

Problem 3077: Maximum Strength of K Disjoint Subarrays

Problem Information

Difficulty: Hard

Acceptance Rate: 27.29%

Paid Only: No

Tags: Array, Dynamic Programming, Prefix Sum

Problem Description

You are given an array of integers `nums` with length `n`, and a positive **odd** integer `k`.

Select exactly **k** disjoint subarrays **sub 1, sub2, ..., subk** from `nums` such that the last element of `subi` appears before the first element of `sub{i+1}` for all **1 <= i <= k-1**. The goal is to maximize their combined strength.

The strength of the selected subarrays is defined as:

$$\text{strength} = k * \text{sum}(\text{sub1}) - (k - 1) * \text{sum}(\text{sub2}) + (k - 2) * \text{sum}(\text{sub3}) - \dots - 2 * \text{sum}(\text{sub}{k-1}) + \text{sum}(\text{subk})$$

where **sum(sub i)** is the sum of the elements in the **i**-th subarray.

Return the **maximum** possible strength that can be obtained from selecting exactly **k** disjoint subarrays from `nums`.

Note that the chosen subarrays **don't** need to cover the entire array.

Example 1:

Input: nums = [1,2,3,-1,2], k = 3

Output: 22

****Explanation:****

The best possible way to select 3 subarrays is: nums[0..2], nums[3..3], and nums[4..4]. The strength is calculated as follows:

`strength = 3 * (1 + 2 + 3) - 2 * (-1) + 2 = 22`

****Example 2:****

****Input:**** nums = [12,-2,-2,-2,-2], k = 5

****Output:**** 64

****Explanation:****

The only possible way to select 5 disjoint subarrays is: nums[0..0], nums[1..1], nums[2..2], nums[3..3], and nums[4..4]. The strength is calculated as follows:

`strength = 5 * 12 - 4 * (-2) + 3 * (-2) - 2 * (-2) + (-2) = 64`

****Example 3:****

****Input:**** nums = [-1,-2,-3], k = 1

****Output:**** -1

****Explanation:****

The best possible way to select 1 subarray is: nums[0..0]. The strength is -1.

****Constraints:****

* `1 <= n <= 104` * `-109 <= nums[i] <= 109` * `1 <= k <= n` * `1 <= n * k <= 106` * `k` is odd.

Code Snippets

C++:

```
class Solution {  
public:  
    long long maximumStrength(vector<int>& nums, int k) {  
  
    }  
};
```

Java:

```
class Solution {  
public long maximumStrength(int[] nums, int k) {  
  
}  
}
```

Python3:

```
class Solution:  
    def maximumStrength(self, nums: List[int], k: int) -> int:
```