

# Problem 987: Vertical Order Traversal of a Binary Tree

## Problem Information

Difficulty: Hard

Acceptance Rate: 0.00%

Paid Only: No

## Problem Description

Given the

root

of a binary tree, calculate the

vertical order traversal

of the binary tree.

For each node at position

(row, col)

, its left and right children will be at positions

(row + 1, col - 1)

and

(row + 1, col + 1)

respectively. The root of the tree is at

(0, 0)

The

vertical order traversal

of a binary tree is a list of top-to-bottom orderings for each column index starting from the leftmost column and ending on the rightmost column. There may be multiple nodes in the same row and same column. In such a case, sort these nodes by their values.

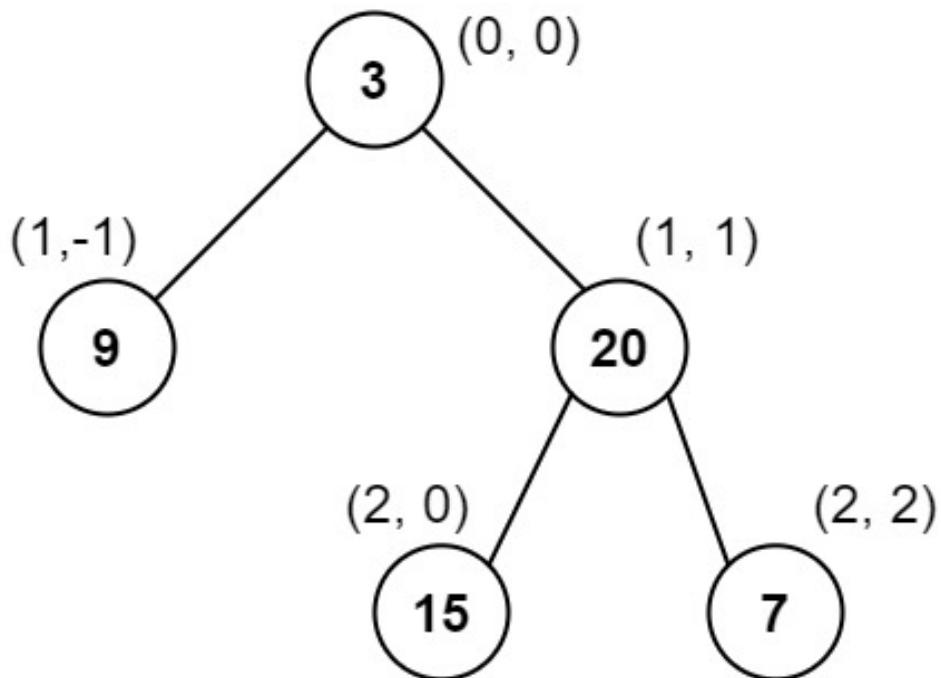
Return

the

vertical order traversal

of the binary tree

Example 1:



