

Problem 2435: Paths in Matrix Whose Sum Is Divisible by K

Problem Information

Difficulty: **Hard**

Acceptance Rate: 44.87%

Paid Only: No

Tags: Array, Dynamic Programming, Matrix

Problem Description

You are given a **0-indexed** $m \times n$ integer matrix `grid` and an integer `k`. You are currently at position `(0, 0)` and you want to reach position `(m - 1, n - 1)` moving only **down** or **right**.

Return the number of paths where the sum of the elements on the path is divisible by `k`. Since the answer may be very large, return it **modulo** $10^9 + 7$.

Example 1:

Input: `grid = [[5,2,4],[3,0,5],[0,7,2]]`, `k = 3` **Output:** `2` **Explanation:** There are two paths where the sum of the elements on the path is divisible by `k`. The first path highlighted in red has a sum of $5 + 2 + 4 + 5 + 2 = 18$ which is divisible by 3. The second path highlighted in blue has a sum of $5 + 3 + 0 + 5 + 2 = 15$ which is divisible by 3.

Example 2:

Input: `grid = [[0,0]]`, `k = 5` **Output:** `1` **Explanation:** The path highlighted in red has a sum of $0 + 0 = 0$ which is divisible by 5.

Example 3:

Input: grid = [[7,3,4,9],[2,3,6,2],[2,3,7,0]], k = 1 **Output:** 10 **Explanation:** Every integer is divisible by 1 so the sum of the elements on every possible path is divisible by k.

Constraints:

$m == \text{grid.length}$ $n == \text{grid}[i].\text{length}$ $1 \leq m, n \leq 5 \cdot 10^4$ $1 \leq m \cdot n \leq 5 \cdot 10^4$ $0 \leq \text{grid}[i][j] \leq 100$ $1 \leq k \leq 50$

Code Snippets

C++:

```
class Solution {
public:
    int numberOfPaths(vector<vector<int>>& grid, int k) {

    }
};
```

Java:

```
class Solution {
    public int numberOfPaths(int[][] grid, int k) {

    }
}
```

Python3:

```
class Solution:
    def numberOfPaths(self, grid: List[List[int]], k: int) -> int:
```