Computer Languages

Transformations of the IR

Verónica Gaspes

School of Information Science, Computer and Electrical Engineering

Mars 2
www2.hh.se/staff/vero/languages

Source: unstructured text

```
class A {
  public static void ...
    System.out.print(3);}
class B {
  int x;
  int f(int y){
    return x+y;}}
```

Abstract syntax: strucutured

Intermediate representation

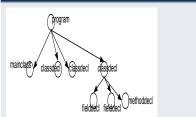
Target: unstructured text

```
subu $sp, $sp, 3
sw $ra, 20($sp)
sd $a0, 32($sp)
sw $0, 24($sp)
sw $0, 28($sp)
```

```
Source: unstructured text
class A {
  public static void ...
    System.out.print(3);}
class B {
```

```
int x;
int f(int y){
  return x+y;}}
```

Abstract syntax: strucutured



Intermediate representation

Target: unstructured text

```
subu $sp, $sp, 3s

sw $ra, 20($sp)

sd $a0, 32($sp)

sw $0, 24($sp)

sw $0, 28($sp)
```

Source: unstructured text

```
class A {
  public static void ...
    System.out.print(3);}
class B {
  int x;
  int f(int y){
    return x+y;}}
```

Abstract syntax: strucutured program mainclass dassded classded classded classded methodded

Intermediate representation MOVE CONST(1) PLUS CONST(3) CONST(2)

```
main:

subu $sp, $sp, 32

sw $ra, 20($sp)

sd $a0, 32($sp)

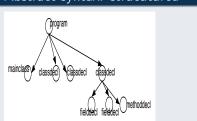
sw $0, 24($sp)

sw $0, 28($sp)
```

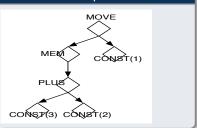
Source: unstructured text

```
class A {
  public static void ...
    System.out.print(3);}
class B {
  int x;
  int f(int y){
    return x+y;}}
```

Abstract syntax: strucutured



Intermediate representation



Target: unstructured text

main:
 subu \$sp, \$sp, 32
 sw \$ra, 20(\$sp)
 sd \$a0, 32(\$sp)
 sw \$0, 24(\$sp)
 sw \$0, 28(\$sp)

Today I will explain things that you will not have to implement. You will be provided with the code for doing this.

However, we need to explain what kind of modifications compilers do to the IR so that it is easier to translate to assembler!

You find the details in chapter 8 of the course book

Today I will explain things that you will not have to implement. You will be provided with the code for doing this.

However, we need to explain what kind of modifications compilers do to the IR so that it is easier to translate to assembler!

You find the details in chapter 8 of the course book.

Today I will explain things that you will not have to implement. You will be provided with the code for doing this.

However, we need to explain what kind of modifications compilers do to the IR so that it is easier to translate to assembler!

You find the details in chapter 8 of the course book.

- CJUMP (op,e_1,e_2,l_1,l_2) ! In real machines conditional jumps fall to the next instruction!
- ESEQ(s,e) makes different evaluation orders yield different results!
- $CALL(f,e_1,\ldots,e_n)$ too!
- $CALL(f,e_1,...,e_n)$ within other CALL() disturb using dedicated registers for parameters.

Solution

- CJUMP(op,e_1,e_2,l_1,l_2)! In real machines conditional jumps fall to the next instruction!
- ESEQ(s,e) makes different evaluation orders yield different results!
- $CALL(f,e_1,\ldots,e_n)$ too!
- CALL (f,e_1,\ldots,e_n) within other CALL() disturb using dedicated registers for parameters.

Solution

- CJUMP(op,e_1,e_2,l_1,l_2)! In real machines conditional jumps fall to the next instruction!
- ESEQ(s,e) makes different evaluation orders yield different results!
- $CALL(f,e_1,\ldots,e_n)$ too!
- CALL (f,e_1,\ldots,e_n) within other CALL() disturb using dedicated registers for parameters.

