EXPERIMENTAL DATA COLLECTION AND DESCRIPTIVE STATISTICS PART- II

Submitted by

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I Nelson Joseph did not give or receive any assistance on this project, and the report submitted is wholly on my own.

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Introduction

Examining real-world data is the major goal of the research. I investigated and analysed two different sets of actual data for this investigation. Dataset 1 includes a sample of 100 people's US shoe sizes. Dataset 2 examined the time difference between two students who entered the library through the main door and was collected at the University of Texas at Arlington Central Library. The data is statistically aggregated and presented to help understand the trend of the population based on the sample. The information from the descriptive statistics is utilized in the Chi-square Goodness of Fit-Test. Data classes with enough observations are grouped together. The number of observations, Class probability, Class expected value, and Chi-square component values are computed for each data class. With the aid of Excel tools, the goodness of fit test is carried out to make predictions about the distribution of a population based on a sample. The explanation is followed by the chi-square values, degrees of freedom, and test conclusions.

Goodness-of-Fit Test

The Goodness of Fit Test is used to determine whether the sample data chosen truly represents the data that is expected to be found in a population. The Chi-Square test is the goodness of fit test used

in this project. The Chi-square goodness of fit test compares a randomly collected sample with a single categorical variable to a larger population. This test is most used to compare a random sample data

to the population from which it was possibly drawn.

The test begins with the assumption of a Null hypothesis (Ho) and Alternative hypothesis(H1).

Null Hypothesis (Ho): The sample data collected is consistent with the population distribution.

Alternative Hypothesis (H1): The sample data collected is not consistent with the population

distribution.

Chi-Square Formula

 $\chi 2 = \sum (O_i - E_i)^2 / E_i$

• **n** = Total number of observations or total frequency

• χ2 = The χ2 statistic derived from the chi-square goodness of fit table.

• **O**_i = It is the observed value from the frequency table for each class interval.

• E_i = It is calculated by multiplying the class probabilities of each class by n.

• Each value of (Oi - Ei)2/Ei is referred to as a " χ2 Class Component."

Degree of Freedom (v) = number of groups - 1

There are several assumptions made by the Chi-Square test, including that the expected value of the observations should be more than 5, or else the groups should be combined appropriately. The Chi-Square test also presupposes that the level of significance for statistical analysis is set at 0.05

i.e., $\alpha = 0.05$

Using the significance level(α) and degree of freedom(ν), the estimated $\chi 2$ statistic is

compared with the **Tabulated value** that is derived from **Table A.5**.

• If χ2 statistic > Tabulated value

Conclusion: Reject HO

• If χ2 statistic < Tabulated value

Conclusion: Fail to Reject H0

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Chi-Square Goodness-of-Fit Test for Data set 1

The chi-square goodness of-Fit Test is performed using the descriptive statistical analysis results of Data set 1, the sample of 100 people's US shoe sizes. The Excel functions **AVERAGE** (), **MEDIAN** (), **STDEV.S** (), and **VAR.S** () are used to calculate the sample mean, sample median, sample standard deviation, and sample variance, respectively.

Statistics Value Units	Values	Units
Sample Mean	9.92	US
Sample Median	10.00	US
Sample Variance	3.57	US
Sample Standard Deviation	1.89	US

Table 1.1 Descriptive Statistics Exploring the US shoe size of randomly selected 100 people within UTA Campus.

For the chi-square goodness of fit test, the sample mean and sample standard deviation are taken from **Table 1.1**.

Making a hypothesis regarding Sample Data Set 1 is the first stage of the test, which has a level of significance of 0.05.

Null Hypothesis (H0): The sample Data set 1 is sampled from Normal distribution with population mean equal to the sample mean and a population standard deviation equal to the sample standard deviation.

Alternative Hypothesis (H1): The sample Data set 1 is not sampled from Normal distribution with population mean equal to the sample mean and a population standard deviation equal to the sample standard deviation.

