

# Problem 1359: Count All Valid Pickup and Delivery Options

## Problem Information

**Difficulty:** Hard

**Acceptance Rate:** 64.88%

**Paid Only:** No

**Tags:** Math, Dynamic Programming, Combinatorics

## Problem Description

Given  $n$  orders, each order consists of a pickup and a delivery service.

Count all valid pickup/delivery possible sequences such that  $\text{delivery}(i)$  is always after of  $\text{pickup}(i)$ .

Since the answer may be too large, return it modulo  $10^9 + 7$ .

**Example 1:**

**Input:**  $n = 1$  **Output:** 1 **Explanation:** Unique order (P1, D1), Delivery 1 always is after of Pickup 1.

**Example 2:**

**Input:**  $n = 2$  **Output:** 6 **Explanation:** All possible orders: (P1,P2,D1,D2), (P1,P2,D2,D1), (P1,D1,P2,D2), (P2,P1,D1,D2), (P2,P1,D2,D1) and (P2,D2,P1,D1). This is an invalid order (P1,D2,P2,D1) because Pickup 2 is after of Delivery 2.

**Example 3:**

**Input:**  $n = 3$  **Output:** 90

**Constraints:**

\*`1 <= n <= 500`

## Code Snippets

### C++:

```
class Solution {  
public:  
    int countOrders(int n) {  
  
    }  
};
```

### Java:

```
class Solution {  
    public int countOrders(int n) {  
  
    }  
}
```

### Python3:

```
class Solution:  
    def countOrders(self, n: int) -> int:
```