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>
> mes := <<m1, m2, m3>>

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$$mes := \begin{bmatrix} m1 \\ m2 \\ m3 \end{bmatrix} \quad (1)$$

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> B := <<t7, t8, t9>>

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$$B := \begin{bmatrix} t7 \\ t8 \\ t9 \end{bmatrix} \quad (2)$$

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>
> T := <<t1, t2, t4>|<0, t3, t5>|<0, 0, t6>>

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$$T := \begin{bmatrix} t1 & 0 & 0 \\ t2 & t3 & 0 \\ t4 & t5 & t6 \end{bmatrix} \quad (3)$$

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> modelVector := LinearAlgebra[Multiply](T, mes) - B

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$$modelVector := \begin{bmatrix} m1 t1 - t7 \\ m1 t2 + m2 t3 - t8 \\ m1 t4 + m2 t5 + m3 t6 - t9 \end{bmatrix} \quad (4)$$

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> modelFonctionnel := modelVector[1, 1]·modelVector[1, 1] + modelVector[2, 1]
·modelVector[2, 1] + modelVector[3, 1]·modelVector[3, 1]
modelFonctionnel := (m1 t1 - t7)2 + (m1 t2 + m2 t3 - t8)2 + (m1 t4 + m2 t5 + m3 t6 - t9)2

```

$$modelFonctionnel := (m1 t1 - t7)^2 + (m1 t2 + m2 t3 - t8)^2 + (m1 t4 + m2 t5 + m3 t6 - t9)^2 \quad (5)$$

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>
>
> model := (t1, t2, t3, t4, t5, t6, t7, t8, t9) → ((m1 t1 - t7)2 + (m1 t2 + m2 t3 - t8)2 + (m1 t4
+ m2 t5 + m3 t6 - t9)2)0.5
model := (t1, t2, t3, t4, t5, t6, t7, t8, t9) → ((m1 t1 - t7)2 + (m1 t2 + m2 t3 - t8)2 + (m1 t4
+ m2 t5 + m3 t6 - t9)2)0.5

```

$$model := (t1, t2, t3, t4, t5, t6, t7, t8, t9) \rightarrow ((m1 t1 - t7)^2 + (m1 t2 + m2 t3 - t8)^2 + (m1 t4 + m2 t5 + m3 t6 - t9)^2)^{0.5} \quad (6)$$

```

>
> diff(model(t1, t2, t3, t4, t5, t6, t7, t8, t9), t1)

```

$$\frac{1.0 (m1 t1 - t7) m1}{((m1 t1 - t7)^2 + (m1 t2 + m2 t3 - t8)^2 + (m1 t4 + m2 t5 + m3 t6 - t9)^2)^{0.5}} \quad (7)$$

```

> diff(model(t1, t2, t3, t4, t5, t6, t7, t8, t9), t2)

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$$\frac{1.0 (m1 t2 + m2 t3 - t8) m1}{((m1 t1 - t7)^2 + (m1 t2 + m2 t3 - t8)^2 + (m1 t4 + m2 t5 + m3 t6 - t9)^2)^{0.5}} \quad (8)$$

```

> diff(model(t1, t2, t3, t4, t5, t6, t7, t8, t9), t3)

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$$\frac{1.0 (m1 t2 + m2 t3 - t8) m2}{((m1 t1 - t7)^2 + (m1 t2 + m2 t3 - t8)^2 + (m1 t4 + m2 t5 + m3 t6 - t9)^2)^{0.5}} \quad (9)$$

$$\begin{aligned} &> \text{diff}(\text{model}(t1, t2, t3, t4, t5, t6, t7, t8, t9), t4) \\ &\quad \frac{1.0 (m1 t4 + m2 t5 + m3 t6 - t9) m1}{((m1 t1 - t7)^2 + (m1 t2 + m2 t3 - t8)^2 + (m1 t4 + m2 t5 + m3 t6 - t9)^2)^{0.5}} \end{aligned} \quad (10)$$

