## **EVERT NASEDKIN**

SIMULATED INSTRUMENTAL CONSTRAINTS ON SUB-STELLAR ATMOSPHERIC RETRIEVALS FOR THE JAMES WEBB SPACE TELESCOPE'S MID-INFRARED INSTRUMENT.

## Evert Nasedkin

Simulated Instrumental Constraints on Sub-Stellar Atmospheric Retrievals for the James Webb Space Telescope's Mid-Infrared Instrument.

Copyright © 2020

#### TITLEBACK

This document was written with  $\LaTeX$  on Ubuntu using ArsClassica, designed by André Miede.

CONTACTS

rewertn@student.ethz.ch



Eidgenössische Technische Hochschule Zürich Swiss Federal Institute of Technology Zurich

## **Declaration of originality**

The signed declaration of originality is a component of every semester paper, Bachelor's thesis, Master's thesis and any other degree paper undertaken during the course of studies, including the respective electronic versions.

respective electronic versions.	
Lecturers may also require a declaration of o courses.	originality for other written papers compiled for their
I hereby confirm that I am the sole author of in my own words. Parts excepted are correct	the written work here enclosed and that I have compiled it ions of form and content by the supervisor.
Title of work (in block letters):	
Authored by (in block letters): For papers written by groups the names of all authors a	re required
Name(s):	First name(s):
With my signature I confirm that	
- I have committed none of the forms of p	plagiarism described in the 'Citation etiquette' information
<ul><li>sheet.</li><li>I have documented all methods, data ar</li></ul>	nd processes truthfully
<ul> <li>I have not manipulated any data.</li> </ul>	ia processes tratifically.
- I have mentioned all persons who were	significant facilitators of the work.
I am aware that the work may be screened e	electronically for plagiarism.
Place, date	Signature(s)

For papers written by groups the names of all authors are required. Their signatures collectively guarantee the entire content of the written paper.

## ACKNOWLEDGEMENTS

\_

## **ABSTRACT**

Following its launch in 2021, the James Webb Telescope will provide the best infrared observations of exoplanets and brown dwarfs to date. In particular, the Mid-Infrared Instrument (MIRI), will allow for medium resolution spectroscopy across a wide wavelength band, from 4.9-28.8 µm. This will allow us to derive atmospheric properties of objects at lower temperatures than currently possible. MIRI's medium resolution spectrometer (MRS) is an integrated field unit that will perform these observations, providing both spatial and spectral information about targets. Understanding the instrumental effects is critical to analyzing data from MIRI. With that in mind, the MIRISIM instrumental simulator was developed to provide observational simulations of the various sub instruments of MIRI.

This thesis improves the implementation of a thin-film fringing model for point sources to MIRISIM, considering how the fringing effect from the detector layers varies with position. Fringing is a periodic, wavelength dependent effect, and thus has a strong impact on any spectroscopic observations. A comparison to the existing model was made, demonstrating the necessity of considering this effect when analyzing data. We will improve the fringing removal by identifying the point source location from the constructed data cube, and select the correct fringe flat for removal.

Understanding the instrumental effects is key to quantifying the ability of MIRI to derive atmospheric properties. Existing literature has considered the NIRCAM instrument and the MIRI Low-Resolution Spectrometer, but to date no retrieval studies have been performed using MIRISIM, or for the MIRI MRS, though it is critical to extend wavelength coverage to improve the results of an atmospheric retrieval. Model atmospheres will be generated using PetitRadTrans, and processed using MIRISIM and the JWST pipeline to produce a mock observation. An atmospheric retrieval will be performed, demonstrating to what extent MIRI will be able to retrieve atmospheric parameters such as temperature, pressure and composition. The posterior distributions of these parameters are compared with and without the fringing removal, again demonstrating the importance of correcting for this effect.

## CONTENTS

```
INTRODUCTION
1.1 Exoplanets
1.2 Brown Dwarfs
            Physics
     1.2.1
            Observational Properties
     1.2.2
1.3 Motivation
           Current Status of Atmospheric Characterization
     1.3.1
     1.3.2 JWST Studies
           Biosignatures and Future Missions
     1.3.3
    Thesis Overview
MIRI: THE MID-INFRARED INSTRUMENT
2.1 The James Webb Space Telescope
2.2 MIRI
2.3
     The Medium Resolution Spectrograph
           Coordinates
     2.3.1
           Integrated Field Spectroscopy
     2.3.2
           Optical Systems
     2.3.3
     2.3.4
           Detectors
     Observations
     2.4.1 Dithering
                         10
     2.4.2 Exposure time calculations
                                         10
FRINGING EFFECTS IN MIRI
3.1 Fringing
                 13
3.2 MIRISIM
                  14
     3.2.1
           Architecture
                           14
     3.2.2 Data Products
     3.2.3 Instrumental effects
     3.2.4 Fringing
                        15
     3.2.5 Fringing Implementation
                                       16
3.3 JWST Pipeline
                      16
           Stage 1 Processing
                                 16
     3.3.1
           Stage 2 Processing
                                 16
     3.3.2
     3.3.3 Cross-Correlation
                                17
           Residual Statistics
                                 18
     3.3.4
3.4 Fringing Results
     3.4.1 Effects of fringing on spectral extraction
                                                     19
ATMOSPHERIC RETRIVALS
                            21
4.1 petitRADTRANS
           Radiative Transfer
     4.1.2 Opacity Sources
                               23
4.2 Bayesian Inference
           MCMC
     4.2.1
                       24
           Nested Sampling
     4.2.2
                                24
           Multinest
     4.2.3
```

		4.2.4	Prior ch	oice	26	
		4.2.5	Bayesia	n Mode	l Selection	26
	4.3	Targets	26			
		4.3.1	Atmosp	heric Pa	arameters	26
		4.3.2	petitRad	dTrans	27	
	4.4	Results	27			
		4.4.1	Posterio	r Distri	butions	27
5	CON	CLUSIO	15 29	)		
Α	APP	ENDICE	31			
	A.1	Packag	e Requi	rements	31	
	WOR	KS CITE	D 33			

## 1 INTRODUCTION

Since the first detection of a planet around a sun-like star (Mayor et al., 1995) the field of exoplanets has evolved rapidly. Thousands of companions have been identified using the radial velocity and transit detection methods, and a handful have been imaged directly using both ground and space based observatories. In the last decade, many advances have been made that allow us to begin to characterize the properties of a few of these planets using spectroscopy. With the launch of the James Webb Space Telescope (JWST) in 2021, and the dawn of the era of extremely large telescopes, we will be able to peer deeper into these planets and further constrain atmospheric or geological properties, allowing us to answer questions about their formation history, climate, and even the prospects for habitability and life.

JWST will operate in near to mid infrared wavelengths, which will provide a new window into studying the atmospheres of exoplanets and brown dwarfs. The Mid Infrared Instrument (MIRI) will provide unprecedented spectral resolution in the mid infrared, allowing for the measurement of composition, pressure and temperature. Novel instrumentation does not come without challenges. Optical and instrumental effects will constrain the ability to which we can measure spectral features, which will ultimately limit the science that can be accomplished.

In this thesis, we will measure the impact of thin-film fringing in the layers of the detectors in the MIRI Medium-Resolution Spectrometer on measurements of atmospheric parameters of brown dwarfs and exoplanets. This will provide a baseline for determining the level of correction necessary to minimize the impact of fringing, as well as providing a first look into the ability of the MRS to characterize atmospheres.

#### 1.1 EXOPLANETS

The last quarter century of observations has revealed the diversity of exoplanets and extra-solar systems. Both the architecture and individual planetary characteristics vary greatly when compared to each other, as well as to our own solar system. From the hot Jupiters initially found by Mayor and Queloz (Mayor et al., 1995) to the thousands of planets discovered by the Kepler mission, the variety in exoplanets has raised questions about their formation and development, as well as their present day structure, climate, and even prospects for life. Improvements to observational techniques have allowed us to improve our understanding of these planets. Secondary eclipse and transmission spectroscopy has opened the door to the study of planets in close orbits to their host stars, while emission spectroscopy of young planet has allowed for constraints on models of planet formation. Over the next decades, new instruments will be developed that improve sensitivity,

allowing us to study smaller, colder and fainter planets: with the ultimate goal of studying atmospheric and surface features of an earth-like planet.

Of particular interest are observable features that allow us to measure physical properties of exoplanets. The radial velocity (RV) method provides a measure of the planet mass, while a transit can constrain the radius. Already these properties tell us something about the overall structure of the planet. Spectroscopy can provide insight into the composition of the planet's atmosphere, as well as its temperature and pressure. These properties are linked to its age and location of formation in the circumstellar disk. The atmosphere, combined with the distance between the planet and its star determine the climate of the planet.

## Direct Imaging

While the majority of exoplanet detections have been made using the radial velocity or transit techniques, direct imaging opens up the possibility of collecting light from the planet itself. This provides a window into the planet's atmosphere and surface. Most direct imaging to date has used nearto-mid infrared wavelengths, where the contrast between the thermal emission from the planet and the star is at a minimum. This has its drawbacks: we are so far only able to image young planets that have retained some of the heat from their formation.

Direct imaging can make use of both ground and space based observatories. However, the high spatial resolution required drives the need for a large primary mirror, limiting the possibilities of space-based telescopes. On the other hand, atmospheric turbulence necessitates the use of an adaptive optics equipped facility to observe from the ground. Atmospheric absorption due to telluric lines (absorption lines of Earth's atmosphere) also restrict infrared observations to narrow bands.

In addition to the requiring high spatial resolution, it is also challenging to separate the light emitted by the planet from that of the star. Imaging techniques such as Angular Differential Imaging (ADI) (Marois2007) and Reference Differential Imaging (RDI) (Lefreniere2009; Soummer2012) provide methods for reducing the stellar point-spread-function (PSF). Coronagraphs are optical elements which suppress the stellar PSF through self-destructive interference or physical occultation, depending on the position in the optical path. The difference in spectra between the planet and the star can also be used to separate the two sources.

Presently, 10m class telescopes such as the Very Large Telescope (VLT) in Paranal, Chile or the Gemini Observatory split between Hawaii and Chile provide the best combination of resolution and instrumentation to perform direct imaging of exoplanets. The NACO instrument at the VLT provided the first image of an exoplanet in 2004 (Chauvin et al., 2004). These observatories are among those equipped with an adaptive optics system, corongraphic instrumentation and near to mid infrared imaging and spectroscopic capabilities to directly image exoplanets, with several exemplar systems becoming standard objects of interest. While it's terribly interesting to explore the details of each of these objects, we will focus our discussion on objects will be used further in this study, due to their scheduled observation as part

of the JWST GTO and Early Release Science (ERS) programs (Charles A Beichman et al., 2019c). The parameters of these and other directly imaged exoplanets and brown dwarfs are summarized in table 1.

Name	d [pc]	Mass [M <sub>jup</sub> ] Sep [au]	Sep [au]	Sep ["]	Age [Myr]	Sep ["] Age [Myr] $\log(\mathbf{L}_{bol}/\mathbf{L}_{\odot})$ $\mathbf{T}_{eff}$ [K]	$T_{eff}$ [K]	References
				Widely	Widely separated companions	ompanions		
VHS 1256b Fomalhaut b	$12.7 \pm 1.0$ $7.704 \pm 0.028$	2±1 ≤2	102 119	8.1	$10^3 - 10^4$ $440 \pm 40$	$-5.05 \pm 0.22$	880 1600 ± 100	(Gauza et al., 2015a)
				ַ כו	Close in companions	nions		
2M1207b	$152.4 \pm 1.1$	2±1	41	0.8	10±3	$-4.68 \pm 0.05$	$1600 \pm 100$	
51 Eridani b	$29.4\pm0.3$	$2\pm 1$	13	0.45	$23 \pm 3$	$-5.06\pm0.2$	200	(Macintosh et al., 2015)
$\hat{\beta}$ Pic b	$19.3\pm0.2$	$2\pm 1$	6	0.4	$23 \pm 3$	$-3.78 \pm 0.03$	$1600\pm100$	(Quanz et al., 2010)
GJ 504b	$17.56 \pm 0.08$	3 - 30	44	2.5	100 - 6500	$-6.13\pm0.03$	544	(Skemer et al., 2016a)
HD 95086b	$90.4 \pm 3.3$	$5\pm 2$	56	9.0	$17\pm4$	$-4.96\pm0.10$	1050	(De Rosa et al., 2016)
HR8799b	$39.4\pm1.0$	$5\pm 1$	89	1.7	$40 \pm 5$	$-5.1\pm0.1$	$870^{+30}_{-70}$	(Marois et al., 2008; Skemer et al., 2012)
HR8799c	$39.4\pm1.0$	$7\pm 2$	38	0.95	$40 \pm 5$	$-4.7\pm0.1$	$1090^{+10}_{-90}$	(Marois et al., 2008; Skemer et al., 2012)
HR8799d	$39.4\pm1.0$	$7\pm 2$	24	0.62	$40 \pm 5$	$-4.7\pm0.2$	$1090^{+10}_{-90}$	(Marois et al., 2008; Skemer et al., 2012)
HR8799e	$39.4\pm1.0$	$7\pm 2$	14	0.38	$40 \pm 5$	$-4.7\pm0.2$	1000	(Marois et al., 2008; Skemer et al., 2012)
LkCa 15b	$145\pm15$	$6\pm4$	20	80.0	$2\pm1$	:	:	
PDS 70b	$113.43 \pm 0.52$	$7\pm 2$	23	0.19	$5\pm1$	:	006	(Haffert et al., 2019)
PDS 70c	$113.43\pm0.52$	$4.4\pm1$	30	0.24	$5\pm1$	:	$10^{4}$	(Haffert et al., 2019)
				Ne	Nearby Brown Dwarfs	Owarfs		
WISE 0855	$2.2 \pm 0.2$	3 - 10	:	:	$10^3 - 10^4$	-10.5	225 – 260	(Luhman, 2014; Tinney et al., 2014)
Luhman 16B	$1.998 \pm 0.0004$	$28.6 \pm 0.3$	:	:	008 - 009	-4.68	1201	(Garcia et al., 2017; Sahlmann et al., 2015)

Table 1: Summary of directly imaged planet and brown dwarf parameters based on (Bowler, 2016) and references therein. Luminosity for WISE 0855 is calculated in H band.

