

# Multispectral Extended Depth-of-Field Imaging via Stochastic Wavefront Optimization

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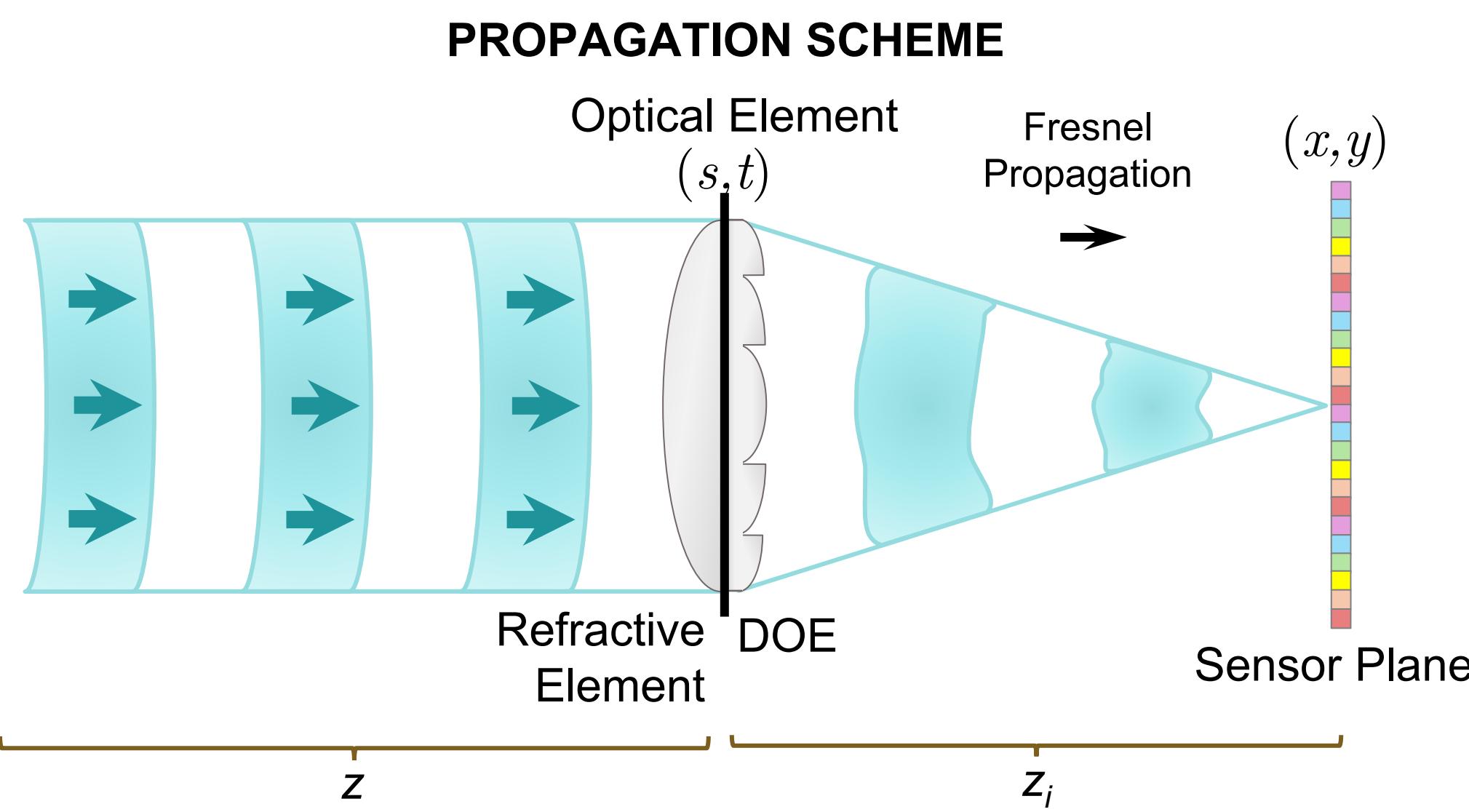
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## INTRODUCTION

We propose a wavefront coding approach using a diffractive optical element (DOE) optimized via stochastic methods to achieve **multispectral (MS) extended depth-of-field (EDoF)**. Our simulation-driven design improves both spectral fidelity and depth invariance, and it is compared against three state-of-the-art designs: the cubic phase mask [1], End-to-End (E2E) design [2], and Hardware-in-the-Loop (HIL) design [3].

