



# Applying Statistical Process Control to the Adaptive Rate Control Problem



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# Introduction and Motivation

- **Goal**
  - integration of meaningful feedback about the requirements and performance of multimedia applications into adaptive multimedia networking.
- **We would like to explore**
  - mechanisms for long-term characterization of network variability (e.g., delay, bandwidth, buffer size).
  - mechanisms for inducing application requirements into adaptive multimedia networking.
- **We would these mechanisms**
  - to be robust and easy to implement.

# Outline of the Talk

- **Statistical Process Control & Multimedia Networking**

- Long-Term vs. Short-Term Variability
- Statistical Quality Control
- Long-Term Stability Monitor



- **Applications of SPC to Adaptive Rate Control**

- Adaptive Media Coding
- Adaptive Media Synchronization

- **Conclusions**

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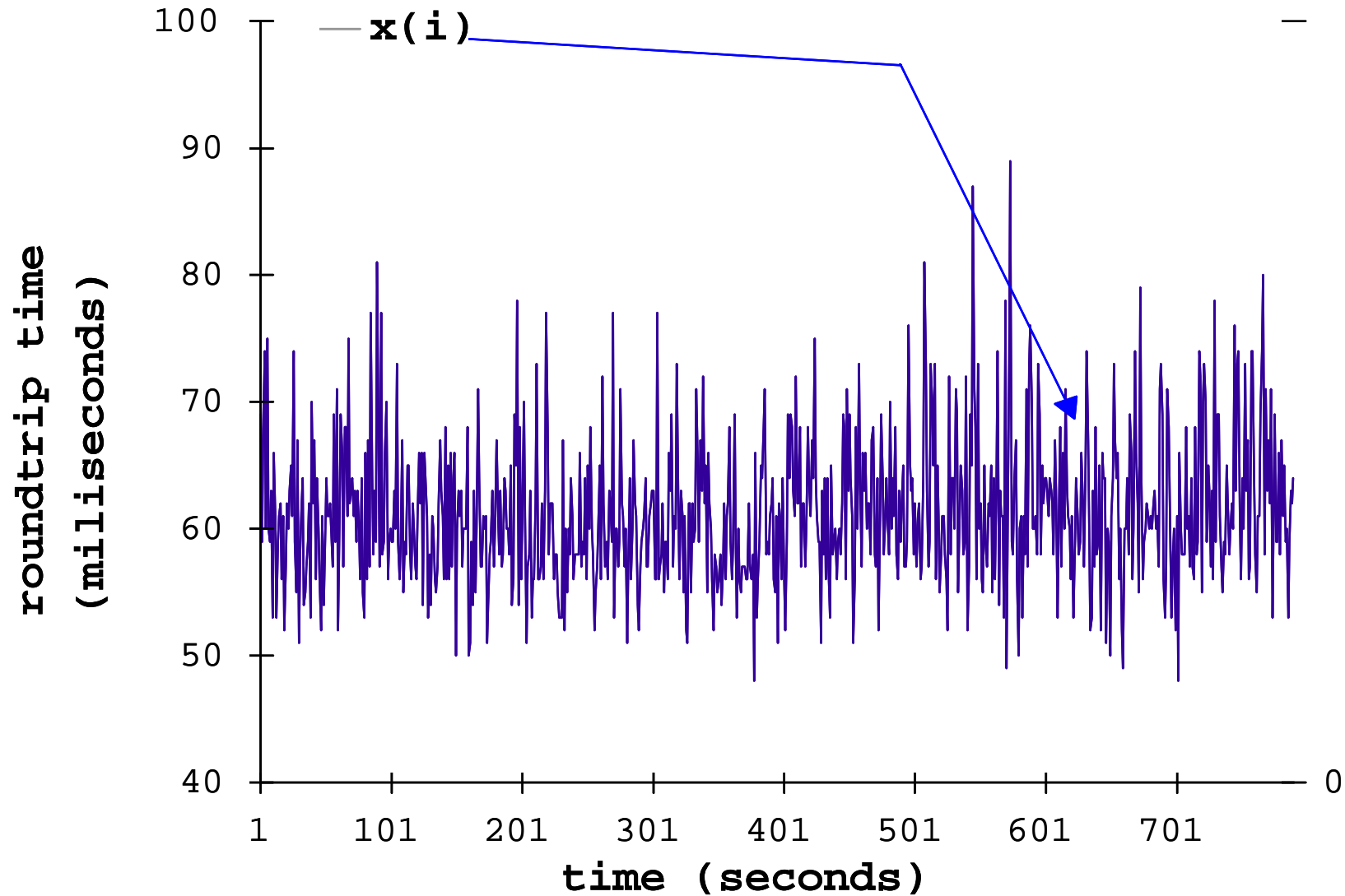
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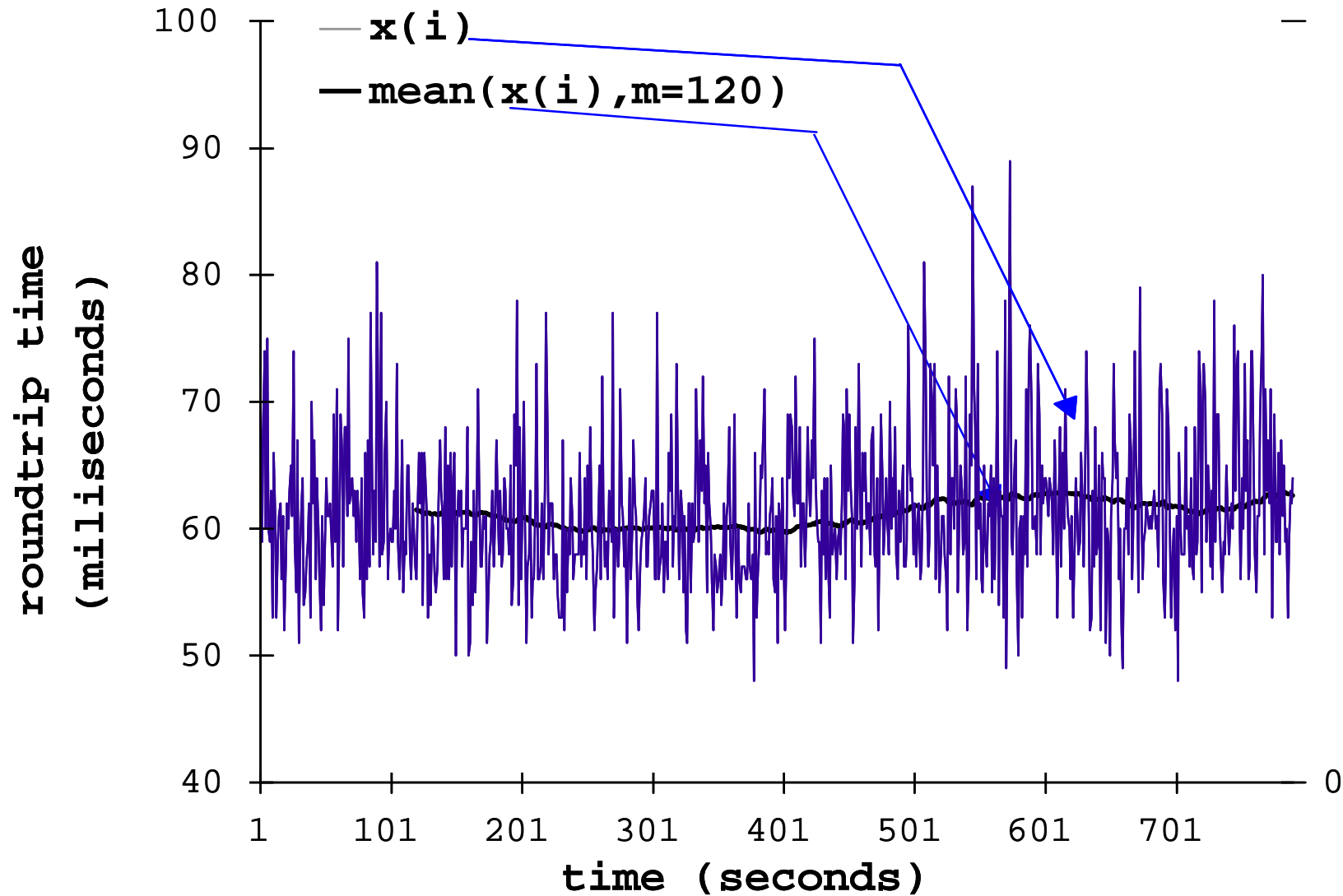