Input:

```
root = [3,9,20,null,null,15,7]
```

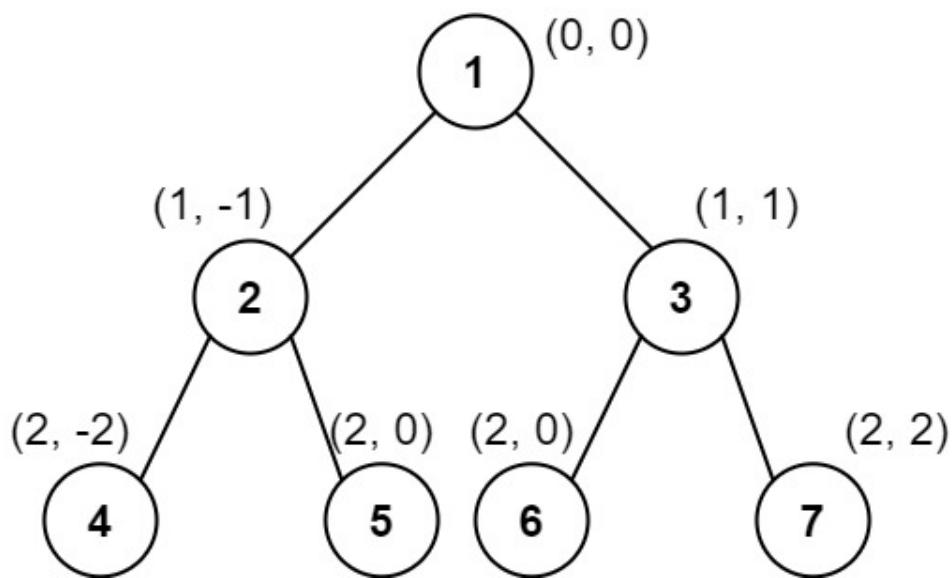
Output:

```
[[9],[3,15],[20],[7]]
```

Explanation:

Column -1: Only node 9 is in this column. Column 0: Nodes 3 and 15 are in this column in that order from top to bottom. Column 1: Only node 20 is in this column. Column 2: Only node 7 is in this column.

Example 2:



Input:

```
root = [1,2,3,4,5,6,7]
```

Output:

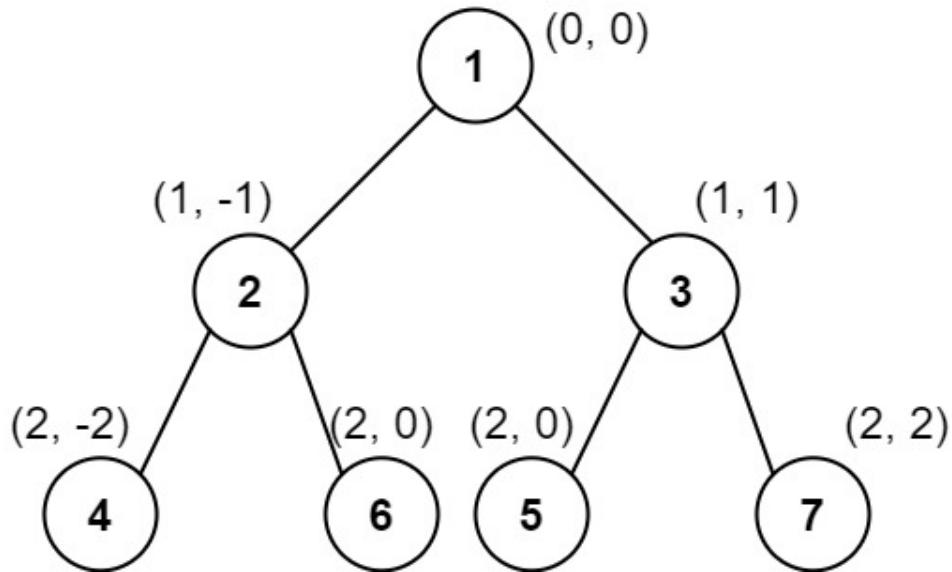
```
[[4],[2],[1,5,6],[3],[7]]
```

Explanation:

Column -2: Only node 4 is in this column. Column -1: Only node 2 is in this column. Column 0: Nodes 1, 5, and 6 are in this column. 1 is at the top, so it comes first. 5 and 6 are at the same

position  $(2, 0)$ , so we order them by their value, 5 before 6. Column 1: Only node 3 is in this column. Column 2: Only node 7 is in this column.

Example 3:



Input:

root = [1,2,3,4,6,5,7]

Output:

[[4],[2],[1,5,6],[3],[7]]

Explanation:

This case is the exact same as example 2, but with nodes 5 and 6 swapped. Note that the solution remains the same since 5 and 6 are in the same location and should be ordered by their values.