(Lagage2015)

VHS 1256 b

2M1207b

#### **BROWN DWARFS** 1.2

(Oliveira) (Helling et al., 2014)(Cooper2014) (Nikku Madhusudhan et al., 2018) (Burrows2003) (Marley2014) (Manjavacas, 2014) (B. Biller, 2017) (Jacqueline K Faherty et al., 2018) (Morley et al., 2014)

- **Physics** 1.2.1
- 1.2.2 Observational Properties

T-Type

L-Type

Luhman 16B

Y-Type

WISE 0855-0714

- 1.3 MOTIVATION
- 1.3.1 Current Status of Atmospheric Characterization

(Kreidberg, 2018)(B. A. Biller et al., 2018) (Bozza et al., nodate) (Danielski et al., 2018) (Nikku Madhusudhan et al., 2016)

## Transmission Spectroscopy

(Lee et al., 2012) (MacDonald et al., 2017) (Madhusudhan)

## Emission Spectroscopy

1.3.2 JWST Studies

(Charles A Beichman et al., 2019c)

- Biosignatures and Future Missions 1.3.3
- THESIS OVERVIEW 1.4

# MIRI: THE MID-INFRARED INSTRUMENT

MIRI is an instrument that will provide unique capabilities for studying exoplanets and other cold and distant objects. This chapter will provide a detailed overview of the technical details and capabilities of the instrument. A complete description of MIRI is provided in (Boccaletti et al., 2015; Bouchet et al., 2015; Glasse et al., 2015; P. Lagage et al., 2015; Ressler et al., 2015; Rieke et al., 2015b,c; Wells et al., 2015; Wright et al., 2015)

#### 2.1 THE JAMES WEBB SPACE TELESCOPE

JWST is a 6.5m space based observatory built in collaboration between NASA, ESA and CSA that will be located in a halo orbit at the L2 Earth-Sun Lagrange point. As the successor to the Hubble Space Telescope and the Spitzer Space Telescope, it will provide a new perspective for infrared astronomy. It is currently scheduled to launch in March 2021.

James Webb is fully optimized for infrared astronomy. To reduce instrumental thermal background, the entire telescope will operate at cryogenic temperatures. A large sun-shield will help block solar infrared radiation. The lightweight beryllium mirrors are coated in gold to maximize reflectivity out to the mid infrared.

Of key interest to exoplanet science is the both the sensitivity and spatial resolution of the instrument. With its 6.5m primary, JWST will have a spatial resolution from 0.01" at 0.6 micron to 0.92" at 29 micron. The increase in sensitivity is due in part to the larger collecting area, but also to advances in detector technology since the previous generation of infrared observatories. For example, the MIRI instrument will have a minimum detectable flux of 0.13  $\mu$ Jy at 5.6 micron, or roughly a factor of 1000 better than what was possible with the Spitzer Space Telescope (Glasse et al., 2015).

There are four primary instruments that constitute the Integrated Science Instrument Module (ISIM). Near-Infrared Camera (NIRCam), which provides imaging with coronagraphic capabilities from 0.6-5 micron. The Near-Infrared Spectrograph (NIRSpec) provides fixed slit and integrated field unit spectroscopy capable of analyzing multiple objects simultaneously, and operates in the same wavelength range as NIRCam. The Fine Guidance Sensor/ Near-Infrared Imager and Slitless Spectrograph (FGS/NIRISS) allows for low and medium resolution spectroscopy with high photometric stability, as well as aperture masking interferometry. The final instrument, MIRI, is the subject of this thesis.

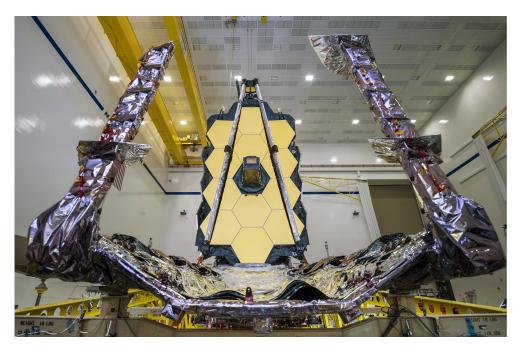


Figure 1: The James Webb Space Telescope during integration of the telescope into the Spacecraft Element (assembled).

## Subsystem

**Imaging** 4QPM Coronagraphic Imaging Lyot Coronagraphic Imaging Low Resolution Spectroscopy Medium Resolution Spectroscopy

Table 2: Summary of MIRI observing modes.

#### 2.2 MIRI

The Mid-Infrared Instrument (MIRI) provides imaging, fixed slit and integrated field spectroscopy between 4.8 and 28 micron (Rieke2015). It will operate at a temperature of 6.7K to reduce instrumental backgrounds over its wavelength range of 0.6-28.8 micron.

(Kendrew2015)

#### 2.3 THE MEDIUM RESOLUTION SPECTROGRAPH

The Medium Resolution Spectrograph (MRS) consists of four integrated field spectrographs projected onto two detectors, covering 4.8-28 micron with a spectral resolution varying from R=1700 to R=3500.

(Wells2015)

Channel	Sub-band	Band	Detector	$\lambda$ Range [ $\mu$ m]	FOV [as]	λ/Δλ
	Short	1A		4.83 - 5.82	3.46×3.72	3500
1	Medium	1B	SW	5.62 - 6.73	$3.46 \times 3.72$	3500
	Long	1C		6.46 - 7.76	$3.41 \times 3.72$	3300
	Short	2A		7.44 - 8.90	4.16×4.76	3000
2	Medium	2B	SW	8.61 - 10.28	$4.16 \times 4.76$	3000
	Long	2C		9.94 - 11.87	4.12×4.76	3000
	Short	3A		11.47 - 13.67	6.00×6.24	2700
3	Medium	3B	LW	13.25 - 15.80	5.96×6.24	2300
	Long	3C		15.30 - 18.24	$5.91 \times 6.24$	2300
	Short	3A		17.54 - 21.10	7.14×7.87	1700
4	Medium	3B	LW	20.44 - 24.72	7.06×7.06	1700
	Long	3C		23.84 - 28.82	$6.99 \times 7.87$	1500

**Table 3:** Properties of the MIRI MRS channels (Wells et al., 2015).

#### Coordinates 2.3.1

There are three primary coordinate systems in use with JWST/MIRI-MRS, of which two will be relevant for this thesis, with the detector and local MRS coordinates described in Fig. 2 (Argyriou et al., nodate).

The detector coordinate grid is formed by counting x/y pixels, as well as the slice number. Each of the two MRS detectors is an array of 1032×1024 pixels, though only 1024 are photosensitive in the horizontal direction. Each image slice from the IFU appears as a curved stripe on the detector, though neighboring stripes on the detector do not correspond to neighbouring slices of the image.

The local MRS coordinate system is described in terms of  $\alpha$ ,  $\beta$  and  $\lambda$ . The continuous  $\alpha$  coordinate is the along slice direction, while *beta* is perpendicular and discrete, corresponding to the slice number.  $\lambda$  is the wavelength. Both  $\alpha$  and  $\lambda$  are fit by a second order polynomial to account for along and across slice distortion (Wells et al., 2015). Each detector sub array has its own mapping to  $\alpha$ ,  $\beta$ ,  $\lambda$  space, due to the differences in FoV, slice count, distortion and spectral resolution.

The third coordinate frame is the global coordinate system of JWST itself, V1,V2,V3. The V1 coordinate refers to the symmetry axis of the telescope, V<sub>3</sub> points towards the foldable secondary mirror support structure strut. V2 completes the coordinate system, being orthogonal to V1 and V3. This coordinate system will not be used in this thesis.

#### Integrated Field Spectroscopy

#### **Optical Systems** 2.3.3

Channels, bands, etc ref:Chen2019

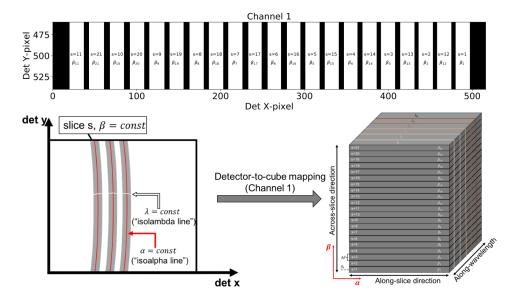


Figure 2: Description of the MRS detector (x,y,s) coordinate system to the local MRS  $(\alpha, \beta, \lambda)$  cube coordinates. **Top**: Detector coordinates. Note that the consecutive stripe numbers  $s_i$ ,  $s_{i+1}$  correspond to neighbouring image slices. Bottom: Description of the (invertible) detector-to-cube transformation (Argyriou et al., nodate).

Figure 3: Detector images of a spatially and spectrally flat calibration source for the SW detector (left) and LW detector (right).

#### 2.3.4 **Detectors**

#### Readout Modes

#### **OBSERVATIONS** 2.4

#### Dithering 2.4.1

## 2.4.2 Exposure time calculations

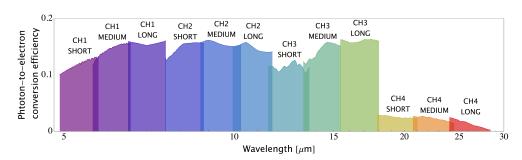


Figure 4: Average photon-to-electron conversion efficiencies for the MIRI MRS detectors

## FRINGING EFFECTS IN MIRI

Understanding optical and instrumental effects is critical for creating accurate simulated observations and for characterizing systematics. These systematics and uncertainties in turn impact the potential science results from any instrument by biasing measurements, reducing the signal to noise ratio of measurements or by injecting non-physical signals and correlations. The aim of this chapter is to examine fringing in the MIRI detectors and how this effect is modeled in the instrumental simulator (MIRISIM).

## 3.1 FRINGING

Thin film interference occurs when light is coherently reflected at the boundary between two layers and interferes with the incident light. This is the principle on which Fabry-Pérot interferometers function. As we wish to determine the effect of fringing on the=-o amplitude of the signal received by the detector, we are effectively interested in the transmittance of a series of Fabry–Pérot interferometers. Assuming an ideal plane-parallel optical cavity with a reflectance R at both boundaries, thickness D, and an angle  $\theta$  at which the light travels within the cavity, we can compute the transmittance as:

$$T_c = \frac{1}{1 + \frac{4R}{(1 - R)^2} \sin^2\left(\frac{\delta}{2}\right)} \tag{1}$$

Where the phase  $\delta$  at half a wavelength ( $\phi = \pi$ ), with wavenumber  $\sigma$  is:

$$\delta = 4\pi\sigma D\cos\theta - (\phi - \pi) \tag{2}$$

Systems with a spacing on the order of millimeters produces significant interference for infrared light (Lahuis et al., 2003).

The detectors of the MRS consist of several layers, as shown in Fig. 5, with a characteristic thickness of 500µm, which results in significant (10%-30%) 'fringing' in a spectrally flat signal - visible in Fig. 3. While this is typical for infrared detectors such as those in the Spitzer Space Telescope (Lahuis et al., 2003) or in the Space Telescope Imaging Spectrograph on board HST (Malumuth2003), the sensitivity and spectral resolution of the MRS increase the significance of this issue. The MIRI consortium has stated that the error budget for all detector effects must be 3.3% or less. Present fringing corrections result in a 5% deviation from a photometrically accurate signal, and can introduce correlated noise which will degrade any measured spectrum. Therefore it is critical to examine the impact of fringing on a signal, the parameters that influence the fringing strength and phase, and possible solutions for fringe correction. While a more complete treatment of proposed fringe correction can be found in (Argryiou2020), this work will examine the implementation of fringing into the MIRI instrumental simulator and

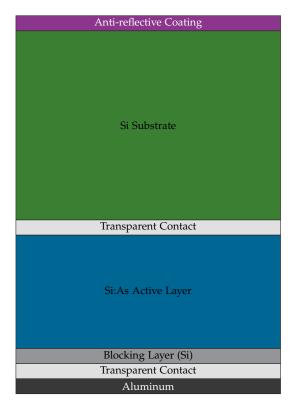


Figure 5: Layers of the MIRI MRS detectors. Note that thicknesses are not to scale (Rieke et al., 2015c).

address the current state of fringe correction in the JWST Data Calibration Pipeline.