- **Conclusions**

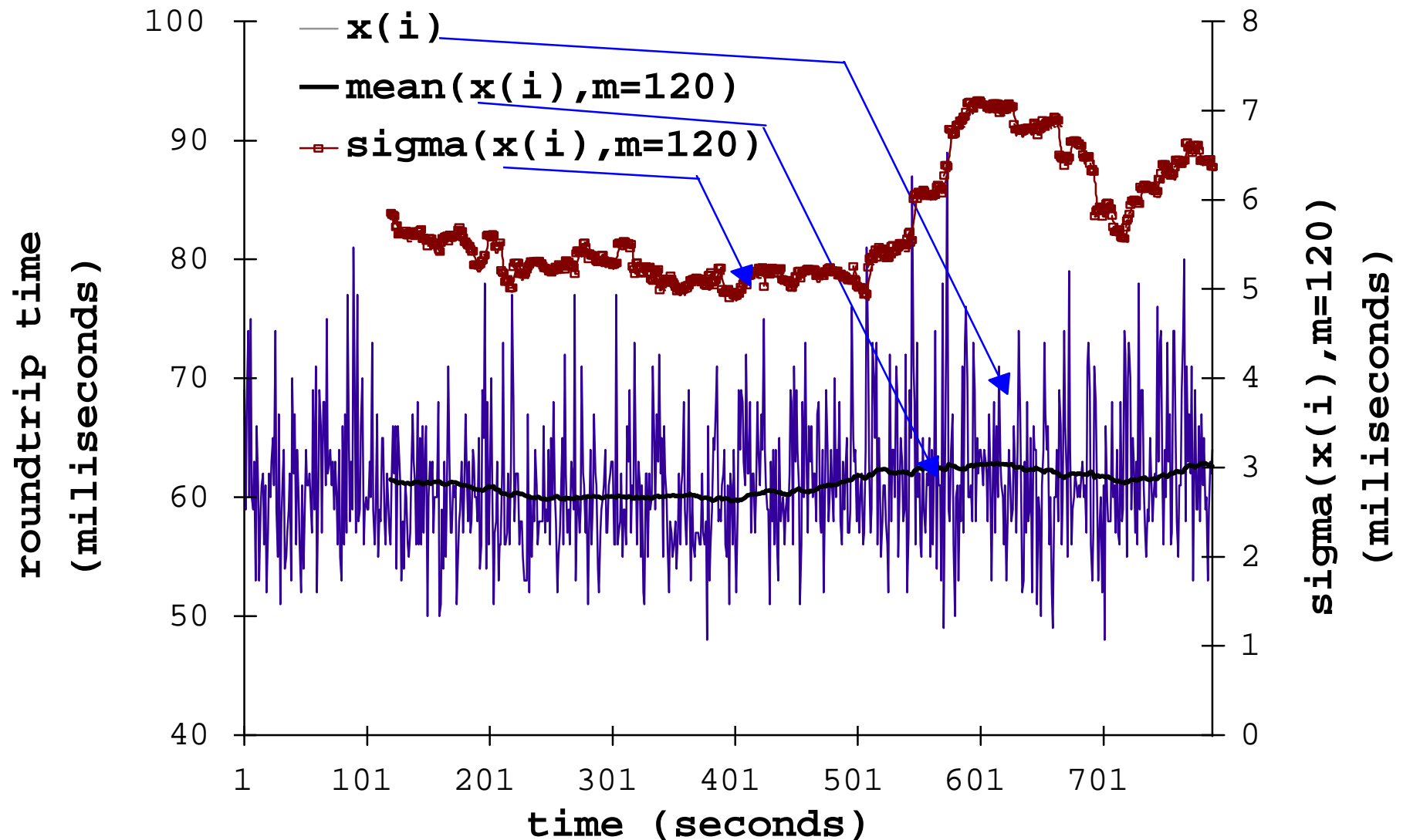
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- # Long-Term vs. Short-Term Variability



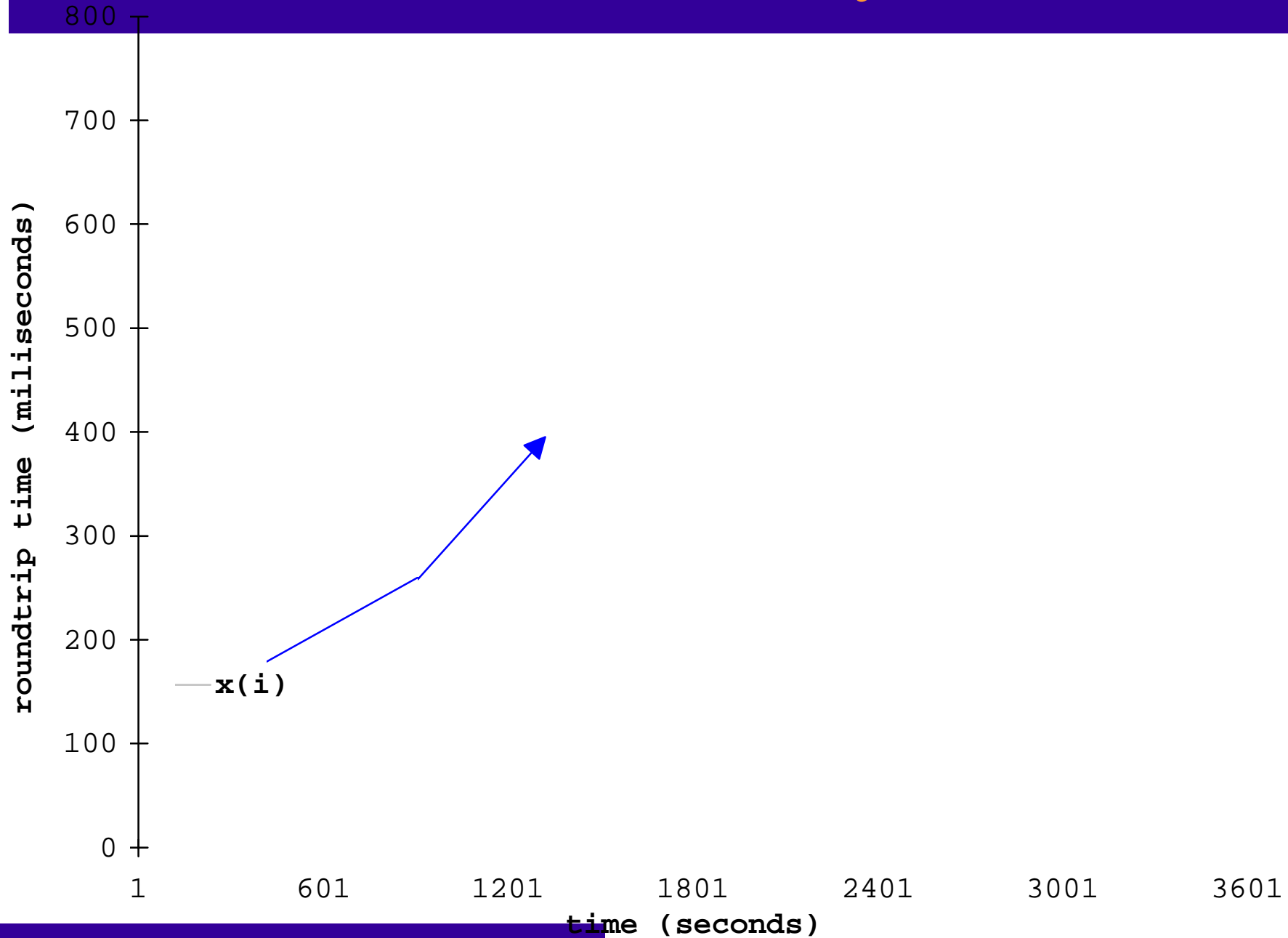
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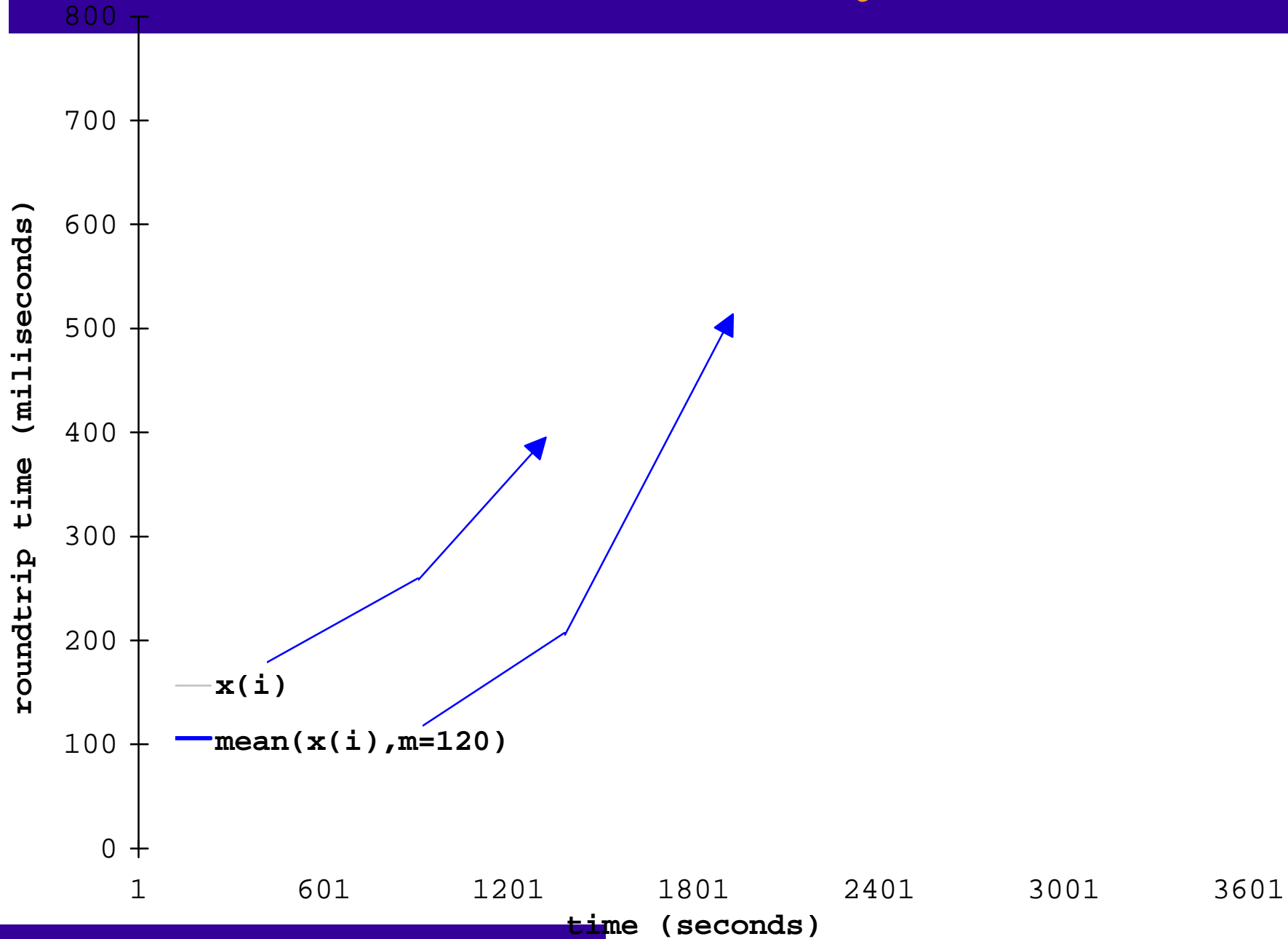


