

Problem 3013: Divide an Array Into Subarrays With Minimum Cost II

Problem Information

Difficulty: Hard

Acceptance Rate: 31.22%

Paid Only: No

Tags: Array, Hash Table, Sliding Window, Heap (Priority Queue)

Problem Description

You are given a **0-indexed** array of integers `nums` of length `n`, and two **positive** integers `k` and `dist`.

The **cost** of an array is the value of its **first** element. For example, the cost of `[1,2,3]` is `1` while the cost of `[3,4,1]` is `3`.

You need to divide `nums` into `k` **disjoint contiguous** subarrays, such that the difference between the starting index of the **second** subarray and the starting index of the `kth` subarray should be **less than or equal to** `dist`. In other words, if you divide `nums` into the subarrays `nums[0..(i1 - 1)]`, `nums[i1..(i2 - 1)]`, ..., `nums[ik-1..(n - 1)]`, then $i_{k-1} - i_1 \leq dist$.

Return the**minimum** possible sum of the cost of these subarrays.

Example 1:

Input: `nums = [1,3,2,6,4,2]`, `k = 3`, `dist = 3` **Output:** 5 **Explanation:** The best possible way to divide `nums` into 3 subarrays is: [1,3], [2,6,4], and [2]. This choice is valid because $i_{k-1} - i_1$ is $5 - 2 = 3$ which is equal to `dist`. The total cost is $nums[0] + nums[2] + nums[5]$ which is $1 + 2 + 2 = 5$. It can be shown that there is no possible way to divide `nums` into 3 subarrays at a cost lower than 5.

Example 2:

Input: `nums = [10,1,2,2,2,1]`, `k = 4`, `dist = 3` **Output:** 15 **Explanation:** The best possible way to divide `nums` into 4 subarrays is: [10], [1], [2], and [2,2,1]. This choice is valid

because $i_{k-1} - i_1$ is $3 - 1 = 2$ which is less than dist. The total cost is $\text{nums}[0] + \text{nums}[1] + \text{nums}[2] + \text{nums}[3]$ which is $10 + 1 + 2 + 2 = 15$. The division [10], [1], [2,2,2], and [1] is not valid, because the difference between i_{k-1} and i_1 is $5 - 1 = 4$, which is greater than dist. It can be shown that there is no possible way to divide nums into 4 subarrays at a cost lower than 15.

Example 3:

Input: `nums = [10,8,18,9], k = 3, dist = 1` **Output:** `36` **Explanation:** The best possible way to divide nums into 4 subarrays is: [10], [8], and [18,9]. This choice is valid because $i_{k-1} - i_1$ is $2 - 1 = 1$ which is equal to dist. The total cost is $\text{nums}[0] + \text{nums}[1] + \text{nums}[2]$ which is $10 + 8 + 18 = 36$. The division [10], [8,18], and [9] is not valid, because the difference between i_{k-1} and i_1 is $3 - 1 = 2$, which is greater than dist. It can be shown that there is no possible way to divide nums into 3 subarrays at a cost lower than 36.

Constraints:

`* `3 <= n <= 105` * `1 <= nums[i] <= 109` * `3 <= k <= n` * `k - 2 <= dist <= n - 2``

Code Snippets

C++:

```
class Solution {
public:
    long long minimumCost(vector<int>& nums, int k, int dist) {
    }
};
```

Java:

```
class Solution {
public long minimumCost(int[] nums, int k, int dist) {
    }
}
```

Python3:

```
class Solution:  
    def minimumCost(self, nums: List[int], k: int, dist: int) -> int:
```