Constraints:

The number of nodes in the tree is in the range

[1, 1000]

$0 \leq \text{Node.val} \leq 1000$

## Code Snippets

### C++:

```
/**
 * Definition for a binary tree node.
 * struct TreeNode {
 *     int val;
 *     TreeNode *left;
 *     TreeNode *right;
 *     TreeNode() : val(0), left(nullptr), right(nullptr) {}
 *     TreeNode(int x) : val(x), left(nullptr), right(nullptr) {}
 *     TreeNode(int x, TreeNode *left, TreeNode *right) : val(x), left(left),
 *     right(right) {}
 * };
 */
class Solution {
public:
    vector<vector<int>> verticalTraversal(TreeNode* root) {
        }
    };
}
```

### Java:

```
/**
 * Definition for a binary tree node.
 * public class TreeNode {
 *     int val;
 *     TreeNode left;
 *     TreeNode right;
 *     TreeNode() {}
 *     TreeNode(int val) { this.val = val; }
 *     TreeNode(int val, TreeNode left, TreeNode right) {
 *         this.val = val;
 *         this.left = left;
 *         this.right = right;
 *     }
 * }
```

```

*/
class Solution {
public List<List<Integer>> verticalTraversal(TreeNode root) {

}
}

```

### Python3:

```

# Definition for a binary tree node.
# class TreeNode:
#     def __init__(self, val=0, left=None, right=None):
#         self.val = val
#         self.left = left
#         self.right = right
class Solution:
    def verticalTraversal(self, root: Optional[TreeNode]) -> List[List[int]]:

```

### Python:

```

# Definition for a binary tree node.
# class TreeNode(object):
#     def __init__(self, val=0, left=None, right=None):
#         self.val = val
#         self.left = left
#         self.right = right
class Solution(object):
    def verticalTraversal(self, root):
        """
        :type root: Optional[TreeNode]
        :rtype: List[List[int]]
        """

```

### JavaScript:

```

/**
 * Definition for a binary tree node.
 * function TreeNode(val, left, right) {
 *     this.val = (val===undefined ? 0 : val)
 *     this.left = (left===undefined ? null : left)
 *     this.right = (right===undefined ? null : right)
 * }

```

```

*/
/**
 * @param {TreeNode} root
 * @return {number[][]}
 */
var verticalTraversal = function(root) {

};

```

### TypeScript:

```

/**
 * Definition for a binary tree node.
 * class TreeNode {
 *   val: number
 *   left: TreeNode | null
 *   right: TreeNode | null
 *   constructor(val?: number, left?: TreeNode | null, right?: TreeNode | null)
 *   {
 *     this.val = (val==undefined ? 0 : val)
 *     this.left = (left==undefined ? null : left)
 *     this.right = (right==undefined ? null : right)
 *   }
 * }
 */

function verticalTraversal(root: TreeNode | null): number[][] {
}

```

### C#:

```

/**
 * Definition for a binary tree node.
 * public class TreeNode {
 *   public int val;
 *   public TreeNode left;
 *   public TreeNode right;
 *   public TreeNode(int val=0, TreeNode left=null, TreeNode right=null) {
 *     this.val = val;
 *     this.left = left;
 *     this.right = right;
 * }

```

```

* }
* }
*/
public class Solution {
    public IList<IList<int>> VerticalTraversal(TreeNode root) {
        }

    }
}

```

## C:

```

/**
 * Definition for a binary tree node.
 * struct TreeNode {
 *     int val;
 *     struct TreeNode *left;
 *     struct TreeNode *right;
 * };
 */
/**
 * Return an array of arrays of size *returnSize.
 * The sizes of the arrays are returned as *returnColumnSizes array.
 * Note: Both returned array and *columnSizes array must be malloced, assume
 * caller calls free().
 */
int** verticalTraversal(struct TreeNode* root, int* returnSize, int** returnColumnSizes) {

}

```

## Go:

```

/**
 * Definition for a binary tree node.
 * type TreeNode struct {
 *     Val int
 *     Left *TreeNode
 *     Right *TreeNode
 * }
 */
func verticalTraversal(root *TreeNode) [][]int {