# Statistical Quality Control

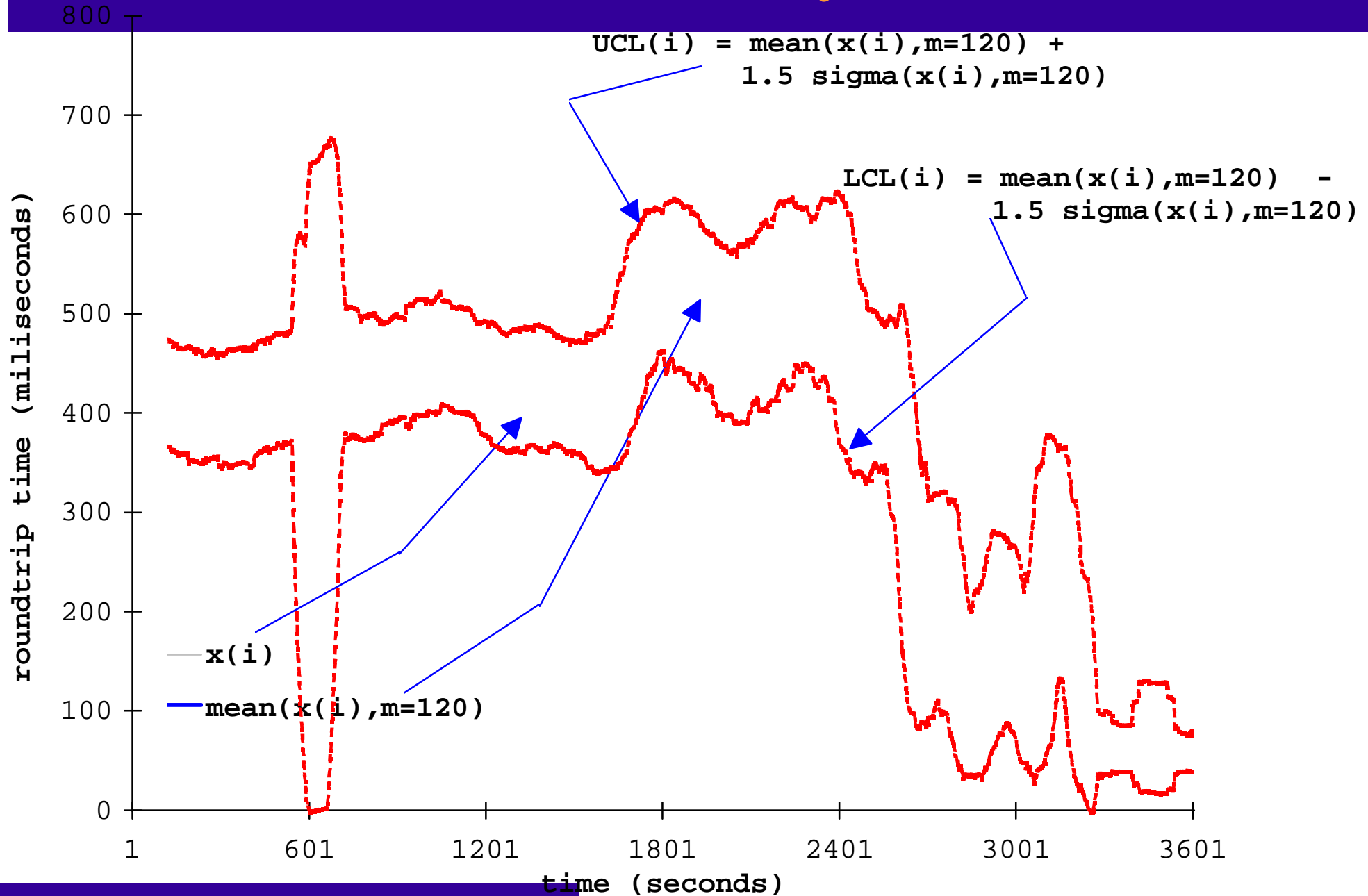




# Statistical Quality Control



# Statistical Quality Control



# • Statistical Process Performance (Specification of a Long-Term Monitor)

- smoothed process indicators (time scale, sampling, weights)

–BMW( $x_i, m$ ) = UWMA smoothing

$$\mu(i, m) = \mu(x_i \dots x_{m-i})$$

$$\sigma(i, m) = \mu(x_i \dots x_{m-i})$$

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- stationarity hypothesis testing

–H0 :  $\mu(i, m') = \mu(i, m)$

–Z0 =  $\mu(i, m') - \mu(i - m/2, m)$

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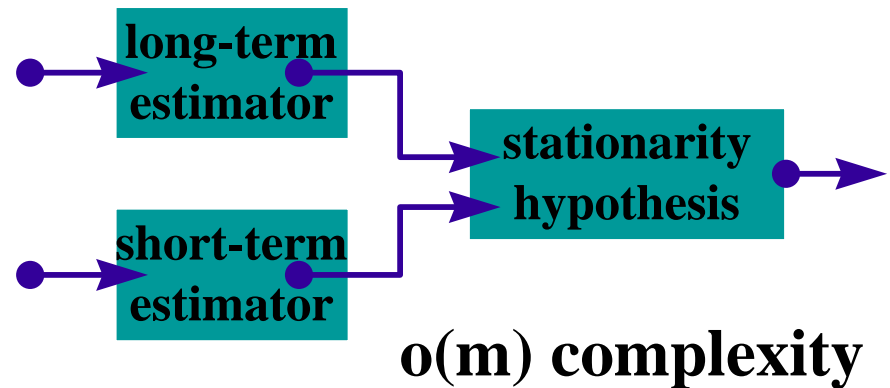
–Z0 =  $\mu(i, m') - \mu(i - m/2, m)$

- confidence interval & forecast estimation

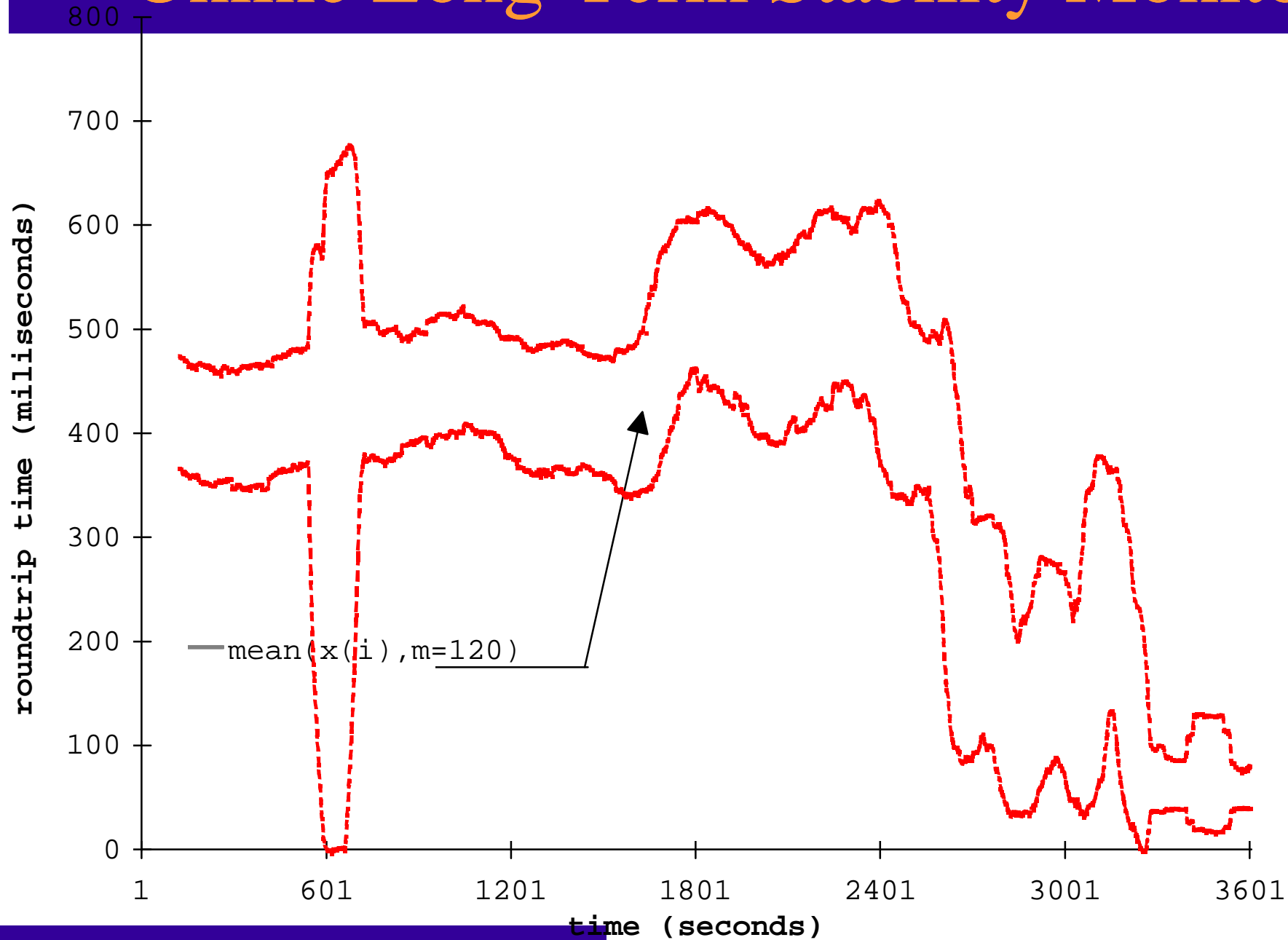
–if  $|Z0| < k * \sigma(i, m)$  then  $\text{mon}_i = \text{mon}_{i-1}$

