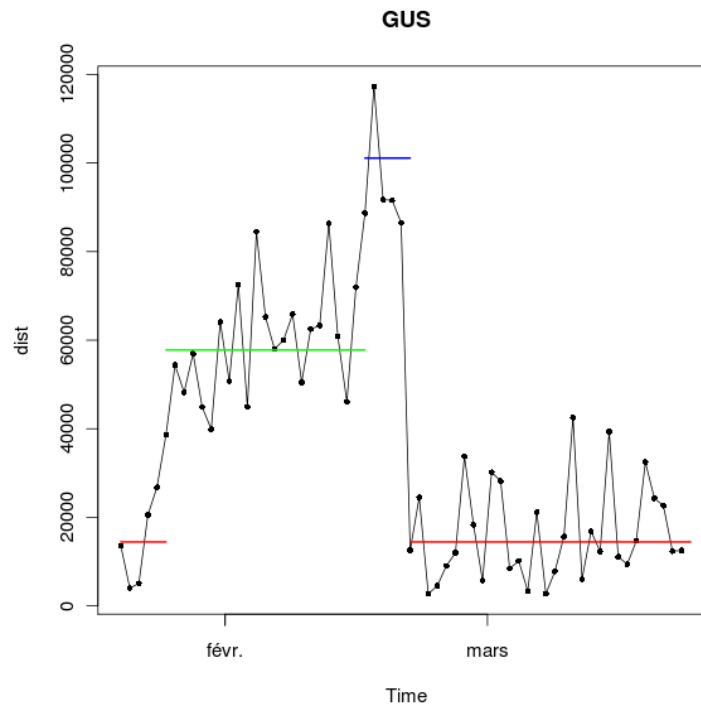
```
> plot(pm)
```





This is very interesting: we already noted that the movements at the very beginning and the end of the trajectory were much slower than the rest of the trajectory, and this is confirmed by this partition. However, this partition illustrates a change of speed at the middle of the “migration”. The end of the migration is much faster than the beginning. This is clearer on the graph showing the changes in distance between successive relocations with the date. Let us plot this graph together with the partition:

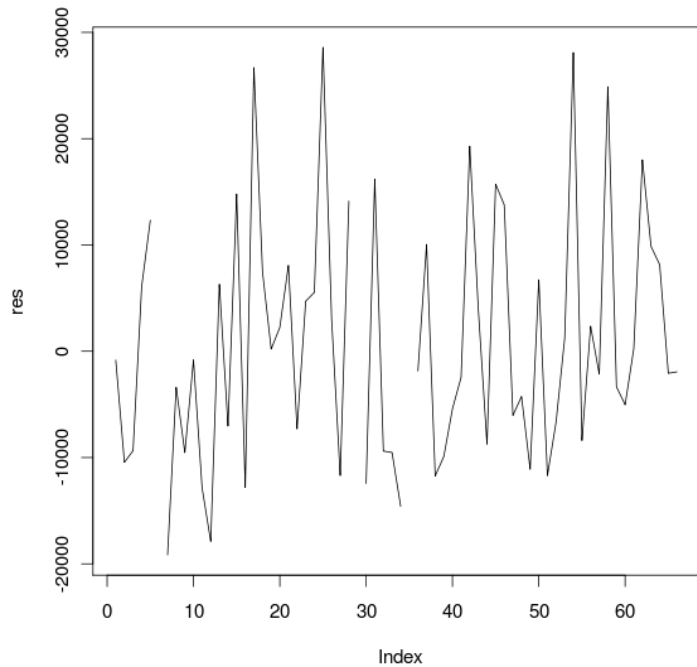
```
> plotltr(gus, "dist")
> tmp <- lapply(1:length(pm$ltraj), function(i) {
+   coul <- c("red", "green", "blue")[as.numeric(factor(pm$stats$mod))[i]]
+   lines(pm$ltraj[[i]]$date, rep(tested.means[pm$stats$mod[i]],
+     nrow(pm$ltraj[[i]])), col = coul, lwd = 2)
+ })
```



The end of the migration is nearly two times faster than the beginning of the migration.

