

Problem 3426: Manhattan Distances of All Arrangements of Pieces

Problem Information

Difficulty: Hard

Acceptance Rate: 0.00%

Paid Only: No

Problem Description

You are given three integers

m

,

n

, and

k

.

There is a rectangular grid of size

$m \times n$

containing

k

identical pieces. Return the sum of Manhattan distances between every pair of pieces over all

valid arrangements

of pieces.

A

valid arrangement

is a placement of all

k

pieces on the grid with

at most

one piece per cell.

Since the answer may be very large, return it

modulo

10

9

+ 7

.

The Manhattan Distance between two cells

(x

i

, y

i

)

and

(x

j

, y

j

)

is

|x

i

- x

j

| + |y

i

- y

j

|

.

Example 1:

Input:

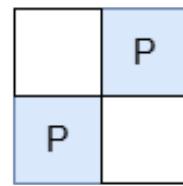
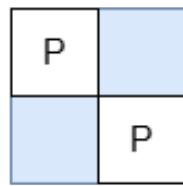
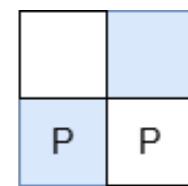
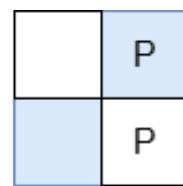
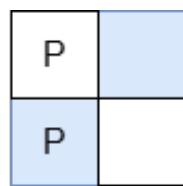
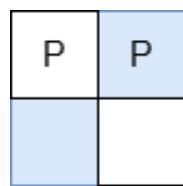
$m = 2, n = 2, k = 2$

Output:

8

Explanation:

The valid arrangements of pieces on the board are:



In the first 4 arrangements, the Manhattan distance between the two pieces is 1.

In the last 2 arrangements, the Manhattan distance between the two pieces is 2.

Thus, the total Manhattan distance across all valid arrangements is

$$1 + 1 + 1 + 1 + 2 + 2 = 8$$

Example 2:

Input:

$m = 1, n = 4, k = 3$

Output:

20

Explanation:

The valid arrangements of pieces on the board are:



The first and last arrangements have a total Manhattan distance of

$$1 + 1 + 2 = 4$$

.

The middle two arrangements have a total Manhattan distance of

$$1 + 2 + 3 = 6$$

.

The total Manhattan distance between all pairs of pieces across all arrangements is

$$4 + 6 + 6 + 4 = 20$$

.

Constraints:

$$1 \leq m, n \leq 10$$

5

$$2 \leq m * n \leq 10$$

5

$$2 \leq k \leq m * n$$

Code Snippets

C++:

```
class Solution {  
public:  
    int distanceSum(int m, int n, int k) {  
  
    }  
};
```

Java:

```
class Solution {  
    public int distanceSum(int m, int n, int k) {  
  
    }  
}
```

Python3:

```
class Solution:  
    def distanceSum(self, m: int, n: int, k: int) -> int:
```

Python:

```
class Solution(object):  
    def distanceSum(self, m, n, k):  
        """  
        :type m: int  
        :type n: int  
        :type k: int  
        :rtype: int  
        """
```

JavaScript:

```
/**  
 * @param {number} m  
 * @param {number} n  
 * @param {number} k  
 * @return {number}  
 */
```

```
var distanceSum = function(m, n, k) {  
};
```

TypeScript:

```
function distanceSum(m: number, n: number, k: number): number {  
};
```

C#:

```
public class Solution {  
    public int DistanceSum(int m, int n, int k) {  
        }  
    }
```

C:

```
int distanceSum(int m, int n, int k) {  
}
```

Go:

```
func distanceSum(m int, n int, k int) int {  
}
```

Kotlin:

```
class Solution {  
    fun distanceSum(m: Int, n: Int, k: Int): Int {  
        }  
    }
```

Swift:

```
class Solution {  
    func distanceSum(_ m: Int, _ n: Int, _ k: Int) -> Int {
```

```
}
```

```
}
```

Rust:

```
impl Solution {
    pub fn distance_sum(m: i32, n: i32, k: i32) -> i32 {
        }
    }
```

Ruby:

```
# @param {Integer} m
# @param {Integer} n
# @param {Integer} k
# @return {Integer}
def distance_sum(m, n, k)

end
```

PHP:

```
class Solution {

    /**
     * @param Integer $m
     * @param Integer $n
     * @param Integer $k
     * @return Integer
     */
    function distanceSum($m, $n, $k) {

    }
}
```

Dart:

```
class Solution {
    int distanceSum(int m, int n, int k) {
```

```
}
```

```
}
```

Scala:

```
object Solution {  
    def distanceSum(m: Int, n: Int, k: Int): Int = {  
  
    }  
}
```

Elixir:

```
defmodule Solution do  
  @spec distance_sum(m :: integer, n :: integer, k :: integer) :: integer  
  def distance_sum(m, n, k) do  
  
  end  
end
```

Erlang:

```
-spec distance_sum(M :: integer(), N :: integer(), K :: integer()) ->  
integer().  
distance_sum(M, N, K) ->  
.
```

Racket:

```
(define/contract (distance-sum m n k)  
  (-> exact-integer? exact-integer? exact-integer? exact-integer?)  
)
```

Solutions

C++ Solution:

```
/*  
 * Problem: Manhattan Distances of All Arrangements of Pieces  
 * Difficulty: Hard
```

```

* Tags: math
*
* Approach: Optimized algorithm based on problem constraints
* Time Complexity: O(n) to O(n^2) depending on approach
* Space Complexity: O(1) to O(n) depending on approach
*/

