

Problem 3515: Shortest Path in a Weighted Tree

Problem Information

Difficulty: Hard

Acceptance Rate: 41.29%

Paid Only: No

Tags: Array, Tree, Depth-First Search, Binary Indexed Tree, Segment Tree

Problem Description

You are given an integer n and an undirected, weighted tree rooted at node 1 with n nodes numbered from 1 to n . This is represented by a 2D array `edges` of length $n - 1$, where `edges[i] = [ui, vi, wi]` indicates an undirected edge from node `ui` to `vi` with weight `wi`.

You are also given a 2D integer array `queries` of length q , where each `queries[i]` is either:

* `[1, u, v, w]` - **Update** the weight of the edge between nodes `u` and `v` to `w`, where `(u, v)` is guaranteed to be an edge present in `edges`. * `[2, x]` - **Compute** the **shortest** path distance from the root node 1 to node `x`.

Return an integer array `answer`, where `answer[i]` is the **shortest** path distance from node 1 to `x` for the i th query of `[2, x]`.

Example 1:

Input: $n = 2$, `edges = [[1,2,7]]`, `queries = [[2,2],[1,1,2,4],[2,2]]`

Output: `[7,4]`

Explanation:

* Query `[2,2]`: The shortest path from root node 1 to node 2 is 7. * Query `[1,1,2,4]`: The weight of edge `(1,2)` changes from 7 to 4. * Query `[2,2]`: The shortest path from root node 1 to node 2 is 4.

Example 2.

Input: $n = 3$, $edges = [[1,2,2],[1,3,4]]$, $queries = [[2,1],[2,3],[1,1,3,7],[2,2],[2,3]]$

Output: $[0,4,2,7]$

Explanation:



* Query $[2,1]$: The shortest path from root node 1 to node 1 is 0. * Query $[2,3]$: The shortest path from root node 1 to node 3 is 4. * Query $[1,1,3,7]$: The weight of edge $(1,3)$ changes from 4 to 7. * Query $[2,2]$: The shortest path from root node 1 to node 2 is 2. * Query $[2,3]$: The shortest path from root node 1 to node 3 is 7.

Example 3.

Input: $n = 4$, $edges = [[1,2,2],[2,3,1],[3,4,5]]$, $queries = [[2,4],[2,3],[1,2,3,3],[2,2],[2,3]]$

Output: $[8,3,2,5]$

Explanation:



* Query $[2,4]$: The shortest path from root node 1 to node 4 consists of edges $(1,2)$, $(2,3)$, and $(3,4)$ with weights $2 + 1 + 5 = 8$. * Query $[2,3]$: The shortest path from root node 1 to node 3 consists of edges $(1,2)$ and $(2,3)$ with weights $2 + 1 = 3$. * Query $[1,2,3,3]$: The weight of edge $(2,3)$ changes from 1 to 3. * Query $[2,2]$: The shortest path from root node 1 to node 2 is 2. * Query $[2,3]$: The shortest path from root node 1 to node 3 consists of edges $(1,2)$ and $(2,3)$ with updated weights $2 + 3 = 5$.

Constraints:

* $1 \leq n \leq 105$ * $edges.length == n - 1$ * $edges[i] == [ui, vi, wi]$ * $1 \leq ui, vi \leq n$ * $1 \leq wi \leq 104$ * The input is generated such that $edges$ represents a valid tree. * $1 \leq queries.length == q \leq 105$ * $queries[i].length == 2$ or 4 * $queries[i] == [1, u, v, w]$ or, * $queries[i] == [2, x]$ * $1 \leq u, v, x \leq n$ * (u, v) is always an edge from $edges$. * $1 \leq w \leq 104$

Code Snippets

C++:

```
class Solution {
public:
    vector<int> treeQueries(int n, vector<vector<int>>& edges,
        vector<vector<int>>& queries) {

    }
};
```

Java:

```
class Solution {
    public int[] treeQueries(int n, int[][] edges, int[][] queries) {

    }
}
```

Python3:

```
class Solution:
    def treeQueries(self, n: int, edges: List[List[int]], queries:
        List[List[int]]) -> List[int]:
```