–else  $\text{mon}_i = \mu(i, m)$

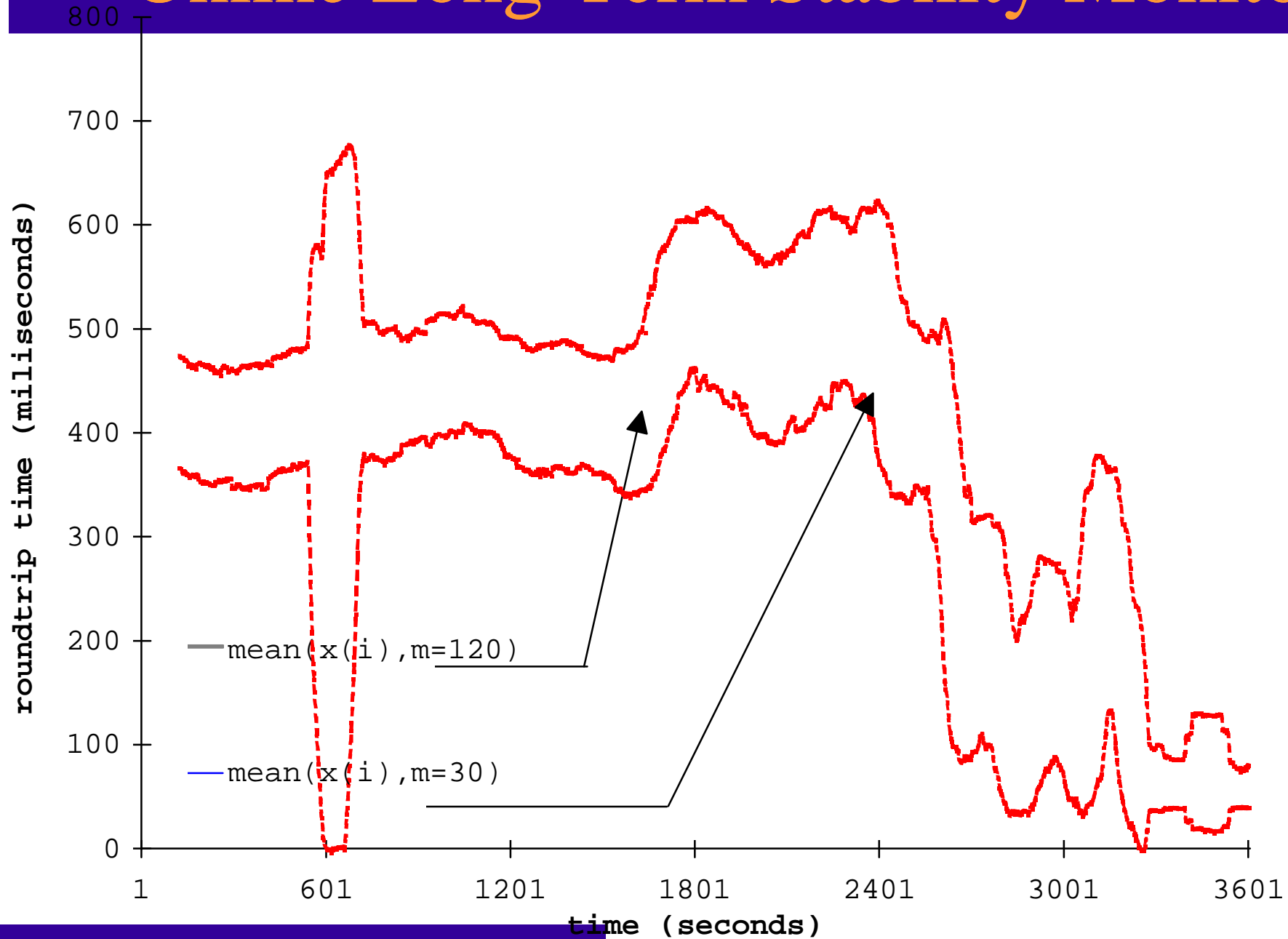
– $\text{mon}_{i+1}^* = \text{mon}_i$



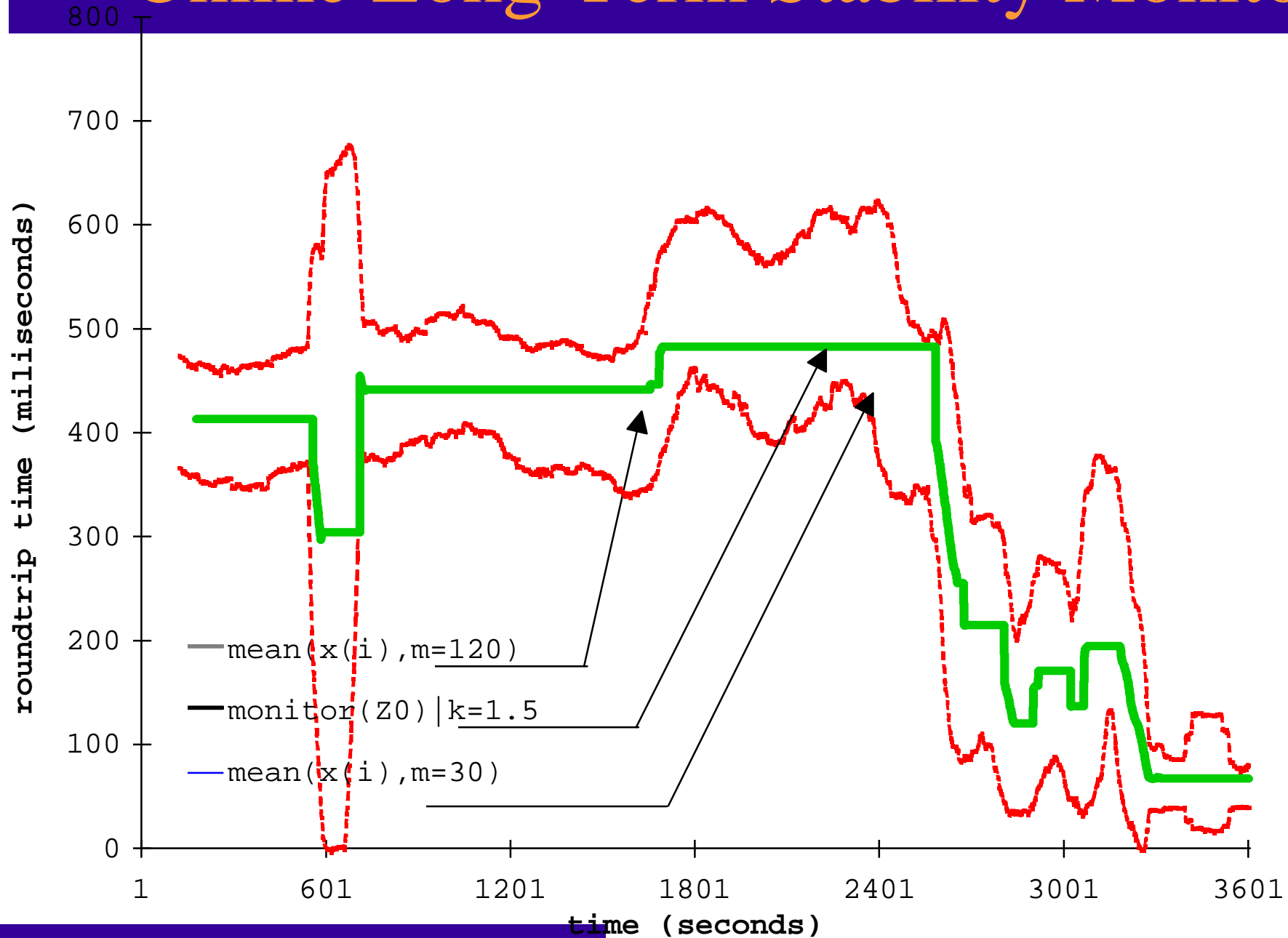
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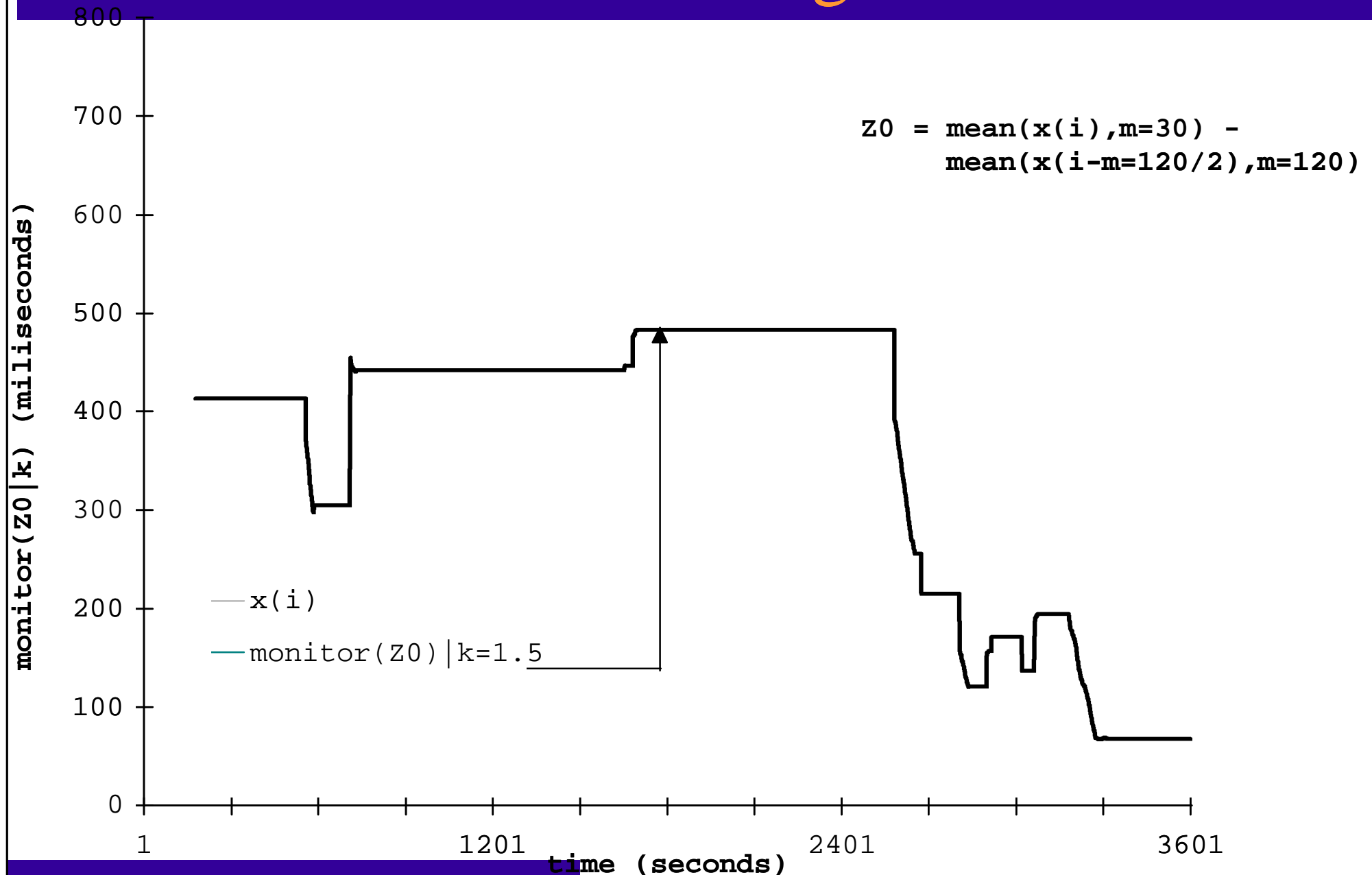


