

Problem 2172: Maximum AND Sum of Array

Problem Information

Difficulty: Hard

Acceptance Rate: 50.41%

Paid Only: No

Tags: Array, Dynamic Programming, Bit Manipulation, Bitmask

Problem Description

You are given an integer array `nums` of length `n` and an integer `numSlots` such that `2 * numSlots >= n`. There are `numSlots` slots numbered from `1` to `numSlots`.

You have to place all `n` integers into the slots such that each slot contains at **most** two numbers. The **AND sum** of a given placement is the sum of the **bitwise** `AND` of every number with its respective slot number.

* For example, the **AND sum** of placing the numbers `[1, 3]` into slot `1` and `[4, 6]` into slot `2` is equal to `(1 AND 1) + (3 AND 1) + (4 AND 2) + (6 AND 2) = 1 + 1 + 0 + 2 = 4`.

Return _the maximum possible**AND sum** of `nums`_ given `numSlots`_ slots._

Example 1:

Input: nums = [1,2,3,4,5,6], numSlots = 3 **Output:** 9 **Explanation:** One possible placement is [1, 4] into slot `1`, [2, 6] into slot `2`, and [3, 5] into slot `3`. This gives the maximum AND sum of $(1 \text{ AND } 1) + (4 \text{ AND } 1) + (2 \text{ AND } 2) + (6 \text{ AND } 2) + (3 \text{ AND } 3) + (5 \text{ AND } 3) = 1 + 0 + 2 + 2 + 3 + 1 = 9$.

Example 2:

Input: nums = [1,3,10,4,7,1], numSlots = 9 **Output:** 24 **Explanation:** One possible placement is [1, 1] into slot `1`, [3] into slot `3`, [4] into slot `4`, [7] into slot `7`, and [10] into slot `9`. This gives the maximum AND sum of $(1 \text{ AND } 1) + (1 \text{ AND } 1) + (3 \text{ AND } 3) + (4 \text{ AND } 4) + (7 \text{ AND } 7) + (10 \text{ AND } 9) = 1 + 1 + 3 + 4 + 7 + 8 = 24$. Note that slots 2,

5, 6, and 8 are empty which is permitted.

****Constraints:****

`* `n == nums.length` * `1 <= numSlots <= 9` * `1 <= n <= 2 * numSlots` * `1 <= nums[i] <= 15``

Code Snippets

C++:

```
class Solution {
public:
    int maximumANDSum(vector<int>& nums, int numSlots) {
        ...
    }
};
```

Java:

```
class Solution {
    public int maximumANDSum(int[] nums, int numSlots) {
        ...
    }
}
```

Python3:

```
class Solution:
    def maximumANDSum(self, nums: List[int], numSlots: int) -> int:
```