

# Problem 3608: Minimum Time for K Connected Components

## Problem Information

**Difficulty:** Medium

**Acceptance Rate:** 44.92%

**Paid Only:** No

**Tags:** Binary Search, Union Find, Graph, Sorting

## Problem Description

You are given an integer `n` and an undirected graph with `n` nodes labeled from 0 to `n - 1`. This is represented by a 2D array `edges`, where `edges[i] = [ui, vi, timei]` indicates an undirected edge between nodes `ui` and `vi` that can be removed at `timei`.

You are also given an integer `k`.

Initially, the graph may be connected or disconnected. Your task is to find the \*\*minimum\*\* time `t` such that after removing all edges with `time <= t`, the graph contains \*\*at least\*\* `k` connected components.

Return the \*\*minimum\*\* time `t`.

A \*\*connected component\*\* is a subgraph of a graph in which there exists a path between any two vertices, and no vertex of the subgraph shares an edge with a vertex outside of the subgraph.

**Example 1:**

**Input:** n = 2, edges = [[0,1,3]], k = 2

**Output:** 3

**Explanation:**



\* Initially, there is one connected component  $\{0, 1\}$ . \* At  $\text{time} = 1$  or  $2$ , the graph remains unchanged. \* At  $\text{time} = 3$ , edge  $[0, 1]$  is removed, resulting in  $k = 2$  connected components  $\{0\}$ ,  $\{1\}$ . Thus, the answer is 3.

**Example 2:**

**Input:**  $n = 3$ , edges =  $[[0,1,2],[1,2,4]]$ ,  $k = 3$

**Output:** 4

**Explanation:**



\* Initially, there is one connected component  $\{0, 1, 2\}$ . \* At  $\text{time} = 2$ , edge  $[0, 1]$  is removed, resulting in two connected components  $\{0\}$ ,  $\{1, 2\}$ . \* At  $\text{time} = 4$ , edge  $[1, 2]$  is removed, resulting in  $k = 3$  connected components  $\{0\}$ ,  $\{1\}$ ,  $\{2\}$ . Thus, the answer is 4.

**Example 3:**

**Input:**  $n = 3$ , edges =  $[[0,2,5]]$ ,  $k = 2$

**Output:** 0

**Explanation:**



\* Since there are already  $k = 2$  disconnected components  $\{1\}$ ,  $\{0, 2\}$ , no edge removal is needed. Thus, the answer is 0.

**Constraints:**

\*  $1 \leq n \leq 105$  \*  $0 \leq \text{edges.length} \leq 105$  \*  $\text{edges}[i] = [ui, vi, timei]$  \*  $0 \leq ui, vi < n$  \*  $ui \neq vi$  \*  $1 \leq \text{timei} \leq 109$  \*  $1 \leq k \leq n$  \* There are no duplicate edges.

## Code Snippets

### C++:

```
class Solution {  
public:  
    int minTime(int n, vector<vector<int>>& edges, int k) {  
  
    }  
};
```

### Java:

```
class Solution {  
    public int minTime(int n, int[][] edges, int k) {  
  
    }  
}
```

### Python3:

```
class Solution:  
    def minTime(self, n: int, edges: List[List[int]], k: int) -> int:
```