Fred Lahuis et al., 2018

#### **MIRISIM** 3.2

Consortium2018 Cossou2019 The MIRI instrument has been modeled in python as a program known as MIRISM. This program takes in an astronomical 'scene' along with some configuration parameters to output a detector data product, similar to what will be produced by the actual instrument. This is relatively full-featured simulator, modelling the instrumental PSF, various noise sources and distortion maps, among other effects. While MIRISIM is functional for all of the MIRI sub-instruments, this report will only deal with the Medium-Resolution Spectrometer (MRS) sub instrument, described in section 2.3. The goal of this section is to describe the implementation and testing of an updated optical model of the 'fringing' effect - an optical effect caused by thin film interference from the multiple layers of the detector.

#### Architecture 3.2.1

SCENE - SEDs SIMULATOR PYSPECSIM

#### Figure 6

#### Table 4

- 3.2.2 **Data Products**
- Instrumental effects 3.2.3

#### Fringing 3.2.4

Lahuis et al., 2003 VanderPlas, 2018 A key effect on spectral data is fringing, described in ref:Argyriou2018. MIRI uses a total of three Si:As impurity band conduction detector arrays, two of which are used by the MRS. These detectors consist of 7 layers, listed in table 4 and illustrated in Fig. 5.

If all of the parameters were known, this would be sufficient to numerically solve for the fringing pattern within MIRI. Unfortunately, uncertainties in the thickness in the detector layers, variations in the layer deposition thickness, and the uncertainty of transmittance and reflectance of the materials used at cryogenic temperatures prevents the implementation of such a numerical model.

Instead, we turn to calibration data taken to characterize the fringing pattern.

#### \*\*\*DESCRIBE CURRENT MODEL - GENERIC FRINGING\*\*\*

However, due to the dependance of fringing on the incident angle of the light, a single model of fringing is insufficient to describe the full effect. Therefore, we use data taken in XXXXXXXXX at various points across the detector and quantify how this changes the extracted spectra after processing in the JWST pipeline.

\*\*\*DESCRIBE HOW THE DATA WAS TAKEN HERE\*\*\*. - Problems with point vs extended sources - multiple collection runs

Ultimately this data collection produced a series of 'fringe-flats' of an almost point like at various position across the detector and in each channel. We implemented a new routine into the pySpecSim portion of MIRISIM to read in the location of point sources within a scene, and apply the correct position dependent fringe flat. This implementation comes with several caveats: namely that the fringing model is not yet fully developed, so it can only be considered accurate for point sources located at the same  $(\alpha, \beta)$  location as the source used to produce the fringe flat. Additionally, the source used to generate the data is not a true point source, nor are there fringe flats produced for the full MRS wavelength range. We stress that the goal of this testing is to demonstrate the significance of this effect to justify the need for a more complete model along with additional calibration data to constrain the detector layer parameters.

FM Data

CV Data

3.2.5 Fringing Implementation

JWST PIPELINE 3.3

Bushouse et al., 2015 Labiano-Ortega2016

- Stage 1 Processing 3.3.1
- 3.3.2 Stage 2 Processing

#### Photometric Calibration

Photometric calibration is the process of removing detector and optical biases to ensure that the measured output corresponds to the true flux incident onto the telescope. This process occurs in the PHOTOM step of the JWST pipeline, and uses reference files which store per-pixel photon-to-electron conversion efficiencies to transform the count rate data product to a flux measurement. This corrects for the wavelength dependent bias shown in Fig. 4.

However, this step remains under development, and does not produce absolutely calibrated images. In particular, even using the most up to date reference files (v8D.04.00) there remains discontinuities between channels, and poorly calibrated slopes.

#### Fringing correction

Carnall, 2017

## Cube Building

#### Aperture Photometry

Once the data from the pipeline has been transformed into a spectral cube, we can perform aperture photometry using the photutils package to extract a 1D spectrum of the source. For each frame in each sub-band the coordinates of the spaxel at with the peak flux is detected using photutils find\_peaks, which provides the location for the center of a circular aperture. A radius of 5 spaxels is used to encompass the entire PSF for a point source. If the files have already been photometrically calibrated, measuring the flux requires just adding the flux from each spaxel within the defined radius for each frame. While optimal extraction techniques exist, given our known input signal and background, this procedure is adequate for producing a spectrum in each sub-band, which can then be combined into a single spectrum for all measured sub-band.

Unfortunately, due to the issues described above with the PHOTOM step of the JWST pipeline, the spectrum built using aperture photometry does not accurately reflect the input spectrum in slope or absolute photometry. Therefore, we correct the extracted spectrum channel by channel. We fit a cubic

polynomial to a median filtered copy of both the template spectrum and the extracted spectra. The cubic fit to the extracted spectra is subtracted from the data, and the fit to the template is added. Thus this procedure corrects the slope and median flux value, but does not affect high frequency noise or signals. Fig. 7 shows an example of the results of this procedure. We believe that this is a justified measure, as the errors with photometric calibration in the pipeline should be resolved before first light of the telescope.

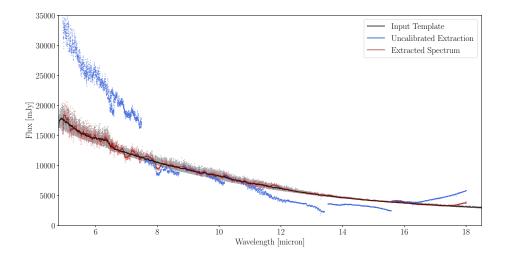


Figure 7: Comparison of an input spectrum generated using petitRadTrans and the empirically calibrated output spectrum after extraction from the cube produced by the JWST pipeline.

#### **Cross-Correlation** 3.3.3

Ignas Snellen et al., 2014Simkin, 1974 Tonry1979 Petermann, 2019 Bodis, 2007 To quantify the similarity of the spectrum output by the JWST pipeline to the input into MIRISIM, we rely on the technique of cross correlation. For two arbitrary, complex-valued functions f(t) and g(t), we can compute the cross correlation as as function of the shift  $\tau$  between the functions (typically in time or velocity space):

$$(f \star g)(\tau) \equiv \int_{-\infty}^{\infty} f^*(t)g(t+\tau)dt \tag{3}$$

Our signals of interest are astrophysical spectra, measured in a finite number of discrete wavelength bins. For such a signal with *M* bins:

$$(f \star g)[n] \equiv \sum_{m=0}^{M} f^*[m]g[m+n]$$
 (4)

Care must be taken when cross-correlating signals, as differences in normalization can result in changes in the correlation coefficient. Our procedure takes in two spectra. The first is an emission spectrum produced by the petitRadTrans program P. Mollière et al., 2019, which provides our forward model with which we compare our data spectrum. Our data is the result of

passing the template spectrum through MIRISIM, and extracting it from the resulting detector image using the JWST pipeline. We then rebin the highresolution input spectrum to the same wavelength bins as the data spectrum, using the spectres package. Prior to normalization, we remove any outliers from the spectrum (due to binning errors or instrumental effects) by setting any data points separater by more than 15 standard deviations from the mean to the median value of the spectrum. For each spectrum, we subtract the minimum value to remove any offset in the spectrum, and divide by the maximum value to restrict the range to [0,1]. We then use apply a Savitzky-Golay filter with a window of 1/4 the length of the spectrum and a polynomial order of 3, which we then subtract from the unfiltered spectrum. This removes the continuum emission from the spectrum, and centers it around o. We then renormalize the spectrum by dividing by the maximum absolute value such that the range is in [-1,1]. The cross correlation between the forward model and itself is computed, excluding the region of interest around o offset. This 'autocorrelation' is subtracted from the cross correlation between the forward model and the data spectrum in order to remove secondary peaks. Finally, we normalize the cross correlation by the standard deviation of the cross correlation (excluding the central peak), giving an output measured as a signal to noise ratio.

## 3.3.4 Residual Statistics

In addition to computing the cross correlation between the forward model and the data spectrum, we also examine the residuals between the two spectra. Here we can see any unexpected variations between the two (periodic signals, offsets or other features). We can also examine a histogram of the residuals, normalized by the standard deviation of the data spectrum. This provides us with a distribution which should have a mean of o and unit width if the data are unbiased and share a distribution with the true input spectrum.

#### FRINGING RESULTS 3.4

1. A stronger input signal results in a stronger correlation. 2. Fringing does NOT necessarily degrade the cross correlation SNR, but rather increases it. The scale of this increase seems to depend on the absolute magnitude of the correlation (ie, a larger increase at higher SNR) 3. The residuals from subtracting the template from the data has structure. 4. If the residuals are histogrammed (and normalized by the standard deviation of the data), the width of the distribution may correspond to the cross correlation SNR (wider distribution = lower SNR) 5. Only when strongly increasing the fringing effect does the SNR decrease. 6. Correcting for fringing using the standard JWST fringe map decreases the SNR when compared to the case of fringing with no correction, but is typically still above the no-fringing case. 7. The JWST correction performs worse in the off axis case, as the fringe pattern begins to vary more when compared to the CV fringing model.

## 3.4.1 Effects of fringing on spectral extraction

## 4 ATMOSPHERIC RETRIVALS

Everything photon of light that we receive from an exoplanet will interact with its atmosphere, and will therefore provide us with a hint of what that atmosphere may look like. An atmospheric retrieval is the process of reconstructing the atmosphere of an object based on an observed spectrum. This process relies heavily on having accurate models which can be parameterized by the physical quantities we are interested in: generally the temperature, pressure and composition (Nikku Madhusudhan, 2018). As these models cover a very large parameter space (>10 parameters, each covering several orders of magnitude), it is necessary to have an efficient method for sampling this space, computing a model and comparing this model to the data (Bjoern Benneke et al., 2012).

This chapter will outline the process of an atmospheric retrieval from modelling to marginalization of posteriors, and will examine the impact that the instrumental effects described in chapter 3 have on the retrieved parameters. Additionally, this will provide an example of how the MIRI MRS can be used to explore exoplanet and brown dwarf atmospheres, and what observational parameters should be considered when studying these objects.

Schlawin et al., 2018 Fisher et al., 2019 **Oreshenko2019**Barman et al., 2015 Björn Benneke, 2013 Bjoern Benneke et al., 2012 **Blanco-Cuaresma2018** Konopacky et al., 2013

(Morley et al., 2018) Lupu et al., 2016 Gandhi et al., 2018 Baudino et al., 2017 Line et al., 2013 **Madhusudhan2018b** Irwin et al., 2008 Robinson et al., 2016 Waldmann et al., 2015b Waldmann et al., 2015a Line et al., 2017; Zalesky et al., 2019

Batalha et al., 2018Feng et al., 2018 P. Mollière et al., 2019

## Atmospheric Modeling

Atmospheric modelling is the task of creating an spectra based on the physical properties of the atmosphere. This is a broad task that can range from a 3D Global Circulation Model (GCM) which accounts for self-consistent atmospheric chemistry (Chen et al., 2019) to a 1D model based around an empirical temperature-pressure profile (P. Mollière et al., 2019). The choice of model depends largely on the requirements for accuracy and computational cost. Considering the potentially millions of possible atmospheres that must be examined in a retrieval problem, whatever model is used must be computationally efficient above all else.

#### 4.1 PETITRADTRANS

For this work we chose to use the petitRADTRANS package due to its user-friendly python implementation, high speed computation for retrieval

Property	Description
Temperature	Parameterized, e.g. (Guillot, 2010)
Abundances	Parameterized, e.g. vertically constant
Scattering	Cloud scattering, transmission spectra only
Clouds	Power law and condensation clouds
Cloud particle size	$f_{SED}$ and $K_{ZZ}$ or parameterized
Particle size distribution	log-normal, variable width
Cloud abundance	Parameterized
Wavelength spacing	R=1000 (c-k), 10 <sup>6</sup> (lbl)
Valid emission spectra	Clear, from NIR and longer

Table 5: Description of the parameters available in petitRADTRANS. For cloud particles,  $f_{SED}$  is the mass-averaged ratio of the cloud particle settling speed and mixing velocity. K<sub>ZZ</sub> is the atmospheric eddy diffusion coefficient (Ackerman et al., 2001)

use and extensive high resolution, line-by-line spectral library for generating planetary spectra (P. Mollière et al., 2019). It is a 1D, radiative transfer package with many parameters options, described in table 5 PetitRADTRANS can compute both emission and transmission spectra, with an output spectral resolution of R=1000 in correlated k mode, or R=1 000 000 in line-by-line mode.

