

'votess: A fast, multi-target voronoi tessellator using the SYCL framework'

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Statement of need

Voronoi tessellation is a fundamental spatial decomposition technique widely used in scientific domains such as astrophysics [], earth sciences [], materials science [], and biochemistry []. It enables the partitioning of space into regions based on proximity to given points, which is essential for analyzing large datasets. Although performing Voronoi tessellations on large datasets has been feasible for some time, the increasing complexity and size of modern data have underscored the need for faster, more efficient computation. With the rise of accelerator architectures like GPUs and FPGAs, the computational power available today has greatly improved the ability to handle these large datasets more effectively.

However, despite these advancements, most existing implementations of Voronoi tessellations are tailored to specific platforms and architectures, limiting their portability. This results in the need for bespoke solutions for different hardware setups, creating inefficiencies and increasing development time.

To address this problem, votess provides a portable solution that can operate across various accelerator architectures, without modification to the source code, enabling developers within various scientific fields to be able to make use of the new computing architectures.

!! be explicit that votess provides such portable solution compared to the ray18 reference implementation (focusing on cpu+cuda?)

Summary

votess is a library for performing 3D Voronoi tessellations on heterogeneous platforms via the SYCL framework. votess was designed to be portable yet performant, with an easy-to-use interface.

The underlying algorithm is based on a paper (?), which highlights that many applications, such as in astrophysics [] or fluid simulations [], only require the geometry of the Voronoi cells and their neighboring information, rather than a full combinatorial mesh data structure. This observation allows for a simplified algorithm, as presented here, which avoids the need for classical mesh-based approaches like the Bowyer-Watson algorithm.

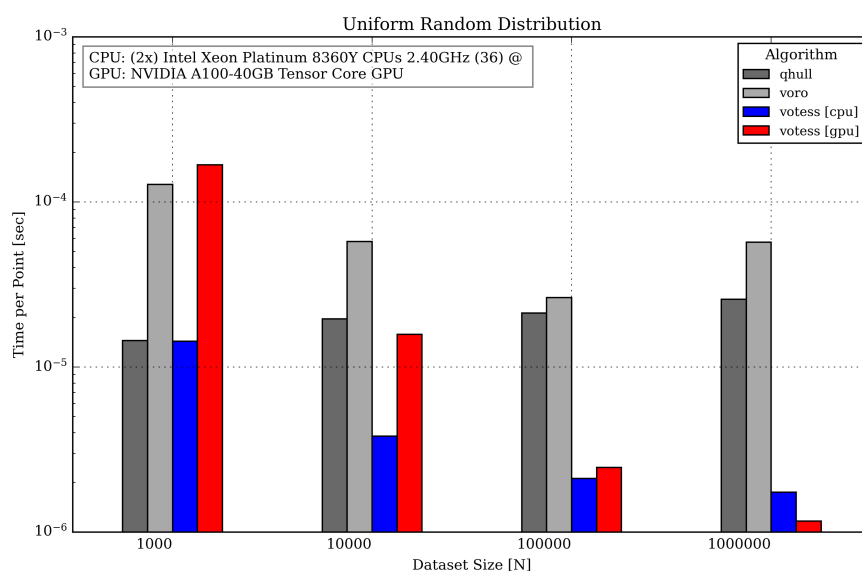
The core algorithm employed by votess consists of two main steps. First, the input set of points is sorted into a grid, and a k-nearest neighbors search is performed. Once the nearest neighbors are identified for each point, the Voronoi cell is computed by iteratively clipping a bounding box using the perpendicular bisectors between the point and its neighbors. To optimize the process and avoid iterating through all neighbors, a security radius condition is applied. If a Voronoi cell cannot be validated, a CPU fallback mechanism is used to ensure robustness.

This efficient algorithm allows for independent thread execution, making it highly suitable for GPU parallelism. Unlike previous algorithms that relied on sequential execution due to their mesh insertion methods [], votess leverages the independence of cell computations to achieve significant speedups in parallel environments.

Performance

With a working implementation of votess, it can be seen that it outperforms several single-threaded applications:

In Figure 1, we show the performance of votess compared to two other single-threaded Voronoi tessellation libraries: Qhull and Voro++. Qhull is a well-known computational geometry library that constructs convex hulls and Voronoi diagrams using an indirect projection method (Barber et al., 1996), while Voro++ is a C++ library specifically designed for three-dimensional Voronoi tessellations, utilizing a cell-based computation approach that is well-suited for physical applications (?, ++).



It can be seen that performance is best on larger datasets. The CPU implementation outperforms other applications of at least tenfold, and at most a hundred fold on large datasets. It must be noted, that the benchmarks were taken before either the CPU and GPU implementations have recieved optimizations.

There also exists other multithreaded Voronoi tesellelation codes, such as ParVoro++ (Wu et al., 2023), CGAL (The CGAL Project, 2018), and GEOGRAM (Inria, 2018), which are also widely used in large-scale computational geometry applications.

Features

votess provides a versatile and efficient tool for computing Voronoi tessellations, supporting multiple output formats including neighbor information for each Voronoi cell. It has been tested on various CPU and GPU architectures, delivering high performance on both platforms.

Users can leverage votess in three ways: through the C++ library, a command-line interface clvotess, and a Python interface pyvotess. The C++ library offers a simple interface with a primary function, tessellate, that computes the tessellation. Additionally, users can select the

68 target device to run said tessellation. The Python wrapper, pyvotess, mirrors the functionality
69 of the C++ version, providing the same ease of use for Python-based workflows.

70 To fine-tune the behavior of votess, the class vtargs is provided, allowing users to adjust
71 parameters much like `std::unordered_map` from the STL. These parameters can be used to
72 optimize runtime performance if needed. The tessellate function outputs a templated class
73 `dnn`, representing a 2D jagged array of neighbors contributing to each particle's Voronoi cell of
74 the sorted input dataset, as managed via `vtargs`.

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