

Problem 3218: Minimum Cost for Cutting Cake I

Problem Information

Difficulty: **Medium**

Acceptance Rate: 0.00%

Paid Only: No

Problem Description

There is an

$m \times n$

cake that needs to be cut into

1×1

pieces.

You are given integers

m

,

n

, and two arrays:

$horizontalCut$

of size

$m - 1$

, where

$\text{horizontalCut}[i]$

represents the cost to cut along the horizontal line

i

.

verticalCut

of size

$n - 1$

, where

$\text{verticalCut}[j]$

represents the cost to cut along the vertical line

j

.

In one operation, you can choose any piece of cake that is not yet a

1×1

square and perform one of the following cuts:

Cut along a horizontal line

i

at a cost of

$\text{horizontalCut}[i]$

.

Cut along a vertical line

j

at a cost of

verticalCut[j]

.

After the cut, the piece of cake is divided into two distinct pieces.

The cost of a cut depends only on the initial cost of the line and does not change.

Return the

minimum

total cost to cut the entire cake into

1 x 1

pieces.

Example 1:

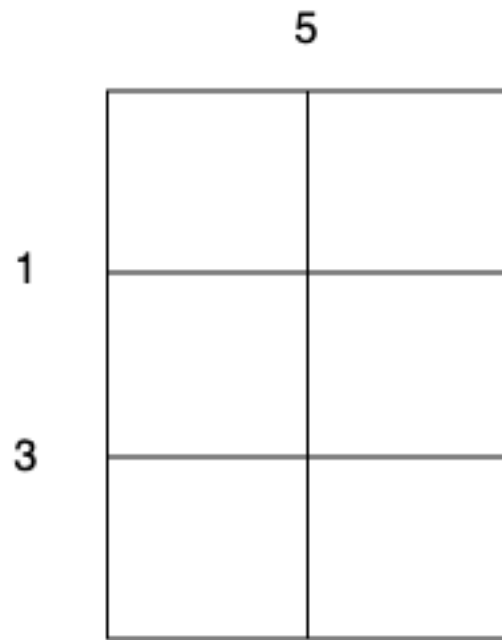
Input:

m = 3, n = 2, horizontalCut = [1,3], verticalCut = [5]

Output:

13

Explanation:



Perform a cut on the vertical line 0 with cost 5, current total cost is 5.

Perform a cut on the horizontal line 0 on

3 x 1

subgrid with cost 1.

Perform a cut on the horizontal line 0 on

3 x 1

subgrid with cost 1.

Perform a cut on the horizontal line 1 on

2 x 1

subgrid with cost 3.

Perform a cut on the horizontal line 1 on

2 x 1

subgrid with cost 3.

The total cost is

$$5 + 1 + 1 + 3 + 3 = 13$$

.

Example 2:

Input:

m = 2, n = 2, horizontalCut = [7], verticalCut = [4]

Output:

15

Explanation:

Perform a cut on the horizontal line 0 with cost 7.

Perform a cut on the vertical line 0 on

1 x 2

subgrid with cost 4.

Perform a cut on the vertical line 0 on

1 x 2

subgrid with cost 4.

The total cost is

$$7 + 4 + 4 = 15$$

.

Constraints:

$$1 \leq m, n \leq 20$$

$$\text{horizontalCut.length} == m - 1$$

$$\text{verticalCut.length} == n - 1$$

$$1 \leq \text{horizontalCut}[i], \text{verticalCut}[i] \leq 10$$

3

Code Snippets

C++:

```
class Solution {
public:
    int minimumCost(int m, int n, vector<int>& horizontalCut, vector<int>&
verticalCut) {

    }
};
```

Java:

```
class Solution {
    public int minimumCost(int m, int n, int[] horizontalCut, int[] verticalCut)
    {

    }
}
```

Python3:

```

class Solution:
    def minimumCost(self, m: int, n: int, horizontalCut: List[int], verticalCut:
List[int]) -> int:

```

Python:

```

class Solution(object):
    def minimumCost(self, m, n, horizontalCut, verticalCut):
        """
        :type m: int
        :type n: int
        :type horizontalCut: List[int]
        :type verticalCut: List[int]
        :rtype: int
        """

```

JavaScript:

```

/**
 * @param {number} m
 * @param {number} n
 * @param {number[]} horizontalCut
 * @param {number[]} verticalCut
 * @return {number}
 */
var minimumCost = function(m, n, horizontalCut, verticalCut) {

};

```

TypeScript:

```

function minimumCost(m: number, n: number, horizontalCut: number[],
verticalCut: number[]): number {

};

```

C#:

```

public class Solution {
    public int MinimumCost(int m, int n, int[] horizontalCut, int[] verticalCut)
    {

    }
}

