

Problem 2867: Count Valid Paths in a Tree

Problem Information

Difficulty: **Hard**

Acceptance Rate: 0.00%

Paid Only: No

Problem Description

There is an undirected tree with

n

nodes labeled from

1

to

n .

You are given the integer

n

and a 2D integer array

edges

of length

$n - 1$

, where

`edges[i] = [u`

`i`

`, v`

`i`

`]`

indicates that there is an edge between nodes

`u`

`i`

and

`v`

`i`

in the tree.

Return

the

number of valid paths

in the tree

.

A path

(a, b)

is

valid

if there exists

exactly one

prime number among the node labels in the path from

a

to

b

.

Note

that:

The path

(a, b)

is a sequence of

distinct

nodes starting with node

a

and ending with node

b

such that every two adjacent nodes in the sequence share an edge in the tree.

Path

(a, b)

and path

(b, a)

are considered the

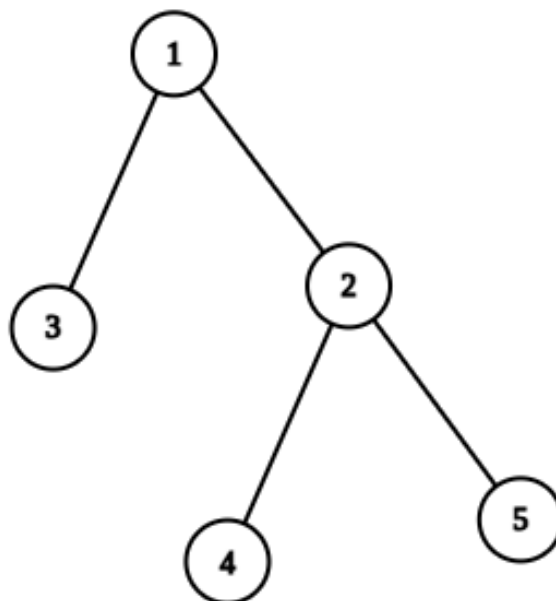
same

and counted only

once

.

Example 1:



Input:

$n = 5$, edges = $[[1,2],[1,3],[2,4],[2,5]]$

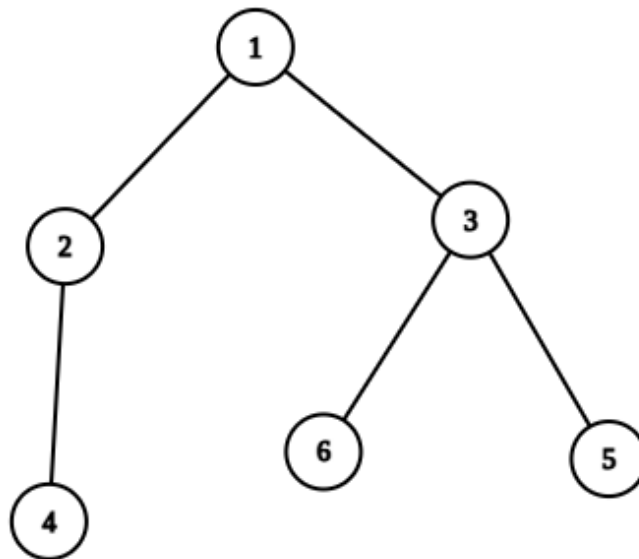
Output:

4

Explanation:

The pairs with exactly one prime number on the path between them are: - (1, 2) since the path from 1 to 2 contains prime number 2. - (1, 3) since the path from 1 to 3 contains prime number 3. - (1, 4) since the path from 1 to 4 contains prime number 2. - (2, 4) since the path from 2 to 4 contains prime number 2. It can be shown that there are only 4 valid paths.

Example 2:



Input:

$n = 6$, edges = $[[1,2],[1,3],[2,4],[3,5],[3,6]]$

Output:

6

Explanation:

The pairs with exactly one prime number on the path between them are: - (1, 2) since the path from 1 to 2 contains prime number 2. - (1, 3) since the path from 1 to 3 contains prime number 3. - (1, 4) since the path from 1 to 4 contains prime number 2. - (1, 6) since the path from 1 to 6 contains prime number 3. - (2, 4) since the path from 2 to 4 contains prime number 2. - (3, 6) since the path from 3 to 6 contains prime number 3. It can be shown that there are only 6 valid paths.

Constraints:

$1 \leq n \leq 10$

5

`edges.length == n - 1`

`edges[i].length == 2`

$1 \leq u$

`i`

`, v`

`i`

$\leq n$

The input is generated such that

`edges`

represent a valid tree.

Code Snippets

C++:

```

class Solution {
public:
    long long countPaths(int n, vector<vector<int>>& edges) {

    }

};

```

Java:

```

class Solution {
    public long countPaths(int n, int[][] edges) {

    }

}

```

Python3:

```

class Solution:
    def countPaths(self, n: int, edges: List[List[int]]) -> int:

```

Python:

```

class Solution(object):
    def countPaths(self, n, edges):
        """
        :type n: int
        :type edges: List[List[int]]
        :rtype: int
        """

```

JavaScript:

```

/**
 * @param {number} n
 * @param {number[][]} edges
 * @return {number}
 */
var countPaths = function(n, edges) {

};

```

TypeScript:

```
function countPaths(n: number, edges: number[][]): number {  
  
};
```

C#:

```
public class Solution {  
    public long CountPaths(int n, int[][] edges) {  
  
    }  
}
```

C:

```
long long countPaths(int n, int** edges, int edgesSize, int* edgesColSize) {  
  
}
```

Go:

```
func countPaths(n int, edges [][]int) int64 {  
  
}
```

Kotlin:

```
class Solution {  
    fun countPaths(n: Int, edges: Array<IntArray>): Long {  
  
    }  
}
```