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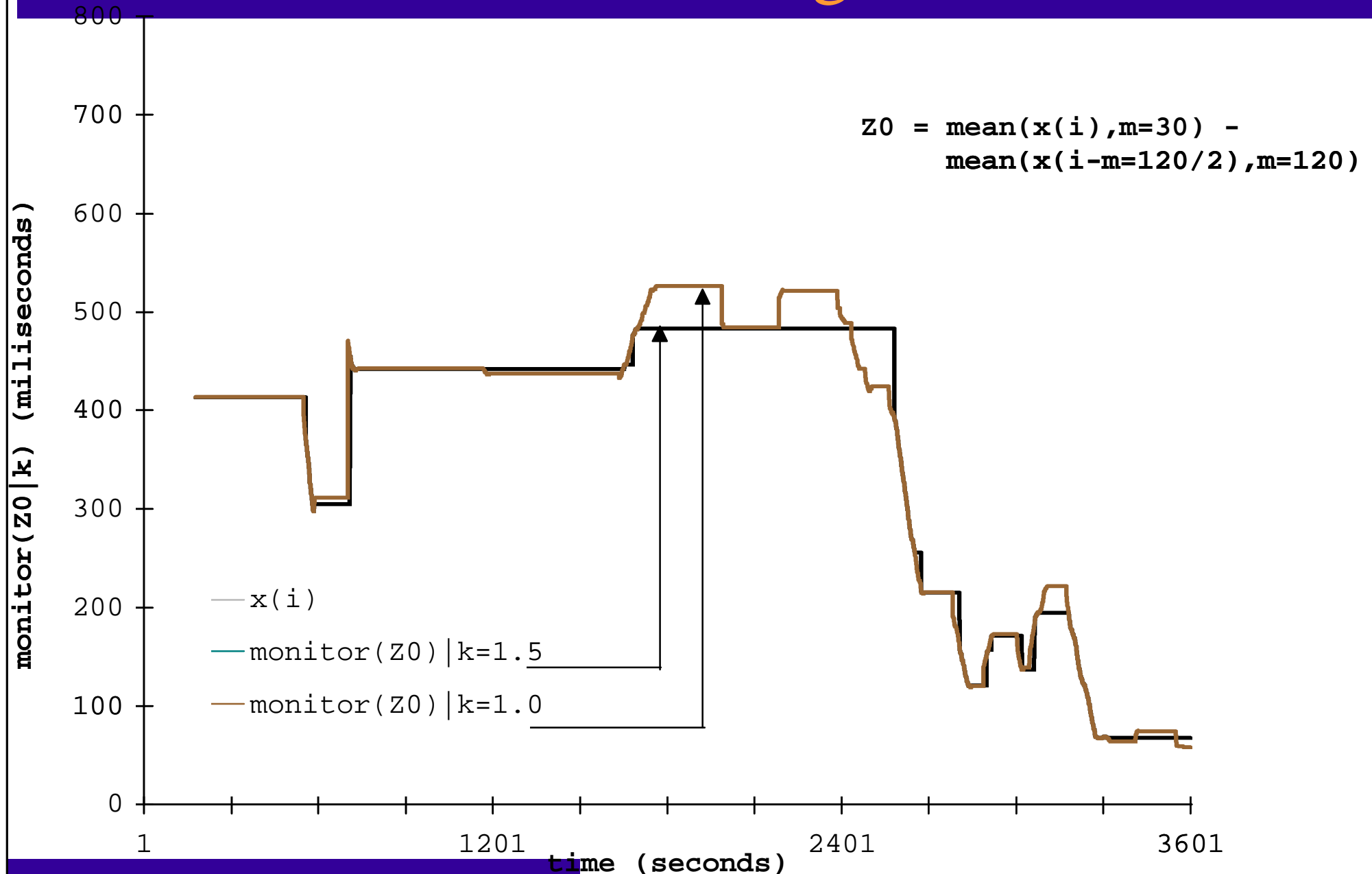




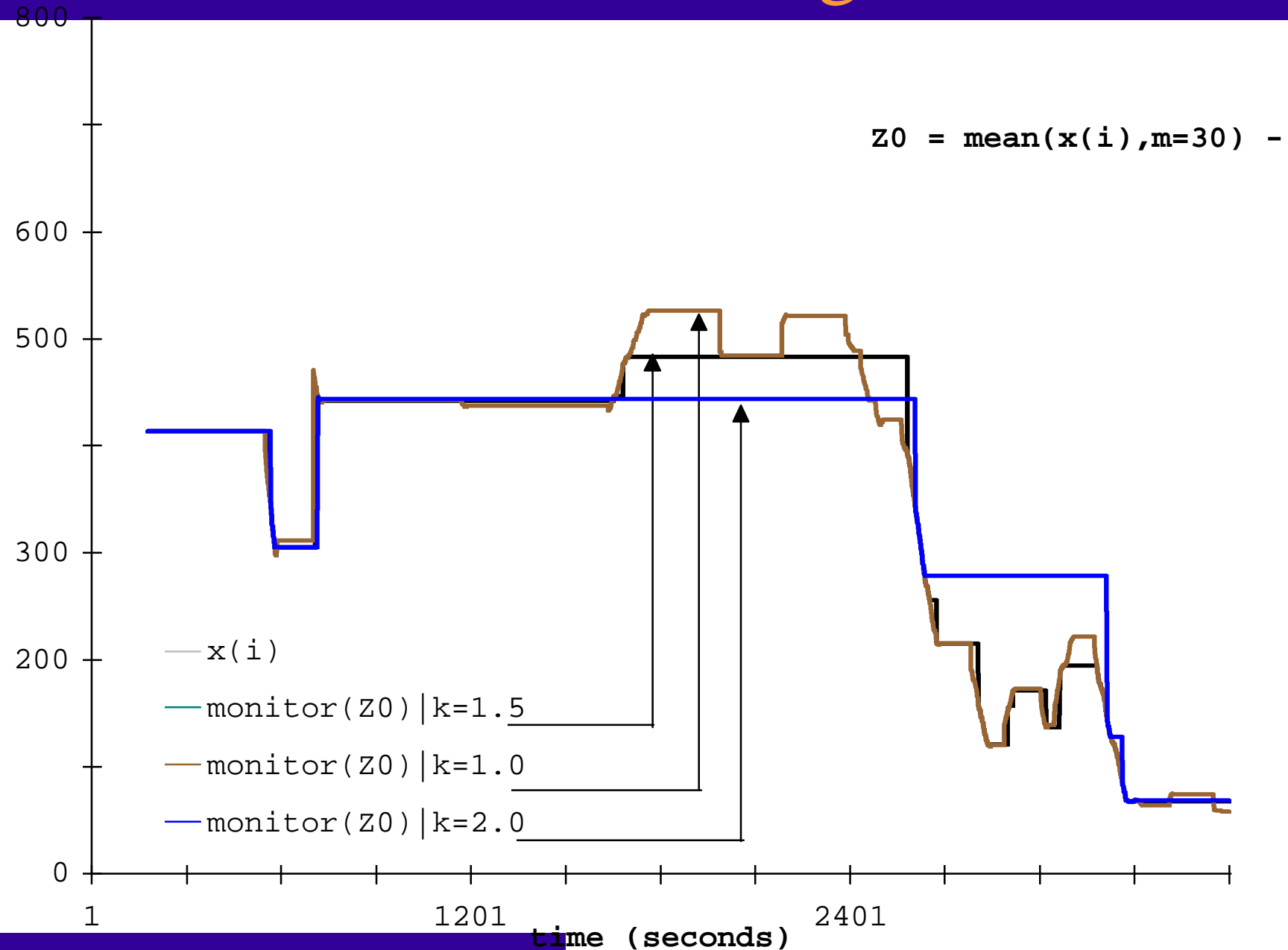
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- **Statistical Process Control & Multimedia Networking**

