

As you observe the timings for Hanoi, what do you notice? Is this a performance class we have seen before or a different one? How would you describe the rate at which the runtime of Hanoi is increasing? No formal analysis is necessary here; just describe what you see and what is causing it. Including `Delimiter_Check`, we have now seen several examples of python programs that accept arguments/parameters when they are invoked on the command line. Describe how you could employ this together with factory method infrastructure provided by `Deque_Generator`, to allow a deque, stack or queue program to use either an array-based deque or linked list-based deque depending how it is invoked from the command line. Finally, describe the process through which you tested Hanoi and `Delimiter_Check` to ensure that they function correctly.

The performance of Hanoi is exponential,  $O(2^n)$  which we have not seen before in previous projects. The number of steps can be computed by -- the number of steps of  $n-1 + 2^n$  -- this is likely due to the recursion. Each new step involves doing all the steps of  $n-1$  and additional steps of  $2^n$ .

We can make a constructor that is similar to the `Deque_Generator`

```
Linked_List = 0
```

```
Array = 1
```

```
def __init__(self, type):
```

```
    self.type = type
```

```
    self.__dq = get_deque(type)
```

This way we can change which type of stack, queue, or deque we want, whether it be array or linked list by choosing 0 or 1.

For testing `Delimiter_Check`, I made a few files where some were supposed to be correct, and some were supposed to cause errors and ran it through the program. The results returned were exactly what I was looking for.

For testing Towers of Hanoi, I recorded the average time it took to run  $n=1$ ,  $n=2$ ,  $n=3$ ,  $n=4$ ,  $n=5$  and compared them. My computer is pretty slow so the timing was inconsistent, but after multiple trials it was clear that the performance was, for the most part, exponential. I also counted the steps printed and it was clearly exponential. Additionally, I followed through the printed steps of Hanoi and it matched what I was expected (for example  $n=3$  was identical to the described result in the project instruction)