

Problem 3624: Number of Integers With Popcount-Depth Equal to K II

Problem Information

Difficulty: **Hard**

Acceptance Rate: 50.16%

Paid Only: No

Tags: Array, Divide and Conquer, Binary Indexed Tree, Segment Tree

Problem Description

You are given an integer array `nums`.

For any positive integer `x`, define the following sequence:

$p_0 = x$ $p_{i+1} = \text{popcount}(p_i)$ for all $i \geq 0$, where `popcount(y)` is the number of set bits (1's) in the binary representation of `y`.

This sequence will eventually reach the value 1.

The **popcount-depth** of `x` is defined as the **smallest** integer `d` ≥ 0 such that $p_d = 1$.

For example, if `x = 7` (binary representation `"111"`). Then, the sequence is: `7 -> 3 -> 2 -> 1`, so the popcount-depth of 7 is 3.

You are also given a 2D integer array `queries`, where each `queries[i]` is either:

`[1, l, r, k]` - **Determine** the number of indices `j` such that $l \leq j \leq r$ and the **popcount-depth** of `nums[j]` is equal to `k`. `[2, idx, val]` - **Update** `nums[idx]` to `val`.

Return an integer array `answer`, where `answer[i]` is the number of indices for the `i`th query of type `[1, l, r, k]`.

Example 1:

****Input:**** nums = [2,4], queries = [[1,0,1,1],[2,1,1],[1,0,1,0]]

****Output:**** [2,1]

****Explanation:****

`i` | `queries[i]` | `nums` | binary(`nums`) | popcount- depth | `[l, r]` | `k` | Valid `nums[j]` |
updated `nums` | Answer ---|---|---|---|---|---|---|---|--- 0 | [1,0,1,1] | [2,4] | [10, 100] | [1, 1] | [0,
1] | 1 | [0, 1] | -- | 2 1 | [2,1,1] | [2,4] | [10, 100] | [1, 1] | -- | -- | [2,1] | -- 2 | [1,0,1,0] | [2,1] |
[10, 1] | [1, 0] | [0, 1] | 0 | [1] | -- | 1 Thus, the final `answer` is `[2, 1]`.

****Example 2:****

****Input:**** nums = [3,5,6], queries = [[1,0,2,2],[2,1,4],[1,1,2,1],[1,0,1,0]]

****Output:**** [3,1,0]

****Explanation:****

`i` | `queries[i]` | `nums` | binary(`nums`) | popcount- depth | `[l, r]` | `k` | Valid `nums[j]` |
updated `nums` | Answer ---|---|---|---|---|---|---|---|--- 0 | [1,0,2,2] | [3, 5, 6] | [11, 101, 110] |
[2, 2, 2] | [0, 2] | 2 | [0, 1, 2] | -- | 3 1 | [2,1,4] | [3, 5, 6] | [11, 101, 110] | [2, 2, 2] | -- | -- | -- | [3, 4,
6] | -- 2 | [1,1,2,1] | [3, 4, 6] | [11, 100, 110] | [2, 1, 2] | [1, 2] | 1 | [1] | -- | 1 3 | [1,0,1,0] | [3, 4, 6]
| [11, 100, 110] | [2, 1, 2] | [0, 1] | 0 | [] | -- | 0 Thus, the final `answer` is `[3, 1, 0]`.

****Example 3:****

****Input:**** nums = [1,2], queries = [[1,0,1,1],[2,0,3],[1,0,0,1],[1,0,0,2]]

****Output:**** [1,0,1]

****Explanation:****

`i` | `queries[i]` | `nums` | binary(`nums`) | popcount- depth | `[l, r]` | `k` | Valid `nums[j]` |
updated `nums` | Answer ---|---|---|---|---|---|---|---|--- 0 | [1,0,1,1] | [1, 2] | [1, 10] | [0, 1] | [0,
1] | 1 | [1] | -- | 1 1 | [2,0,3] | [1, 2] | [1, 10] | [0, 1] | -- | -- | -- | [3, 2] | 2 | [1,0,0,1] | [3, 2] | [11, 10]
| [2, 1] | [0, 0] | 1 | [] | -- | 0 3 | [1,0,0,2] | [3, 2] | [11, 10] | [2, 1] | [0, 0] | 2 | [0] | -- | 1 Thus, the
final `answer` is `[1, 0, 1]`.

****Constraints:****

```
*`1 <= n == nums.length <= 105` *`1 <= nums[i] <= 1015` *`1 <= queries.length <= 105` *  
`queries[i].length == 3` or `4` *`queries[i] == [1, l, r, k]` or, *`queries[i] == [2, idx, val]` *`0 <= l  
<= r <= n - 1` *`0 <= k <= 5` *`0 <= idx <= n - 1` *`1 <= val <= 1015`
```

Code Snippets

C++:

```
class Solution {  
public:  
    vector<int> popcountDepth(vector<long long>& nums, vector<vector<long long>>&  
        queries) {  
  
    }  
};
```

Java:

```
class Solution {  
    public int[] popcountDepth(long[] nums, long[][] queries) {  
  
    }  
}
```

Python3:

```
class Solution:  
    def popcountDepth(self, nums: List[int], queries: List[List[int]]) ->  
        List[int]:
```