```

```
}
```

## Kotlin:

```
/**  
 * Example:  
 * var ti = TreeNode(5)  
 * var v = ti.`val`  
 * Definition for a binary tree node.  
 * class TreeNode(var `val`: Int) {  
 *     var left: TreeNode? = null  
 *     var right: TreeNode? = null  
 * }  
 */  
class Solution {  
    fun verticalTraversal(root: TreeNode?): List<List<Int>> {  
        }  
    }
```

## Swift:

```
/**  
 * Definition for a binary tree node.  
 * public class TreeNode {  
 *     public var val: Int  
 *     public var left: TreeNode?  
 *     public var right: TreeNode?  
 *     public init() { self.val = 0; self.left = nil; self.right = nil; }  
 *     public init(_ val: Int) { self.val = val; self.left = nil; self.right = nil; }  
 *     public init(_ val: Int, _ left: TreeNode?, _ right: TreeNode?) {  
 *         self.val = val  
 *         self.left = left  
 *         self.right = right  
 *     }  
 * }  
 */  
class Solution {  
    func verticalTraversal(_ root: TreeNode?) -> [[Int]] {  
        }
```

```
}
```

## Rust:

```
// Definition for a binary tree node.
// #[derive(Debug, PartialEq, Eq)]
// pub struct TreeNode {
//     pub val: i32,
//     pub left: Option<Rc<RefCell<TreeNode>>,
//     pub right: Option<Rc<RefCell<TreeNode>>,
// }
//
// impl TreeNode {
//     #[inline]
//     pub fn new(val: i32) -> Self {
//         TreeNode {
//             val,
//             left: None,
//             right: None
//         }
//     }
// }
use std::rc::Rc;
use std::cell::RefCell;
impl Solution {
    pub fn vertical_traversal(root: Option<Rc<RefCell<TreeNode>> ) ->
        Vec<Vec<i32>> {
        }

    }
}
```

## Ruby:

```
# Definition for a binary tree node.
# class TreeNode
# attr_accessor :val, :left, :right
# def initialize(val = 0, left = nil, right = nil)
#   @val = val
#   @left = left
#   @right = right
# end
# end
```

```

# @param {TreeNode} root
# @return {Integer[][]}
def vertical_traversal(root)

end

```

## PHP:

```

/**
 * Definition for a binary tree node.
 * class TreeNode {
 *     public $val = null;
 *     public $left = null;
 *     public $right = null;
 *     function __construct($val = 0, $left = null, $right = null) {
 *         $this->val = $val;
 *         $this->left = $left;
 *         $this->right = $right;
 *     }
 * }
 */
class Solution {

    /**
     * @param TreeNode $root
     * @return Integer[][]
     */
    function verticalTraversal($root) {

    }
}

```

## Dart:

```

/**
 * Definition for a binary tree node.
 * class TreeNode {
 *     int val;
 *     TreeNode? left;
 *     TreeNode? right;
 *     TreeNode([this.val = 0, this.left, this.right]);
 * }

```

```

*/
class Solution {
List<List<int>> verticalTraversal(TreeNode? root) {

}
}

```

### Scala:

```

/** 
 * Definition for a binary tree node.
 * class TreeNode(_value: Int = 0, _left: TreeNode = null, _right: TreeNode = null) {
 *   var value: Int = _value
 *   var left: TreeNode = _left
 *   var right: TreeNode = _right
 * }
 */
object Solution {
def verticalTraversal(root: TreeNode): List[List[Int]] = {

}
}

```

### Elixir:

```

# Definition for a binary tree node.
#
# defmodule TreeNode do
# @type t :: %__MODULE__{
#   val: integer,
#   left: TreeNode.t() | nil,
#   right: TreeNode.t() | nil
# }
# defstruct val: 0, left: nil, right: nil
# end

defmodule Solution do
@spec vertical_traversal(root :: TreeNode.t | nil) :: [[integer]]
def vertical_traversal(root) do

end

```

```
end
```

### Erlang:

```
%% Definition for a binary tree node.  
%%  
%% -record(tree_node, {val = 0 :: integer(),  
%% left = null :: 'null' | #tree_node{},  
%% right = null :: 'null' | #tree_node{}}).  
  
-spec vertical_traversal(Root :: #tree_node{} | null) -> [[integer()]].  
vertical_traversal(Root) ->  
.
```

