

# Problem 3416: Subsequences with a Unique Middle Mode II

## Problem Information

**Difficulty:** Hard

**Acceptance Rate:** 12.44%

**Paid Only:** Yes

**Tags:** Array, Hash Table, Math, Combinatorics

## Problem Description

Given an integer array `nums`, find the number of subsequences of size 5 of `nums` with a **unique middle mode**.

Since the answer may be very large, return it **modulo**  $10^9 + 7$ .

A **mode** of a sequence of numbers is defined as the element that appears the **maximum** number of times in the sequence.

A sequence of numbers contains a **unique mode** if it has only one mode.

A sequence of numbers `seq` of size 5 contains a **unique middle mode** if the `_middle` element (`seq[2]`) is a **unique mode**.

**Example 1:**

**Input:** `nums = [1,1,1,1,1]`

**Output:** 6

**Explanation:**

`[1, 1, 1, 1, 1]` is the only subsequence of size 5 that can be formed from this list, and it has a unique middle mode of 1.

**\*\*Example 2:\*\***

**\*\*Input:\*\*** nums = [1,2,2,3,3,4]

**\*\*Output:\*\*** 4

**\*\*Explanation:\*\***

`[1, 2, 2, 3, 4]` and `[1, 2, 3, 3, 4]` have unique middle modes because the number at index 2 has the greatest frequency in the subsequence. `[1, 2, 2, 3, 3]` does not have a unique middle mode because 2 and 3 both appear twice in the subsequence.

**\*\*Example 3:\*\***

**\*\*Input:\*\*** nums = [0,1,2,3,4,5,6,7,8]

**\*\*Output:\*\*** 0

**\*\*Explanation:\*\***

There does not exist a subsequence of length 5 with a unique middle mode.

**\*\*Constraints:\*\***

\* `5 <= nums.length <= 105` \* `-109 <= nums[i] <= 109`

## Code Snippets

**C++:**

```
class Solution {
public:
    int subsequencesWithMiddleMode(vector<int>& nums) {

    }

};
```

**Java:**

```
class Solution {  
    public int subsequencesWithMiddleMode(int[] nums) {  
  
    }  
}
```

### Python3:

```
class Solution:  
    def subsequencesWithMiddleMode(self, nums: List[int]) -> int:
```