

Problem 2748: Number of Beautiful Pairs

Problem Information

Difficulty: Easy

Acceptance Rate: 51.60%

Paid Only: No

Tags: Array, Hash Table, Math, Counting, Number Theory

Problem Description

You are given a **0-indexed** integer array `nums`. A pair of indices `i`, `j` where $0 \leq i < j < \text{nums.length}$ is called beautiful if the **first digit** of `nums[i]` and the **last digit** of `nums[j]` are **coprime**.

Return `_` the total number of beautiful pairs in `nums`.

Two integers `x` and `y` are **coprime** if there is no integer greater than 1 that divides both of them. In other words, `x` and `y` are coprime if $\text{gcd}(x, y) == 1$, where $\text{gcd}(x, y)$ is the **greatest common divisor** of `x` and `y`.

Example 1:

Input: `nums = [2,5,1,4]` **Output:** 5 **Explanation:** There are 5 beautiful pairs in `nums`:
When `i = 0` and `j = 1`: the first digit of `nums[0]` is 2, and the last digit of `nums[1]` is 5. We can confirm that 2 and 5 are coprime, since $\text{gcd}(2,5) == 1$.
When `i = 0` and `j = 2`: the first digit of `nums[0]` is 2, and the last digit of `nums[2]` is 1. Indeed, $\text{gcd}(2,1) == 1$.
When `i = 1` and `j = 2`: the first digit of `nums[1]` is 5, and the last digit of `nums[2]` is 1. Indeed, $\text{gcd}(5,1) == 1$.
When `i = 1` and `j = 3`: the first digit of `nums[1]` is 5, and the last digit of `nums[3]` is 4. Indeed, $\text{gcd}(5,4) == 1$.
When `i = 2` and `j = 3`: the first digit of `nums[2]` is 1, and the last digit of `nums[3]` is 4. Indeed, $\text{gcd}(1,4) == 1$. Thus, we return 5.

Example 2:

Input: `nums = [11,21,12]` **Output:** 2 **Explanation:** There are 2 beautiful pairs: When `i = 0` and `j = 1`: the first digit of `nums[0]` is 1, and the last digit of `nums[1]` is 1. Indeed, $\text{gcd}(1,1) == 1$.
When `i = 0` and `j = 2`: the first digit of `nums[0]` is 1, and the last digit of `nums[2]` is 2.

Indeed, $\text{gcd}(1,2) = 1$. Thus, we return 2.

****Constraints:****

$2 \leq \text{nums.length} \leq 100$ $1 \leq \text{nums}[i] \leq 9999$ $\text{nums}[i] \% 10 \neq 0$

Code Snippets

C++:

```
class Solution {
public:
    int countBeautifulPairs(vector<int>& nums) {

    }
};
```

Java:

```
class Solution {
    public int countBeautifulPairs(int[] nums) {

    }
}
```

Python3:

```
class Solution:
    def countBeautifulPairs(self, nums: List[int]) -> int:
```