

[My Courses](#) / [My courses](#) / [Algorithms and Data Structures, MSc \(Spring 2023\)](#) / [Exercise Quizzes](#)

/ [Week 9: Amortized Analysis](#)

Started on Wednesday, 29 March 2023, 18:14

State Finished

Completed on Wednesday, 29 March 2023, 18:15

Time taken 1 min 54 secs

Grade 7.00 out of 7.00 (100%)

Question 1

Correct

Mark 1.00 out of 1.00

Assume I have a function $f(\text{int } K)$ that runs in amortized logarithmic time in K , but linear worst case time. What is the running time of:

```
# python 3
for i in range(N):
    f(N)
```

```
// java
for (int i = 0; i < N; i=i+1)
    f(N)
```

Select one:

- ☐ a. Impossible to say from the information given
- ☐ b. Linear in N
- ☒ c. Linerarithmic in N
- ☐ d. Quadratic in N



Your answer is correct.

The correct answer is: Linerarithmic in N

Question 2

Correct

Mark 1.00 out of 1.00

Assume I have a function $f(\text{int } K)$ that runs in amortized constant time in K , but logarithmic worst case time. What is the running time of

```
# python 3
for i in range(N):
    f(N)
```

```
// java
for (int i = 0; i < N; i=i+1)
    f(N)
```

Select one:

- ☐ a. Linearithmic in N
- ☒ b. Linear in N
- ☐ c. Quadratic in N
- ☐ d. Impossible to say from the information given



Your answer is correct.

The correct answer is: Linear in N

Question 3

Correct

Mark 1.00 out of 1.00

Assume I have a function $f(\text{int } K)$ that runs in amortized constant time in K , but linear worst case time. What is the running time of

```
# python 3
for i in range(N):
    f(N)
```

```
// java
for (int i = 0; i < N; i=i+1)
    f(N)
```

Select one:

- ☐ a. Impossible to say from the information given
- ☐ b. Quadratic in N
- ☒ c. Linear in N
- ☐ d. Linearithmic in N



Your answer is correct.

The correct answer is: Linear in N

For the questions on this page consider below class Y:

```
public class Y<Key extends Comparable<Key>>
{
    private Key[] A = (Key[]) new Comparable[1];
    private int lo, hi, N;

    public void insert(Key in)
    {
        A[hi] = in;
        hi = hi + 1;
        if (hi == A.length) hi = 0;
        N = N + 1;
        if (N == A.length) rebuild();
    }

    public Key remove() // assumes Y is not empty
    {
        Key out = A[lo];
        A[lo] = null;
        lo = lo + 1;
        if (lo == A.length) lo = 0;
        N = N - 1;
        return out;
    }

    private void rebuild()
    {
        Key[] tmp = (Key[]) new Comparable[2*A.length];
        for (int i = 0; i < N; i++ )
            tmp[i] = A[(i + lo) % A.length];
        A = tmp;
        lo = 0;
        hi = N;
    }
}
```

Question 4

Correct

Mark 1.00 out of 1.00

What is the amortized number of array accesses per operation in a sequence of k `Y.insert` operations beginning in an empty data structure?

Select one:

- ☒ a. Constant
- ☐ b. Quadratic in K
- ☐ c. Linearithmic in K
- ☐ d. Linear in K



Your answer is correct.

The correct answer is: Constant

Question 5

Correct

Mark 1.00 out of 1.00

What is a best bound on the number of array accesses **per operation** in the following sequence of $2k$ operations, starting from an empty data structure:

```
y.insert(1);  
y.remove();  
y.insert(2);  
y.remove();  
y.insert(3);  
y.remove();  
...  
y.insert(k);  
y.remove();
```

Select one:

- ☐ a. linear in k in the worst case and in the amortized sense
- ☒ b. Constant in the worst case
- ☐ c. Quadratic in the worst case
- ☐ d. Constant in the amortized sense, but linear in the worst case



Your answer is correct.

The correct answer is: Constant in the worst case

For the questions on this page consider the following class:

```
public class X<Key extends Comparable<Key>>
{
    private Key[] A = (Key[]) new Comparable[1];
    private int N = 0;

    public void insert(Key in)
    {
        A[N] = in;
        N = N + 1;
        if (N == A.length) rebuild();
    }

    public Key remove() // assumes X is not empty
    {
        // search for maximum key:
        int max = 0;
        for (int i = 1; i < N; i++)
            if (A[i].compareTo(A[max]) > 0)
                max = i;
        // exchange with last element:
        Key tmp = A[max];
        A[max] = A[N-1];

        N = N - 1;
        return tmp;
    }

    private void rebuild()
    {
        Key[] tmp = (Key[]) new Comparable[2*A.length];
        for (int i = 0; i < N; i++ )
            tmp[i] = A[i];
        A = tmp;
    }
}
```

Question 6

Correct

Mark 1.00 out of 1.00

What is the amortized number of array accesses per operation in a sequence of k insert operations beginning in an empty data structure?

Select one:

- ☐ a. Linear in k
- ☒ b. Constant
- ☐ c. Linearithmic in k
- ☐ d. Quadratic in k



Your answer is correct.

The correct answer is: Constant

Question 7

Correct

Mark 1.00 out of 1.00

What is the amortized number of array accesses per operation in a sequence of k remove operations beginning in a data structure with k elements?

Select one:

- ☐ a. Linearithmic in k
- ☐ b. Constant
- ☐ c. Quadratic in k
- ☒ d. Linear in k



Your answer is correct.

The correct answer is: Linear in k