For performing the chi-square goodness of test on Data set 1, an expanded frequency table is constructed by adding the columns into 5 group intervals. Found class probability, Class expected value, and class chi-square components from the expanded frequency table

Class	Observed Frequency(oi)	Class Probability	Expected value(ei)	χ2 Class Component
X ≤ 8	23	0.154845	15.48	3.647703887
8 < X ≤ 10	41	0.362036	36.20	0.6354331503
10 < X ≤ 12	25	0.347568	34.76	2.738881448
12 < X ≤ 14	10	0.120115	12.01	0.3368633071
X >14	1	0.015436	1.54	0.1914103344
Total	100	1.00	100.00	7.550292127

Table 1.2 Expanded Frequency table for performing Goodness of Fit Test on Data set 1

The observed Frequency is found by adding up the number of observations in the interval. The Class probability of each class intervals are calculated by:

The class probabilities are:

$$\begin{array}{ll} P \ [X \le 8] & = 0.154845 \\ P \ [8 < X \le 10] & = P \ [X \le 10] - P \ [X \le 8] & = 0.362036 \\ P \ [10 < X \le 12] & = P \ [X \le 12] - P \ [X \le 10] & = 0.347568 \\ P \ [12 < X \le 14] & = P \ [X \le 14] - P \ [X \le 12] & = 0.120115 \\ P \ [X > 14] & = 1 - P \ [X \le 14] & = 0.015436 \end{array}$$

For the Normal distribution, the sample mean (μ) and the sample standard deviation (σ) are the two parameters taken to calculate the class probabilities. The excel formula NORMDIST (x, μ , σ , 1) is used to calculate P [$X \le x$].

Expected values are found by multiplying each class probabilities by total number of observations(n), here n = 100. But here the expected value in the class X > 14 is less than 5, so the class is regrouped as below.

Class	Observed Frequency(oi)	Class Probability	Expected value(ei)	χ2 Class Component
X ≤ 8	23	0.154845	15.48	3.647703887
8 < X ≤ 10	41	0.362036	36.20	0.6354331503
10 < X ≤ 12	25	0.347568	34.76	2.738881448
X > 12	11	0.135551	13.56	0.4816236518
Total	100	1.00	100.00	7.503642138

Table 1.3 Expanded frequecny table with all the values with intervals combined.

$$P[X > 12] = 1 - P[X \le 12] = 0.135551$$

Chi-square class components are found by the chi-square formula (Oi – Ei)2/ Ei for each class and added up to get χ 2 test statistic, here the χ 2 test statistic is 7.503642138.

The Tabulated value for the Dataset 1 is found from **Table A.5**, Critical values of the Chi-Squared Distribution.

Significance level(
$$\alpha$$
) = 0.05
Degree of freedom(ν) = No of groups – 1 = 4-1 = 3

Therefore $\chi 2(\alpha, \nu) = \chi 2(0.05, 3) = 7.815$

The **Tabulated value** is compared with χ2 test statistic to test our hypothesis.

Here the χ2 test statistic < Tabulated value i.e., 7.503642138 < 7.815 Conclusion: Fail to Reject Null Hypothesis(H0)

Thus, a weak conclusion is obtained that Dataset 1 is sampled from Normal distribution with population mean equal to the sample mean and a population standard deviation equal to the sample standard deviation.

Chi-Square Goodness-of-Fit Test for Data set 2

The chi-square goodness of-Fit Test is performed using the descriptive statistical analysis results of Data set 2, the samples of the time differences between two students entering the library through the main door. The Excel functions **AVERAGE** (), **MEDIAN** (), **STDEV.S** (), **QUARTILE** (), and **VAR.S** () are used to calculate the sample mean, sample median, sample standard deviation, and sample variance, respectively.

Statistics Value Units	Values	Units
Sample Mean	7.23	Seconds
Sample Median	6.00	Seconds
Sample Variation	17.82	Seconds
Sample Standard Deviation	4.22	Seconds

Table 2.1 Descriptive Statistics Exploring the time interval between students entering the UTA Central Library

Table 2.1 displays the descriptive statistics values for the intervals between students entering the library. The 7.23 second obtained mean is used as β parameter for determining the class probabilities for each class.

The test is done with a level of significance of 0.05 and the first step is to make the hypothesis about the sample data set 2.