### Racket:

```
; Definition for a binary tree node.  
#|  
  
; val : integer?  
; left : (or/c tree-node? #f)  
; right : (or/c tree-node? #f)  
(struct tree-node  
(val left right) #:mutable #:transparent)  
  
; constructor  
(define (make-tree-node [val 0])  
(tree-node val #f #f))  
  
|#  
  
(define/contract (vertical-traversal root)  
(-> (or/c tree-node? #f) (listof (listof exact-integer?)))  
)
```

## Solutions

### C++ Solution:

```

/*
 * Problem: Vertical Order Traversal of a Binary Tree
 * Difficulty: Hard
 * Tags: tree, hash, sort, search
 *
 * Approach: DFS or BFS traversal
 * Time Complexity: O(n) where n is number of nodes
 * Space Complexity: O(h) for recursion stack where h is height
 */

/**
 * Definition for a binary tree node.
 * struct TreeNode {
 *     int val;
 *     TreeNode *left;
 *     TreeNode *right;
 *     TreeNode() : val(0), left(nullptr), right(nullptr) {}
 *     TreeNode(int x) : val(x), left(nullptr), right(nullptr) {}
 *     TreeNode(int x, TreeNode *left, TreeNode *right) : val(x), left(left),
 * right(right) {}
 * };
 */
class Solution {
public:
    vector<vector<int>> verticalTraversal(TreeNode* root) {
}
};

```

## Java Solution:

```

/**
 * Problem: Vertical Order Traversal of a Binary Tree
 * Difficulty: Hard
 * Tags: tree, hash, sort, search
 *
 * Approach: DFS or BFS traversal
 * Time Complexity: O(n) where n is number of nodes
 * Space Complexity: O(h) for recursion stack where h is height
 */

/**

```

```

* Definition for a binary tree node.
* public class TreeNode {
* int val;
* TreeNode left;
* TreeNode right;
* TreeNode() {}
* TreeNode(int val) { this.val = val; }
* TreeNode(int val, TreeNode left, TreeNode right) {
* this.val = val;
* this.left = left;
* this.right = right;
* }
* }
*/
class Solution {
public List<List<Integer>> verticalTraversal(TreeNode root) {
}

}

```

### Python3 Solution:

```

"""
Problem: Vertical Order Traversal of a Binary Tree
Difficulty: Hard
Tags: tree, hash, sort, search

Approach: DFS or BFS traversal
Time Complexity: O(n) where n is number of nodes
Space Complexity: O(h) for recursion stack where h is height
"""

```

```

# Definition for a binary tree node.
# class TreeNode:
#     def __init__(self, val=0, left=None, right=None):
#         self.val = val
#         self.left = left
#         self.right = right
class Solution:

    def verticalTraversal(self, root: Optional[TreeNode]) -> List[List[int]]:
        # TODO: Implement optimized solution

```

```
pass
```

## Python Solution:

```
# Definition for a binary tree node.
# class TreeNode(object):
#     def __init__(self, val=0, left=None, right=None):
#         self.val = val
#         self.left = left
#         self.right = right
class Solution(object):
    def verticalTraversal(self, root):
        """
        :type root: Optional[TreeNode]
        :rtype: List[List[int]]
        """

```

## JavaScript Solution:

```
/**
 * Problem: Vertical Order Traversal of a Binary Tree
 * Difficulty: Hard
 * Tags: tree, hash, sort, search
 *
 * Approach: DFS or BFS traversal
 * Time Complexity: O(n) where n is number of nodes
 * Space Complexity: O(h) for recursion stack where h is height
 */

/**
 * Definition for a binary tree node.
 * function TreeNode(val, left, right) {
 *     this.val = (val===undefined ? 0 : val)
 *     this.left = (left===undefined ? null : left)
 *     this.right = (right===undefined ? null : right)
 * }
 */
/**
 * @param {TreeNode} root
 * @return {number[][]}
 */
```

```
var verticalTraversal = function(root) {  
};
```