Note that much of the following sections applies to many other similar 1D radiative transfer atmospheric modelling programs such as ATMO (Goyal2018), Planetary Spectrum Generator (Villanueva2018), HELIOS (Malik et al., 2017, 2019) and others. Many (or even most) of these programs rely on the same set of high-resolution molecular line lists, including HI-TRAN/HITEMP (Rothman1973; Gordon et al., 2017; Rothman et al., 2010), ExoMol/ExoCross (Tennyson2016a; Tennyson et al., 2016; Yurchenko et al., 2018) and others.

#### Radiative Transfer

In order to compute the emission spectrum an initial featureless blackbody spectrum  $B(T_{int})$  is passed through multiple discrete layers of the atmosphere, parameterized by their temperature, pressure, and the opacities of each of the species present in a given layer. Modeling each layer as plane parallel, the intensity is computed as in (Irwin et al., 2008; P. Mollière et al., 2017, 2019)

$$I_{top} = B(T_{int})\mathcal{T}^{atmo} + \frac{1}{2} \sum_{i=0}^{N_L - 1} \left[ B(T^i) + B(T^{i+1}) \right] \left( \mathcal{T}^i - \mathcal{T}^{i+1} \right)$$
 (5)

 $N_L$  is the number of layers in the atmosphere, and  $\mathcal{T}$  is the transmission from a given layer to the top of the atmosphere. All quantities are averaged per wavelength bin in c-k mode, while they are evaluated at each wavelength point in line-by-line mode.

(Guillot, 2010)

#### 4.1.2 Opacity Sources

To compute the emission spectra of an atmosphere, petitRADTRANS accounts for various opacity contributions including absorption and emission lines, collisionally induced absorption, cloud opacity and scattering and Rayleigh scattering cross sections. These sources are described in detail in (P. Mollière et al., 2019), summarized in tables 2 and 3. For this work we consider only the case of a cloud-free atmosphere due to the complexity of realistic cloud modeling.

#### Line-by-line

In its high resolution line-by-line mode, petitRADTRANS computes emission spectra with R=10<sup>6</sup>. These spectra are computed using opacity sources for molecular and atomic lines from ExoMol/ExoCross library (Yurchenko et al., 2018). Pressure broadening is taken into account using the coefficients from HITRAN/HITEMP (Rothman et al., 2010, 2013) or from (**Sharp2007**) (Eqn. 15). The line opacities are computed from 80-3000K, and from 0.3- $28\mu$ m in high resolution mode.

#### Correlated K

The low resolution mode of petitRADTRANS uses the correlated-k (c-k) method of computing line opacities (Fu et al., 1992; Goody et al., 1989; Lacis et al., 1991). This method for calculating emission and absorption features assumes that the opacity distribution functions between differing species are uncorrelated, which permits simple computation of overlapping features. While petitRADTRANS implements a c-k method with a spectral resolution of 1000, in principle it is accurate to much higher resolutions. However, the principle utility of the c-k method is in the dramatic reduction in computational cost for computing a spectra such that petitRADTRANS can be used as the foundation for an atmospheric retrieval code requiring hundreds of thousands or millions of models to be generated. (P. Mollière et al., 2019) discusses the variations between the results of the line-by-line method and the c-k method, finding discrepancy of at most 6%. Typical variation is much lower, as seen in Fig. 2 of (P. Mollière et al., 2019).

#### Clouds

Line et al., 2016 Jacqueline K Faherty et al., 2018 Morley et al., 2014 Lavie et al., 2017

#### 4.2 BAYESIAN INFERENCE

An atmospheric retrieval is the process of extracting information about physical parameters from a measured spectrum. In general this procedure involves comparing the data to a series of template spectra with known parameters and identifying the best fit model. Unfortunately for astronomers, atmospheres are complicated: typical one 1D models still require many (>15) parameters to generate a somewhat realistic model. This results in a very large parameter space in which to search for the correct set of properties that describe our measurement.

Monte Carlo methods, including Nested Sampling, are used to effectively search this large space using the Baysian evidence as a goodness-of-fit metric. Here we will follow (Joshua S. Speagle, 2019) to provide a brief overview of Bayesian inference.

To measure the likelihood of a given model, we turn to Bayes' Theorem:

$$P(\mathbf{\Theta}_{M}|\mathbf{D}, M) = \frac{P(\mathbf{D}|\mathbf{\Theta}, M)P(\mathbf{\Theta}|M)}{P(\mathbf{D}|M)}$$
(6)

In our notation,  $\Theta$  is the set of parameters that describe a model M, that is fit to the data D. Bayes' theorem asks what is the probability that the parameters  $\Theta$  are true given the data and model. The distributions for each parameter are the **posterior** distributions.

This is then related to the **likelihood**  $P(\mathbf{D}|\mathbf{\Theta}, M)$  of measuring the data given the model, the **prior** probability  $P(\Theta|M)$  which describes our degree of belief in our model and the evidence  $P(\mathbf{D}|M)$ , which is marginalized over all possible  $\Theta$  and quantifies how well the model describes the data. To simplify notation, we adopt the following convention for Bayes' theorem:

$$\mathcal{P}(\mathbf{\Theta}) = \frac{\mathcal{L}(\mathbf{\Theta})\pi(\mathbf{\Theta})}{\mathcal{Z}} \tag{7}$$

In general, the goal of an atmospheric retrieval is to find the best fit model by maximizing the evidence  $\mathcal{Z}$ , and as a by product finding the marginalized posterior distributions for each parameter. This comes with many challenges, especially when dealing with large numbers of parameters. Selection of the priors and model will determine the extent to which a result can be interpreted, while sampling large parameter spaces and computing likelihoods introduces substantial numerical challenges. The Markov Chain Monte Carlo method and the Nested Sampling method described below attempt to solve the challenges of exploring a large parameter space.

#### MCMC 4.2.1

Foreman-Mackey et al., 2013 MacKay, 2003

## Nested Sampling

Nested sampling attempts to address several of the shortcomings of MCMC methods while simultaneously improving computational efficiency (Skilling, 2004). MCMC methods generate samples 'proportional to' the true posterior distributions, which lead to difficulties in computing the evidence  $\mathcal{Z}$ (Joshua S Speagle, 2020). In contrast, nested sampling puts the evidence first and provides estimates of the posterior distributions from the importance weights of the final set of samples. First described in (Skilling, 2004), nested sampling has been adopted as the sampling algorithm of choice within the astrophysics community (Buchner et al., 2014; F. Feroz et al., 2009; Farhan Feroz et al., 2019; Joshua S Speagle, 2020).

With the goal of parameter estimation, nested sampling attempts to estimate the evidence  $\mathcal{Z}$  rather than directly sampling the posteriors (Skilling, 2004). This is done by integrating over the entire parameter space of  $\Theta$ 

$$\mathcal{Z} = \int_{\Omega_{\mathbf{\Theta}}} \mathcal{L}(\mathbf{\Theta}) \pi(\mathbf{\Theta}) d\mathbf{\Theta}$$
 (8)

This is difficult.

Rather than attempting to directly solve the entire multidimensional integral, nested sampling transforms this into an integration over the prior volume X:

$$\mathcal{Z} = \int_{\Omega_{\mathbf{\Theta}}} \mathcal{L}(\mathbf{\Theta}) \pi(\mathbf{\Theta}) d\mathbf{\Theta} = \int_{0}^{1} \mathcal{L}(X) dX$$
 (9)

This is now a contour integral over isocontours  $\mathcal{L}(X)$  which bound the prior volume

$$X(\lambda) = \int_{\Omega_{\mathbf{\Theta}}: \mathcal{L}(\mathbf{\Theta}) > \lambda} \pi(\mathbf{\Theta}) d\mathbf{\Theta}$$
 (10)

which is the fraction of the prior where the likelihood of the data given the model is above some threshold  $\lambda$ . The integration is now simplified into a 1D integration over X, given proper prior selection.

#### Method

Consider a parameter space with D dimensions. We will describe this space as a unit hypercube, where each parameter runs from o to 1. Priors are thus transformations from this space to a physical parameter space. Often the prior is a uniform distribution, which simply scales the space, but it may also be an informative prior such as a normal distribution centered at an expected physical value. In order to sample this space,  $N_L$  'live points' are generated, each of which provides a set of parameters  $\Theta$ .  $N_L$  must be greater than D+1, and typically values on the order of  $50 \times D$  are used (F. Feroz et al., 2009). Using a likelihood function  $\mathcal{L}(\Theta)$ , the evidence  $\mathcal{Z}$  can be computed by comparing the model to the data. Having computed the evidence at each point, the live points are then sorted and the point with the lowest evidence is discarded. A set of ellipsoids is drawn around the remaining points. The procedure for computing these ellipsoids is given in (F. Feroz et al., 2008, 2009). By using a set of ellipsoids, multiple modes in the parameter space can be encompassed. Once the ellipsoids bounding the remaining points are drawn, a new sample is drawn from within the restricted sample space. The evidence for the new point is computed, and it is accepted if the evidence is greater than the minimum evidence of the previous remaining set of points. The entire procedure is repeated until some convergence criteria is satisfied, with each iteration resulting in a smaller volume being encompassed by the ellipsoids, nested within the previous volume.

This procedure can be improved in many ways, including importance nested sampling (Farhan Feroz et al., 2019) and dyamic nested sampling (Joshua S Speagle, 2020).

Parameter	Prior	Constraints
$\log \delta$	$\mathcal{N}(-5.5, 2.5)$	
$\log \gamma$	$\mathcal{N}(0,2)$	
$T_{int}$	U(0,3500)	
$T_{equ}$	U(0,30)	
$\log P_{Trans}$	$\mathcal{N}(-3,3)$	
α	$\mathcal{N}(0.25, 0.4)$	$\alpha < 1$
$\log g$	U(2.0, 4.5)	
$\log P_0$	U(-5,2)	
$ln(X_i)$	U(-18,0)	$\sum X_i < 1$

**Table 6:** Prior choices for atmospheric retrievals. U(a,b) is a uniform distribution from a to b.  $\mathcal{N}(\mu, \sigma)$  is a normal distribution.  $T_{int}$  corresponds to the effective temperature of an object, while  $T_{equ}$  is the equilibrium temperature between an object and a host star. For free floating objects,  $T_{equ}$  is set to 3.4K, justifying the small range of the prior.  $\delta$  is in units of bar<sup>-1</sup>, temperatures are in K, and pressures in bar.

#### Multinest 4.2.3

For our implementation of an atmospheric retrieval code, we chose to use the Multinest algorithm (F. Feroz et al., 2009) using the pyMultinest wrapper (Buchner et al., 2014) and using importance nested sampling to improve the accuracy of the Bayesian evidence calculation (Farhan Feroz et al., 2019). This particular implementation of nested sampling is commonly used in atmospheric retrieval codes due to its fast Fortran implementation, though it was initially developed for cosmological problems.

Using the pyMultinest package, we implemented the required log-prior function which transforms the unit hypercube to physical parameter space and the log-likelihood function used to compare the model to the data. The full code is available at https://github.com/nenasedk/petitRetrieval, and is based of the emission spectrum retrieval described in (P. Mollière et al., 2019). Retrievals were typically performed using 500 or 1000 live points, with the convergence criteria

$$\Delta \ln \mathcal{Z} = \ln Z_i - Z_{i+1} \tag{11}$$

set to 0.3 for parameter estimation and 0.8 for model comparison, as suggested in the pyMultinest documentation.