Swift:

```
class Solution {  
    func countPaths(_ n: Int, _ edges: [[Int]]) -> Int {  
  
    }  
}
```

Rust:


```

impl Solution {
  pub fn count_paths(n: i32, edges: Vec<Vec<i32>>) -> i64 {

  }
}

```

Ruby:

```

# @param {Integer} n
# @param {Integer[][]} edges
# @return {Integer}
def count_paths(n, edges)

end

```

PHP:

```

class Solution {

  /**
   * @param Integer $n
   * @param Integer[][] $edges
   * @return Integer
   */
  function countPaths($n, $edges) {

  }
}

```

Dart:

```

class Solution {
  int countPaths(int n, List<List<int>> edges) {

  }
}

```

Scala:

```

object Solution {
  def countPaths(n: Int, edges: Array[Array[Int]]): Long = {

  }
}

```

```
}
```

Elixir:

```
defmodule Solution do
  @spec count_paths(n :: integer, edges :: [[integer]]) :: integer
  def count_paths(n, edges) do

  end
end
```

Erlang:

```
-spec count_paths(N :: integer(), Edges :: [[integer()]]) -> integer().
count_paths(N, Edges) ->
.
```

Racket:

```
(define/contract (count-paths n edges)
  (-> exact-integer? (listof (listof exact-integer?)) exact-integer?)
)
```

Solutions

C++ Solution:

```
/*
 * Problem: Count Valid Paths in a Tree
 * Difficulty: Hard
 * Tags: array, tree, dp, math, search
 *
 * Approach: Use two pointers or sliding window technique
 * Time Complexity: O(n) or O(n log n)
 * Space Complexity: O(n) or O(n * m) for DP table
 */

class Solution {
public:
    long long countPaths(int n, vector<vector<int>>& edges) {
```

```
}  
};
```

Java Solution:

```
/**  
 * Problem: Count Valid Paths in a Tree  
 * Difficulty: Hard  
 * Tags: array, tree, dp, math, search  
 *  
 * Approach: Use two pointers or sliding window technique  
 * Time Complexity: O(n) or O(n log n)  
 * Space Complexity: O(n) or O(n * m) for DP table  
 */  
  
class Solution {  
    public long countPaths(int n, int[][] edges) {  
  
    }  
}
```

Python3 Solution:

```
"""  
Problem: Count Valid Paths in a Tree  
Difficulty: Hard  
Tags: array, tree, dp, math, search  
  
Approach: Use two pointers or sliding window technique  
Time Complexity: O(n) or O(n log n)  
Space Complexity: O(n) or O(n * m) for DP table  
"""  
  
class Solution:  
    def countPaths(self, n: int, edges: List[List[int]]) -> int:  
        # TODO: Implement optimized solution  
        pass
```

Python Solution:

```

class Solution(object):
def countPaths(self, n, edges):
    """
    :type n: int
    :type edges: List[List[int]]
    :rtype: int
    """

```

JavaScript Solution:

```

/**
 * Problem: Count Valid Paths in a Tree
 * Difficulty: Hard
 * Tags: array, tree, dp, math, search
 *
 * Approach: Use two pointers or sliding window technique
 * Time Complexity: O(n) or O(n log n)
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 */

/**
 * @param {number} n
 * @param {number[][]} edges
 * @return {number}
 */
var countPaths = function(n, edges) {

};

```

TypeScript Solution:

```

/**
 * Problem: Count Valid Paths in a Tree
 * Difficulty: Hard
 * Tags: array, tree, dp, math, search
 *
 * Approach: Use two pointers or sliding window technique
 * Time Complexity: O(n) or O(n log n)
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 */

function countPaths(n: number, edges: number[][]): number {

```

```
};
```

C# Solution:

```
/*
 * Problem: Count Valid Paths in a Tree
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 * Time Complexity: O(n) or O(n log n)
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 */

public class Solution {
    public long CountPaths(int n, int[][] edges) {

    }
}
```

C Solution:

```
/*
 * Problem: Count Valid Paths in a Tree
 * Difficulty: Hard
 * Tags: array, tree, dp, math, search
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 * Time Complexity: O(n) or O(n log n)
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 */

long long countPaths(int n, int** edges, int edgesSize, int* edgesColSize) {

}
```

Go Solution:

```
// Problem: Count Valid Paths in a Tree
// Difficulty: Hard
```

```

// Tags: array, tree, dp, math, search
//
// Approach: Use two pointers or sliding window technique
// Time Complexity: O(n) or O(n log n)
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func countPaths(n int, edges [][]int) int64 {

}

```

Kotlin Solution:

```

class Solution {
    fun countPaths(n: Int, edges: Array<IntArray>): Long {

    }
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Swift Solution:

```

class Solution {
    func countPaths(_ n: Int, _ edges: [[Int]]) -> Int {

    }
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Rust Solution:

```

// Problem: Count Valid Paths in a Tree
// Difficulty: Hard
// Tags: array, tree, dp, math, search
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// Approach: Use two pointers or sliding window technique
// Time Complexity: O(n) or O(n log n)
// Space Complexity: O(n) or O(n * m) for DP table

impl Solution {
    pub fn count_paths(n: i32, edges: Vec<Vec<i32>>)> -> i64 {

    }
}

```

Ruby Solution:

```
# @param {Integer} n
# @param {Integer[][]} edges
# @return {Integer}
def count_paths(n, edges)

end
```

PHP Solution:

```
class Solution {

    /**
     * @param Integer $n
     * @param Integer[][] $edges
     * @return Integer
     */
    function countPaths($n, $edges) {

    }

}
```

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