

# Problem 378: Kth Smallest Element in a Sorted Matrix

## Problem Information

**Difficulty:** Medium

**Acceptance Rate:** 64.07%

**Paid Only:** No

**Tags:** Array, Binary Search, Sorting, Heap (Priority Queue), Matrix

## Problem Description

Given an  $n \times n$  matrix where each of the rows and columns is sorted in ascending order, return the  $k$ th smallest element in the matrix.

Note that it is the  $k$ th smallest element in the sorted order, not the  $k$ th distinct element.

You must find a solution with a memory complexity better than  $O(n^2)$ .

**Example 1:**

**Input:** matrix = [[1,5,9],[10,11,13],[12,13,15]], k = 8 **Output:** 13 **Explanation:** The elements in the matrix are [1,5,9,10,11,12,13,13,15], and the 8th smallest number is 13

**Example 2:**

**Input:** matrix = [[-5]], k = 1 **Output:** -5

**Constraints:**

$n == \text{matrix.length} == \text{matrix}[i].\text{length}$ ,  $1 \leq n \leq 300$ ,  $-109 \leq \text{matrix}[i][j] \leq 109$ . All the rows and columns of matrix are guaranteed to be sorted in non-decreasing order.  
 $1 \leq k \leq n^2$

**Follow up:**

\* Could you solve the problem with a constant memory (i.e.,  $O(1)$  memory complexity)? \*  
Could you solve the problem in  $O(n)$  time complexity? The solution may be too advanced for an interview but you may find reading [this paper](<http://www.cse.yorku.ca/~andy/pubs/X+Y.pdf>) fun.

## Code Snippets

### C++:

```
class Solution {  
public:  
    int kthSmallest(vector<vector<int>>& matrix, int k) {  
  
    }  
};
```

### Java:

```
class Solution {  
    public int kthSmallest(int[][] matrix, int k) {  
  
    }  
}
```

### Python3:

```
class Solution:  
    def kthSmallest(self, matrix: List[List[int]], k: int) -> int:
```