

# Problem 3068: Find the Maximum Sum of Node Values

## Problem Information

**Difficulty:** Hard

**Acceptance Rate:** 69.60%

**Paid Only:** No

**Tags:** Array, Dynamic Programming, Greedy, Bit Manipulation, Tree, Sorting

## Problem Description

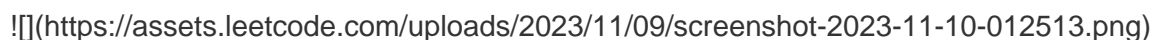
There exists an **undirected** tree with  $n$  nodes numbered  $0$  to  $n - 1$ . You are given a **0-indexed** 2D integer array `edges` of length  $n - 1$ , where `edges[i] = [ui, vi]` indicates that there is an edge between nodes `ui` and `vi` in the tree. You are also given a **positive** integer  $k$ , and a **0-indexed** array of **non-negative** integers `nums` of length  $n$ , where `nums[i]` represents the **value** of the node numbered  $i$ .

Alice wants the sum of values of tree nodes to be **maximum**, for which Alice can perform the following operation **any** number of times (**including zero**) on the tree:

\* Choose any edge `[u, v]` connecting the nodes `u` and `v`, and update their values as follows:  $\text{nums}[u] = \text{nums}[u] \text{ XOR } k$  \*  $\text{nums}[v] = \text{nums}[v] \text{ XOR } k$

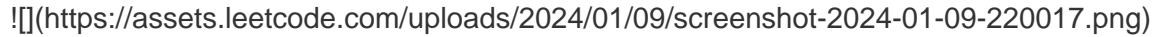
Return the **maximum** possible **sum** of the **values** Alice can achieve by performing the operation **any** number of times.

**Example 1:**



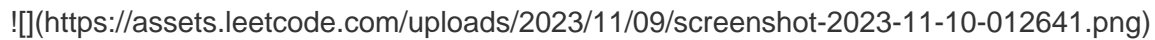
**Input:** `nums = [1,2,1]`, `k = 3`, `edges = [[0,1],[0,2]]` **Output:** 6 **Explanation:** Alice can achieve the maximum sum of 6 using a single operation: - Choose the edge `[0,2]`. `nums[0]` and `nums[2]` become:  $1 \text{ XOR } 3 = 2$ , and the array `nums` becomes: `[1,2,1] -> [2,2,2]`. The total sum of values is  $2 + 2 + 2 = 6$ . It can be shown that 6 is the maximum achievable sum of values.

### **\*\*Example 2:\*\***

 (https://assets.leetcode.com/uploads/2024/01/09/screenshot-2024-01-09-220017.png)

**\*\*Input:\*\*** nums = [2,3], k = 7, edges = [[0,1]] **\*\*Output:\*\*** 9 **\*\*Explanation:\*\*** Alice can achieve the maximum sum of 9 using a single operation: - Choose the edge [0,1]. nums[0] becomes: 2 XOR 7 = 5 and nums[1] become: 3 XOR 7 = 4, and the array nums becomes: [2,3] -> [5,4]. The total sum of values is 5 + 4 = 9. It can be shown that 9 is the maximum achievable sum of values.

### **\*\*Example 3:\*\***

 (https://assets.leetcode.com/uploads/2023/11/09/screenshot-2023-11-10-012641.png)

**\*\*Input:\*\*** nums = [7,7,7,7,7,7], k = 3, edges = [[0,1],[0,2],[0,3],[0,4],[0,5]] **\*\*Output:\*\*** 42

**\*\*Explanation:\*\*** The maximum achievable sum is 42 which can be achieved by Alice performing no operations.

### **\*\*Constraints:\*\***

$2 \leq n \leq 2 \cdot 10^4$ ,  $1 \leq k \leq 109$ ,  $0 \leq \text{nums}[i] \leq 109$ ,  $0 \leq \text{edges.length} \leq n - 1$ ,  $0 \leq \text{edges}[i].\text{length} \leq 2$ ,  $0 \leq \text{edges}[i][0], \text{edges}[i][1] \leq n - 1$  \* The input is generated such that `edges` represent a valid tree.

## **Code Snippets**

### **C++:**

```
class Solution {
public:
    long long maximumValueSum(vector<int>& nums, int k, vector<vector<int>>& edges) {

    }
};
```

### **Java:**

```
class Solution {
    public long maximumValueSum(int[] nums, int k, int[][] edges) {
```

```
}  
}
```

### Python3:

```
class Solution:  
    def maximumValueSum(self, nums: List[int], k: int, edges: List[List[int]]) ->  
        int:
```