Loading Dataset

```
from models.vectorUtils import loadData
x, y = loadData()
print("Input features: ", x)
Input features: 9.1
    8.0
    9.1
1
2
    8.4
3
    6.9
4
   7.7
   7.8
94
95 10.2
96
   6.1
97 7.3
98 7.3
[99 rows x 1 columns]
print("Output Labels: ", y)
Output Labels: 0.99523
   0.99007
   0.99769
1
2
   0.99386
3
  0.99508
4
   0.99630
94 0.99620
95 0.99760
96 0.99464
97 0.99830
98 0.99670
[99 rows x 1 columns]
```

Normalisation

```
from models.vectorUtils import MinMaxScaler

scaler = MinMaxScaler()
xNorm = scaler.fitTransform(x)
yNorm = scaler.fitTransform(y)
```

```
print(xNorm)
print(yNorm)
         9.1
0
    0.254902
1
    0.362745
2
   0.294118
3
   0.147059
4
    0.225490
94 0.235294
95 0.470588
96 0.068627
97 0.186275
98 0.186275
[99 rows x 1 columns]
     0.99523
    0.000000
1
    0.580350
2
    0.288652
3
   0.381569
4 0.474486
94 0.466870
95 0.573496
96 0.348058
97 0.626809
98 0.504950
[99 rows x 1 columns]
```

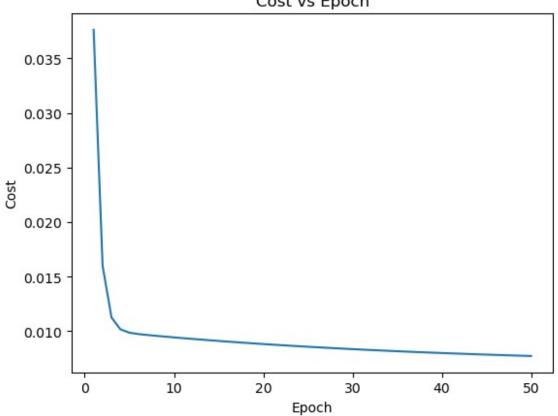
Batch Gradient Descent

```
from models.vectorUtils import LinearRegression

model = LinearRegression()
lr = 0.5
model.fit(xNorm, yNorm, epochs=50, learning_rate=lr)
yHat = model.predict(10)
print("Prediction for input (10) =", yHat)
print(f"Final cost = {model.costFunc(xNorm.to_numpy(),
yNorm.to_numpy())}")
print(f"Parameters:\tw = {model.w}, b = {model.b}")

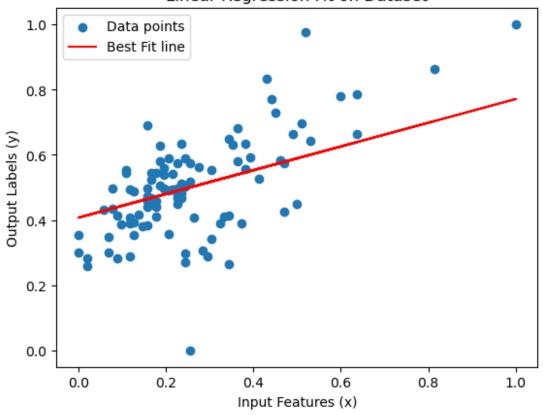
Prediction for input (10) = 4.045135392012695
Final cost = 0.007730905347767666
Parameters: w = 0.3638003476515592, b = 0.4071319154971029
```

BGD with Learning Rate = 0.5 Cost vs Epoch



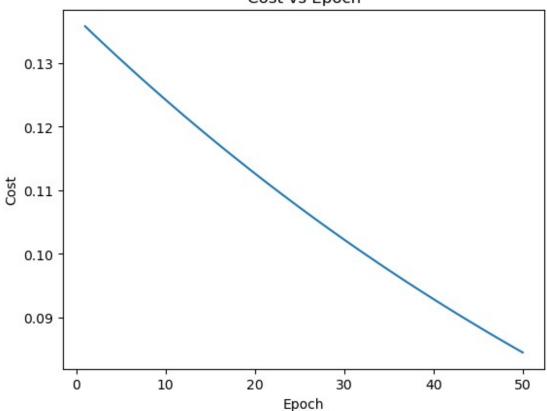
```
model.scatterPlot(xNorm, yNorm, subtitle=f"Parameters: weight (w) =
{model.w:.3f} & bias (b) = {model.b:.3f}")
```

Parameters: weight (w) = 0.364 & bias (b) = 0.407Linear Regression Fit on Dataset



```
lr = 0.005
model = LinearRegression()
model.fit(xNorm, yNorm, epochs=50, learning_rate=lr)
yHat = model.predict(10)
print("Prediction for input (10) =", yHat)
Prediction for input (10) = 0.43793493346817175
model.plotCost(epochs=50, subtitle=f"BGD with Learning Rate = {lr}")
```

