

Problem 1766: Tree of Coprimes

Problem Information

Difficulty: Hard

Acceptance Rate: 43.37%

Paid Only: No

Tags: Array, Math, Tree, Depth-First Search, Number Theory

Problem Description

There is a tree (i.e., a connected, undirected graph that has no cycles) consisting of n nodes numbered from 0 to $n - 1$ and exactly $n - 1$ edges. Each node has a value associated with it, and the **root** of the tree is node 0 .

To represent this tree, you are given an integer array `nums` and a 2D array `edges`. Each `nums[i]` represents the i th node's value, and each `edges[j] = [u, v]` represents an edge between nodes u and v in the tree.

Two values x and y are **coprime** if $\text{gcd}(x, y) == 1$ where $\text{gcd}(x, y)$ is the **greatest common divisor** of x and y .

An ancestor of a node i is any other node on the shortest path from node i to the **root**. A node is **not** considered an ancestor of itself.

Return an array `ans` of size n , where `ans[i]` is the closest ancestor to node i such that `nums[i]` and `nums[ans[i]]` are **coprime**, or -1 if there is no such ancestor.

Example 1:



Input: `nums = [2,3,3,2]`, `edges = [[0,1],[1,2],[1,3]]` **Output:** `[-1,0,0,1]` **Explanation:** In the above figure, each node's value is in parentheses. - Node 0 has no coprime ancestors. - Node 1 has only one ancestor, node 0. Their values are coprime ($\text{gcd}(2,3) == 1$). - Node 2 has two ancestors, nodes 1 and 0. Node 1's value is not coprime ($\text{gcd}(3,3) == 3$), but node 0's

value is $\text{gcd}(2,3) == 1$, so node 0 is the closest valid ancestor. - Node 3 has two ancestors, nodes 1 and 0. It is coprime with node 1 ($\text{gcd}(3,2) == 1$), so node 1 is its closest valid ancestor.

Example 2:

Input: `nums = [5,6,10,2,3,6,15]`, `edges = [[0,1],[0,2],[1,3],[1,4],[2,5],[2,6]]` **Output:** `[-1,0,-1,0,0,0,-1]`

Constraints:

`nums.length == n` * `1 <= nums[i] <= 50` * `1 <= n <= 105` * `edges.length == n - 1` *
`edges[j].length == 2` * `0 <= u_j, v_j < n` * `u_j != v_j``

Code Snippets

C++:

```
class Solution {
public:
    vector<int> getCoprimes(vector<int>& nums, vector<vector<int>>& edges) {

    }
};
```

Java:

```
class Solution {
    public int[] getCoprimes(int[] nums, int[][] edges) {

    }
}
```

Python3:

```
class Solution:
    def getCoprimes(self, nums: List[int], edges: List[List[int]]) -> List[int]:
```