```

```

class Solution {
public:
    int distanceSum(int m, int n, int k) {
}
};

```

Java Solution:

```

/**
 * Problem: Manhattan Distances of All Arrangements of Pieces
 * Difficulty: Hard
 * Tags: math
 *
* Approach: Optimized algorithm based on problem constraints
* Time Complexity: O(n) to O(n^2) depending on approach
* Space Complexity: O(1) to O(n) depending on approach
*/

```

```

class Solution {
public int distanceSum(int m, int n, int k) {
}
}

```

Python3 Solution:

```

"""
Problem: Manhattan Distances of All Arrangements of Pieces
Difficulty: Hard
Tags: math

Approach: Optimized algorithm based on problem constraints
Time Complexity: O(n) to O(n^2) depending on approach

```

```
Space Complexity: O(1) to O(n) depending on approach
```

```
"""
```

```
class Solution:  
    def distanceSum(self, m: int, n: int, k: int) -> int:  
        # TODO: Implement optimized solution  
        pass
```

Python Solution:

```
class Solution(object):  
    def distanceSum(self, m, n, k):  
        """  
        :type m: int  
        :type n: int  
        :type k: int  
        :rtype: int  
        """
```

JavaScript Solution:

```
/**  
 * Problem: Manhattan Distances of All Arrangements of Pieces  
 * Difficulty: Hard  
 * Tags: math  
 *  
 * Approach: Optimized algorithm based on problem constraints  
 * Time Complexity: O(n) to O(n^2) depending on approach  
 * Space Complexity: O(1) to O(n) depending on approach  
 */  
  
/**  
 * @param {number} m  
 * @param {number} n  
 * @param {number} k  
 * @return {number}  
 */  
var distanceSum = function(m, n, k) {  
  
};
```

TypeScript Solution:

```
/**  
 * Problem: Manhattan Distances of All Arrangements of Pieces  
 * Difficulty: Hard  
 * Tags: math  
 *  
 * Approach: Optimized algorithm based on problem constraints  
 * Time Complexity: O(n) to O(n^2) depending on approach  
 * Space Complexity: O(1) to O(n) depending on approach  
 */  
  
function distanceSum(m: number, n: number, k: number): number {  
}  
;
```

C# Solution:

```
/*  
 * Problem: Manhattan Distances of All Arrangements of Pieces  
 * Difficulty: Hard  
 * Tags: math  
 *  
 * Approach: Optimized algorithm based on problem constraints  
 * Time Complexity: O(n) to O(n^2) depending on approach  
 * Space Complexity: O(1) to O(n) depending on approach  
 */  
  
public class Solution {  
    public int DistanceSum(int m, int n, int k) {  
        return 0;  
    }  
}
```

C Solution:

```
/*  
 * Problem: Manhattan Distances of All Arrangements of Pieces  
 * Difficulty: Hard  
 * Tags: math  
 *  
 * Approach: Optimized algorithm based on problem constraints  
 * Time Complexity: O(n) to O(n^2) depending on approach  
 */
```

```
* Space Complexity: O(1) to O(n) depending on approach
*/
int distanceSum(int m, int n, int k) {
}
```

Go Solution:

```
// Problem: Manhattan Distances of All Arrangements of Pieces
// Difficulty: Hard
// Tags: math
//
// Approach: Optimized algorithm based on problem constraints
// Time Complexity: O(n) to O(n^2) depending on approach
// Space Complexity: O(1) to O(n) depending on approach

func distanceSum(m int, n int, k int) int {
}
```

Kotlin Solution:

```
class Solution {
    fun distanceSum(m: Int, n: Int, k: Int): Int {
    }
}
```

Swift Solution:

```
class Solution {
    func distanceSum(_ m: Int, _ n: Int, _ k: Int) -> Int {
    }
}
```

Rust Solution:

```
// Problem: Manhattan Distances of All Arrangements of Pieces
// Difficulty: Hard
```

```

// Tags: math
//
// Approach: Optimized algorithm based on problem constraints
// Time Complexity: O(n) to O(n^2) depending on approach
// Space Complexity: O(1) to O(n) depending on approach

impl Solution {
    pub fn distance_sum(m: i32, n: i32, k: i32) -> i32 {
        ...
    }
}

```

Ruby Solution:

```

# @param {Integer} m
# @param {Integer} n
# @param {Integer} k
# @return {Integer}
def distance_sum(m, n, k)

end

```

PHP Solution:

```

class Solution {

    /**
     * @param Integer $m
     * @param Integer $n
     * @param Integer $k
     * @return Integer
     */
    function distanceSum($m, $n, $k) {
        ...
    }
}

```

Dart Solution:

```

class Solution {
    int distanceSum(int m, int n, int k) {

```

```
}
```

```
}
```

Scala Solution:

```
object Solution {  
    def distanceSum(m: Int, n: Int, k: Int): Int = {  
  
    }  
}
```

Elixir Solution:

```
defmodule Solution do  
  @spec distance_sum(m :: integer, n :: integer, k :: integer) :: integer  
  def distance_sum(m, n, k) do  
  
  end  
end
```

Erlang Solution:

```
-spec distance_sum(M :: integer(), N :: integer(), K :: integer()) ->  
integer().  
distance_sum(M, N, K) ->  
.
```

Racket Solution:

```
(define/contract (distance-sum m n k)  
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)
```