

Problem 2065: Maximum Path Quality of a Graph

Problem Information

Difficulty: Hard

Acceptance Rate: 60.58%

Paid Only: No

Tags: Array, Backtracking, Graph

Problem Description

There is an **undirected** graph with `n` nodes numbered from `0` to `n - 1` (**inclusive**). You are given a **0-indexed** integer array `values` where `values[i]` is the **value** of the `ith` node. You are also given a **0-indexed** 2D integer array `edges`, where each `edges[j] = [uj, vj, timej]` indicates that there is an undirected edge between the nodes `uj` and `vj`, and it takes `timej` seconds to travel between the two nodes. Finally, you are given an integer **maxTime**.

A **valid path** in the graph is any path that starts at node `0`, ends at node `0`, and takes **at most** **maxTime** seconds to complete. You may visit the same node multiple times. The **quality** of a valid path is the **sum** of the values of the **unique nodes** visited in the path (each node's value is added **at most once** to the sum).

Return **the maximum quality of a valid path**.

Note: There are **at most four** edges connected to each node.

Example 1:

Input: values = [0,32,10,43], edges = [[0,1,10],[1,2,15],[0,3,10]], maxTime = 49 **Output:** 75
Explanation: One possible path is 0 -> 1 -> 0 -> 3 -> 0. The total time taken is 10 + 10 + 10 + 10 = 40 <= 49. The nodes visited are 0, 1, and 3, giving a maximal path quality of 0 + 32 + 43 = 75.

****Example 2:****

****Input:**** values = [5,10,15,20], edges = [[0,1,10],[1,2,10],[0,3,10]], maxTime = 30 ****Output:**** 25
****Explanation:**** One possible path is 0 -> 3 -> 0. The total time taken is $10 + 10 = 20 \leq 30$. The nodes visited are 0 and 3, giving a maximal path quality of $5 + 20 = 25$.

****Example 3:****

****Input:**** values = [1,2,3,4], edges = [[0,1,10],[1,2,11],[2,3,12],[1,3,13]], maxTime = 50
****Output:**** 7 ****Explanation:**** One possible path is 0 -> 1 -> 3 -> 1 -> 0. The total time taken is $10 + 13 + 13 + 10 = 46 \leq 50$. The nodes visited are 0, 1, and 3, giving a maximal path quality of $1 + 2 + 4 = 7$.

****Constraints:****

* `n == values.length` * `1 <= n <= 1000` * `0 <= values[i] <= 108` * `0 <= edges.length <= 2000` * `edges[j].length == 3` * `0 <= uj < vj <= n - 1` * `10 <= timej, maxTime <= 100` * All the pairs `[uj, vj]` are **unique**. * There are **at most four** edges connected to each node. * The graph may not be connected.

Code Snippets

C++:

```
class Solution {
public:
    int maximalPathQuality(vector<int>& values, vector<vector<int>>& edges, int maxTime) {
        ...
    }
};
```

Java:

```
class Solution {
    public int maximalPathQuality(int[] values, int[][] edges, int maxTime) {
```

```
    }  
}
```

Python3:

```
class Solution:  
    def maximalPathQuality(self, values: List[int], edges: List[List[int]],  
                           maxTime: int) -> int:
```