- Prior choice 4.2.4
- **Bayesian Model Selection**
- **TARGETS** 4.3

#### Atmospheric Parameters 4.3.1

Nikku Madhusudhan, 2012Moses2012Garland et al., 2019 Bowler, 2016 Fegley et al., 1994 Tokunaga, 1983

- 4.3.2 petitRadTrans
- 4.4 RESULTS
- 4.4.1 Posterior Distributions

## 5 conclusions



## A.1 PACKAGE REQUIREMENTS

numpy=1.4.0
scipy=1.5

## **WORKS CITED**

- Ackerman, Andrew S. and Mark S. Marley. "Precipitating condensation clouds in substellar atmospheres". *Astrophysical Journal* 596. ISSN: 15384357. DOI: 10.1088/0004-637X/765/1/75 (2001): 872–885. Print.
- Aoyama, Yuhiko and Masahiro Ikoma. "Constraining Planetary Gas Accretion Rate from H α Linewidth and Intensity: Case of PDS 70 b and c". arXiv eprint. arXiv: arXiv: 1909 . 08175v2 (2019). arXiv: arXiv: 1909 . 08175v2. arXiv: arXiv: 1909 . 08175v2.
- Argyriou, Ioannis, Ruymán Azzollini, and Bart Vandenbussche. "Spectrum extraction from detector plane images for the medium-resolution spectrometer of the mid-Infrared Instrument on-board the James Webb Space Telescope." SPIE. 2018. 124. Print.
- Argyriou, Ioannis, Bart Vandenbussche, and Martyn Wells. "Fringing solution for the mid-infrared instrument on-board the James Webb Space Telescope". SPIE. 2018. 127. Print.
- Argyriou, Ioannis, et al. "Nature of point source fringes in mid-infrared spectra acquired with the James Webb Space Telescope". *Astronomy & Astrophysics* (): 1–13. Print.
- Barman, Travis S., Quinn M. Konopacky, Bruce Macintosh, and Christian Marois. "Simultaneous detection of water, methane, and carbon monoxide in the atmosphere of Exoplanet hr 8799 b". *Astrophysical Journal* 804.1. ISSN: 15384357. DOI: 10.1088/0004-637X/804/1/61. arXiv: 1503.03539 (2015): 1–10. arXiv: 1503.03539. arXiv: 1503.03539. Web. <a href="http://dx.doi.org/10.1088/0004-637X/804/1/61">http://dx.doi.org/10.1088/0004-637X/804/1/61</a>.
- Batalha, Natasha E., et al. "Strategies for Constraining the Atmospheres of Temperate Terrestrial Planets with JWST". *The Astrophysical Journal* 856.2. ISSN: 2041-8213. DOI: 10.3847/2041-8213/aab896. arXiv: 1803.07983 (2018): L34. arXiv: 1803.07983. arXiv: 1803.07983. Web. <a href="http://dx.doi.org/10.3847/2041-8213/aab896">http://dx.doi.org/10.3847/2041-8213/aab896</a>>.
- Baudino, Jean-loup, et al. "Toward the Analysis of JWST Exoplanet Spectra : Identifying Troublesome Model Parameters". *The Astrophysical Journal* 850.2. ISSN: 1538-4357. DOI: 10.3847/1538-4357/aa95be (2017): 150. Web. <a href="http://dx.doi.org/10.3847/1538-4357/aa95be">http://dx.doi.org/10.3847/1538-4357/aa95be</a>.
- Beamín, J. C., et al. "Temperature constraints on the coldest brown dwarf known: WISE 0855-0714". *Astronomy and Astrophysics* 570. ISSN: 14320746. DOI: 10.1051/0004-6361/201424505 (2014): 1–4. Print.
- Behmard, Aida, Erik A. Petigura, and Andrew W. Howard. "Data-driven Spectroscopy of Cool Stars at High Spectral Resolution". *The Astrophysical Journal* 876.1. DOI: 10.3847/1538-4357/ab14e0. arXiv: arXiv: 1904.00094v1 (2019): 68. arXiv: arXiv:1904.00094v1. arXiv: arXiv:1904.00094v1.
- Beichman, Charles A., Pierre-olivier Lagage, and Marie Ygouf. "1188 Spectroscopy of Young, Widely Separated Exoplanets". 4. Print.
- Beichman, Charles A., et al. "1194 Characterization of the HR 8799 planetary system and planet search". Print.

- Beichman, Charles A and Thomas P Greene. "Observing Exoplanets with the James Webb Space Telescope". Handbook of Exoplanets 2009. DOI: 10. 1007/978-3-319-55333-7\_85 (2018): 1283-1308. Print.
- Benneke, Bjoern and Sara Seager. "Atmospheric retrieval for super-earths: Uniquely constraining the atmospheric composition with transmission spectroscopy". Astrophysical Journal 753.2. ISSN: 15384357. DOI: 10.1088/0004-637X/753/2/100. arXiv: 1203.4018 (2012). arXiv: 1203.4018. arXiv: 1203. 4018.
- Benneke, Björn. "Bayesian Atmospheric Retrieval for Exoplanets". Diss. Massachusetts Institute of Technology, 2013. Print.
- Biller, Beth. "The time domain for brown dwarfs and directly imaged giant exoplanets: the power of variability monitoring". Astronomical Review 13.1. ISSN: 2167-2857. DOI: 10.1080/21672857.2017.1303105 (2017): 1-27. Web. <http://dx.doi.org/10.1080/21672857.2017.1303105>.
- Biller, Beth A. and Mickaël Bonnefoy. "Exoplanet Atmosphere Measurements from Direct Imaging". Handbook of Exoplanets. DOI: 10.1007/978-3-319-55333-7\_101. arXiv: arXiv: 1807.05136v1 (2018): 2107–2135. arXiv: arXiv: 1807.05136v1. arXiv: arXiv: 1807.05136v1.
- Blanco-Cuaresma, Sergi. "Modern stellar spectroscopy caveats". Monthly Notices of the Royal Astronomical Society 486.2. arXiv: arXiv: 1902.09558v2 (2019): 2075–2101. arXiv: arXiv: 1902.09558v2. arXiv: arXiv: 1902.09558v2.
- Boccaletti, A., et al. "The Mid-Infrared Instrument for the James Webb Space Telescope, V: Predicted Performance of the MIRI Coronagraphs". Publications of the Astronomical Society of the Pacific 127.953. ISSN: 00046280. DOI: 10.1086/682256. arXiv: 1508.02352 (2015): 633-645. arXiv: 1508.02352. arXiv: 1508.02352.
- Bodis, Lorant. "Quantification of spectral similarity towards automatic spectra verification". Diss. ETH Zurich, 2007. Web. <a href="https://doi.org/10">https://doi.org/10</a>. 3929/ethz-a-005479205>.
- Bouchet, Patrice, et al. "The Mid-Infrared Instrument for the James Webb Space Telescope, III: MIRIM, The MIRI Imager". Publications of the Astronomical Society of the Pacific 127.953. ISSN: 00046280, 15383873 (2015): 612-622. Web. <a href="http://www.jstor.org/stable/10.1086/682254">http://www.jstor.org/stable/10.1086/682254</a>.
- Bowler, Brendan P. "Imaging Extrasolar Giant Planets". Publications of the Astronomical Society of the Pacific 128.968. ISSN: 1538-3873. DOI: 10.1088/ 1538-3873/128/968/102001 (2016): 1-38. Web. <a href="http://dx.doi.org/10">http://dx.doi.org/10</a>. 1088/1538-3873/128/968/102001>.
- Bozza, Valerio, Luigi Mancini, and Alessandro Sozzetti. Astrophysics of Exoplanetary Atmospheres. Print.
- Buchner, J., et al. "X-ray spectral modelling of the AGN obscuring region in the CDFS: Bayesian model selection and catalogue". Astronomy and Astrophysics 564. ISSN: 14320746. DOI: 10.1051/0004-6361/201322971. arXiv: 1402.0004 (2014): 1–25. arXiv: 1402.0004. arXiv: 1402.0004.
- Buenzli, Esther, et al. "Cloud Structure of the Nearest Brown Dwarfs II: High Amplitude Variability for Luhman 16 A and B In and Out of the 0.99\$\$m FeH Feature". Astrophysical Journal 812.2. ISSN: 15384357. DOI: 10.1088/ 0004 - 637X / 812 / 2 / 163. arXiv: 1509 . 06148 (2015). arXiv: 1509 . 06148. arXiv: 1509.06148.

- Buenzli, Esther, et al. "Cloud structure of the nearest brown dwarfs: Spectroscopic variability of Luhman 16AB from the Hubble space telescope". Astrophysical Journal 798.2. ISSN: 15384357. DOI: 10.1088/0004-637X/798/ 2/127. arXiv: 1411.0003 (2015). arXiv: 1411.0003. arXiv: 1411.0003.
- Burrows, Adam, David Sudarsky, and Jonathan I. Lunine. "Beyond the T Dwarfs: Theoretical Spectra, Colors, and Detectability of the Coolest Brown Dwarfs". The Astrophysical Journal 596. DOI: 10.1086/377709. arXiv: arXiv: 1306.2144v2 (2003): 587-596. arXiv: arXiv: 1306.2144v2. arXiv: arXiv: 1306.2144v2. Web. <a href="http://dx.doi.org/10.3847/0004-6256/152/6/">http://dx.doi.org/10.3847/0004-6256/152/6/</a> 217>.
- Bushouse, Howard, Michael Droettboom, and Perry Greenfield. "The James Webb Space Telescope Data Calibration Pipeline". 14th Python in Science Conf. 2015. 289. arXiv: 0606175 [astro-ph].
- Chauvin, G., et al. "A giant planet candidate near a young brown dwarf Direct VLT/NACO observations using IR wavefront sensing". Astronomy and Astrophysics 425.2. ISSN: 00046361. DOI: 10.1051/0004-6361:200400056 (2004): 29-32. Print.
- Chauvin, G., et al. "Orbital characterization of the  $\beta$  Pictoris b giant planet". Astronomy and Astrophysics 542. ISSN: 00046361. DOI: 10.1051/0004-6361/ 201118346. arXiv: 1202.2655 (2012): 1-9. arXiv: 1202.2655. arXiv: 1202. 2655.
- Chen, Howard, Eric T. Wolf, Zhuchang Zhan, and Daniel E. Horton. "Habitability and Spectroscopic Observability of Warm M-dwarf Exoplanets Evaluated with a 3D Chemistry-Climate Model". arXiv: 1907.10048 (2019). arXiv: 1907.10048. arXiv: 1907.10048. Web. <a href="http://arxiv.org/abs/">http://arxiv.org/abs/</a> 1907.10048>.
- Chilcote, Jeffrey, et al. " 1–2.4  $\mu$  m Near-IR Spectrum of the Giant Planet  $\beta$  Pictoris b Obtained with the Gemini Planet Imager ". The Astronomical Journal 153.4. ISSN: 0004-6256. DOI: 10.3847/1538-3881/aa63e9. arXiv: 1703.00011 (2017): 182. arXiv: 1703.00011. arXiv: 1703.00011. Web. <a href="http://dx.doi.">http://dx.doi.</a> org/10.3847/1538-3881/aa63e9>.
- Chilcote, Jeffrey, et al. "The first H-band spectrum of the giant planet  $\beta$ Pictoris b". Astrophysical Journal Letters 798.1. ISSN: 20418213. DOI: 10.1088/ 2041-8205/798/1/L3 (2015): 1-5. Print.
- Christiaens, Valentin, et al. "Evidence for a Circumplanetary Disk around Protoplanet PDS 70 b". The Astrophysical Journal 877.2. ISSN: 2041-8213. DOI: 10.3847/2041-8213/ab212b. arXiv: 1905.06370 (2019): L33. arXiv: 1905. 06370. arXiv: 1905.06370. Web. <a href="http://dx.doi.org/10.3847/2041-">http://dx.doi.org/10.3847/2041-</a> 8213/ab212b>.
- Consortium, Miri European. "MIRISim Documentation" (2018). Print.
- Cooper, Curtis S, David Sudarsky, John A Milsom, and Jonathan I Lunine. "Modeling the Formation of Clouds in Brown Dwarf Atmospheres". The Astrophysical Journal 156.2. DOI: 10.1086/367763. arXiv: 0205192v3 [arXiv:astro-ph] (2003): 1320-1337. arXiv: 0205192v3 [arXiv:astro-ph]. arXiv: 0205192v3 [arXiv:astro-ph].
- Cossou, Christophe. "MIRISim Spreadsheet and Quick examples" (2018): 1-12. Print.

- Danielski, Camilla, et al. "Atmospheric Characterization of Directly Imaged Exoplanets with JWST /MIRI ". The Astronomical Journal 156.6. ISSN: 1538-3881. DOI: 10.3847/1538-3881/aae651. arXiv: 1810.00894 (2018): 276. arXiv: 1810.00894. arXiv: 1810.00894.
- De Rosa, Robert J., et al. "Spectroscopic characterization of HD 95086 b with the Gemini Planet Imager". *The Astrophysical Journal* 824.2. ISSN: 1538-4357. DOI: 10.3847/0004-637x/824/2/121. arXiv: 1604.01411 (2016): 121. arXiv: 1604.01411. arXiv: 1604.01411. Web. <a href="http://dx.doi.org/10.3847/">http://dx.doi.org/10.3847/</a> 0004-637X/824/2/121>.
- Faherty, Jacqueline K., et al. "Signatures of cloud, temperature, and gravity from spectra of the closest brown dwarfs". Astrophysical Journal 790.2. ISSN: 15384357. DOI: 10.1088/0004-637X/790/2/90 (2014). Print.
- Faherty, Jacqueline K, C G Tinney, Andrew Skemer, and Andrew J Monson. "Indications of water clouds in the coldest known brown dwarf". The Astrophysical Journal Letters 793.1. arXiv: arXiv: 1408.4671v2 (2018). arXiv: arXiv:1408.4671v2. arXiv: arXiv:1408.4671v2.
- Fegley, Bruce and Katharina Lodders. "Chemical Models of the Deep Atmospheres of Jupiter and Saturn". Icarus 110 (1994): 117-154. Print.
- Feng, Y. Katherina, et al. "Characterizing Earth Analogs in Reflected Light: Atmospheric Retrieval Studies for Future Space Telescopes". The Astronomical Journal 155.5. ISSN: 1538-3881. DOI: 10.3847/1538-3881/aab95c (2018): 200. Web. <http://dx.doi.org/10.3847/1538-3881/aab95c>.
- Feroz, F. and M. P. Hobson. "Multimodal nested sampling: An efficient and robust alternative to Markov Chain Monte Carlo methods for astronomical data analyses". Monthly Notices of the Royal Astronomical Society 384.2. ISSN: 00358711. DOI: 10.1111/j.1365-2966.2007.12353.x. arXiv: 0704.3704 (2008): 449-463. arXiv: 0704.3704. arXiv: 0704.3704.
- Feroz, F., M. P. Hobson, and M. Bridges. "MultiNest: An efficient and robust Bayesian inference tool for cosmology and particle physics". Monthly Notices of the Royal Astronomical Society 398.4. ISSN: 00358711. DOI: 10.1111/ j.1365-2966.2009.14548.x. arXiv: 0809.3437 (2009): 1601-1614. arXiv: 0809.3437. arXiv: 0809.3437.
- Feroz, Farhan, Michael P. Hobson, Ewan Cameron, and Anthony N. Pettitt. "Importance Nested Sampling and the MultiNest Algorithm". The Open Journal of Astrophysics 2.1. DOI: 10.21105/astro.1306.2144. arXiv: 1306. 2144 (2019): 1-17. arXiv: 1306.2144. arXiv: 1306.2144.
- Fisher, Chloe, et al. "Interpreting High-Resolution Spectroscopy of Exoplanets Using Cross-Correlations and Supervised Machine Learning". arXiv: 1910 . 11627 (2019): 1-15. arXiv: 1910 . 11627. arXiv: 1910 . 11627. Web. <http://arxiv.org/abs/1910.11627>.
- Foreman-Mackey, Daniel, David W. Hogg, Dustin Lang, and Jonathan Goodman. "emcee: The MCMC Hammer". Publications of the Astronomical Society of the Pacific 125.925. ISSN: 00046280. DOI: 10.1086/670067. arXiv: 1202.3665 (2013): 306-312. arXiv: 1202.3665. arXiv: 1202.3665.
- Gandhi, Siddharth and Nikku Madhusudhan. "Retrieval of exoplanet emission spectra with HyDRA". Monthly Notices of the Royal Astronomical Soci-

