

Problem 1681: Minimum Incompatibility

Problem Information

Difficulty: Hard

Acceptance Rate: 40.68%

Paid Only: No

Tags: Array, Dynamic Programming, Bit Manipulation, Bitmask

Problem Description

You are given an integer array `nums` and an integer `k`. You are asked to distribute this array into `k` subsets of **equal size** such that there are no two equal elements in the same subset.

A subset's **incompatibility** is the difference between the maximum and minimum elements in that array.

Return **the minimum possible sum of incompatibilities** of the `k` subsets after distributing the array optimally, or return `-1` if it is not possible.

A subset is a group integers that appear in the array with no particular order.

Example 1:

Input: `nums = [1,2,1,4], k = 2` **Output:** `4` **Explanation:** The optimal distribution of subsets is `[1,2]` and `[1,4]`. The incompatibility is $(2-1) + (4-1) = 4$. Note that `[1,1]` and `[2,4]` would result in a smaller sum, but the first subset contains 2 equal elements.

Example 2:

Input: `nums = [6,3,8,1,3,1,2,2], k = 4` **Output:** `6` **Explanation:** The optimal distribution of subsets is `[1,2]`, `[2,3]`, `[6,8]`, and `[1,3]`. The incompatibility is $(2-1) + (3-2) + (8-6) + (3-1) = 6$.

Example 3:

****Input:**** nums = [5,3,3,6,3,3], k = 3 ****Output:**** -1 ****Explanation:**** It is impossible to distribute nums into 3 subsets where no two elements are equal in the same subset.

****Constraints:****

*`1 <= k <= nums.length <= 16` *`nums.length` is divisible by `k` *`1 <= nums[i] <= nums.length`

Code Snippets

C++:

```
class Solution {
public:
    int minimumIncompatibility(vector<int>& nums, int k) {

    }
};
```

Java:

```
class Solution {
    public int minimumIncompatibility(int[] nums, int k) {

    }
}
```

Python3:

```
class Solution:
    def minimumIncompatibility(self, nums: List[int], k: int) -> int:
```