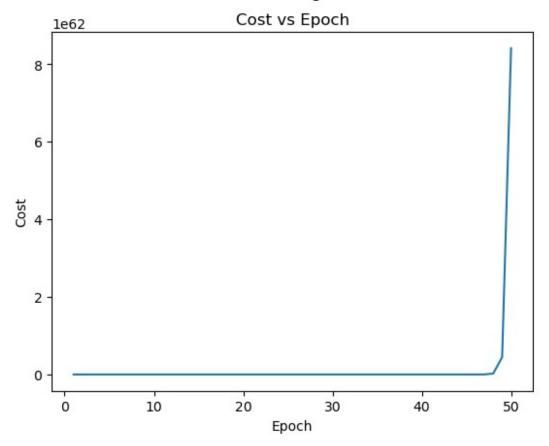
BGD with Learning Rate = 0.005 Cost vs Epoch



```
lr = 5
model = LinearRegression()
model.fit(xNorm, yNorm, epochs=50, learning_rate=lr)
yHat = model.predict(10)
print("Prediction for input (10) =", yHat)

Prediction for input (10) = -1.4062656248784365e+32
model.plotCost(epochs=50, subtitle=f"BGD with Learning Rate = {lr}")
```





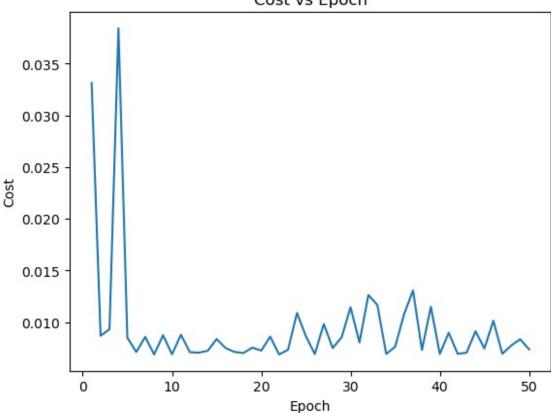
Stochastic Gradient Descent

Same learning rate as BGD

```
lr = 0.5
model = LinearRegression()
model.sgdFit(xNorm, yNorm, epochs=50, learning_rate=lr)
yHat = model.predict(10)
print("Prediction for input (10) =", yHat)

Prediction for input (10) = 5.7983831088447895
model.plotCost(epochs=50, subtitle=f"SGD with Learning Rate = {lr}")
```

SGD with Learning Rate = 0.5 Cost vs Epoch

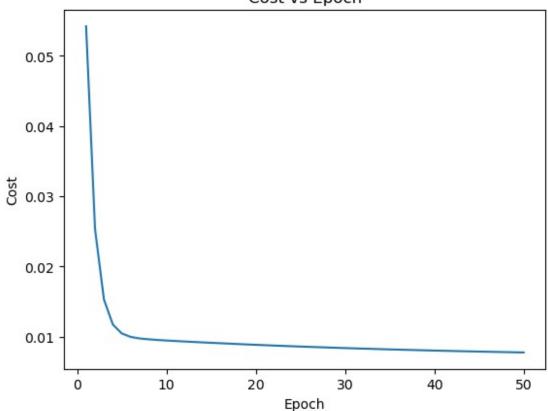


Optimal learning rate

```
lr = 0.005
model = LinearRegression()
model.sgdFit(xNorm, yNorm, epochs=50, learning_rate=lr)
yHat = model.predict(10)
print("Prediction for input (10) =", yHat)

Prediction for input (10) = 4.019389221470472
model.plotCost(epochs=50, subtitle=f"SGD with Learning Rate = {lr}")
```

SGD with Learning Rate = 0.005 Cost vs Epoch



Mini-Batch Gradient Descent

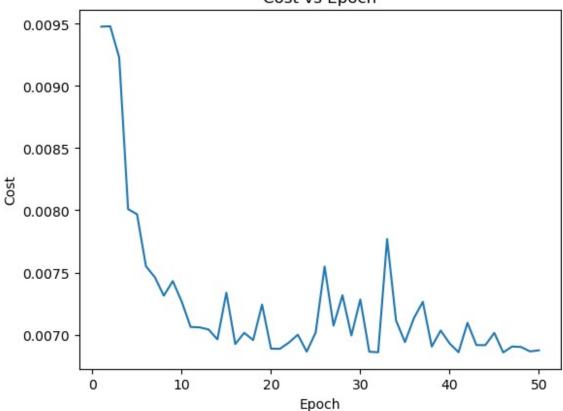
Same Learning Rate as BGD

```
lr = 0.5
model = LinearRegression()
model.mbgdFit(xNorm, yNorm, epochs=50, batch_size=10,
learning_rate=lr)
yHat = model.predict(10)
print("Prediction for input (10) =", yHat)

Prediction for input (10) = 6.369295609598814

model.plotCost(epochs=50, subtitle=f"MBGD with Learning Rate = {lr}")
```

MBGD with Learning Rate = 0.5 Cost vs Epoch



Optimal learning rate

```
lr = 0.05
model = LinearRegression()
model.mbgdFit(xNorm, yNorm, epochs=50, batch_size=10,
learning_rate=lr)
yHat = model.predict(10)
print("Prediction for input (10) =", yHat)

Prediction for input (10) = 4.043960040429436

model.plotCost(epochs=50, subtitle=f"MBGD with Learning Rate = {lr}")
```

MBGD with Learning Rate = 0.05 Cost vs Epoch