To conclude, have a look at the residuals of this partitionning:

```
> res <- unlist(lapply(1:length(pm$ltraj), function(i) {
+   pm$ltraj[[i]]$dist - rep(tested.means[pm$stats$mod[i]], nrow(pm$ltraj[[i]]))
+ })))
> plot(res, ty = "l")
```



And a Wald and Wolfowitz test suggests that the residuals of this partition are independent, confirming the validity of the approach:

```
> wawotest(res)
4 NA removed
      a      ea      va      za      p
-5.4712718 -1.0000000 59.2571538 -0.5808456 0.7193277
```

## 5.6 Models of animal movements

Several movement models have been proposed in the litterature to describe animal movements. The package **adehabitatLT** contains several functions allowing to simulate these models. Such simulations can be very useful to test hypotheses concerning a trajectory, because all the descriptive parameters of the steps are also generated by the functions. Actually, the package proposes 6 functions to simulate such models:

- **simm.brown** can be used to simulate a Brownian motion;
- **simm.crw** can be used to simulate a correlated random walk. This model has been often used to describe animal movements (Kareiva and Shigesada 1983);

- `simm.mba` can be used to simulate an arithmetic Brownian motion (with a drift parameter and a covariance between the coordinates, see Brillinger et al. 2002);
- `simm.bb` can be used to simulate a Brownian bridge motion (i.e. a Brownian motion constrained by a fixed start and end point);
- `simm.mou` can be used to simulate a bivariate Ornstein-Uhlenbeck motion (often used to describe the sedentarity of an animal, e.g. Dunn and Gipson 1977);
- `simm.levy` can be used to simulate a Levy walk, as described (Bartumeus et al. 2005).

All these functions return an object of class `ltraj`. For example, simulate a correlated random walk built by 1000 steps characterized by a mean cosine of the relative angles equal to 0.95 and a scale parameter for the step length equal to 1 (see the help page of `simm.crw` for additional details on the meaning of these parameters):

```
> sim <- simm.crw(1:1000, r = 0.95)
> sim
```

```
***** List of class ltraj *****
```

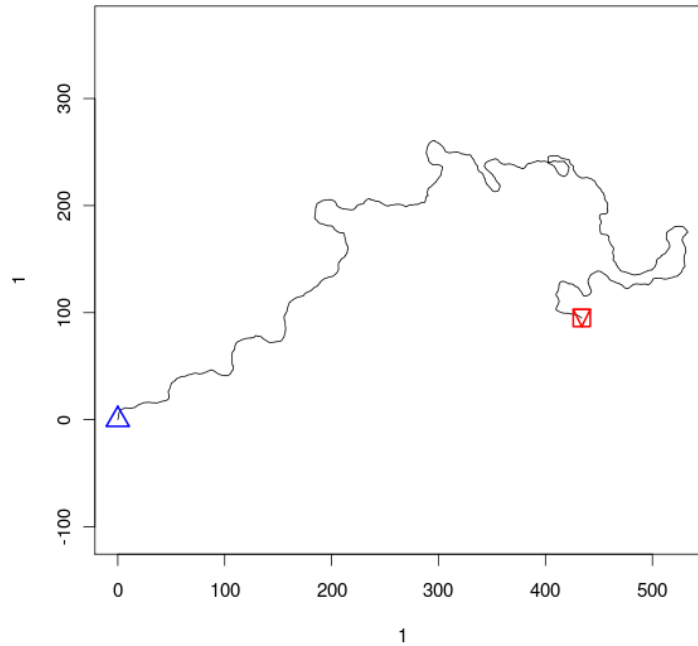
```
Type of the traject: Type II (time recorded)
Regular traject. Time lag between two locs: 1 seconds
```

```
Characteristics of the bursts:
```

	id	burst	nb.reloc	NAs	date.begin	date.end
1	A1	A1	1000	0	1970-01-01 01:00:01	1970-01-01 01:16:40

Note that the vector `1:1000` passes as an argument is considered here as a vector of dates (it is converted to the class `POSIXct` by the function, see section 3.4 for more details on this class). Other dates can be passed to the functions. Have a look at the simulated trajectory:

```
> plot(sim, addp = FALSE)
```



## 6 Conclusion and perspectives

Several other methods can be used to analyze a trajectory. Thus, the first passage time method, developed by Fauchald and Tveraa (2003) to identify the areas where *area restricted search* occur is implemented in the function `fpt`. Several methods are available in the package `adehabitatHR` to estimate a home range based on objects of class `ltraj`. Thus, the Brownian bridge kernel method (Bullard 1999, Horne et al. 2007) and the product kernel algorithm (Keating and Cherry 2009) are implemented in the functions `kernelbb` and `kernelkc` respectively.

But one thing is important: at many places in this vignette, we have noted that the descriptive parameters of the steps can be analysed as a (possibly multiple) time series. The R environment provides many functions to perform such analyses, and **we stress that the package `adehabitatLT` should be considered as a springboard toward such functions.**

We included in the package `adehabitatLT` several functions allowing the analysis of animal movements. All the brother packages `adehabitat*` contain a vignette similar to this one, which explains not only the functions, but also in

some cases the philosophy underlying the analysis of animal space use.

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