Problem 3593: Minimum Increments to Equalize Leaf Paths

Problem Information

Difficulty: Medium
Acceptance Rate: 40.77%
Paid Only: No
Tags: Array, Dynamic Programming, Tree, Depth-First Search

Problem Description

You are given an integer `n` and an undirected tree rooted at node 0 with `n` nodes numbered from 0 to `n - 1`. This is represented by a 2D array `edges` of length `n - 1`, where `edges[i] = [ui, vi]` indicates an edge from node `ui` to `vi` .

Each node `i` has an associated cost given by `cost[i]`, representing the cost to traverse that node.

The **score** of a path is defined as the sum of the costs of all nodes along the path.

Your goal is to make the scores of all **root-to-leaf** paths **equal** by **increasing** the cost of any number of nodes by **any non-negative** amount.

Return the **minimum** number of nodes whose cost must be increased to make all root-to-leaf path scores equal.

Example 1:

Input: n = 3, edges = [[0,1],[0,2]], cost = [2,1,3]

Output: 1

Explanation:

There are two root-to-leaf paths:

* Path `0 -> 1` has a score of `2 + 1 = 3`. * Path `0 -> 2` has a score of `2 + 3 = 5`.

To make all root-to-leaf path scores equal to 5, increase the cost of node 1 by 2. Only one node is increased, so the output is 1.

Example 2:

Input: n = 3, edges = [[0,1],[1,2]], cost = [5,1,4]

Output: 0

Explanation:

There is only**** one root-to-leaf path:

* Path `0 -> 1 -> 2` has a score of `5 + 1 + 4 = 10`.

Since only one root-to-leaf path exists, all path costs are trivially equal, and the output is 0.

Example 3:

Input: n = 5, edges = [[0,4],[0,1],[1,2],[1,3]], cost = [3,4,1,1,7]

Output: 1

Explanation:

There are three root-to-leaf paths:

* Path `0 -> 4` has a score of `3 + 7 = 10`. * Path `0 -> 1 -> 2` has a score of `3 + 4 + 1 = 8`. * Path `0 -> 1 -> 3` has a score of `3 + 4 + 1 = 8`.

To make all root-to-leaf path scores equal to 10, increase the cost of node 1 by 2. Thus, the output is 1.

Constraints:

* `2 <= n <= 105` * `edges.length == n - 1` * `edges[i] == [ui, vi]` * `0 <= ui, vi < n` * `cost.length == n` * `1 <= cost[i] <= 109` * The input is generated such that `edges` represents a valid tree.

Code Snippets

C++:

```
class Solution {
public:
int minIncrease(int n, vector<vector<int>>& edges, vector<int>& cost) {

}
};
```

Java:

```
class Solution {
public int minIncrease(int n, int[][] edges, int[] cost) {

}
}
```

Python3:

```
class Solution:
def minIncrease(self, n: int, edges: List[List[int]], cost: List[int]) ->
int:
```