- ety 474.1. ISSN: 13652966. DOI: 10.1093/mnras/stx2748. arXiv: 1710.06433 (2018): 271–278. arXiv: 1710.06433. arXiv: 1710.06433.
- Garcia, E. Victor, et al. "Individual, Model-independent Masses of the Closest Known Brown Dwarf Binary to the Sun". The Astrophysical Journal 846.2. ISSN: 1538-4357. DOI: 10.3847/1538-4357/aa844f. arXiv: 1708.02714 (2017): 97. arXiv: 1708.02714. arXiv: 1708.02714.
- Garland, R. and P. G. J. Irwin. "Effectively Calculating Gaseous Absorption in Radiative Transfer Models of Exoplanetary and Brown Dwarf Atmospheres". March. arXiv: 1903.03997 (2019). arXiv: 1903.03997. arXiv: 1903.03997. Web. <a href="http://arxiv.org/abs/1903.03997">http://arxiv.org/abs/1903.03997</a>.
- Gauza, Bartosz, et al. "Discovery of a young planetary mass companion to the nearby M dwarf VHS J125601.92-125723.9". Astrophysical Journal 804.2. ISSN: 15384357. DOI: 10.1088/0004-637X/804/2/96. arXiv: 1505.00806 (2015). arXiv: 1505.00806. arXiv: 1505.00806.
- —. "Discovery of a young planetary mass companion to the nearby M dwarf VHS J125601.92-125723.9". Astrophysical Journal 804.2. ISSN: 15384357. DOI: 10.1088/0004-637X/804/2/96. arXiv: 1505.00806 (2015): 1-18. arXiv: 1505.00806. arXiv: 1505.00806. Web. <a href="http://dx.doi.org/10.1088/">http://dx.doi.org/10.1088/</a> 0004-637X/804/2/96>.
- Glasse, Alistair, et al. "The Mid-Infrared Instrument for the James Webb Space Telescope, IX: Predicted Sensitivity". Publications of the Astronomical Society of the Pacific 127.953. ISSN: 00046280. DOI: 10.1086/682259. arXiv: 1508.02427 (2015): 686-695. arXiv: 1508.02427. arXiv: 1508.02427.
- Goody, Richard, Robert West, Luke Chen, and David Crisp. "The correlatedk method for radiation calculations in nonhomogeneous atmospheres". Journal of Quantitative Spectroscopy and Radiative Transfer 42.6. ISSN: 00224073. DOI: 10.1016/0022-4073(89)90044-7 (1989): 539-550. Print.
- Gordon, I. E., et al. "The HITRAN2016 molecular spectroscopic database". Journal of Quantitative Spectroscopy and Radiative Transfer 203. ISSN: 00224073. DOI: 10.1016/j.jqsrt.2017.06.038 (2017): 3-69. Print.
- Goyal, Jayesh M., et al. "Fully scalable forward model grid of exoplanet transmission spectra". Monthly Notices of the Royal Astronomical Society 482.4. ISSN: 13652966. DOI: 10.1093/mnras/sty3001. arXiv: 1810.12971 (2019): 4503–4513. arXiv: 1810.12971. arXiv: 1810.12971.
- GRAVITY Collaboration, et al. "Peering into the formation history of beta Pictoris b with VLTI/GRAVITY long baseline interferometry". Astronomy & Astrophysics 633. DOI: 10.1051/0004-6361/201936898. arXiv: 1912.04651 (2020): 1-21. arXiv: 1912.04651. arXiv: 1912.04651. Web. <a href="http://arxiv.">http://arxiv.</a> org/abs/1912.04651>.
- Greenbaum, Alexandra Z., et al. "GPI Spectra of HR 8799 c, d, and e from 1.5 to 2.4 µm with KLIP Forward Modeling". The Astronomical Journal 155.6. ISSN: 0004-6256. DOI: 10.3847/1538-3881/aabcb8. arXiv: 1804.07774 (2018): 226. arXiv: 1804.07774. arXiv: 1804.07774.
- Guillot, T. "On the radiative equilibrium of irradiated planetary atmospheres". Astronomy and Astrophysics 520.18. ISSN: 00046361. DOI: 10.1051/0004-6361/200913396. arXiv: 1006.4702 (2010): 1–13. arXiv: 1006.4702. arXiv: 1006.4702.
- Haffert, S. Y., et al. "Two accreting protoplanets around the young star PDS 70". Nature Astronomy 3.8. ISSN: 23973366. DOI: 10.1038/s41550-019-0780-

- 5 (2019): 749-754. Web. <a href="http://dx.doi.org/10.1038/s41550-019-0780-">http://dx.doi.org/10.1038/s41550-019-0780-</a> **5**>.
- Helling, Christiane and Sarah Casewell. "Atmospheres of Brown Dwarfs". The Astronomy and Astrophysics Review 22. arXiv: arXiv:1410.6029v2 (2014): 1-53. arXiv: arXiv:1410.6029v2. arXiv: arXiv:1410.6029v2.
- Hoeijmakers, H. J., et al. "Medium-resolution integral-field spectroscopy for high-contrast exoplanet imaging: Molecule maps of the  $\beta$  Pictoris system with SINFONI". Astronomy and Astrophysics 617. ISSN: 14320746. DOI: 10. 1051/0004-6361/201832902. arXiv: 1802.09721 (2018): 1–11. arXiv: 1802. 09721. arXiv: 1802.09721.
- Irwin, P. G.J., et al. "The NEMESIS planetary atmosphere radiative transfer and retrieval tool". Journal of Quantitative Spectroscopy and Radiative Transfer 109.6. ISSN: 00224073. DOI: 10.1016/j.jqsrt.2007.11.006 (2008): 1136-1150. Print.
- Keppler, M., et al. "Discovery of a planetary-mass companion within the gap of the transition disk around PDS 70". Astronomy and Astrophysics 617. ISSN: 14320746. DOI: 10.1051/0004-6361/201832957. arXiv: 1806.11568 (2018): 1–21. arXiv: 1806.11568. arXiv: 1806.11568.
- Konopacky, Quinn M., Travis S. Barman, Bruce A. Macintosh, and Christian Marois. "Detection of carbon monoxide and water absorption lines in an exoplanet atmosphere". Science 339.6126. ISSN: 10959203. DOI: 10.1126/ science.1232003 (2013): 1398-1401. Print.
- Kreidberg, Laura. "Exoplanet Atmosphere Measurements from Transmission Spectroscopy and Other Planet Star Combined Light Observations". *Handbook of Exoplanets.* DOI: 10.1007/978-3-319-55333-7\_100. arXiv: arXiv:1709.05941v2 (2018): 2083-2105. arXiv: arXiv: 1709.05941v2. arXiv: arXiv:1709.05941v2.
- Labiano-Ortega, Alvaro, et al. "The MIRI Medium Resolution Spectrometer calibration pipeline". exposure 1. DOI: 10.1117/12.2232554 (2016): 117.
- Lacis, A. A. and V. Oinas. "A description of the correlated k distribution method for modeling nongray gaseous absorption, thermal emission, and multiple scattering in vertically inhomogeneous atmospheres". Journal of Geophysical Research 96.D5. ISSN: 01480227. DOI: 10.1029/90JD01945 (1991): 9027–9063. Print.
- Lacour, S., et al. "First direct detection of an exoplanet by optical interferometry". Astronomy & Astrophysics 623. ISSN: 0004-6361. DOI: 10.1051/0004-6361/201935253 (2019): L11. Print.
- Lafrenière, David, Christian Marois, René Doyon, and Travis Barman. "HST/nicmos detection of HR 8799 B in 1998". Astrophysical Journal 694.2. ISSN: 15384357. DOI: 10.1088/0004-637X/694/2/L148 (2009): 148-152. Print.
- Lagage, Pierre-olivier and David Barrado. "1278 MIRI Spectroscopic Observations of Brown Dwarfs". Print.
- Lagage, Pierre-olivier, J. Bouwman, and Fred Lahuis. "1275 Spectroscopic characterization of PSO J318". Print.
- Lagage, Pierre-olivier and Thomas L Roellig. "1276 Spectroscopic Observations of WD 0806-661B". Print.

- Lagage, P, et al. "The Mid-Infrared Instrument for the James Webb Space Telescope, IV: The Low Resolution Spectrometer". Publications of the Astronomical Society of the Pacific 127.953. DOI: 10.1086/682255. arXiv: 1512: 03000 (2015): 1-23. arXiv: 1512:03000. arXiv: 1512:03000.
- Lagrange, A. M., et al. "A probable giant planet imaged in the  $\beta$  Pictoris disk\* VLT/NaCo deep L'-band imaging". Astronomy and Astrophysics 493.2. ISSN: 00046361. DOI: 10.1051/0004-6361:200811325 (2009): 21-25. Print.
- Lagrange, A. M., et al. "Evidence for an additional planet in the  $\beta$  Pictoris system". Nature Astronomy 3.12. ISSN: 23973366. DOI: 10.1038/s41550-019-0857-1 (2019): 1135-1142. Web. <a href="http://dx.doi.org/10.1038/s41550">http://dx.doi.org/10.1038/s41550</a> 019 - 0857 - 1 >.
- Lahuis, F and A Boogert. "How to Get Rid of Fringes in SIRTF/IRS Data". SFChem 2002: Chemistry as a Diagnostic of Star Formation. Waterloo, 2003. 335. Print.
- Lavie, Baptiste, et al. "HELIOS-RETRIEVAL: An Open-source, Nested Sampling Atmospheric Retrieval Code; Application to the HR 8799 Exoplanets and Inferred Constraints for Planet Formation ". The Astronomical Journal 154.3. ISSN: 0004-6256. DOI: 10.3847/1538-3881/aa7ed8. arXiv: 1610.03216 (2017): 91. arXiv: 1610.03216. arXiv: 1610.03216.
- Lee, J. M., L. N. Fletcher, and P. G.J. Irwin. "Optimal estimation retrievals of the atmospheric structure and composition of HD189733b from secondary eclipse spectroscopy". Monthly Notices of the Royal Astronomical Society 420.1. ISSN: 00358711. DOI: 10.1111/j.1365-2966.2011.20013.x. arXiv: 1110.2934 (2012): 170–182. arXiv: 1110.2934. arXiv: 1110.2934.
- Li, Jianfeng, D. Brynn Hibbert, Stephen Fuller, and Gary Vaughn. "A comparative study of point-to-point algorithms for matching spectra". Chemometrics and Intelligent Laboratory Systems 82.1-2 SPEC. ISS. ISSN: 01697439. DOI: 10.1016/j.chemolab.2005.05.015 (2006): 50-58. Print.
- Line, Michael R. and Vivien Parmentier. "the Influence of Nonuniform Cloud Cover on Transit Transmission Spectra". The Astrophysical Journal 820.1. ISSN: 1538-4357. DOI: 10.3847/0004-637x/820/1/78. arXiv: 1511.09443 (2016): 78. arXiv: 1511.09443. arXiv: 1511.09443. Web. <a href="http://dx.doi.">http://dx.doi.</a> org/10.3847/0004-637X/820/1/78>.
- Line, Michael R., et al. "A systematic retrieval analysis of secondary eclipse spectra. I. A comparison of atmospheric retrieval techniques". Astrophysical Journal 775.2. ISSN: 15384357. DOI: 10.1088/0004-637X/775/2/137. arXiv: 1304.5561 (2013). arXiv: 1304.5561. arXiv: 1304.5561.
- Line, Michael R., et al. "Uniform Atmospheric Retrieval Analysis of Ultracool Dwarfs. I. Characterizing Benchmarks, Gl 570D and HD 3651B". Astrophysical Journal 807.2. ISSN: 15384357. DOI: 10.1088/0004-637X/807/2/183. arXiv: 1504.06670 (2015): 183. arXiv: 1504.06670. arXiv: 1504.06670. Web. <http://dx.doi.org/10.1088/0004-637X/807/2/183>.
- Line, Michael R., et al. "Uniform Atmospheric Retrieval Analysis of Ultracool Dwarfs. II. Properties of 11 T dwarfs". The Astrophysical Journal 848.2. ISSN: 1538-4357. DOI: 10.3847/1538-4357/aa7ff0.arXiv: 1612.02809 (2017): 83. arXiv: 1612.02809. arXiv: 1612.02809.