## SENSING MODEL



The acquisition of our system captures a blur measurement given by

$$\bar{\mathbf{X}}_{\lambda,z} = \text{PSF}_{\lambda,z} * \mathbf{X}_{\lambda,z} + \Omega_{\lambda,z},$$

where  $\mathbf{X}_{\lambda,z} \in \mathbb{R}^{M \times N \times L \times Z}$  represents the spectral-depth datacube, with M and N as spatial dimensions, L as the spectral dimension, and Z as depth for a single spectral band at a depth z. The operator  $*(\cdot)$  denotes convolution, corresponds to the 4D point spread function (PSF), and  $\text{PSF}_{\lambda,z} = |\mathcal{F}\{\mathbf{Q}_{\lambda,z}(s,t)\}|^2$  is the PSF for each spectral-depth. Here,  $\mathcal{F}(\cdot)$  denotes the Fourier transform,  $\mathbf{Q}_{\lambda,z}(s,t)$  represents the generalized pupil function, and  $\Omega_{\lambda,z}$  represents the additive noise. The DOE phase mask is defined by

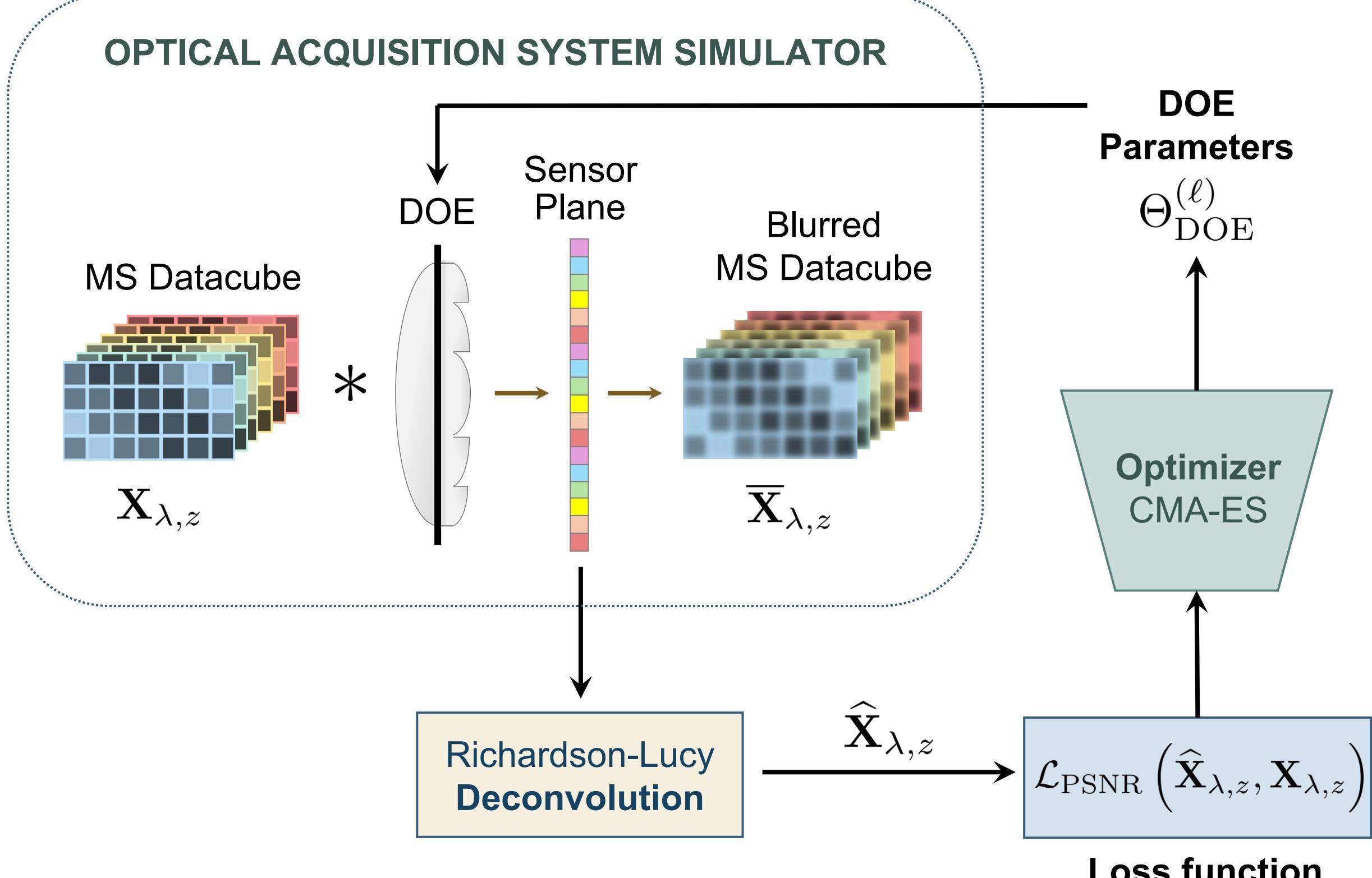
$$h(s,t) = \alpha(s^3 + t^3) + \sum_{p=1}^{14} \rho_p Z_p(s,t),$$

where  $Z_p(s,t)$  are the p<sup>th</sup> Zernike Polynomial with coefficient  $\rho_p$  to be estimated, and  $\alpha$  is the cubic phase coefficient.