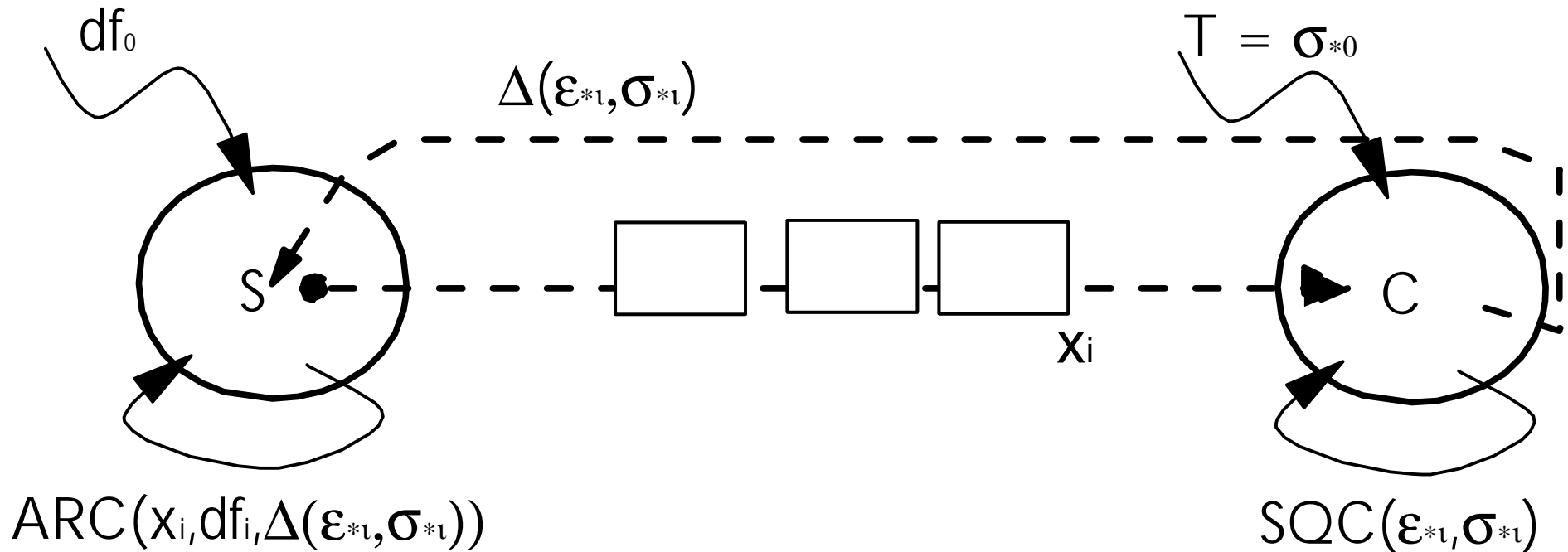
- Long-Term vs. Short-Term Variability
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- Long-Term Stability Monitor

- **Applications of SPC to Adaptive Rate Control**

- Adaptive Media Coding/Streaming
- Adaptive Media Synchronization

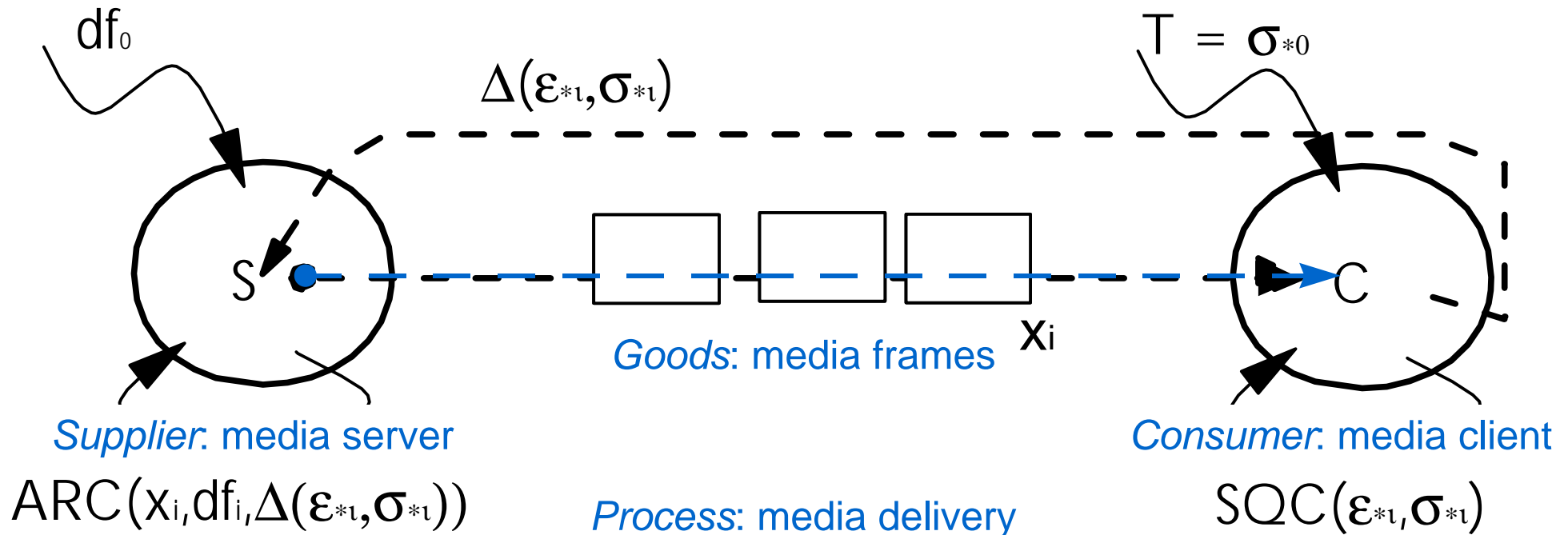
- **Conclusions**

# Long-Term Media Adaptation



- **adaptive rate problem**
  - $ARC(\text{media}, \text{degree of freedom}, \text{feedback})$
- **statistical quality control**
  - $SQC(\text{process indicator}, \text{process variability})$

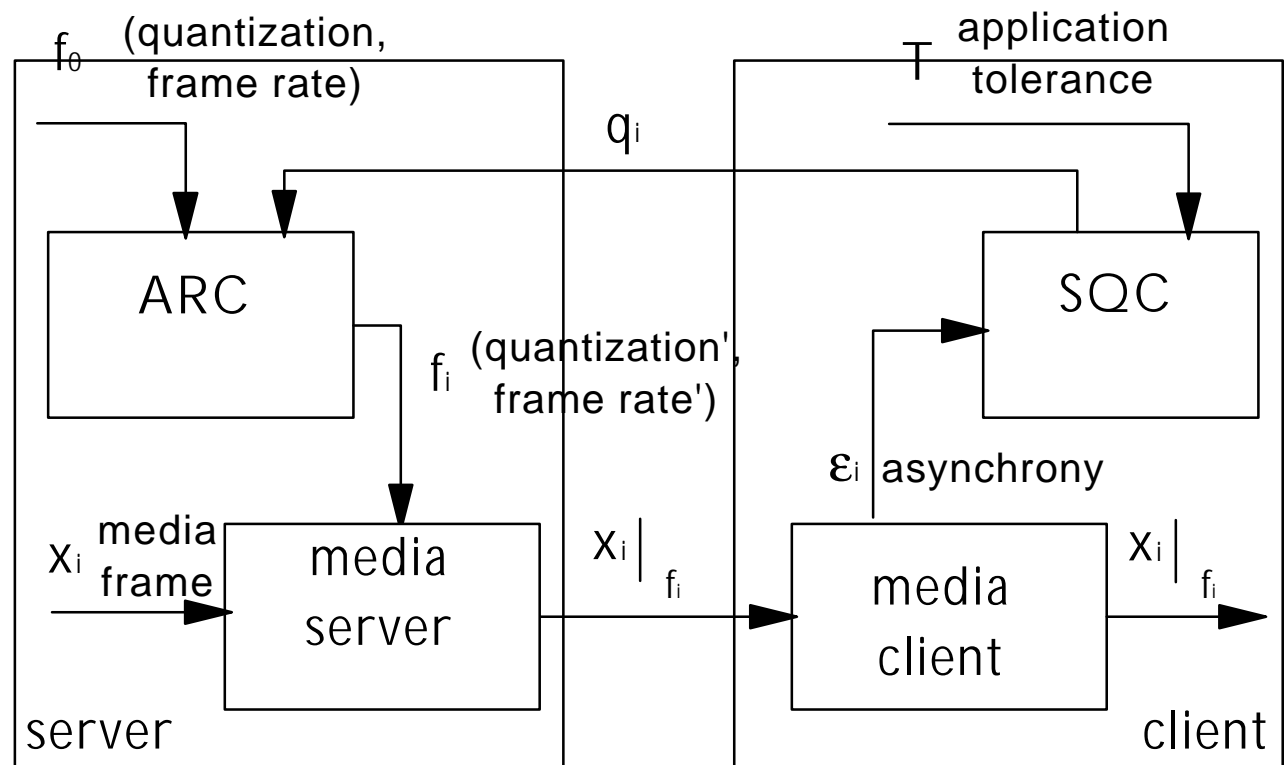
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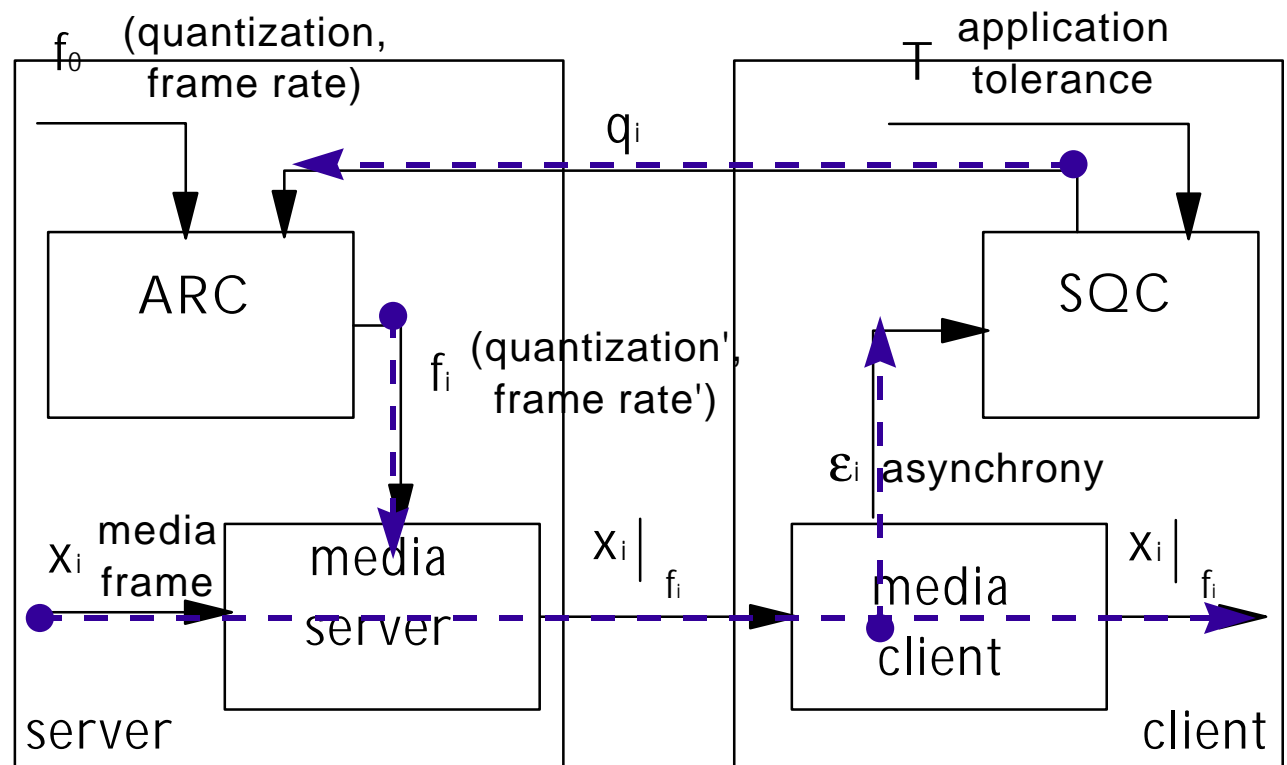
# End-to-End Adaptive Media Coding

