

Problem 3608: Minimum Time for K Connected Components

Problem Information

Difficulty: Medium

Acceptance Rate: 44.92%

Paid Only: No

Tags: Binary Search, Union Find, Graph, Sorting

Problem Description

You are given an integer n and an undirected graph with n nodes labeled from 0 to $n - 1$. This is represented by a 2D array `edges`, where `edges[i] = [ui, vi, timei]` indicates an undirected edge between nodes `ui` and `vi` that can be removed at `timei`.

You are also given an integer k .

Initially, the graph may be connected or disconnected. Your task is to find the **minimum** time t such that after removing all edges with `time $\leq t$` , the graph contains **at least** k connected components.

Return the **minimum** time t .

A **connected component** is a subgraph of a graph in which there exists a path between any two vertices, and no vertex of the subgraph shares an edge with a vertex outside of the subgraph.

Example 1:

Input: $n = 2$, `edges = [[0,1,3]]`, $k = 2$

Output: 3

Explanation:

* Initially, there is one connected component $\{0, 1\}$. * At $\text{time} = 1$ or 2 , the graph remains unchanged. * At $\text{time} = 3$, edge $[0, 1]$ is removed, resulting in $k = 2$ connected components $\{0\}$, $\{1\}$. Thus, the answer is 3.

Example 2:

Input: $n = 3$, $\text{edges} = [[0, 1, 2], [1, 2, 4]]$, $k = 3$

Output: 4

Explanation:

* Initially, there is one connected component $\{0, 1, 2\}$. * At $\text{time} = 2$, edge $[0, 1]$ is removed, resulting in two connected components $\{0\}$, $\{1, 2\}$. * At $\text{time} = 4$, edge $[1, 2]$ is removed, resulting in $k = 3$ connected components $\{0\}$, $\{1\}$, $\{2\}$. Thus, the answer is 4.

Example 3:

Input: $n = 3$, $\text{edges} = [[0, 2, 5]]$, $k = 2$

Output: 0

Explanation:

* Since there are already $k = 2$ disconnected components $\{1\}$, $\{0, 2\}$, no edge removal is needed. Thus, the answer is 0.

Constraints:

* $1 \leq n \leq 10^5$ * $0 \leq \text{edges.length} \leq 10^5$ * $\text{edges}[i] = [\text{ui}, \text{vi}, \text{timei}]$ * $0 \leq \text{ui}, \text{vi} < n$ * $\text{ui} \neq \text{vi}$ * $1 \leq \text{timei} \leq 10^9$ * $1 \leq k \leq n$ * There are no duplicate edges.

Code Snippets

C++:

```
class Solution {  
public:  
    int minTime(int n, vector<vector<int>>& edges, int k) {  
  
    }  
};
```

Java:

```
class Solution {  
    public int minTime(int n, int[][] edges, int k) {  
  
    }  
}
```

Python3:

```
class Solution:  
    def minTime(self, n: int, edges: List[List[int]], k: int) -> int:
```