

Problem 2748: Number of Beautiful Pairs

Problem Information

Difficulty: Easy

Acceptance Rate: 51.60%

Paid Only: No

Tags: Array, Hash Table, Math, Counting, Number Theory

Problem Description

You are given a **0-indexed** integer array `nums`. A pair of indices i, j where $0 \leq i < j < \text{nums.length}$ is called beautiful if the **first digit** of `nums[i]` and the **last digit** of `nums[j]` are **coprime**.

Return the total number of beautiful pairs in `nums`.

Two integers x and y are **coprime** if there is no integer greater than 1 that divides both of them. In other words, x and y are coprime if $\text{gcd}(x, y) == 1$, where $\text{gcd}(x, y)$ is the **greatest common divisor** of x and y .

Example 1:

Input: nums = [2,5,1,4] **Output:** 5 **Explanation:** There are 5 beautiful pairs in nums: When $i = 0$ and $j = 1$: the first digit of nums[0] is 2, and the last digit of nums[1] is 5. We can confirm that 2 and 5 are coprime, since $\text{gcd}(2,5) == 1$. When $i = 0$ and $j = 2$: the first digit of nums[0] is 2, and the last digit of nums[2] is 1. Indeed, $\text{gcd}(2,1) == 1$. When $i = 1$ and $j = 2$: the first digit of nums[1] is 5, and the last digit of nums[2] is 1. Indeed, $\text{gcd}(5,1) == 1$. When $i = 1$ and $j = 3$: the first digit of nums[1] is 5, and the last digit of nums[3] is 4. Indeed, $\text{gcd}(5,4) == 1$. When $i = 2$ and $j = 3$: the first digit of nums[2] is 1, and the last digit of nums[3] is 4. Indeed, $\text{gcd}(1,4) == 1$. Thus, we return 5.

Example 2:

Input: nums = [11,21,12] **Output:** 2 **Explanation:** There are 2 beautiful pairs: When $i = 0$ and $j = 1$: the first digit of nums[0] is 1, and the last digit of nums[1] is 1. Indeed, $\text{gcd}(1,1) == 1$. When $i = 0$ and $j = 2$: the first digit of nums[0] is 1, and the last digit of nums[2] is 2.

Indeed, $\text{gcd}(1,2) == 1$. Thus, we return 2.

****Constraints:****

```
* `2 <= nums.length <= 100` * `1 <= nums[i] <= 9999` * `nums[i] % 10 != 0`
```

Code Snippets

C++:

```
class Solution {
public:
    int countBeautifulPairs(vector<int>& nums) {
        }
};
```

Java:

```
class Solution {
    public int countBeautifulPairs(int[] nums) {
        }
}
```

Python3:

```
class Solution:
    def countBeautifulPairs(self, nums: List[int]) -> int:
```