### TypeScript Solution:

```
/**  
 * Problem: Vertical Order Traversal of a Binary Tree  
 * Difficulty: Hard  
 * Tags: tree, hash, sort, search  
 *  
 * Approach: DFS or BFS traversal  
 * Time Complexity: O(n) where n is number of nodes  
 * Space Complexity: O(h) for recursion stack where h is height  
 */  
  
/**  
 * Definition for a binary tree node.  
 * class TreeNode {  
 *   val: number  
 *   left: TreeNode | null  
 *   right: TreeNode | null  
 *   constructor(val?: number, left?: TreeNode | null, right?: TreeNode | null)  
 {  
   this.val = (val==undefined ? 0 : val)  
   this.left = (left==undefined ? null : left)  
   this.right = (right==undefined ? null : right)  
 }  
 }  
 */  
  
function verticalTraversal(root: TreeNode | null): number[][] {  
};
```

### C# Solution:

```
/*  
 * Problem: Vertical Order Traversal of a Binary Tree  
 * Difficulty: Hard  
 * Tags: tree, hash, sort, search
```

```

/*
 * Approach: DFS or BFS traversal
 * Time Complexity: O(n) where n is number of nodes
 * Space Complexity: O(h) for recursion stack where h is height
 */

/**
 * Definition for a binary tree node.
 * public class TreeNode {
 *     public int val;
 *     public TreeNode left;
 *     public TreeNode right;
 *     public TreeNode(int val=0, TreeNode left=null, TreeNode right=null) {
 *         this.val = val;
 *         this.left = left;
 *         this.right = right;
 *     }
 * }
 */
public class Solution {
    public IList<IList<int>> VerticalTraversal(TreeNode root) {
        }

    }
}

```

## C Solution:

```

/*
 * Problem: Vertical Order Traversal of a Binary Tree
 * Difficulty: Hard
 * Tags: tree, hash, sort, search
 *
 * Approach: DFS or BFS traversal
 * Time Complexity: O(n) where n is number of nodes
 * Space Complexity: O(h) for recursion stack where h is height
 */

/**
 * Definition for a binary tree node.
 * struct TreeNode {
 *     int val;
 *
```

```

* struct TreeNode *left;
* struct TreeNode *right;
* };
*/
/***
* Return an array of arrays of size *returnSize.
* The sizes of the arrays are returned as *returnColumnSizes array.
* Note: Both returned array and *columnSizes array must be malloced, assume
caller calls free().
*/
int** verticalTraversal(struct TreeNode* root, int* returnSize, int** returnColumnSizes) {

}

```

## Go Solution:

```

// Problem: Vertical Order Traversal of a Binary Tree
// Difficulty: Hard
// Tags: tree, hash, sort, search
//
// Approach: DFS or BFS traversal
// Time Complexity: O(n) where n is number of nodes
// Space Complexity: O(h) for recursion stack where h is height

/***
* Definition for a binary tree node.
* type TreeNode struct {
*     Val int
*     Left *TreeNode
*     Right *TreeNode
* }
*/
func verticalTraversal(root *TreeNode) [][]int {

}

```

## Kotlin Solution:

```

/***
* Example:

```

```

* var ti = TreeNode(5)
* var v = ti.`val`
* Definition for a binary tree node.
* class TreeNode(var `val`: Int) {
* var left: TreeNode? = null
* var right: TreeNode? = null
* }
*/
class Solution {
fun verticalTraversal(root: TreeNode?): List<List<Int>> {
}
}

```

### Swift Solution:

```

/**
* Definition for a binary tree node.
* public class TreeNode {
* public var val: Int
* public var left: TreeNode?
* public var right: TreeNode?
* public init() { self.val = 0; self.left = nil; self.right = nil; }
* public init(_ val: Int) { self.val = val; self.left = nil; self.right =
nil; }
* public init(_ val: Int, _ left: TreeNode?, _ right: TreeNode?) {
* self.val = val
* self.left = left
* self.right = right
* }
* }
*/
class Solution {
func verticalTraversal(_ root: TreeNode?) -> [[Int]] {
}
}

