

Problem 3559: Number of Ways to Assign Edge Weights II

Problem Information

Difficulty: Hard

Acceptance Rate: 59.86%

Paid Only: No

Tags: Array, Math, Dynamic Programming, Bit Manipulation, Tree, Depth-First Search

Problem Description

There is an undirected tree with n nodes labeled from 1 to n , rooted at node 1. The tree is represented by a 2D integer array `edges` of length $n - 1$, where `edges[i] = [ui, vi]` indicates that there is an edge between nodes `ui` and `vi`.

Initially, all edges have a weight of 0. You must assign each edge a weight of either `1` or `2`.

The **cost** of a path between any two nodes `u` and `v` is the total weight of all edges in the path connecting them.

You are given a 2D integer array `queries`. For each `queries[i] = [ui, vi]`, determine the number of ways to assign weights to edges **in the path** such that the cost of the path between `ui` and `vi` is **odd**.

Return an array `answer`, where `answer[i]` is the number of valid assignments for `queries[i]`.

Since the answer may be large, apply **modulo** $10^9 + 7$ to each `answer[i]`.

Note: For each query, disregard all edges **not** in the path between node `ui` and `vi`.

Example 1:


Input: edges = [[1,2]], queries = [[1,1],[1,2]]

Output: [0,1]

Explanation:

* Query [1,1]: The path from Node 1 to itself consists of no edges, so the cost is 0. Thus, the number of valid assignments is 0. * Query [1,2]: The path from Node 1 to Node 2 consists of one edge (1 -> 2). Assigning weight 1 makes the cost odd, while 2 makes it even. Thus, the number of valid assignments is 1.

Example 2:



Input: edges = [[1,2],[1,3],[3,4],[3,5]], queries = [[1,4],[3,4],[2,5]]

Output: [2,1,4]

Explanation:

* Query [1,4]: The path from Node 1 to Node 4 consists of two edges (1 -> 3 and 3 -> 4). Assigning weights (1,2) or (2,1) results in an odd cost. Thus, the number of valid assignments is 2. * Query [3,4]: The path from Node 3 to Node 4 consists of one edge (3 -> 4). Assigning weight 1 makes the cost odd, while 2 makes it even. Thus, the number of valid assignments is 1. * Query [2,5]: The path from Node 2 to Node 5 consists of three edges (2 -> 1, 1 -> 3, and 3 -> 5). Assigning (1,2,2), (2,1,2), (2,2,1), or (1,1,1) makes the cost odd. Thus, the number of valid assignments is 4.

Constraints:

* 2 <= n <= 105 * edges.length == n - 1 * edges[i] == [ui, vi] * 1 <= queries.length <= 105 * queries[i] == [ui, vi] * 1 <= ui, vi <= n * edges represents a valid tree.

Code Snippets

C++:

```
class Solution {  
public:  
    vector<int> assignEdgeWeights(vector<vector<int>>& edges,  
    vector<vector<int>>& queries) {  
  
    }  
};
```

Java:

```
class Solution {  
    public int[] assignEdgeWeights(int[][] edges, int[][] queries) {  
  
    }  
}
```

Python3:

```
class Solution:  
    def assignEdgeWeights(self, edges: List[List[int]], queries: List[List[int]])  
    -> List[int]:
```