

# Problem 2312: Selling Pieces of Wood

## Problem Information

Difficulty: **Hard**

Acceptance Rate: 52.31%

Paid Only: No

Tags: Array, Dynamic Programming, Memoization

## Problem Description

You are given two integers  $m$  and  $n$  that represent the height and width of a rectangular piece of wood. You are also given a 2D integer array `prices`, where `prices[i] = [hi, wi, pricei]` indicates you can sell a rectangular piece of wood of height  $hi$  and width  $wi$  for  $pricei$  dollars.

To cut a piece of wood, you must make a vertical or horizontal cut across the **entire** height or width of the piece to split it into two smaller pieces. After cutting a piece of wood into some number of smaller pieces, you can sell pieces according to `prices`. You may sell multiple pieces of the same shape, and you do not have to sell all the shapes. The grain of the wood makes a difference, so you **cannot** rotate a piece to swap its height and width.

Return **the maximum** money you can earn after cutting an  $m \times n$  piece of wood.

Note that you can cut the piece of wood as many times as you want.

**Example 1.**



**Input:**  $m = 3, n = 5, \text{prices} = [[1,4,2],[2,2,7],[2,1,3]]$  **Output:** 19 **Explanation:** The diagram above shows a possible scenario. It consists of: - 2 pieces of wood shaped  $2 \times 2$ , selling for a price of  $2 * 7 = 14$ . - 1 piece of wood shaped  $2 \times 1$ , selling for a price of  $1 * 3 = 3$ . - 1 piece of wood shaped  $1 \times 4$ , selling for a price of  $1 * 2 = 2$ . This obtains a total of  $14 + 3 + 2 = 19$  money earned. It can be shown that 19 is the maximum amount of money that can be earned.

**Example 2:**



**Input:**  $m = 4$ ,  $n = 6$ ,  $prices = [[3,2,10],[1,4,2],[4,1,3]]$  **Output:** 32 **Explanation:** The diagram above shows a possible scenario. It consists of: - 3 pieces of wood shaped  $3 \times 2$ , selling for a price of  $3 \times 10 = 30$ . - 1 piece of wood shaped  $1 \times 4$ , selling for a price of  $1 \times 2 = 2$ . This obtains a total of  $30 + 2 = 32$  money earned. It can be shown that 32 is the maximum amount of money that can be earned. Notice that we cannot rotate the  $1 \times 4$  piece of wood to obtain a  $4 \times 1$  piece of wood.

**Constraints:**

$1 \leq m, n \leq 200$   $1 \leq prices.length \leq 2 \times 10^4$   $prices[i].length == 3$   $1 \leq hi \leq m$   $1 \leq wi \leq n$   $1 \leq price_i \leq 10^6$  All the shapes of wood  $(hi, wi)$  are pairwise **distinct**.

## Code Snippets

**C++:**

```
class Solution {
public:
    long long sellingWood(int m, int n, vector<vector<int>>& prices) {

    }
};
```

**Java:**

```
class Solution {
    public long sellingWood(int m, int n, int[][] prices) {

    }
}
```

**Python3:**

```
class Solution:
    def sellingWood(self, m: int, n: int, prices: List[List[int]]) -> int:
```