- Luhman, K L. "Discovery of a ~250K Brown Dwarf at 2pc from the Sun". The Astrophysical Journal Letters 18. DOI: 10.1088/2041-8205/786/2/L18 (2014): 2-7. Print.
- Lupu, Roxana E., et al. "Developing Atmospheric Retrieval Methods for Direct Imaging Spectroscopy of Gas Giants in Reflected Light. I. Methane Abundances and Basic Cloud Properties". The Astronomical Journal 152.6. ISSN: 0004-6256. DOI: 10.3847/0004-6256/152/6/217. arXiv: 1604.05370 (2016): 217. arXiv: 1604.05370. arXiv: 1604.05370. Web. <a href="http://dx.doi.">http://dx.doi.</a> org/10.3847/0004-6256/152/6/217>.
- MacDonald, Ryan J. and Nikku Madhusudhan. "HD 209458b in new light: evidence of nitrogen chemistry, patchy clouds and sub-solar water". Monthly Notices of the Royal Astronomical Society 469.2. ISSN: 0035-8711. DOI: 10. 1093/mnras/stx804. arXiv: 1701.01113 (2017): 1979—1996. arXiv: 1701. 01113. arXiv: 1701.01113.
- Macintosh, B., et al. "Discovery and spectroscopy of the young jovian planet 51 Eri b with the Gemini Planet Imager". Science 350.6256. ISSN: 10959203. DOI: 10.1126/science.aac5891 (2015): 64-67. Print.
- MacKay, David J.C. Information Theory, Inference, and Learning Algorithms. Fourth Edi. Cambridge University Press, 2003. Print.
- Madhusudhan, N and S Seager. "A Temperature and Abundance Retrieval Method for Exoplanet Atmospheres". The Astrophysical Journal 707.1. DOI: 10.1088/0004-637X/707/1/24. arXiv: arXiv: 0910.1347v2 (2009): 24-39. arXiv: arXiv:0910.1347v2. arXiv: arXiv:0910.1347v2.
- Madhusudhan, Nikku. "Atmospheric Retrieval of Exoplanets". Handbook of Exoplanets. DOI: 10.1007/978-3-319-55333-7\_104. arXiv: 1808.04824 (2018): 2153–2182. arXiv: 1808.04824. arXiv: 1808.04824.
- —. "C/O ratio as a dimension for characterizing exoplanetary atmospheres". Astrophysical Journal 758.1. ISSN: 15384357. DOI: 10.1088/0004-637X/758/ 1/36. arXiv: 1209.2412 (2012). arXiv: 1209.2412. arXiv: 1209.2412.
- Madhusudhan, Nikku, Marcelino Agúndez, Julianne I. Moses, and Yongyun Hu. "Exoplanetary Atmospheres—Chemistry, Formation Conditions, and Habitability". Space Science Reviews 205.1-4. ISSN: 15729672. DOI: 10.1007/ s11214 - 016 - 0254 - 3. arXiv: arXiv: 1604 . 06092v1 (2016): 285-348. arXiv: arXiv: 1604.06092v1. arXiv: arXiv: 1604.06092v1.
- Madhusudhan, Nikku, Heather Knutson, Jonathan J Fortney, and Travis Barman. "Exoplanetary Atmospheres". 2014. arXiv: arXiv: 1402.1169v1. arXiv: arXiv:1402.1169v1.
- Madhusudhan, Nikku, et al. "High C / O Ratio and Weak Thermal Inversion in the Very Hot Atmosphere of Exoplanet WASP-12b". Nature 469.7328. DOI: 10.1038/nature09602. arXiv: arXiv: 1012.1603 (2011): 64-67. arXiv: arXiv:1012.1603. arXiv: arXiv:1012.1603.
- Malik, Matej, et al. "Helios: an Open-Source, Gpu-Accelerated Radiative Transfer Code for Self-Consistent Exoplanetary Atmospheres". The Astronomical Journal 153.2. ISSN: 0004-6256. DOI: 10.3847/1538-3881/153/2/56. arXiv: 1606.05474 (2017): 56. arXiv: 1606.05474. arXiv: 1606.05474. Web. <http://dx.doi.org/10.3847/1538-3881/153/2/56>.
- Malik, Matej, et al. "Self-luminous and Irradiated Exoplanetary Atmospheres Explored with HELIOS ". The Astronomical Journal 157.5. ISSN: 0004-6256.

```
DOI: 10.3847/1538-3881/ab1084. arXiv: 1903.06794 (2019): 170. arXiv:
1903.06794. arXiv: 1903.06794. Web. <a href="http://dx.doi.org/10.3847/">http://dx.doi.org/10.3847/</a>
1538-3881/ab1084>.
```

- Mamajek, Eric E. and Cameron P.M. Bell. "On the age of the  $\beta$  pictoris moving group". Monthly Notices of the Royal Astronomical Society 445.3. ISSN: 13652966. DOI: 10.1093/mnras/stu1894 (2014): 2169–2180. Print.
- Manjavacas, Elena. "Physical characterization of brown dwarfs". Diss. Ruperto-Carola-University of Heidelberg, 2014. Print.
- Marley, M S and T D Robinson. "On the Cool Side: Modeling the Atmospheres of Brown Dwarfs and Giant Planets arXiv: 1410.6512v1 [astroph . EP ] 23 Oct 2014". Annual Review of Astronomy and Astrophysics 53. DOI: 10.1146/annurev-astro-082214-122522. arXiv: arXiv:1410.6512v1 (2015): 279-323. arXiv: arXiv: 1410.6512v1. arXiv: arXiv: 1410.6512v1.
- Marois, Christian, Bruce Macintosh, Daniel Nadeau, and David Lafrenie. "Angular Differential Imaging: A Powerful High-Contrast Imaging Technique". The Astrophysical Journal 641 (2006): 556-564. Print.
- Marois, Christian, et al. "Direct imaging of multiple planets orbiting the star HR 8799". Science 322.5906. ISSN: 00368075. DOI: 10.1126/science. 1166585. arXiv: 0811 . 2606 (2008): 1348-1352. arXiv: 0811 . 2606. arXiv: 0811.2606.
- Mayor, M and D Queloz. "A Jupiter-mass companion to a solar-type star". Nature 378 (1995): 667-668. Print.
- Mesa, D., et al. "VLT/SPHERE exploration of the young multiplanetary system PDS70". Astronomy and Astrophysics 632. ISSN: 14320746. DOI: 10.1051/ 0004-6361/201936764. arXiv: 1910.11169 (2019): 1-12. arXiv: 1910.11169. arXiv: 1910.11169.
- Miles, Brittany E., et al. "Methane in Analogs of Young Directly Imaged Exoplanets". The Astrophysical Journal 869.1. ISSN: 1538-4357. DOI: 10.3847/ 1538-4357/aae6cd. arXiv: 1810.04684 (2018): 18. arXiv: 1810.04684. arXiv: 1810.04684. Web. <a href="http://dx.doi.org/10.3847/1538-4357/aae6cd">http://dx.doi.org/10.3847/1538-4357/aae6cd</a>.
- Molliere, P. and I. A.G. Snellen. "Detecting isotopologues in exoplanet atmospheres using ground-based high-dispersion spectroscopy". Astronomy and Astrophysics 622. ISSN: 14320746. DOI: 10.1051/0004-6361/201834169. arXiv: 1809.01156 (). arXiv: 1809.01156. arXiv: 1809.01156.
- Mollière, P., et al. "Observing transiting planets with JWST: Prime targets and their synthetic spectral observations". Astronomy and Astrophysics 600. ISSN: 14320746. DOI: 10.1051/0004-6361/201629800. arXiv: 1611.08608 (2017): 1–23. arXiv: 1611.08608. arXiv: 1611.08608.
- Mollière, P., et al. "petitRADTRANS: a Python radiative transfer package for exoplanet characterization and retrieval". Astronomy & Astrophysics 627. ISSN: 0004-6361. DOI: 10.1051/0004-6361/201935470. arXiv: 1904.11504 (2019): 1–17. arXiv: 1904.11504. arXiv: 1904.11504. Web. <a href="http://arxiv.">http://arxiv.</a> org/abs/1904.11504%7B%5C%%7D0Ahttp://dx.doi.org/10.1051/0004-6361/201935470>.
- Mollière, P, et al. "Model Atmospheres of Irradiated Exoplanets: The Influence of Stellar Parameters, Metallicity and the C/O Ratio". The Astrophysical Journal 813.1. ISSN: 1538-4357. DOI: 10.1088/0004-637X/813/1/47 (2015): 47. Web. <a href="http://dx.doi.org/10.1088/0004-637X/813/1/47">http://dx.doi.org/10.1088/0004-637X/813/1/47</a>.

- Morley, Caroline V., et al. "An L Band Spectrum of the Coldest Brown Dwarf". The Astrophysical Journal 858.2. ISSN: 1538-4357. DOI: 10.3847/ 1538-4357/aabe8b. arXiv: 1804.07771 (2018): 97. arXiv: 1804.07771. arXiv: 1804.07771. Web. <a href="http://dx.doi.org/10.3847/1538-4357/aabe8b">http://dx.doi.org/10.3847/1538-4357/aabe8b</a>.
- Morley, Caroline V., et al. "Water clouds in y dwarfs and exoplanets". Astrophysical Journal 787.1. ISSN: 15384357. DOI: 10.1088/0004-637X/787/1/78. arXiv: 1404.0005 (2014). arXiv: 1404.0005. arXiv: 1404.0005.
- Moroz, V.I. "On the infrared spectra of Jupiter and Saturn (0.9-2.5um)". Soviet Astronomy 5.6 (1962). Print.
- Moses, J. I., N. Madhusudhan, C. Visscher, and R. S. Freedman. "Chemical consequences of the C/O ratio on hot jupiters: Examples from WASP-12b, CoRoT-2b, XO-1b, and HD 189733b". Astrophysical Journal 763.1. ISSN: 15384357. DOI: 10.1088/0004-637X/763/1/25. arXiv: 1211.2996 (2013). arXiv: 1211.2996. arXiv: 1211.2996.
- National Academies of Sciences Engineering and Medicine. Exoplanet science strategy. Washington, DC: The National Academies Press, 2018. 1–172. DOI: 10.17226/25187. Print.
- Oreshenko, Maria, et al. "Supervised Machine Learning for Inter-comparision of Model Grids of Brown Dwarfs: Application to GJ 570D and the Epsilon Indi B Binary System". The Astronomical Journal 159.1. DOI: 10.3847/1538-3881/ab5955. arXiv: arXiv: 1910.11795v1 (2020): 15. arXiv: arXiv: 1910. 11795v1. arXiv: arXiv: 1910.11795v1.
- Petermann, R. "Atmospheric characterization of terrestrial planets using highresolution spectroscopy with ELT / METIS A study of Proxima Cen b". Diss. ETH Zurich, 2019. Print.
- Quanz, Sascha P., et al. "First results from very large telescope NACO apodizing phase plate: 4  $\mu$ m images of the exoplanet  $\beta$  Pictoris b". Astrophysical Journal Letters 722.1 PART 2. ISSN: 20418213. DOI: 10.1088/2041-8205/722/ 1/L49 (2010): 49-53. Print.
- Ressler, M. E., et al. "The Mid-Infrared Instrument for the James Webb Space Telescope, VIII: The MIRI Focal Plane System". Publications of the Astronomical Society of the Pacific 127.953. ISSN: 00046280. DOI: 10.1086/682258 (2015): 675–685. Print.
- Rich, Evan A., et al. "Thermal Infrared Imaging and Atmospheric Modeling of VHS J125601.92-125723.9 b: Evidence for Moderately Thick Clouds and Equilibrium Carbon Chemistry in a Hierarchical Triple System." The Astrophysical Journal 830.2. ISSN: 1538-4357. DOI: 10.3847/0004-637x/830/2/114. arXiv: 1607.06007 (2016): 114. arXiv: 1607.06007. arXiv: 1607.06007. Web. <http://dx.doi.org/10.3847/0004-637X/830/2/114>.
- Rieke, G. H., et al. "The Mid-Infrared Instrument for the James Webb Space Telescope, I: Introduction ". Publications of the Astronomical Society of the Pacific 127.953. ISSN: 00046280. DOI: 10.1086/682252 (2015): 584-594. Print.
- —."The Mid-Infrared Instrument for the James Webb Space Telescope , I: Introduction". Publications of the Astronomical Society of the Pacific 127.953. ISSN: 00046280. DOI: 10.1086/682252 (2015): 584-594. Print.
- Rieke, G. H., et al. "The Mid-Infrared Instrument for the James Webb Space Telescope, VII: The MIRI Detectors". Publications of the Astronomical Society

