

Problem 3559: Number of Ways to Assign Edge Weights II

Problem Information

Difficulty: Hard

Acceptance Rate: 59.86%

Paid Only: No

Tags: Array, Math, Dynamic Programming, Bit Manipulation, Tree, Depth-First Search

Problem Description

There is an undirected tree with `n` nodes labeled from 1 to `n`, rooted at node 1. The tree is represented by a 2D integer array `edges` of length `n - 1`, where `edges[i] = [ui, vi]` indicates that there is an edge between nodes `ui` and `vi`.

Initially, all edges have a weight of 0. You must assign each edge a weight of either **1** or **2**.

The **cost** of a path between any two nodes `u` and `v` is the total weight of all edges in the path connecting them.

You are given a 2D integer array `queries`. For each `queries[i] = [ui, vi]`, determine the number of ways to assign weights to edges **in the path** such that the cost of the path between `ui` and `vi` is **odd**.

Return an array `answer`, where `answer[i]` is the number of valid assignments for `queries[i]`.

Since the answer may be large, apply **modulo** `10⁹ + 7` to each `answer[i]`.

Note: For each query, disregard all edges **not** in the path between node `ui` and `vi`.

Example 1:

****Input:**** edges = [[1,2]], queries = [[1,1],[1,2]]

****Output:**** [0,1]

****Explanation:****

* Query `[1,1]` : The path from Node 1 to itself consists of no edges, so the cost is 0. Thus, the number of valid assignments is 0.
* Query `[1,2]` : The path from Node 1 to Node 2 consists of one edge (`1 -> 2`). Assigning weight 1 makes the cost odd, while 2 makes it even. Thus, the number of valid assignments is 1.

****Example 2:****

****Input:**** edges = [[1,2],[1,3],[3,4],[3,5]], queries = [[1,4],[3,4],[2,5]]

****Output:**** [2,1,4]

****Explanation:****

* Query `[1,4]` : The path from Node 1 to Node 4 consists of two edges (`1 -> 3` and `3 -> 4`). Assigning weights (1,2) or (2,1) results in an odd cost. Thus, the number of valid assignments is 2.
* Query `[3,4]` : The path from Node 3 to Node 4 consists of one edge (`3 -> 4`). Assigning weight 1 makes the cost odd, while 2 makes it even. Thus, the number of valid assignments is 1.
* Query `[2,5]` : The path from Node 2 to Node 5 consists of three edges (`2 -> 1, 1 -> 3,` and `3 -> 5`). Assigning (1,2,2), (2,1,2), (2,2,1), or (1,1,1) makes the cost odd. Thus, the number of valid assignments is 4.

****Constraints:****

* `2 <= n <= 105` * `edges.length == n - 1` * `edges[i] == [ui, vi]` * `1 <= queries.length <= 105`
* `queries[i] == [ui, vi]` * `1 <= ui, vi <= n` * `edges` represents a valid tree.

Code Snippets

C++:

```
class Solution {
public:
vector<int> assignEdgeWeights(vector<vector<int>>& edges,
vector<vector<int>>& queries) {

}
};
```

Java:

```
class Solution {
public int[] assignEdgeWeights(int[][] edges, int[][] queries) {

}
}
```

Python3:

```
class Solution:
def assignEdgeWeights(self, edges: List[List[int]], queries: List[List[int]]) -> List[int]:
```