```

```
}
```

C:

```
int minimumCost(int m, int n, int* horizontalCut, int horizontalCutSize, int*
verticalCut, int verticalCutSize) {

}
```

Go:

```
func minimumCost(m int, n int, horizontalCut []int, verticalCut []int) int {

}
```

Kotlin:

```
class Solution {
    fun minimumCost(m: Int, n: Int, horizontalCut: IntArray, verticalCut:
IntArray): Int {

    }
}
```

Swift:

```
class Solution {
    func minimumCost(_ m: Int, _ n: Int, _ horizontalCut: [Int], _ verticalCut:
[Int]) -> Int {

    }
}
```

Rust:

```
impl Solution {
    pub fn minimum_cost(m: i32, n: i32, horizontal_cut: Vec<i32>, vertical_cut:
Vec<i32>) -> i32 {

    }
}
```


Ruby:

```
# @param {Integer} m
# @param {Integer} n
# @param {Integer[]} horizontal_cut
# @param {Integer[]} vertical_cut
# @return {Integer}
def minimum_cost(m, n, horizontal_cut, vertical_cut)

end
```

PHP:

```
class Solution {

    /**
     * @param Integer $m
     * @param Integer $n
     * @param Integer[] $horizontalCut
     * @param Integer[] $verticalCut
     * @return Integer
     */
    function minimumCost($m, $n, $horizontalCut, $verticalCut) {

    }

}
```

Dart:

```
class Solution {
  int minimumCost(int m, int n, List<int> horizontalCut, List<int> verticalCut)
  {

  }

}
```

Scala:

```
object Solution {
  def minimumCost(m: Int, n: Int, horizontalCut: Array[Int], verticalCut:
    Array[Int]): Int = {

  }

}
```

```
}
```

Elixir:

```
defmodule Solution do
  @spec minimum_cost(m :: integer, n :: integer, horizontal_cut :: [integer],
    vertical_cut :: [integer]) :: integer
  def minimum_cost(m, n, horizontal_cut, vertical_cut) do

  end
end
```

Erlang:

```
-spec minimum_cost(M :: integer(), N :: integer(), HorizontalCut ::
  [integer()], VerticalCut :: [integer()]) -> integer().
minimum_cost(M, N, HorizontalCut, VerticalCut) ->
.
```

Racket:

```
(define/contract (minimum-cost m n horizontalCut verticalCut)
  (-> exact-integer? exact-integer? (listof exact-integer?) (listof
    exact-integer?) exact-integer?)
)
```

Solutions

C++ Solution:

```
/*
 * Problem: Minimum Cost for Cutting Cake I
 * Difficulty: Medium
 * Tags: array, dp, greedy, sort
 *
 * Approach: Use two pointers or sliding window technique
 * Time Complexity: O(n) or O(n log n)
 * Space Complexity: O(n) or O(n * m) for DP table
 */
```

```

class Solution {
public:
    int minimumCost(int m, int n, vector<int>& horizontalCut, vector<int>&
verticalCut) {

    }

};

```

Java Solution:

```

/**
 * Problem: Minimum Cost for Cutting Cake I
 * Difficulty: Medium
 * Tags: array, dp, greedy, sort
 *
 * Approach: Use two pointers or sliding window technique
 * Time Complexity: O(n) or O(n log n)
 * Space Complexity: O(n) or O(n * m) for DP table
 */

class Solution {
public int minimumCost(int m, int n, int[] horizontalCut, int[] verticalCut)
{

}

}

```

Python3 Solution:

```

"""
Problem: Minimum Cost for Cutting Cake I
Difficulty: Medium
Tags: array, dp, greedy, sort

Approach: Use two pointers or sliding window technique
Time Complexity: O(n) or O(n log n)
Space Complexity: O(n) or O(n * m) for DP table
"""

class Solution:
    def minimumCost(self, m: int, n: int, horizontalCut: List[int], verticalCut:

```

```
List[int]) -> int:
# TODO: Implement optimized solution
pass
```

Python Solution:

```
class Solution(object):
def minimumCost(self, m, n, horizontalCut, verticalCut):
"""
:type m: int
:type n: int
:type horizontalCut: List[int]
:type verticalCut: List[int]
:rtype: int
"""
```

JavaScript Solution:

```
/**
 * Problem: Minimum Cost for Cutting Cake I
 * Difficulty: Medium
 * Tags: array, dp, greedy, sort
 *
 * Approach: Use two pointers or sliding window technique
 * Time Complexity: O(n) or O(n log n)
 * Space Complexity: O(n) or O(n * m) for DP table
 */

/**
 * @param {number} m
 * @param {number} n
 * @param {number[]} horizontalCut
 * @param {number[]} verticalCut
 * @return {number}
 */
var minimumCost = function(m, n, horizontalCut, verticalCut) {

};
```

