

# Problem 2065: Maximum Path Quality of a Graph

## Problem Information

**Difficulty:** Hard

**Acceptance Rate:** 60.58%

**Paid Only:** No

**Tags:** Array, Backtracking, Graph

## Problem Description

There is an **undirected** graph with  $n$  nodes numbered from  $0$  to  $n - 1$  (**inclusive**). You are given a **0-indexed** integer array `values` where `values[i]` is the **value** of the  $i$ th node. You are also given a **0-indexed** 2D integer array `edges`, where each `edges[j] = [uj, vj, timej]` indicates that there is an undirected edge between the nodes  $uj$  and  $vj$ , and it takes `timej` seconds to travel between the two nodes. Finally, you are given an integer `maxTime`.

A **valid** **path** in the graph is any path that starts at node  $0$ , ends at node  $0$ , and takes **at most** `maxTime` seconds to complete. You may visit the same node multiple times. The **quality** of a valid path is the **sum** of the values of the **unique nodes** visited in the path (each node's value is added **at most once** to the sum).

Return the maximum quality of a valid path.

**Note:** There are **at most four** edges connected to each node.

**Example 1:**



**Input:** `values = [0,32,10,43]`, `edges = [[0,1,10],[1,2,15],[0,3,10]]`, `maxTime = 49` **Output:** `75` **Explanation:** One possible path is  $0 \rightarrow 1 \rightarrow 0 \rightarrow 3 \rightarrow 0$ . The total time taken is  $10 + 10 + 10 + 10 = 40 \leq 49$ . The nodes visited are 0, 1, and 3, giving a maximal path quality of  $0 + 32 + 43 = 75$ .

**Example 2:**



**Input:** values = [5,10,15,20], edges = [[0,1,10],[1,2,10],[0,3,10]], maxTime = 30 **Output:** 25 **Explanation:** One possible path is 0 -> 3 -> 0. The total time taken is 10 + 10 = 20 <= 30. The nodes visited are 0 and 3, giving a maximal path quality of 5 + 20 = 25.

**Example 3:**



**Input:** values = [1,2,3,4], edges = [[0,1,10],[1,2,11],[2,3,12],[1,3,13]], maxTime = 50 **Output:** 7 **Explanation:** One possible path is 0 -> 1 -> 3 -> 1 -> 0. The total time taken is 10 + 13 + 13 + 10 = 46 <= 50. The nodes visited are 0, 1, and 3, giving a maximal path quality of 1 + 2 + 4 = 7.

**Constraints:**

\* n == values.length \* 1 <= n <= 1000 \* 0 <= values[i] <= 108 \* 0 <= edges.length <= 2000 \* edges[j].length == 3 \* 0 <= u\_j < v\_j <= n - 1 \* 10 <= time\_j, maxTime <= 100 \* All the pairs [u\_j, v\_j] are **unique**. \* There are **at most four** edges connected to each node. \* The graph may not be connected.

## Code Snippets

**C++:**

```
class Solution {
public:
    int maximalPathQuality(vector<int>& values, vector<vector<int>>& edges, int maxTime) {

    }
};
```

**Java:**

```
class Solution {
    public int maximalPathQuality(int[] values, int[][] edges, int maxTime) {
```

```
}  
}
```

### Python3:

```
class Solution:  
    def maximalPathQuality(self, values: List[int], edges: List[List[int]],  
        maxTime: int) -> int:
```