

Problem 3378: Count Connected Components in LCM Graph

Problem Information

Difficulty: Hard

Acceptance Rate: 30.32%

Paid Only: No

Tags: Array, Hash Table, Math, Union Find, Number Theory

Problem Description

You are given an array of integers `nums` of size `n` and a **positive** integer `threshold`.

There is a graph consisting of `n` nodes with the `i`th node having a value of `nums[i]`. Two nodes `i` and `j` in the graph are connected via an **undirected** edge if `lcm(nums[i], nums[j]) <= threshold`.

Return the number of **connected components** in this graph.

A **connected component** is a subgraph of a graph in which there exists a path between any two vertices, and no vertex of the subgraph shares an edge with a vertex outside of the subgraph.

The term `lcm(a, b)` denotes the **least common multiple** of `a` and `b`.

Example 1:

Input: `nums = [2,4,8,3,9]`, `threshold = 5`

Output: 4

Explanation:



The four connected components are `(2, 4)`, `(3)`, `(8)`, `(9)`.

Example 2:

Input: `nums = [2,4,8,3,9,12]`, `threshold = 10`

Output: `2`

Explanation:

 <https://assets.leetcode.com/uploads/2024/10/31/example1.png>

The two connected components are `(2, 3, 4, 8, 9)`, and `(12)`.

Constraints:

`1 <= nums.length <= 105` `1 <= nums[i] <= 109` `All elements of `nums` are unique.` `1 <= threshold <= 2 * 105`

Code Snippets

C++:

```
class Solution {
public:
    int countComponents(vector<int>& nums, int threshold) {

    }
};
```

Java:

```
class Solution {
    public int countComponents(int[] nums, int threshold) {

    }
}
```

Python3:

```
class Solution:
    def countComponents(self, nums: List[int], threshold: int) -> int:
```