

‘votess: A fast, multi-target voronoi tessellator using the SYCL framework’

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Statement of need

Voronoi tessellation is a fundamental spatial decomposition technique enabling the partitioning of space into regions based on proximity to a discrete set of points, and is widely used in scientific domains such as astrophysics (Springel, 2010), earth sciences [], materials science [], and biochemistry []. Although performing Voronoi tessellations on large datasets has been feasible for some time, the increasing complexity and size of modern data have underscored the need for faster, more efficient computation. With the rise of powerful many-core CPU and GPU architectures, the computational power available today has greatly improved the ability to handle these large datasets more effectively.

However, despite these advancements, most existing implementations of Voronoi tessellations are tailored to specific processor architectures and platforms, limiting their portability. This results in the need for bespoke solutions for different hardware setups, creating inefficiencies and increasing development time. Additionally, many classic insertion algorithms do not fully leverage the performance potential of multi-core systems, further highlighting the need of a modern solution.

To address this problem, votess provides a portable solution that can operate across various accelerator architectures, without modification to the source code, enabling developers within various scientific fields to be able to make use of the new computing architectures.

To address this problem, votess leverages a SYCL single-source framework abstraction to provide a portable solution that runs efficiently across multiple accelerator architectures, including CPUs and GPUs, without requiring modifications to the source code.

Summary

votess is a library for performing parallel 3D Voronoi tessellations on heterogeneous platforms via the SYCL framework. votess was designed to be portable yet performant, with an easy-to-use interface.

The underlying algorithm is based on a paper (?), which highlights that many applications, such as in astrophysics [] or fluid simulations [], only require the geometry of the Voronoi cells and their neighboring information, rather than a full combinatorial mesh data structure. This observation allows for a simplified algorithm, as presented here, which avoids the need for classical mesh-based approaches like the Bowyer-Watson algorithm.

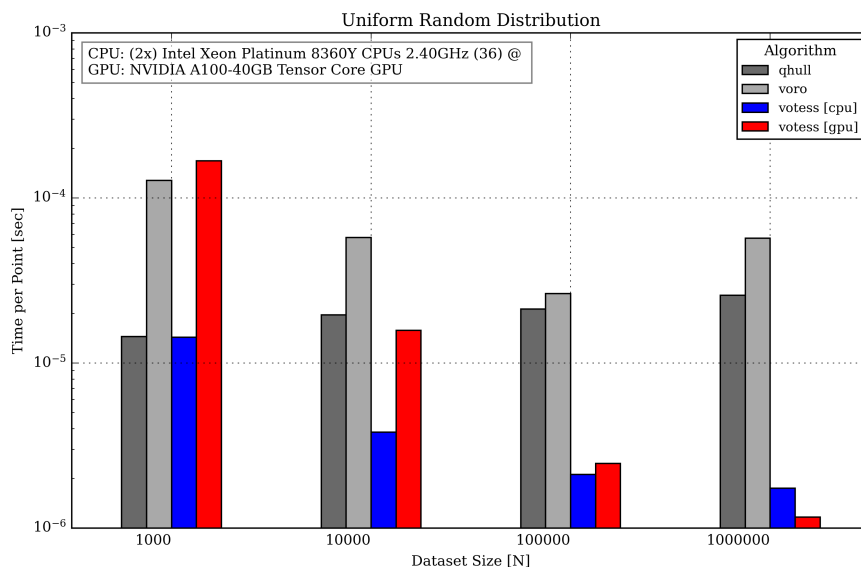
The core algorithm employed by votess consists of two main steps. First, the input set of points is sorted into a grid, and a k-nearest neighbors search is performed. Once the nearest neighbors are identified for each point, the Voronoi cell is computed by iteratively clipping a bounding box using the perpendicular bisectors between the point and its neighbors. To

40 optimize the process and avoid iterating through all neighbors, a security radius condition is
41 applied. If a Voronoi cell cannot be validated, a CPU fallback mechanism is used to ensures
42 robustness.

43 This efficient algorithm allows for independent thread execution, making it highly suitable for
44 GPU parallelism. Unlike previous algorithms that relied on sequential execution due to their
45 mesh insertion methods [], votess leverages the independence of cell computations to achieve
46 significant speedups in parallel environments. ## Performance

47 With a working implementation of votess, it can be seen that it outperforms several single-
48 threaded applications:

49 In Figure 1, we show the performance of votess compared to two other single-threaded Voronoi
50 tessellation libraries: QHULL and VORO++. QHULL is a well-known computational geometry library
51 that constructs convex hulls and Voronoi diagrams using an indirect projection method (Barber
52 et al., 1996), while Voro++ is a C++ library specifically designed for three-dimensional Voronoi
53 tessellations, utilizing a cell-based computation approach that is well-suited for physical
54 applications (Rycroft, 2009).



55 Here, it is clear votess performs best on large datasets. The CPU implementation outperforms
56 other applications of atleast tenfold, and at most a hundred fold on large datasets. It must be
57 noted, that the benchmarks were taken before either the CPU and GPU implementations have
58 recieved optimizations.

60 There also exists other multithreaded Voronoi teselletion codes, such as ParVoro++ (Wu et
61 al., 2023), CGAL (The CGAL Project, 2018), and GEOGRAM (Inria, 2018), and although they do
62 not natively support GPU architectures, they are also widely used in large-scale computational
63 geometry applications.

64 Features

65 votess provides a versatile and efficient tool for computing Voronoi tessellations, supporting
66 multiple output formats including neighbor information for each Voronoi cell. It has been
67 tested on various CPU and GPU architectures, delivering high performance on both platforms.

68 Users can leverage votess in three ways: through the C++ library, a command-line interface
69 clvotess, and a Python interface pyvotess. The C++ library offers a simple interface with a

70 primary function, `tessellate`, that computes the tessellation. Additionally, users can select the
71 target device to run said tessellation. The Python wrapper, `pyvotess`, mirrors the functionality
72 of the C++ version, providing the same ease of use for Python-based workflows.

73 To fine-tune the behavior of `votess`, the class `vtargs` is provided, allowing users to adjust
74 parameters much like `std::unordered_map` from the STL. These parameters can be used to
75 optimize runtime performance if needed. The `tessellate` function outputs a templated class
76 `dnn`, representing a 2D jagged array of neighbors contributing to each particle's Voronoi cell of
77 the sorted input dataset, as managed via `vtargs`.

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