```

### Rust Solution:

```

// Problem: Vertical Order Traversal of a Binary Tree
// Difficulty: Hard
// Tags: tree, hash, sort, search
//
// Approach: DFS or BFS traversal
// Time Complexity: O(n) where n is number of nodes
// Space Complexity: O(h) for recursion stack where h is height

// Definition for a binary tree node.
// #[derive(Debug, PartialEq, Eq)]
// pub struct TreeNode {
//     pub val: i32,
//     pub left: Option<Rc<RefCell<TreeNode>>,
//     pub right: Option<Rc<RefCell<TreeNode>>,
// }
//
// impl TreeNode {
//     #[inline]
//     pub fn new(val: i32) -> Self {
//         TreeNode {
//             val,
//             left: None,
//             right: None
//         }
//     }
// }
use std::rc::Rc;
use std::cell::RefCell;
impl Solution {
    pub fn vertical_traversal(root: Option<Rc<RefCell<TreeNode>>>) -> Vec<Vec<i32>> {
        }

    }
}

```

## Ruby Solution:

```

# Definition for a binary tree node.
# class TreeNode
# attr_accessor :val, :left, :right
# def initialize(val = 0, left = nil, right = nil)
#   @val = val

```

```

# @left = left
# @right = right
# end
# end
# @param {TreeNode} root
# @return {Integer[][]}
def vertical_traversal(root)

end

```

### PHP Solution:

```

/**
 * Definition for a binary tree node.
 * class TreeNode {
 *     public $val = null;
 *     public $left = null;
 *     public $right = null;
 *     function __construct($val = 0, $left = null, $right = null) {
 *         $this->val = $val;
 *         $this->left = $left;
 *         $this->right = $right;
 *     }
 * }
 */
class Solution {

/**
 * @param TreeNode $root
 * @return Integer[][]
 */
function verticalTraversal($root) {

}
}

```

### Dart Solution:

```

/**
 * Definition for a binary tree node.
 * class TreeNode {

```

```

* int val;
* TreeNode? left;
* TreeNode? right;
* TreeNode([this.val = 0, this.left, this.right]);
*
class Solution {
List<List<int>> verticalTraversal(TreeNode? root) {

}
}

```

### Scala Solution:

```

/**
* Definition for a binary tree node.
* class TreeNode(_value: Int = 0, _left: TreeNode = null, _right: TreeNode = null) {
* var value: Int = _value
* var left: TreeNode = _left
* var right: TreeNode = _right
* }
*/
object Solution {
def verticalTraversal(root: TreeNode): List[List[Int]] = {

}
}

```

### Elixir Solution:

```

# Definition for a binary tree node.
#
# defmodule TreeNode do
# @type t :: %__MODULE__{
#   val: integer,
#   left: TreeNode.t() | nil,
#   right: TreeNode.t() | nil
# }
# defstruct val: 0, left: nil, right: nil
# end

```

```

defmodule Solution do
@spec vertical_traversal(root :: TreeNode.t | nil) :: [[integer]]
def vertical_traversal(root) do

end
end

```

### Erlang Solution:

```

%% Definition for a binary tree node.

%% -record(tree_node, {val = 0 :: integer(),
%% left = null :: 'null' | #tree_node{},
%% right = null :: 'null' | #tree_node{}}).

-spec vertical_traversal(Root :: #tree_node{} | null) -> [[integer()]].
vertical_traversal(Root) ->
.
.
```

### Racket Solution:

```

; Definition for a binary tree node.
#|
; val : integer?
; left : (or/c tree-node? #f)
; right : (or/c tree-node? #f)
(struct tree-node
  (val left right) #:mutable #:transparent)

; constructor
(define (make-tree-node [val 0])
  (tree-node val #f #f))

|#
(define/contract (vertical-traversal root)
  (-> (or/c tree-node? #f) (listof (listof exact-integer?))))
)
```