Null Hypothesis (H0): The sample data set 2 is sampled from an Exponential Distribution with a population mean equal to the sample mean.

Alternative Hypothesis (H1): The sample data set 2 is not sampled from an Exponential Distribution with a population mean equal to the sample mean.

For performing the chi-square goodness of test on Data set 2, an expanded frequency table is constructed by adding the columns into 6 group intervals. Found class probability, Class expected value, and class chi-square components from the expanded frequency table.

Class	Observed Frequency(oi)	Class Probability	Expected value(ei)	χ2 Class Component
X ≤ 3	5	0.3396186	33.96	24.69798163
3 < X ≤ 6	56	0.2242778	22.43	50.25436362
6 < X ≤ 9	16	0.1481089	14.81	0.09546926
9 < X ≤ 12	16	0.0978084	9.78	3.95446870
12 < X ≤ 15	1	0.0645908	6.46	4.61390241
X >15	6	0.1255955	12.56	3.42589529
Total	100	1	100.00	87.04208089

Table 2.2 Expanded frequency table for calculating Goodness of Fit Test on Data set 2

The observed Frequency is found by adding up the number of observations in the interval. The Class probability of each class intervals are calculated by:

The class probabilities are:

```
\begin{array}{lll} P \ [X \le 3] & = 0.3396186 \\ P \ [2 < X \le 6] & = P \ [X \le 6] - P \ [X \le 3] & = 0.2242778 \\ P \ [6 < X \le 9] & = P \ [X \le 9] - P \ [X \le 6] & = 0.1481089 \\ P \ [9 < X \le 12] & = P \ [X \le 12] - P \ [X \le 9] & = 0.0978084 \\ P \ [12 < X \le 15] & = P \ [X \le 15] - P \ [X \le 12] & = 0.0645908 \\ P \ [X > 15] & = 1 - P \ [X \le 15] & = 0.1255955 \end{array}
```

For the Exponential distribution, the sample mean (μ) is taken as β parameter to calculate the class probabilities. The excel formula GAMMADIST (x, α , β , 1) is used to calculate $P[X \le x]$. $\alpha = 1$ as we are using the function for exponential distribution.

Chi-square class components are found by the chi-square formula (Oi – Ei)2/ Ei for each class and added up to get χ 2 test statistic, here the χ 2 test statistic is 87.04208089.

The Tabulated value for the Dataset 1 is found from **Table A.5**, Critical values of the Chi-Squared Distribution.

Significance level(α) = 0.05 Degree of freedom(ν) = No of groups - 1 = 6-1 = 5

Therefore $\chi 2(\alpha, \nu) = \chi 2(0.05, 5) = 11.070$

The **Tabulated value** is compared with **\chi2** test statistic to test our hypothesis.

Here the χ2 test statistic < Tabulated value i.e., 87.04208089 > 11.070 Conclusion: Reject Null Hypothesis(H0)

Thus, a make a strong conclusion is obtained that the sample Data set 2 is not sampled from an Exponential Distribution with a population mean equal to the sample mean.

Conclusion

For data visualization and data presentation to be effective, descriptive statistics are essential. I conducted a statistical study on two datasets, starting with the Data set 1 that looked at 100 randomly selected students' US shoe sizes on November 15, 2022. The objective of this research was to check for any patterns in the 100 students whose shoe sizes were randomly selected. On November 15, 2022, between 3 and 4 PM, data for Data Set 2 was collected as the time difference between two students entering the library. Similar information may be acquired for other structures, allowing us to determine which ones draw students in. The assumptions that had previously been made based on the histogram, mean, median, and mode were put to the test using the chi-square goodness of Fit-Test. On Data Sets 1 and 2, the Goodness of Fit-Test was run to determine whether the samples were drawn from populations with normal or exponential distribution, respectively.

Data set 1 was subjected to descriptive statistical analysis, and it was found that the average US shoe size is 9.92. Based on the mean shoe size of 9.92, mode 10, and median 10, the data set was approximated to a normal distribution earlier. The Chi-square goodness of Fit-Test on Data Set 1 also produced results that supported the initial hypothesis. The Data Set 1 is drawn from a population that is assumed to have a normal distribution, with sample mean equal to population mean and sample standard deviation equal to population standard deviation, as the result failed to reject the null hypothesis (H0). A tentative conclusion that the sample follows a Normal Distribution was drawn from the Goodness of Fit-Test, despite the sample data not being perfectly symmetrical with the mean centre.

