

# Problem 3383: Minimum Runes to Add to Cast Spell

## Problem Information

**Difficulty:** Hard

**Acceptance Rate:** 43.33%

**Paid Only:** Yes

**Tags:** Array, Depth-First Search, Breadth-First Search, Union Find, Graph, Topological Sort

## Problem Description

Alice has just graduated from wizard school, and wishes to cast a magic spell to celebrate. The magic spell contains certain **focus points** where magic needs to be concentrated, and some of these focus points contain **magic crystals** which serve as the spell's energy source. Focus points can be linked through **directed runes**, which channel magic flow from one focus point to another.

You are given a integer `n` denoting the `_number_` of focus points and an array of integers `crystals` where `crystals[i]` indicates a focus point which holds a magic crystal. You are also given two integer arrays `flowFrom` and `flowTo`, which represent the existing **directed runes**. The `i`th rune allows magic to freely flow from focus point `flowFrom[i]` to focus point `flowTo[i]`.

You need to find the number of directed runes Alice must add to her spell, such that `_each_` focus point either:

- Contains** a magic crystal.
- Receives** magic flow `_from_` another focus point.


Return the **minimum** number of directed runes that she should add.

**Example 1:**

**Input:** `n = 6, crystals = [0], flowFrom = [0,1,2,3], flowTo = [1,2,3,0]`

**Output:** 2

**\*\*Explanation:\*\***



Add two directed runes:

\* From focus point 0 to focus point 4. \* From focus point 0 to focus point 5.

**\*\*Example 2:\*\***

**\*\*Input:\*\*** n = 7, crystals = [3,5], flowFrom = [0,1,2,3,5], flowTo = [1,2,0,4,6]

**\*\*Output:\*\*** 1

**\*\*Explanation:\*\***



Add a directed rune from focus point 4 to focus point 2.

**\*\*Constraints:\*\***

\*  $2 \leq n \leq 105$  \*  $1 \leq \text{crystals.length} \leq n$  \*  $0 \leq \text{crystals}[i] \leq n - 1$  \*  $1 \leq \text{flowFrom.length} == \text{flowTo.length} \leq \min(2 * 105, (n * (n - 1)) / 2)$  \*  $0 \leq \text{flowFrom}[i], \text{flowTo}[i] \leq n - 1$  \*  $\text{flowFrom}[i] \neq \text{flowTo}[i]$  \* All pre-existing directed runes are **\*\*distinct\*\***.

## Code Snippets

**C++:**

```
class Solution {
public:
    int minRunesToAdd(int n, vector<int>& crystals, vector<int>& flowFrom,
vector<int>& flowTo) {

    }

};
```

**Java:**

```
class Solution {  
    public int minRunesToAdd(int n, int[] crystals, int[] flowFrom, int[] flowTo)  
    {  
  
    }  
}
```

### Python3:

```
class Solution:  
    def minRunesToAdd(self, n: int, crystals: List[int], flowFrom: List[int],  
        flowTo: List[int]) -> int:
```