$$\begin{aligned} &> \text{diff}(\text{model}(t1, t2, t3, t4, t5, t6, t7, t8, t9), t5) \\ &\quad \frac{1.0 (m1 t4 + m2 t5 + m3 t6 - t9) m2}{((m1 t1 - t7)^2 + (m1 t2 + m2 t3 - t8)^2 + (m1 t4 + m2 t5 + m3 t6 - t9)^2)^{0.5}} \end{aligned} \quad (11)$$

$$\begin{aligned} &> \text{diff}(\text{model}(t1, t2, t3, t4, t5, t6, t7, t8, t9), t6) \\ &\quad \frac{1.0 (m1 t4 + m2 t5 + m3 t6 - t9) m3}{((m1 t1 - t7)^2 + (m1 t2 + m2 t3 - t8)^2 + (m1 t4 + m2 t5 + m3 t6 - t9)^2)^{0.5}} \end{aligned} \quad (12)$$

$$\begin{aligned} &> \text{diff}(\text{model}(t1, t2, t3, t4, t5, t6, t7, t8, t9), t7) \\ &\quad \frac{0.5 (-2 m1 t1 + 2 t7)}{((m1 t1 - t7)^2 + (m1 t2 + m2 t3 - t8)^2 + (m1 t4 + m2 t5 + m3 t6 - t9)^2)^{0.5}} \end{aligned} \quad (13)$$

$$\begin{aligned} &> \text{diff}(\text{model}(t1, t2, t3, t4, t5, t6, t7, t8, t9), t8) \\ &\quad \frac{0.5 (-2 m1 t2 - 2 m2 t3 + 2 t8)}{((m1 t1 - t7)^2 + (m1 t2 + m2 t3 - t8)^2 + (m1 t4 + m2 t5 + m3 t6 - t9)^2)^{0.5}} \end{aligned} \quad (14)$$

$$\begin{aligned} &> \text{diff}(\text{model}(t1, t2, t3, t4, t5, t6, t7, t8, t9), t9) \\ &\quad \frac{0.5 (-2 m1 t4 - 2 m2 t5 - 2 m3 t6 + 2 t9)}{((m1 t1 - t7)^2 + (m1 t2 + m2 t3 - t8)^2 + (m1 t4 + m2 t5 + m3 t6 - t9)^2)^{0.5}} \end{aligned} \quad (15)$$

$$\begin{aligned} &> \\ &> \\ &> \text{model} := (m1, m2, m3) \rightarrow ((m1 t1 - t7)^2 + (m1 t2 + m2 t3 - t8)^2 + (m1 t4 + m2 t5 + m3 t6 - t9)^2)^{0.5} \\ &\text{model} := (m1, m2, m3) \rightarrow ((m1 t1 - t7)^2 + (m1 t2 + m2 t3 - t8)^2 + (m1 t4 + m2 t5 + m3 t6 - t9)^2)^{0.5} \end{aligned} \quad (16)$$

$$\begin{aligned} &> \text{diff}(\text{model}(m1, m2, m3), m1) \\ &\quad \frac{0.5 (2 (m1 t1 - t7) t1 + 2 (m1 t2 + m2 t3 - t8) t2 + 2 (m1 t4 + m2 t5 + m3 t6 - t9) t4)}{((m1 t1 - t7)^2 + (m1 t2 + m2 t3 - t8)^2 + (m1 t4 + m2 t5 + m3 t6 - t9)^2)^{0.5}} \end{aligned} \quad (17)$$

$$\begin{aligned} &> \text{diff}(\text{model}(m1, m2, m3), m2) \\ &\quad \frac{0.5 (2 (m1 t2 + m2 t3 - t8) t3 + 2 (m1 t4 + m2 t5 + m3 t6 - t9) t5)}{((m1 t1 - t7)^2 + (m1 t2 + m2 t3 - t8)^2 + (m1 t4 + m2 t5 + m3 t6 - t9)^2)^{0.5}} \end{aligned} \quad (18)$$

$$\begin{aligned} &> \text{diff}(\text{model}(m1, m2, m3), m3) \\ &\quad \frac{1.0 (m1 t4 + m2 t5 + m3 t6 - t9) t6}{((m1 t1 - t7)^2 + (m1 t2 + m2 t3 - t8)^2 + (m1 t4 + m2 t5 + m3 t6 - t9)^2)^{0.5}} \end{aligned} \quad (19)$$