For **Data Set 2**, descriptive statistics reveal that it takes a student, on average, 7.23 seconds to enter the library. The sample data appears to follow an exponential distribution in accordance with the previous analysis based on the histogram. The sample data had previously been divided into only four classes, which produced a frequency histogram that was exponentially declining. A non-exponential trend was observed in frequencies of each class as a result of the variations in class intervals count to 6 from 4. The findings of the Chisquare Goodness of Fit-Test benefited the more recent class interval observations. The null hypothesis (H0), that the sample data is drawn from a population that is expected to have an exponential distribution, was rejected as a result of the goodness of fit test. A strong conclusion that the sample Data Set 2 did not follow an exponential distribution was drawn from the goodness of fit test.

Appendix A

Data set 1

Below is a table of the raw data of data set 1 that was gathered with various values and used for the goodness of fit test and descriptive statistical analysis.

No Race Gender US Shoe Si 1 Asian Male 10.5 2 Asian Male 12 3 Asian Female 8 4 American Female 9 5 American Male 12 6 Asian Female 8 7 Asian Male 8.5 8 Asian Female 9 9 Asian Female 10 11 American Female 10 12 Asian Female 10 12 Asian Female 10 13 Asian Female 10.5 14 Asian Female 10.5 15 Asian Male 11 16 African American Male 11 17 American Female 12 18 Asian Female 7.5	е
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36 American Female 8	
38 American Male 15	
39 American Female 12	
40 African American Male 10	
41 Asian Female 7	
42 Asian Female 6	
43 American Male 9	
44 Asian Male 13	
45 American Female 9	
46 Asian Male 11	
47 Asian Female 8	
48 Asian Male 11	
49 American Male 9	
50 American Female 9.5	
51 Asian Male 13	

No	Race	Gender	US Shoe Size
52	American	Male	13
53	American	Female	13
54	Asian	Male	9.5
55	African American	Male	10.5
56	Asian	Male	9.5
57	American	Male	10
58	Asian	Male	11
59	American	Male	11
60	American	Female	11
61	American	Male	12
62	American	Male	13
63	Asian	Male	10.5
64	Asian	Female	7
65	Asian	Male	10
66	Asian	Female	7
67	Asian	Female	8
68	Asian	Female	8
69	Asian	Female	7
70	Asian	Female	10
71	Asian	Female	7.5
72	Asian	Male	9.5
73	Asian	Male	9.5
74	Asian	Female	9
75	Asian	Male	11
76	Asian	Male	9
77	American	Female	14
78	African American	Female	12
79	Asian	Male	9.5
80	Asian	Female	9.3
			-
81 82	Asian African American	Male Female	10
83			9.5
	African American	Female	10
84	American	Male	
85	Asian	Male	10
86	Asian	Male	10
87	Asian	Female Female	10 7
88	Asian		
89 90	Asian	Female	7 9
	Asian	Female	
91	African American	Male	14
92	Asian	Male	10
93	Asian	Female	10
94	Asian	Female	9
95	Asian	Male	9
96	Asian	Male 	11
97	Asian	Female 	9
98	American	Female	10
99	Asian	Male	8
100	African American	Male	12
99	Asian	Male	8
100	African American	Male	12

Appendix B

Data set 2

Below is a table of the raw data of data set 2 that was gathered with various values and used for the goodness of fit test and descriptive statistical analysis.