- of the Pacific 127.953. ISSN: 00046280. DOI: 10.1086/682257 (2015): 665–674. Print.
- Robinson, Tyler D., Karl R. Stapelfeldt, and Mark S. Marley. "Characterizing rocky and gaseous exoplanets with 2m class space-based coronagraphs". *Publications of the Astronomical Society of the Pacific* 128.960. ISSN: 00046280. DOI: 10.1088/1538-3873/128/960/025003 (2016): 1–22. Web. <a href="http://dx.doi.org/10.1088/1538-3873/128/960/025003">http://dx.doi.org/10.1088/1538-3873/128/960/025003</a>.
- Rothman, L. S., et al. "HITEMP, the high-temperature molecular spectroscopic database". *Journal of Quantitative Spectroscopy and Radiative Transfer* 111.15. ISSN: 00224073. DOI: 10.1016/j.jqsrt.2010.05.001 (2010): 2139–2150. Web. <a href="http://dx.doi.org/10.1016/j.jqsrt.2010.05.001">http://dx.doi.org/10.1016/j.jqsrt.2010.05.001</a>>.
- Rothman, L. S., et al. "The HITRAN2012 molecular spectroscopic database". *Journal of Quantitative Spectroscopy and Radiative Transfer* 130. ISSN: 00224073. DOI: 10.1016/j.jqsrt.2013.07.002 (2013): 4–50. Print.
- Sahlmann, J. and P. F. Lazorenko. "Mass ratio of the 2 pc binary brown dwarf LUH 16 and limits on planetary companions from astrometry". *Monthly Notices of the Royal Astronomical Society: Letters* 453.1. ISSN: 17453933. DOI: 10.1093/mnrasl/slv113. arXiv: 1506.07994 (2015): L103–L107. arXiv: 1506.07994. arXiv: 1506.07994.
- Schlawin, Everett, et al. "Clear and Cloudy Exoplanet Forecasts for JWST: Maps, Retrieved Composition, and Constraints on Formation with MIRI and NIRCam". The Astronomical Journal 156.1. ISSN: 0004-6256. DOI: 10. 3847/1538-3881/aac774. arXiv: 1803.08173 (2018): 40. arXiv: 1803.08173. arXiv: 1803.08173.
- Schneider, Adam C., Michael C. Cushing, J. Davy Kirkpatrick, and Christopher R. Gelino. "the Collapse of the Wien Tail in the Coldest Brown Dwarf? Hubble Space Telescope Near-Infrared Photometry of Wise Jo85510.83–071442.5". The Astrophysical Journal 823.2. ISSN: 2041-8213. DOI: 10.3847/2041-8205/823/2/l35. arXiv: 1605.05618 (2016): L35. arXiv: 1605.05618. arXiv: 1605.05618. Web. <a href="http://dx.doi.org/10.3847/2041-8205/823/2/L35">http://dx.doi.org/10.3847/2041-8205/823/2/L35</a>.
- Simkin, Susan M. "Measurements of Velocity Dispersions and Doppler Shifts from Digitized Optical Spectra". *Astronomy & Astrophysics* 32 (1974): 129–136. Print.
- Skemer, Andrew J., et al. "First light LBT AO images of HR 8799 bcde at 1.6 and 3.3  $\mu$ m: New discrepancies between young planets and old brown dwarfs". *Astrophysical Journal* 753.1. ISSN: 15384357. DOI: 10.1088/0004-637X/753/1/14. arXiv: 1203.2615 (2012). arXiv: 1203.2615. arXiv: 1203.
- Skemer, Andrew J., et al. "The First Spectrum of the Coldest Brown Dwarf". *The Astrophysical Journal* 826.2. ISSN: 2041-8213. DOI: 10.3847/2041-8205/826/2/l17. arXiv: 1605.04902 (2016): L17. arXiv: 1605.04902. arXiv: 1605.04902. Web. <a href="http://dx.doi.org/10.3847/2041-8205/826/2/L17">http://dx.doi.org/10.3847/2041-8205/826/2/L17</a>>.
- Skemer, Andrew J., et al. "The LEECH Exoplanet Imaging Survey: Characterization of the Coldest Directly Imaged Exoplanet, GJ 504 b, and Evidence for Super-Stellar Metallicity". *The Astrophysical Journal* 817.2. ISSN: 1538-4357. DOI: 10.3847/0004-637x/817/2/166. arXiv: 1511.09183 (2016): 166.

- arXiv: 1511.09183. arXiv: 1511.09183. Web. <a href="http://dx.doi.org/10.">http://dx.doi.org/10.</a> 3847/0004-637X/817/2/166>.
- Skilling, John. "Nested Sampling". 395.November 2004, doi: 10.1063/1. 1835238 (2004): 395-405. Print.
- Snellen, I., et al. "Combining high-dispersion spectroscopy with high contrast imaging: Probing rocky planets around our nearest neighbors". Astronomy and Astrophysics 576.3. ISSN: 14320746. DOI: 10.1051/0004-6361/ 201425018. arXiv: 1503.01136 (2015). arXiv: 1503.01136. arXiv: 1503. 01136.
- Snellen, Ignas, et al. "The fast spin-rotation of a young extrasolar planet". *Nature* 509.7498. ISSN: 0028-0836, 1476-4687. DOI: 10.1038/nature13253. arXiv: 1404.7506 [astro-ph.EP] (2014): 63-65. arXiv: 1404.7506 [astro-ph.EP]. arXiv: 1404.7506 [astro-ph.EP]. Web. <a href="http://arxiv.org/abs/1404">http://arxiv.org/abs/1404</a>. 7506%7B%5C%%7D5Cnhttp://www.arxiv.org/pdf/1404.7506.pdf>.
- Soummer, Rémi, et al. "Orbital motion of HR 8799 b, c, d using hubble space telescope data from 1998: Constraints on inclination, eccentricity, and stability". Astrophysical Journal 741.1. ISSN: 15384357. DOI: 10.1088/ 0004 - 637X/741/1/55. arXiv: 1110 . 1382 (2011). arXiv: 1110 . 1382. arXiv: 1110.1382.
- Speagle, Joshua S. "dynest: A Dynamic Nested Smpling Package for Estimating Bayesian Posteriors and Evidences". Monthly Notices of the Royal Astronomical Society 4. ISSN: 0035-8711. DOI: 10.1093/mnras/staa278 (2020). Print.
- —. "A Conceptual Introduction to Markov Chain Monte Carlo Methods". arXiv: 1909 . 12313 (2019). arXiv: 1909 . 12313. arXiv: 1909 . 12313. Web. <http://arxiv.org/abs/1909.12313>.
- Stone, Jordan M., et al. "Adaptive Optics Imaging of Vhs 1256–1257: a Low Mass Companion To a Brown Dwarf Binary System". The Astrophysical Journal 818.1. ISSN: 2041-8213. DOI: 10.3847/2041-8205/818/1/112 (2016): L12. Web. <a href="http://dx.doi.org/10.3847/2041-8205/818/1/L12">http://dx.doi.org/10.3847/2041-8205/818/1/L12</a>.
- Tennyson, Jonathan and Sergei N. Yurchenko. "The ExoMol project: Software for computing large molecular line lists". International Journal of Quantum Chemistry 117.2. ISSN: 1097461X. DOI: 10.1002/qua.25190. arXiv: 1607. 01220 (2017): 92–103. arXiv: 1607.01220. arXiv: 1607.01220.
- Tennyson, Jonathan, et al. "The ExoMol database: Molecular line lists for exoplanet and other hot atmospheres". Journal of Molecular Spectroscopy 327. ISSN: 1096083X. DOI: 10.1016/j.jms.2016.05.002. arXiv: 1603.05890 (2016): 73-94. arXiv: 1603.05890. arXiv: 1603.05890. Web. <a href="http://dx.">http://dx.</a> doi.org/10.1016/j.jms.2016.05.002>.
- Tinney, C G, et al. "The Luminosities of the Coldest Brown Dwarfs". The Astrophysical Journal 39.Luhman. DOI: 10.1088/0004-637X/796/1/39 (2014): 1–13. Print.
- Tokunaga, Alan T. "High-Resolution Infrared Spectroscopy of Planetary Atmospheres". Publications of the Astronomical Society of the Pacific 95.October (1983): 691–699. Print.
- VanderPlas, Jacob T. "Understanding the Lomb-Scargle Periodogram". The Astrophysical Journal Supplement Series 236.1. ISSN: 0067-0049. DOI: 10.3847/ 1538-4365/aab766. arXiv: 1703.09824 (2018): 16. arXiv: 1703.09824. arXiv: 1703.09824. Web. <a href="http://dx.doi.org/10.3847/1538-4365/aab766">http://dx.doi.org/10.3847/1538-4365/aab766</a>.

- Waldmann, I. P., et al. "T-REx. II. Retrieval of Emission Spectra". Astrophysical Journal 813.1. ISSN: 15384357. DOI: 10.1088/0004-637X/813/1/13. arXiv: 1508.07591 (2015): 13. arXiv: 1508.07591. arXiv: 1508.07591. Web. < http: //dx.doi.org/10.1088/0004-637X/813/1/13>.
- Waldmann, I. P., et al. "Tau-REx I: A next generation retrieval code for exoplanetary atmospheres". Astrophysical Journal 802.2. ISSN: 15384357. DOI: 10.1088/0004-637X/802/2/107. arXiv: 1409.2312 (2015): 107. arXiv: 1409.2312. arXiv: 1409.2312. Web. <a href="http://dx.doi.org/10.1088/0004">http://dx.doi.org/10.1088/0004</a>-637X/802/2/107>.
- Wells, Martyn, et al. "The Mid-Infrared Instrument for the James Webb Space Telescope, VI: The Medium Resolution Spectrometer". Publications of the Astronomical Society of the Pacific 127.953. ISSN: 00046280. DOI: 10.1086/ 682281. arXiv: 1508.03070 (2015): 646-664. arXiv: 1508.03070. arXiv: 1508. 03070.
- Wright, G S, et al. "The Mid-Infrared Instrument for JWST, II: Design and Build". Publications of the Astronomical Society of the Pacific 127.953. DOI: 10.1086/682253. arXiv: 1508.02333 (2015): 595. arXiv: 1508.02333. arXiv: 1508.02333.
- Yurchenko, Sergei N., Ahmed F. Al-Refaie, and Jonathan Tennyson. "EXO CROSS: A general program for generating spectra from molecular line lists". Astronomy and Astrophysics 614. ISSN: 14320746. DOI: 10.1051/0004-6361/201732531. arXiv: 1801.09803 (2018): 1-12. arXiv: 1801.09803. arXiv: 1801.09803.
- Zalesky, Joseph A., Michael R. Line, Adam C. Schneider, and Jennifer Patience. "A Uniform Retrieval Analysis of Ultra-cool Dwarfs. III. Properties of Y Dwarfs". The Astrophysical Journal 877.1. ISSN: 1538-4357. DOI: 10.3847/ 1538-4357/ab16db. arXiv: 1903.11658 (2019): 24. arXiv: 1903.11658. arXiv: 1903.11658.
- Zhang, Michael, Yayaati Chachan, Eliza M.R. Kempton, and Heather A. Knutson. "Forward modeling and retrievals with PLATON, a fast open-source tool". Publications of the Astronomical Society of the Pacific 131.997. ISSN: 00046280. DOI: 10.1088/1538-3873/aaf5ad. arXiv: 1811.11761 (2019). arXiv: 1811.11761. arXiv: 1811.11761.
- Zucker, S. "Cross-correlation and maximum-likelihood analysis: a new approach to combining cross-correlation functions 2 F RO M M A X I M U M LIKELIHOODTOCROSS-CORRELATION 1292". Monthly Notices of the Royal Astronomical Society 342 (2003): 1291–1298. Print.
- Zurlo, A., et al. "First light of the VLT planet finder SPHERE: III. New spectrophotometry and astrometry of the HR 8799 exoplanetary system". Astronomy and Astrophysics 587. ISSN: 14320746. DOI: 10.1051/0004-6361/ 201526835. arXiv: 1511.04083 (2016): 1-13. arXiv: 1511.04083. arXiv: 1511. 04083.