- application-oriented
- media-independent feedback
- reactive to long-term (persistent) trends



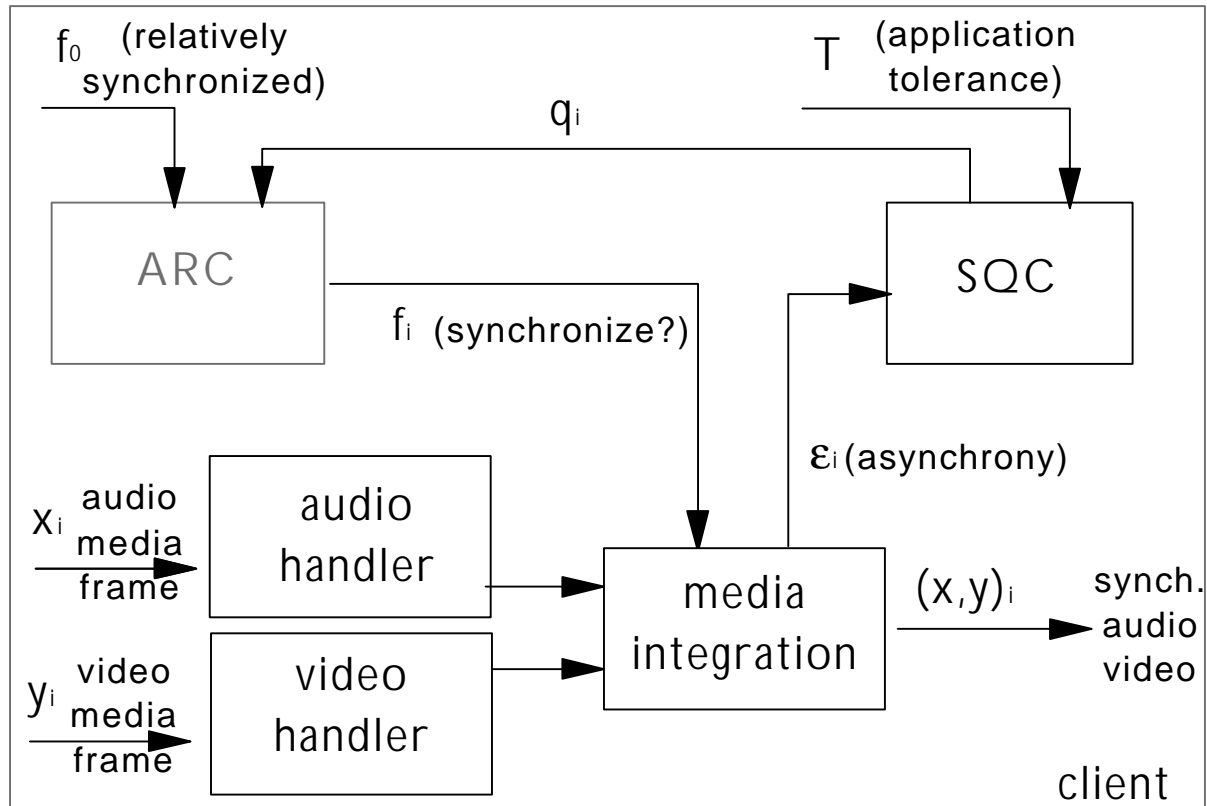
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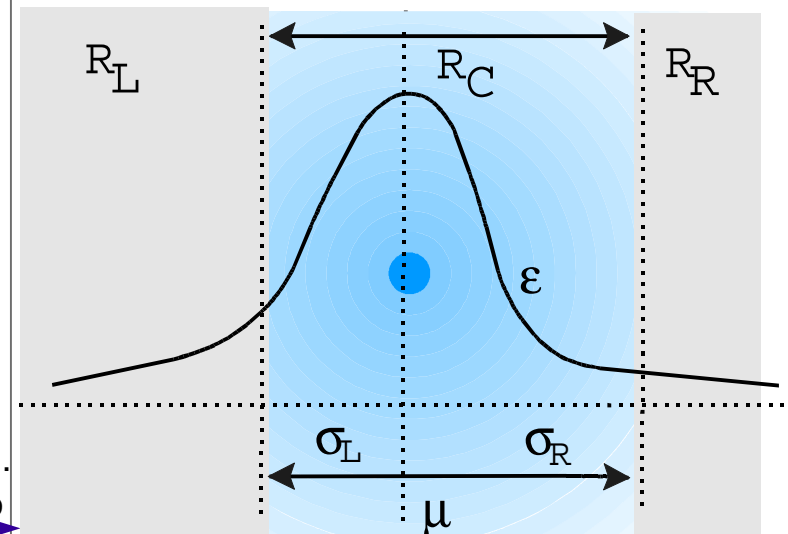
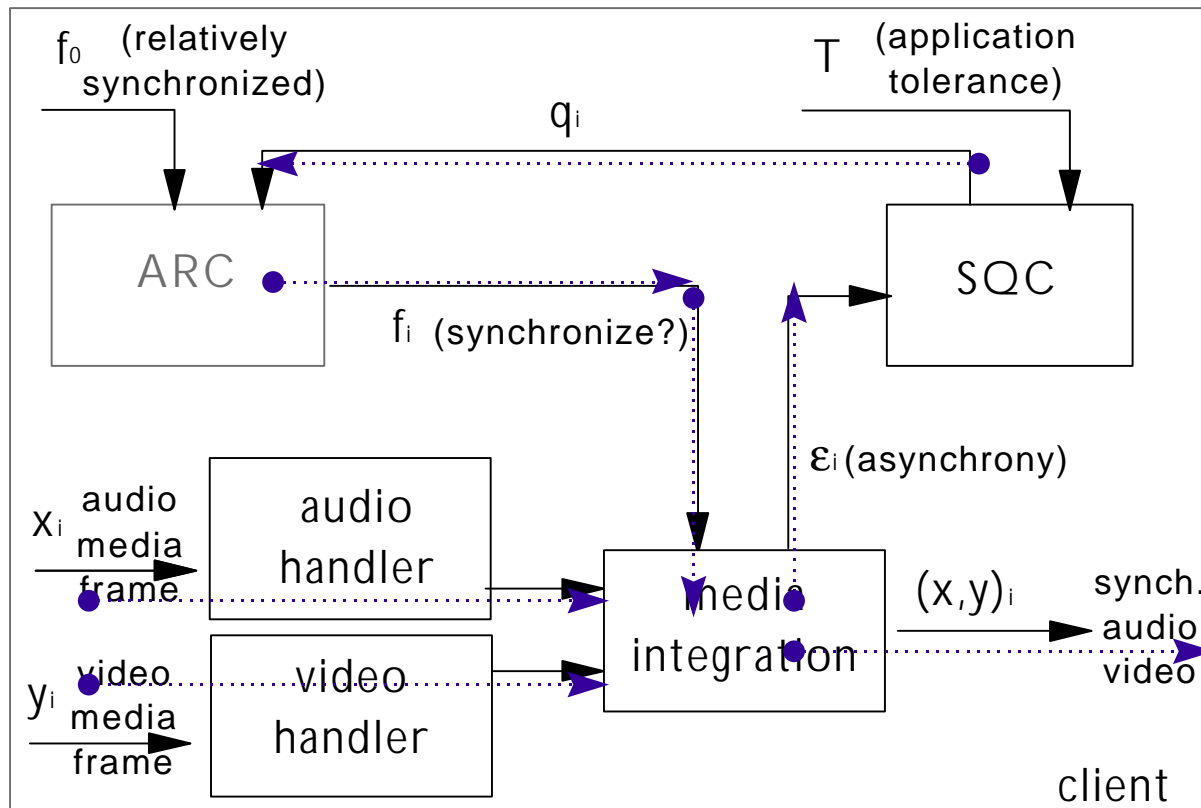




# Adaptive Media Synchronization



# Adaptive Media Synchronization



- **way for specifying long-term performance of its media integration in terms of tradeoffs between:**
  - the playback continuity of audio and
  - the asynchrony tolerance between audio & video.