			Second
No	Time	Time Difference in Seconds	s
1	15:45:29	0	0
2	15:45:46	00:00:17	17
3	15:46:08	00:00:22	22
4	15:46:20	00:00:12	12
5	15:46:25	00:00:05	5
6	15:46:31	00:00:06	6
7	15:46:52	00:00:21	21
8	15:47:10	00:00:18	18
9	15:47:33	00:00:23	23
10	15:47:42	00:00:09	9
11	15:47:48	00:00:06	6
12	15:47:54	00:00:06	6
13	15:48:00	00:00:06	6
14	15:48:05	00:00:05	5
15	15:48:10	00:00:05	5
16	15:48:16	00:00:06	6
17	15:48:28	00:00:12	12
18	15:48:35	00:00:07	7
19	15:48:47	00:00:12	12
20	15:48:56	00:00:09	9
21	15:49:00	00:00:04	4
22	15:49:07	00:00:07	7
23	15:49:12	00:00:05	5
24	15:49:30	00:00:18	18
25	15:49:34	00:00:04	4
26	15:49:43	00:00:09	9
27	15:49:47	00:00:04	4
28	15:49:51	00:00:04	4
29	15:49:55	00:00:04	4
30	15:50:03	00:00:08	8
31	15:50:09	00:00:06	6
32	15:50:20	00:00:11	11
33	15:50:32	00:00:11	12
34	15:50:37	00:00:05	5
35	15:50:43	00:00:06	6
36	15:50:52	00:00:09	9
37	15:50:59	00:00:03	7
38	15:51:10	00:00:11	11
39	15:51:20	00:00:10	10
40	15:51:25	00:00:05	5
41	15:51:32	00:00:07	7
42	15:51:37	00:00:05	5
43	15:51:43	00:00:06	6
44	15:51:50	00:00:07	7
45	15:52:00	00:00:10	10
46	15:52:06	00:00:10	6
47			4
	15:52:10	00:00:04	4
48	15:52:14	00:00:04	
49	15:52:18	00:00:04	4
50	15:52:22	00:00:04	4
51	15:52:26	00:00:04	4

No	Time	Time Difference in Seconds	Second s
52	15:52:31	00:00:05	5
53	15:52:35	00:00:04	4
54	15:52:39	00:00:04	4
55	15:52:50	00:00:11	11
56	15:53:03	00:00:13	13
57	15:53:09	00:00:06	6
58	15:53:13	00:00:04	4
59	15:53:19	00:00:06	6
60	15:53:25	00:00:06	6
61	15:53:29	00:00:04	4
62	15:53:34	00:00:05	5
63	15:53:40	00:00:06	6
64	15:53:48	00:00:08	8
65	15:53:51	00:00:03	3
66	15:53:58	00:00:07	7
67	15:54:03	00:00:05	5
68	15:54:09	00:00:06	6
69	15:54:17	00:00:08	8
70	15:54:21	00:00:04	4
71	15:54:25	00:00:04	4
72	15:54:37	00:00:12	12
73	15:54:43	00:00:06	6
74	15:54:47	00:00:04	4
75	15:54:59	00:00:12	12
76	15:55:02	00:00:03	3
77	15:55:12	00:00:10	10
78	15:55:16	00:00:04	4
79	15:55:20	00:00:04	4
80	15:55:30	00:00:10	10
81	15:55:34	00:00:04	4
82	15:55:38	00:00:04	4
83	15:55:42	00:00:04	4
84	15:55:48	00:00:06	6
85	15:55:54	00:00:06	6
86	15:55:58	00:00:04	4
87	15:56:03	00:00:05	5
88	15:56:07	00:00:04	4
89	15:56:12	00:00:05	5
90	15:56:20	00:00:08	8
91	15:56:22	00:00:02	2
92	15:56:30	00:00:08	8
93	15:56:37	00:00:07	7
94	15:56:39	00:00:02	2
95	15:56:51	00:00:12	12
96	15:57:03	00:00:12	12
97	15:57:09	00:00:06	6
98	15:57:13	00:00:04	4
99	15:57:18	00:00:05	5
100	15:57:21	00:00:03	3
101	15:57:32	00:00:11	11

