

# Problem 2872: Maximum Number of K-Divisible Components

## Problem Information

**Difficulty:** Hard

**Acceptance Rate:** 69.55%

**Paid Only:** No

**Tags:** Tree, Depth-First Search

## Problem Description

There is an undirected tree with `n` nodes labeled from `0` to `n - 1`. You are given the integer `n` and a 2D integer array `edges` of length `n - 1`, where `edges[i] = [ai, bi]` indicates that there is an edge between nodes `ai` and `bi` in the tree.

You are also given a \*\*0-indexed\*\* integer array `values` of length `n`, where `values[i]` is the \*\*value\*\* associated with the `ith` node, and an integer `k`.

A \*\*valid split\*\* of the tree is obtained by removing any set of edges, possibly empty, from the tree such that the resulting components all have values that are divisible by `k`, where the \*\*value of a connected component\*\* is the sum of the values of its nodes.

Return \_the\*\*maximum number of components\*\* in any valid split\_.

**Example 1:**



**Input:** n = 5, edges = [[0,2],[1,2],[1,3],[2,4]], values = [1,8,1,4,4], k = 6 **Output:** 2

**Explanation:** We remove the edge connecting node 1 with 2. The resulting split is valid because: - The value of the component containing nodes 1 and 3 is values[1] + values[3] = 12. - The value of the component containing nodes 0, 2, and 4 is values[0] + values[2] + values[4] = 6. It can be shown that no other valid split has more than 2 connected components.

**Example 2:**



**Input:** n = 7, edges = [[0,1],[0,2],[1,3],[1,4],[2,5],[2,6]], values = [3,0,6,1,5,2,1], k = 3  
**Output:** 3  
**Explanation:** We remove the edge connecting node 0 with 2, and the edge connecting node 0 with 1. The resulting split is valid because:  
- The value of the component containing node 0 is values[0] = 3.  
- The value of the component containing nodes 2, 5, and 6 is values[2] + values[5] + values[6] = 9.  
- The value of the component containing nodes 1, 3, and 4 is values[1] + values[3] + values[4] = 6.  
It can be shown that no other valid split has more than 3 connected components.

**Constraints:**

\* `1 <= n <= 3 \* 104` \* `edges.length == n - 1` \* `edges[i].length == 2` \* `0 <= ai, bi < n` \* `values.length == n` \* `0 <= values[i] <= 109` \* `1 <= k <= 109` \* Sum of `values` is divisible by `k`. \* The input is generated such that `edges` represents a valid tree.

## Code Snippets

**C++:**

```
class Solution {
public:
    int maxKDivisibleComponents(int n, vector<vector<int>>& edges, vector<int>& values, int k) {
        ...
    };
}
```

**Java:**

```
class Solution {
    public int maxKDivisibleComponents(int n, int[][][] edges, int[] values, int k)
    {
        ...
    }
}
```

**Python3:**

```
class Solution:  
    def maxKDivisibleComponents(self, n: int, edges: List[List[int]], values:  
        List[int], k: int) -> int:
```