

Problem 3013: Divide an Array Into Subarrays With Minimum Cost II

Problem Information

Difficulty: Hard

Acceptance Rate: 31.22%

Paid Only: No

Tags: Array, Hash Table, Sliding Window, Heap (Priority Queue)

Problem Description

You are given a **0-indexed** array of integers `nums` of length `n`, and two **positive** integers `k` and `dist`.

The **cost** of an array is the value of its **first** element. For example, the cost of `[1,2,3]` is `1` while the cost of `[3,4,1]` is `3`.

You need to divide `nums` into `k` **disjoint contiguous** subarrays, such that the difference between the starting index of the **second** subarray and the starting index of the `k`th subarray should be **less than or equal to** `dist`. In other words, if you divide `nums` into the subarrays `nums[0..(i1 - 1)]`, `nums[i1..(i2 - 1)]`, ..., `nums[ik-1..(n - 1)]`, then `ik-1 - i1 <= dist`.

Return the **minimum** possible sum of the cost of these subarrays.

Example 1:

Input: `nums = [1,3,2,6,4,2]`, `k = 3`, `dist = 3` **Output:** `5` **Explanation:** The best possible way to divide `nums` into 3 subarrays is: `[1,3]`, `[2,6,4]`, and `[2]`. This choice is valid because `ik-1 - i1` is `5 - 2 = 3` which is equal to `dist`. The total cost is `nums[0] + nums[2] + nums[5]` which is `1 + 2 + 2 = 5`. It can be shown that there is no possible way to divide `nums` into 3 subarrays at a cost lower than 5.

Example 2:

Input: `nums = [10,1,2,2,2,1]`, `k = 4`, `dist = 3` **Output:** `15` **Explanation:** The best possible way to divide `nums` into 4 subarrays is: `[10]`, `[1]`, `[2]`, and `[2,2,1]`. This choice is valid

because $ik-1 - i1$ is $3 - 1 = 2$ which is less than $dist$. The total cost is $nums[0] + nums[1] + nums[2] + nums[3]$ which is $10 + 1 + 2 + 2 = 15$. The division $[10], [1], [2,2,2]$, and $[1]$ is not valid, because the difference between $ik-1$ and $i1$ is $5 - 1 = 4$, which is greater than $dist$. It can be shown that there is no possible way to divide $nums$ into 4 subarrays at a cost lower than 15.

Example 3.

Input: $nums = [10,8,18,9]$, $k = 3$, $dist = 1$ **Output:** 36 **Explanation:** The best possible way to divide $nums$ into 4 subarrays is: $[10]$, $[8]$, and $[18,9]$. This choice is valid because $ik-1 - i1$ is $2 - 1 = 1$ which is equal to $dist$. The total cost is $nums[0] + nums[1] + nums[2]$ which is $10 + 8 + 18 = 36$. The division $[10]$, $[8,18]$, and $[9]$ is not valid, because the difference between $ik-1$ and $i1$ is $3 - 1 = 2$, which is greater than $dist$. It can be shown that there is no possible way to divide $nums$ into 3 subarrays at a cost lower than 36.

Constraints:

$3 \leq n \leq 105$ $1 \leq nums[i] \leq 109$ $3 \leq k \leq n$ $k - 2 \leq dist \leq n - 2$

Code Snippets

C++:

```
class Solution {
public:
    long long minimumCost(vector<int>& nums, int k, int dist) {

    }

};
```

Java:

```
class Solution {
    public long minimumCost(int[] nums, int k, int dist) {

    }

}
```

Python3:

```
class Solution:
    def minimumCost(self, nums: List[int], k: int, dist: int) -> int:
```