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#### Information

These questions reiterate previous material about the analysis of algorithms.

#### Question 1

Answer saved

Marked out of 1.00

Compute, preferably in your head,  $(\log_2(2^{1000} \cdot 8^{100}))$ .

Answer:

#### Question 2

Answer saved

Marked out of 1.00

Whenever a new, eagerly awaited volume of the epic multi-volume young adult fantasy saga *À La Recherche du Temps Perdu* hits the bookstores, young Marcel re-reads all the previous volumes in preparation. Alas, typically he falters in his resolve and only manages half of them. To be precise, when volume  $(i + 1)$  arrives, he re-reads volumes  $1, \dots, \lceil i/2 \rceil$ .

How many books has he read (including re-reads) when the  $n$ th volume is published? (Among the big-Oh estimates, choose the smallest one.)

- ☐ a.  $O(\log n)$
- ☐ b.  $O(\sqrt{n})$
- ☐ c.  $O(n)$
- ☐ d.  $O(n \log n)$
- ☒ e.  $O(n^2)$

[Clear my choice](#)







Question 3

Answer saved

Marked out of 1.00

Pick, for each sum, the same expression in  $\cdots$ -notation, its closed form or approximation, and a useful way to remember that closed form.

(Correction: The sum on the top left should say  $\sum_{i=0}^n \frac{1}{2^i}$ , i.e., run from  $i = 0$  rather than  $i = 1$ .)

$\sum_{i=1}^n \frac{1}{2^i}$	<div><math>1 + 2 + 4 + 8 + \cdots + 2^n</math></div>	<div><math>\sim 2</math></div>	<div></div>
$\sum_{i=1}^n 1$	<div><math>1 + 2 + 3 + \cdots + n</math></div>	<div><math>= n</math></div>	<div></div>
$\sum_{i=1}^n i$	<div><math>1 + 1 + \cdots + 1</math></div>	<div><math>\sim \frac{1}{2}n^2</math></div>	<div></div>
$\sum_{i=0}^n 2^i$	<div><math>\frac{1}{1} + \frac{1}{2} + \frac{1}{4} + \frac{1}{8} + \cdots + \frac{1}{2^n}</math></div>	<div><math>= 2^{n+1} - 1</math></div>	<div></div>
$\sum_{i=1}^n n$	<div><math>n + n + \cdots + n</math></div>	<div><math>= n^2</math></div>	<div></div>
$\sum_{i=1}^n \frac{1}{i}$	<div><math>\frac{1}{1} + \frac{1}{2} + \frac{1}{3} + \frac{1}{4} + \frac{1}{5} + \cdots + \frac{1}{n}</math></div>	<div><math>\sim \ln n</math></div>	<div></div>

