

# Problem 1237: Find Positive Integer Solution for a Given Equation

## Problem Information

Difficulty: **Medium**

Acceptance Rate: 69.70%

Paid Only: No

Tags: Math, Two Pointers, Binary Search, Interactive

## Problem Description

Given a callable function `f(x, y)` with a hidden formula and a value `z`, reverse engineer the formula and return all positive integer pairs `x` and `y` where `f(x,y) == z`. You may return the pairs in any order.

While the exact formula is hidden, the function is monotonically increasing, i.e.:

$f(x, y) < f(x + 1, y)$  and  $f(x, y) < f(x, y + 1)$

The function interface is defined like this:

```
interface CustomFunction { public: // Returns some positive integer f(x, y) for two positive integers x and y based on a formula. int f(int x, int y); };
```

We will judge your solution as follows:

\* The judge has a list of 9 hidden implementations of `CustomFunction`, along with a way to generate an **answer key** of all valid pairs for a specific `z`. \* The judge will receive two inputs: a `function_id` (to determine which implementation to test your code with), and the target `z`. \* The judge will call your `findSolution` and compare your results with the **answer key**. \* If your results match the **answer key**, your solution will be `Accepted`.

**Example 1:**

**Input:** `function_id = 1, z = 5` **Output:** `[[1,4],[2,3],[3,2],[4,1]]` **Explanation:** The hidden formula for `function_id = 1` is `f(x, y) = x + y`. The following positive integer values of `x` and `y`

make  $f(x, y)$  equal to 5:  $x=1, y=4 \rightarrow f(1, 4) = 1 + 4 = 5$ .  $x=2, y=3 \rightarrow f(2, 3) = 2 + 3 = 5$ .  $x=3, y=2 \rightarrow f(3, 2) = 3 + 2 = 5$ .  $x=4, y=1 \rightarrow f(4, 1) = 4 + 1 = 5$ .

**Example 2:**

**Input:** function\_id = 2, z = 5 **Output:** [[1,5],[5,1]] **Explanation:** The hidden formula for function\_id = 2 is  $f(x, y) = x * y$ . The following positive integer values of x and y make  $f(x, y)$  equal to 5:  $x=1, y=5 \rightarrow f(1, 5) = 1 * 5 = 5$ .  $x=5, y=1 \rightarrow f(5, 1) = 5 * 1 = 5$ .

**Constraints:**

$1 \leq \text{function\_id} \leq 9$   $1 \leq z \leq 100$  \* It is guaranteed that the solutions of  $f(x, y) == z$  will be in the range  $1 \leq x, y \leq 1000$ . \* It is also guaranteed that  $f(x, y)$  will fit in 32 bit signed integer if  $1 \leq x, y \leq 1000$ .

## Code Snippets

**C++:**

```
/*
 * // This is the custom function interface.
 * // You should not implement it, or speculate about its implementation
 * class CustomFunction {
 * public:
 * // Returns f(x, y) for any given positive integers x and y.
 * // Note that f(x, y) is increasing with respect to both x and y.
 * // i.e. f(x, y) < f(x + 1, y), f(x, y) < f(x, y + 1)
 * int f(int x, int y);
 * };
 */

class Solution {
public:
    vector<vector<int>> findSolution(CustomFunction& customfunction, int z) {

    }
};
```

**Java:**

```

/*
 * // This is the custom function interface.
 * // You should not implement it, or speculate about its implementation
 * class CustomFunction {
 * // Returns f(x, y) for any given positive integers x and y.
 * // Note that f(x, y) is increasing with respect to both x and y.
 * // i.e. f(x, y) < f(x + 1, y), f(x, y) < f(x, y + 1)
 * public int f(int x, int y);
 * };
 */

class Solution {
public List<List<Integer>> findSolution(CustomFunction customfunction, int z)
{

}

}
}

```

### Python3:

```

"""
This is the custom function interface.
You should not implement it, or speculate about its implementation
class CustomFunction:
# Returns f(x, y) for any given positive integers x and y.
# Note that f(x, y) is increasing with respect to both x and y.
# i.e. f(x, y) < f(x + 1, y), f(x, y) < f(x, y + 1)
def f(self, x, y):

"""

class Solution:
def findSolution(self, customfunction: 'CustomFunction', z: int) ->
List[List[int]]:

```