## METHODS

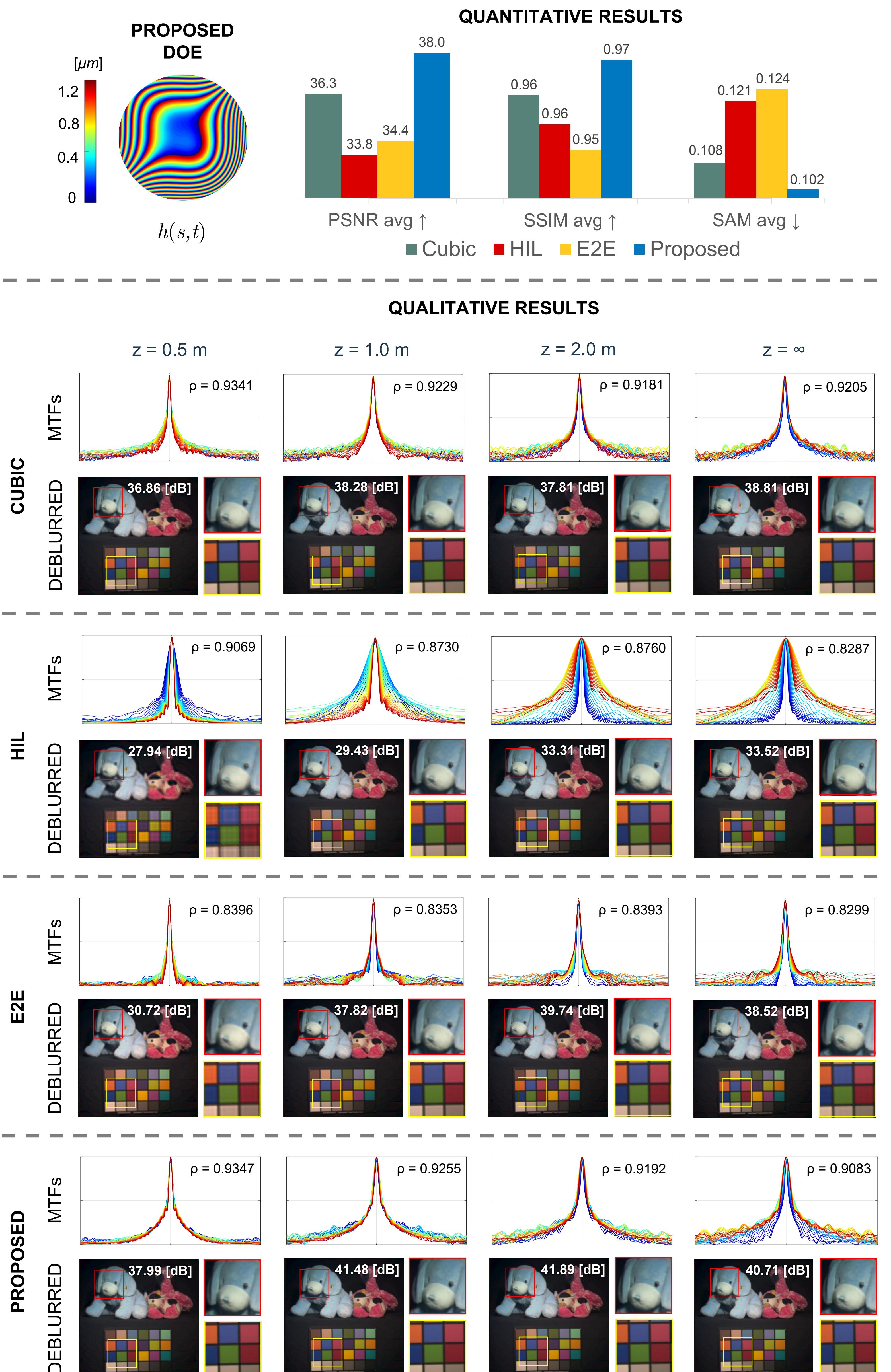
We simulate a multispectral imaging system where a DOE modulates the wavefront before image formation. The DOE phase is optimized using the CMA-ES algorithm to maximize reconstruction quality based on PSNR [2]. The pipeline includes Fresnel propagation, Richardson-Lucy deconvolution for evaluation, PSNR loss and CMA-ES optimizer. The set of parameters to be optimized is given by

$$\Theta_{DOE} = (\alpha, \rho_1, \dots, \rho_P).$$



## RESULTS

Spatial and spectral quantitative and qualitative comparison between three state-of-the-art DOEs and the proposed DOE design. Metrics include averaged PSNR, SSIM, and SAM (Cave dataset), as well as Pearson's correlation coefficient ( $\rho$ ) for similarity between modulation transfer functions (MTFs).



## CONCLUSIONS

The proposed stochastic optimization framework enables the design of a DOE that enhances both spatial and spectral fidelity while extending depth-of-field. It **outperforms state-of-the-art methods across multiple metrics and imaging conditions**. This approach is simulation-driven and compatible with various multispectral sensor architectures.



## REFERENCES

- [1] Dowski Jr, et al. "Extended depth of field through wave-front coding." *Applied optics* 34.11 (1995).
- [2] Akpinar, et al. "Learning wavefront coding for extended depth of field imaging." *IEEE TIP* (2021).
- [3] Pinilla, et al. "Miniature color camera via flat hybrid meta-optics." *Science Advances* 9.21 (2023).