Appendix C

Goodness of fit Calculations of Data set 1

Class	Observed Frequency(oi)	Class Probability Calculations	Expected Frequency (ei)	χ2 Class Component
X ≤ 8	Count the	NORMDIST (8,9.92,1.89,1)	Take the	
8 < X ≤ 10	observations of	NORMDIST (10,9.92,1.89,1)-NORMDIST (8,9.92,1.89,1)	probability for	
10 < X ≤ 12	each class from the	NORMDIST (12,9.92,1.89,1)-NORMDIST (10,9.92,1.89,1)	each class	(oi-ei) ^2/ei
12 < X ≤ 14	frequency table	NORMDIST (14,9.92,1.89,1)-NORMDIST (12,9.92,1.89,1)	and multiply it by n	
X >14		1-NORMDIST (14,9.92,1.89,1)		
Total	n	1.00	n	χ2 statistic

Class	Observed Frequency(oi)	Class Probability Calculations	Expected Frequency (ei)	χ2 Class Component
X ≤ 8	Count the	NORMDIST (8,9.92,1.89,1)	Take the	
8 < X ≤ 10	observations of	NORMDIST (10,9.92,1.89,1)-NORMDIST (8,9.92,1.89,1)	probability for	(oi-ei) ^2/ei
10 < X ≤ 12	each class from the	NORMDIST (12,9.92,1.89,1)-NORMDIST (10,9.92,1.89,1)	each class	(01-61)2/61
X > 12	frequency table	1-NORMDIST (12,9.92,1.89,1)	and multiply it by n	
Total	n	1.00	n	χ2 statistic

The class probabilities are calculated using the excel functions.

```
 \begin{array}{lll} P \ [X \le 8] & = NORMDIST \ (8,9.92,1.89,1) \\ P \ [8 < X \le 10] & = P \ [X \le 10] - P \ [X \le 8] & = NORMDIST \ (10,9.92,1.89,1) - NORMDIST \ (8,9.92,1.89,1) \\ P \ [10 < X \le 12] & = P \ [X \le 12] - P \ [X \le 10] & = NORMDIST \ (12,9.92,1.89,1) - NORMDIST \ (10,9.92,1.89,1) \\ P \ [X > 12] & = 1 - P \ [X \le 12] & = 1 - NORMDIST \ (12,9.92,1.89,1) \end{array}
```

Goodness of fit Calculations of Data set 2

Class	Observed Frequency(oi)	Class Probability Calculations	Expected Frequency (ei)	χ2 Class Component
X ≤ 3	Count the	GAMMADIST (3,1,7.23,1)	Take the	
3 < X ≤ 6	observations of	GAMMADIST (6,1,7.23,1)-GAMMADIST (3,1,7.23,1)	probability for	
6 < X ≤ 9	each class from the	GAMMADIST (9,1,7.23,1)-GAMMADIST (6,1,7.23,1)	each class	(oi-ei) ^2/ei
9 < X ≤ 12	frequency table	GAMMADIST (12,1,7.23,1)-GAMMADIST (9,1,7.23,1)	and multiply it by n	(01-61) ~2/61
12 < X ≤ 15	1	GAMMADIST (15,1,7.23,1)-GAMMADIST (12,1,7.23,1)		
X >15		1-GAMMADIST (15,1,7.23,1)		
Total	n	1.00	n	χ2 statistic

```
P[X \leq 3]
                                           = GAMMADIST (3,1,7.23,1)
                                           = GAMMADIST (6,1,7.23,1)-GAMMADIST (3,1,7.23,1)
P[2 < X \le 6]
                 = P[X \le 6] - P[X \le 3]
P[6 < X \le 9]
                = P[X \le 9] - P[X \le 6]
                                           = GAMMADIST (9,1,7.23,1)-GAMMADIST (6,1,7.23,1)
P[9 < X \le 12]
                = P[X \le 12] - P[X \le 9]
                                          = GAMMADIST (12,1,7.23,1)-GAMMADIST (9,1,7.23,1)
P [12 < X ≤ 15]
                = P[X \le 15] - P[X \le 12]
                                           = GAMMADIST (15,1,7.23,1)-GAMMADIST (12,1,7.23,1)
P [X > 15]
                 = 1 - P [X ≤ 15]
                                           = 1-GAMMADIST (15,1,7.23,1)
```

References

Benjamin Frimodig (2020, December 14). Chi Square (χ 2) Test Statistic https://www.simplypsychology.org/chi-square.html

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