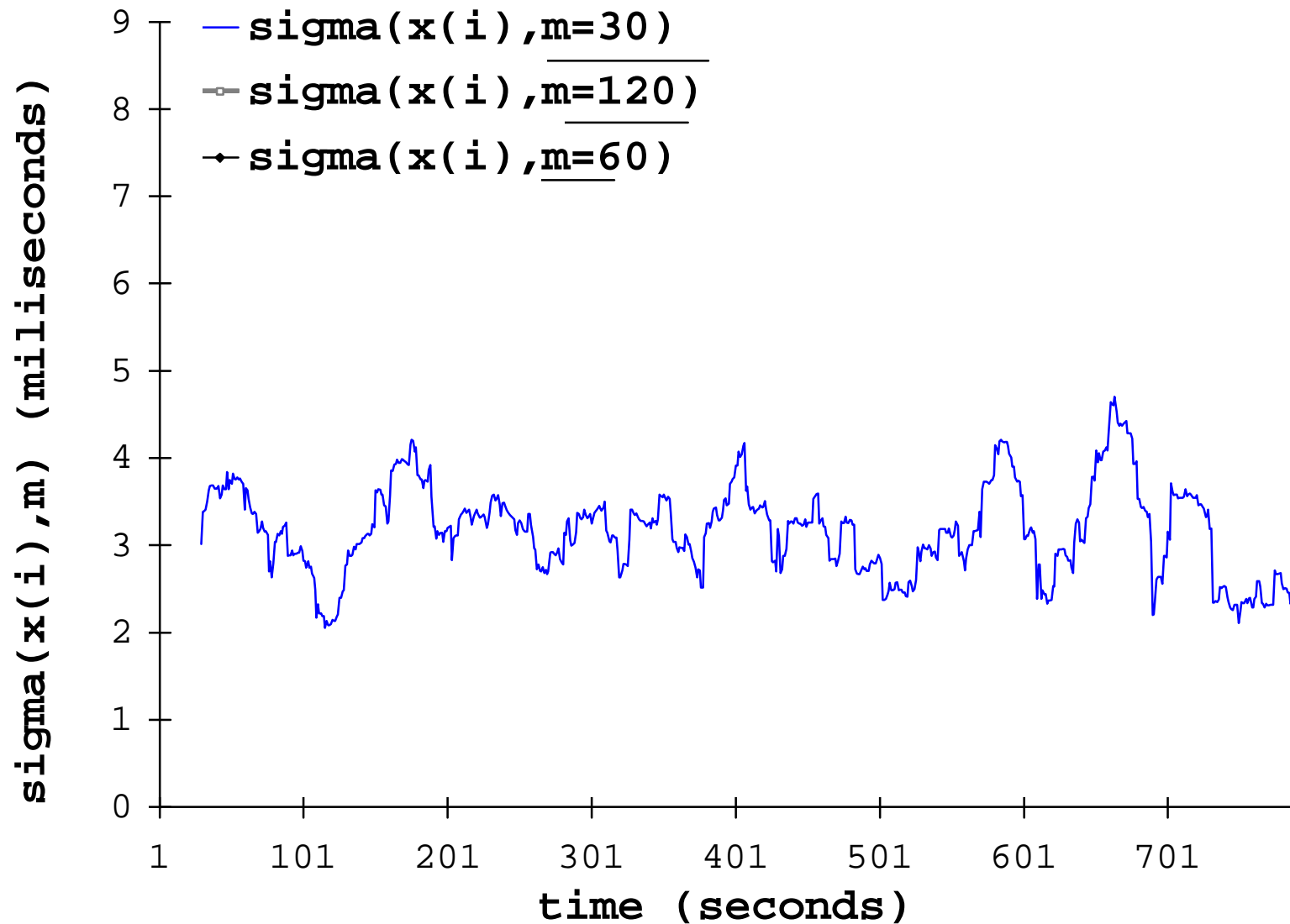
## Concluding Remarks

- Introduced application and relevance of online SPC for multimedia networking
- Proposed a framework for the streaming of heterogeneous media with application-oriented requirements
- Showed the detection and forecast of long-term stationary conditions on network performance indicators

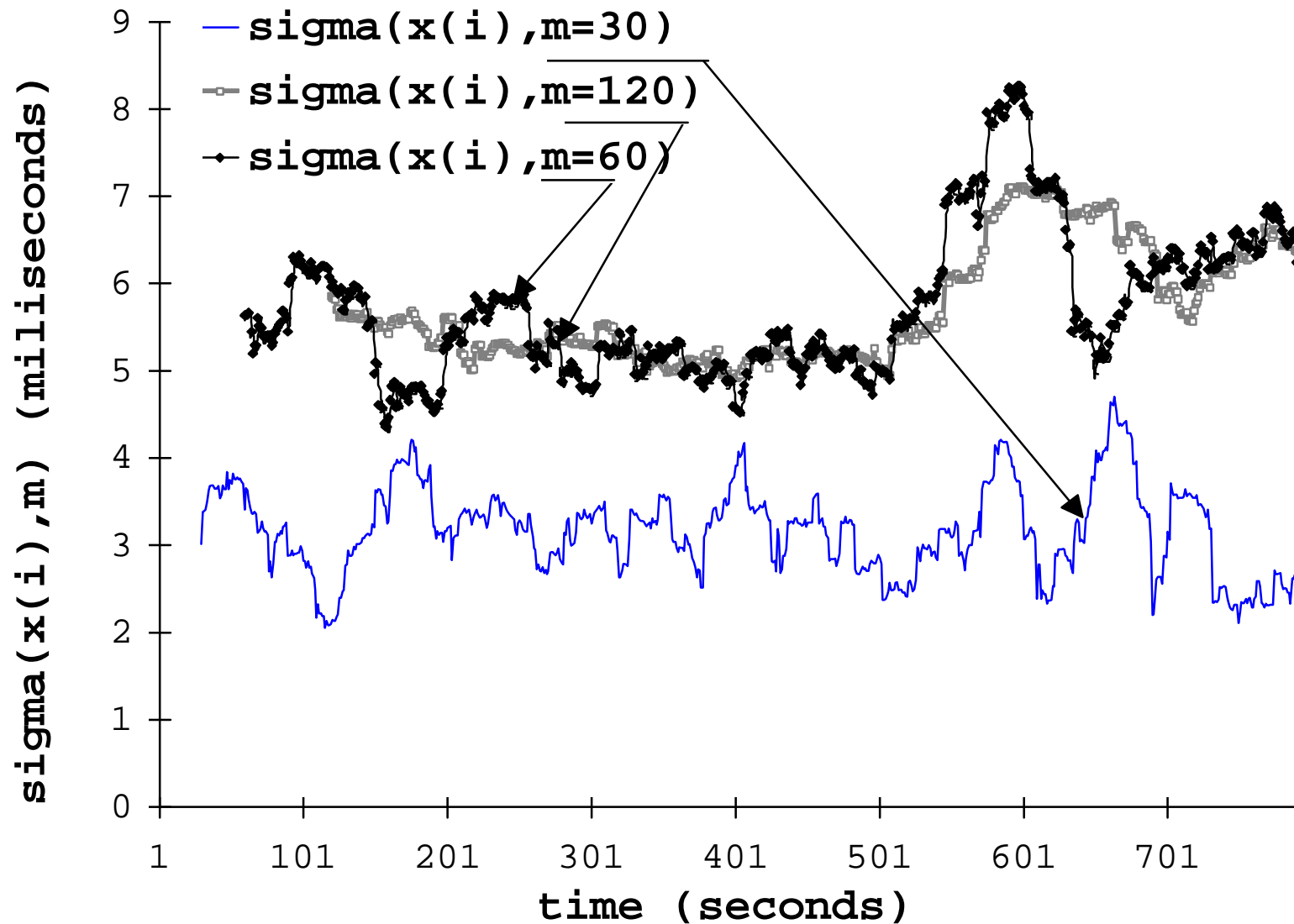
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# End of Presentation

# Long-Term Process Performance



# Long-Term Process Performance



# Assumptions

- **distribution of samples**
  - UWMA smoothed over large horizon
  - central limit theorem ... “roughly” normal
- **autocorrelation between smoothers**
  - sampling frequency between measurements
  - time scale of smoothers (approx. random sampling)
  - relative weight horizons of smoothers ( $m$  and  $m'$ )
- **stationarity**
  - hypothesis testing discards random fluctuations
  - variance prediction confidence over forecast