TypeScript Solution:

```

/**
 * Problem: Minimum Cost for Cutting Cake I
 * Difficulty: Medium
 * Tags: array, dp, greedy, sort
 *
 * Approach: Use two pointers or sliding window technique
 * Time Complexity: O(n) or O(n log n)
 * Space Complexity: O(n) or O(n * m) for DP table
 */

function minimumCost(m: number, n: number, horizontalCut: number[],
verticalCut: number[]): number {

};

```

C# Solution:

```

/*
 * Problem: Minimum Cost for Cutting Cake I
 * Difficulty: Medium
 * Tags: array, dp, greedy, sort
 *
 * Approach: Use two pointers or sliding window technique
 * Time Complexity: O(n) or O(n log n)
 * Space Complexity: O(n) or O(n * m) for DP table
 */

public class Solution {
    public int MinimumCost(int m, int n, int[] horizontalCut, int[] verticalCut)
    {

    }

}

```

C Solution:

```

/*
 * Problem: Minimum Cost for Cutting Cake I
 * Difficulty: Medium
 * Tags: array, dp, greedy, sort
 *
 * Approach: Use two pointers or sliding window technique

```

```

* Time Complexity: O(n) or O(n log n)
* Space Complexity: O(n) or O(n * m) for DP table
*/

int minimumCost(int m, int n, int* horizontalCut, int horizontalCutSize, int*
verticalCut, int verticalCutSize) {

}

```

Go Solution:

```

// Problem: Minimum Cost for Cutting Cake I
// Difficulty: Medium
// Tags: array, dp, greedy, sort
//
// Approach: Use two pointers or sliding window technique
// Time Complexity: O(n) or O(n log n)
// Space Complexity: O(n) or O(n * m) for DP table

func minimumCost(m int, n int, horizontalCut []int, verticalCut []int) int {

}

```

Kotlin Solution:

```

class Solution {
    fun minimumCost(m: Int, n: Int, horizontalCut: IntArray, verticalCut:
IntArray): Int {

    }
}

```

Swift Solution:

```

class Solution {
    func minimumCost(_ m: Int, _ n: Int, _ horizontalCut: [Int], _ verticalCut:
[Int]) -> Int {

    }
}

```

Rust Solution:

```
// Problem: Minimum Cost for Cutting Cake I
// Difficulty: Medium
// Tags: array, dp, greedy, sort
//
// Approach: Use two pointers or sliding window technique
// Time Complexity: O(n) or O(n log n)
// Space Complexity: O(n) or O(n * m) for DP table

impl Solution {
    pub fn minimum_cost(m: i32, n: i32, horizontal_cut: Vec<i32>, vertical_cut:
Vec<i32>) -> i32 {

    }
}
```

Ruby Solution:

```
# @param {Integer} m
# @param {Integer} n
# @param {Integer[]} horizontal_cut
# @param {Integer[]} vertical_cut
# @return {Integer}
def minimum_cost(m, n, horizontal_cut, vertical_cut)

end
```

PHP Solution:

```
class Solution {

    /**
     * @param Integer $m
     * @param Integer $n
     * @param Integer[] $horizontalCut
     * @param Integer[] $verticalCut
     * @return Integer
     */
    function minimumCost($m, $n, $horizontalCut, $verticalCut) {

    }

}
```

Dart Solution:

```
class Solution {  
  int minimumCost(int m, int n, List<int> horizontalCut, List<int> verticalCut)  
  {  
  
  }  
}
```

Scala Solution:

```
object Solution {  
  def minimumCost(m: Int, n: Int, horizontalCut: Array[Int], verticalCut:  
    Array[Int]): Int = {  
  
  }  
}
```

Elixir Solution:

```
defmodule Solution do  
  @spec minimum_cost(m :: integer, n :: integer, horizontal_cut :: [integer],  
    vertical_cut :: [integer]) :: integer  
  def minimum_cost(m, n, horizontal_cut, vertical_cut) do  
  
  end  
end
```

Erlang Solution:

```
-spec minimum_cost(M :: integer(), N :: integer(), HorizontalCut ::  
  [integer()], VerticalCut :: [integer()]) -> integer().  
minimum_cost(M, N, HorizontalCut, VerticalCut) ->  
  .
```

Racket Solution:

```
(define/contract (minimum-cost m n horizontalCut verticalCut)  
  (-> exact-integer? exact-integer? (listof exact-integer?) (listof  
    exact-integer?) exact-integer?)  
  )
```