

Problem 378: Kth Smallest Element in a Sorted Matrix

Problem Information

Difficulty: **Medium**

Acceptance Rate: 0.00%

Paid Only: No

Problem Description

Given an

$n \times n$

matrix

where each of the rows and columns is sorted in ascending order, return

the

k

th

smallest element in the matrix

.

Note that it is the

k

th

smallest element

in the sorted order

, not the

k

th

distinct

element.

You must find a solution with a memory complexity better than

$O(n$

2

)

.

Example 1:

Input:

matrix = [[1,5,9],[10,11,13],[12,13,15]], k = 8

Output:

13

Explanation:

The elements in the matrix are [1,5,9,10,11,12,13,

13

,15], and the 8

th

smallest number is 13

Example 2:

Input:

matrix = [[-5]], k = 1

Output:

-5

Constraints:

$n == \text{matrix.length} == \text{matrix}[i].\text{length}$

$1 \leq n \leq 300$

-10

9

$\leq \text{matrix}[i][j] \leq 10$

9

All the rows and columns of

matrix

are

guaranteed

to be sorted in

non-decreasing order

.

$1 \leq k \leq n$

2

Follow up:

Could you solve the problem with a constant memory (i.e.,

$O(1)$

memory complexity)?

Could you solve the problem in

$O(n)$

time complexity? The solution may be too advanced for an interview but you may find reading

this paper

fun.

Code Snippets

C++:

```
class Solution {
public:
    int kthSmallest(vector<vector<int>>& matrix, int k) {

    }
};
```

Java:

```

class Solution {
public int kthSmallest(int[][] matrix, int k) {

}

}

```

Python3:

```

class Solution:
def kthSmallest(self, matrix: List[List[int]], k: int) -> int:

```

Python:

```

class Solution(object):
def kthSmallest(self, matrix, k):
"""
:type matrix: List[List[int]]
:type k: int
:rtype: int
"""

```

JavaScript:

```

/**
 * @param {number[][]} matrix
 * @param {number} k
 * @return {number}
 */
var kthSmallest = function(matrix, k) {

};

```

TypeScript:

```

function kthSmallest(matrix: number[][], k: number): number {

};

```

C#:

```

public class Solution {
public int KthSmallest(int[][] matrix, int k) {

```

```
}  
}
```

C:

```
int kthSmallest(int** matrix, int matrixSize, int* matrixColSize, int k) {  
  
}
```

Go:

```
func kthSmallest(matrix [][]int, k int) int {  
  
}
```

Kotlin:

```
class Solution {  
    fun kthSmallest(matrix: Array<IntArray>, k: Int): Int {  
  
    }  
}
```

Swift:

```
class Solution {  
    func kthSmallest(_ matrix: [[Int]], _ k: Int) -> Int {  
  
    }  
}
```

Rust:

```
impl Solution {  
    pub fn kth_smallest(matrix: Vec<Vec<i32>>, k: i32) -> i32 {  
  
    }  
}
```

Ruby:

```

# @param {Integer[][]} matrix
# @param {Integer} k
# @return {Integer}
def kth_smallest(matrix, k)

end

```

PHP:

```

class Solution {

    /**
     * @param Integer[][] $matrix
     * @param Integer $k
     * @return Integer
     */
    function kthSmallest($matrix, $k) {

    }

}

```

Dart:

```

class Solution {
  int kthSmallest(List<List<int>> matrix, int k) {

  }

}

```

Scala:

```

object Solution {
  def kthSmallest(matrix: Array[Array[Int]], k: Int): Int = {

  }

}

```

Elixir:

```

defmodule Solution do
  @spec kth_smallest(matrix :: [[integer]], k :: integer) :: integer
  def kth_smallest(matrix, k) do

```

```
end
end
```

Erlang:

```
-spec kth_smallest(Matrix :: [[integer()]], K :: integer()) -> integer().
kth_smallest(Matrix, K) ->
.
```

Racket:

```
(define/contract (kth-smallest matrix k)
  (-> (listof (listof exact-integer?)) exact-integer? exact-integer?)
)
```

Solutions

C++ Solution:

```
/*
 * Problem: Kth Smallest Element in a Sorted Matrix
 * Difficulty: Medium
 * Tags: array, sort, search, queue, heap
 *
 * Approach: Use two pointers or sliding window technique
 * Time Complexity: O(n) or O(n log n)
 * Space Complexity: O(1) to O(n) depending on approach
 */

class Solution {
public:
    int kthSmallest(vector<vector<int>>& matrix, int k) {

    }
};
```

Java Solution:

```
/**
 * Problem: Kth Smallest Element in a Sorted Matrix
```



```

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* Time Complexity: O(n) or O(n log n)
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*/

class Solution {
public int kthSmallest(int[][] matrix, int k) {

}
}

```

Python3 Solution:

```

"""
Problem: Kth Smallest Element in a Sorted Matrix
Difficulty: Medium
Tags: array, sort, search, queue, heap

Approach: Use two pointers or sliding window technique
Time Complexity: O(n) or O(n log n)
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"""

class Solution:
def kthSmallest(self, matrix: List[List[int]], k: int) -> int:
# TODO: Implement optimized solution
pass

```

Python Solution:

```

class Solution(object):
def kthSmallest(self, matrix, k):
"""
:type matrix: List[List[int]]
:type k: int
:rtype: int
"""

```

JavaScript Solution:

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/**
 * @param {number[][]} matrix
 * @param {number} k
 * @return {number}
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var kthSmallest = function(matrix, k) {

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```

TypeScript Solution:

```
/**
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 */

function kthSmallest(matrix: number[][], k: number): number {

};
```

C# Solution:

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*
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public class Solution {
    public int KthSmallest(int[][] matrix, int k) {

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}

```

C Solution:

```

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int kthSmallest(int** matrix, int matrixSize, int* matrixColSize, int k) {

}

```

Go Solution:

```

// Problem: Kth Smallest Element in a Sorted Matrix
// Difficulty: Medium
// Tags: array, sort, search, queue, heap
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// Approach: Use two pointers or sliding window technique
// Time Complexity:  $O(n)$  or  $O(n \log n)$ 
// Space Complexity:  $O(1)$  to  $O(n)$  depending on approach

func kthSmallest(matrix [][]int, k int) int {

}

```

Kotlin Solution:

```
class Solution {  
    fun kthSmallest(matrix: Array<IntArray>, k: Int): Int {  
  
    }  
}
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Swift Solution:

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class Solution {  
    func kthSmallest(_ matrix: [[Int]], _ k: Int) -> Int {  
  
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// Time Complexity: O(n) or O(n log n)  
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impl Solution {  
    pub fn kth_smallest(matrix: Vec<Vec<i32>>, k: i32) -> i32 {  
  
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}
```

Ruby Solution:

```
# @param {Integer[][]} matrix  
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# @return {Integer}  
def kth_smallest(matrix, k)  
  
end
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PHP Solution:

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class Solution {

    /**
     * @param Integer[][] $matrix
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object Solution {
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