Solution

- CJUMP(op,e_1,e_2,l_1,l_2)! In real machines conditional jumps fall to the next instruction!
- ESEQ(s,e) makes different evaluation orders yield different results!
- $CALL(f,e_1,\ldots,e_n)$ too!
- CALL (f,e_1,\ldots,e_n) within other CALL() disturb using dedicated registers for parameters.

Solution

- CJUMP(op,e_1,e_2,l_1,l_2)! In real machines conditional jumps fall to the next instruction!
- ESEQ(s,e) makes different evaluation orders yield different results!
- $CALL(f,e_1,\ldots,e_n)$ too!
- $CALL(f,e_1,...,e_n)$ within other CALL() disturb using dedicated registers for parameters.

Solution

- CJUMP (op,e_1,e_2,l_1,l_2) ! In real machines conditional jumps fall to the next instruction!
- ESEQ(s,e) makes different evaluation orders yield different results!
- $CALL(f,e_1,\ldots,e_n)$ too!
- $CALL(f,e_1,...,e_n)$ within other CALL() disturb using dedicated registers for parameters.

Solution

Canonical Trees

The original IR-tree is transformed into a list of canonical trees without SEQ() or ESEQ() nodes

Basic Blocks

The list of canonical trees is grouped into a set of basic blocks such that there are no jumps or labels inside a block.

Traces

Finally, the basic blocks are reordered into a set of traces where each CJUMP() is immediatelly followed by its false label.

Canonical Trees

The original IR-tree is transformed into a list of canonical trees without SEQ() or ESEQ() nodes

Basic Blocks

The list of canonical trees is grouped into a set of basic blocks such that there are no jumps or labels inside a block.

Traces

Finally, the basic blocks are reordered into a set of traces where each CJUMP() is immediatelly followed by its false label.

Canonical Trees

The original IR-tree is transformed into a list of canonical trees without SEQ() or ESEQ() nodes

Basic Blocks

The list of canonical trees is grouped into a set of basic blocks such that there are no jumps or labels inside a block.

Traces

Finally, the basic blocks are reordered into a set of traces where each CJUMP() is immediatelly followed by its false label.

Canonical Trees

The original IR-tree is transformed into a list of canonical trees without SEQ() or ESEQ() nodes

Basic Blocks

The list of canonical trees is grouped into a set of basic blocks such that there are no jumps or labels inside a block.

Traces

Finally, the basic blocks are reordered into a set of traces where each CJUMP() is immediately followed by its false label.

IR-trees are the *abstract syntax* for the *abstract machine* instruction language!

Example

```
tree.Exp

CONST(1)

TEMP(t_{98})

BINOP(+,CONST(1),TEMP(t_{98}))

CALL(f,TEMP(t_{98}))

MEM(CALL(f,TEMP(t_{98}))

ESPO(MOVE (TEMP(t_{98})) TEMP(t_{98}))
```

```
tree.Stm
JUMP(I_1)
MOVE(TEMP(t_{98}),CONST(1))
MOVE(MEM(CALL(f,TEMP(tox))),CONST(1))
```

IR-trees are the *abstract syntax* for the *abstract machine* instruction language!

Example

CONST(1)

tree.Exp

```
CONST(1)
TEMP(t_{98})
BINOP(+,CONST(1),TEMP(t_{98})
CALL(f,TEMP(t_{98}))
MEM(CALL(f,TEMP(t_{98})))
eseq(move(temp(t_{98}),const(1)),temp(t_{98}))
```

tree.Stm

```
JUMP(I_1)
MOVE(TEMP(t_{98}),CONST(I))
MOVE(MEM(CALL(f,TEMP(t_{98}))),CONST(I))
```

IR-trees are the *abstract syntax* for the *abstract machine* instruction language!

Example

```
tree.Exp

CONST(1)

TEMP(t_{98})

BINOP(+,CONST(1),TEMP(t_{98}))

CALL(f,TEMP(t_{98}))

MEM(CALL(f,TEMP(t_{98})))
```

```
tree.Stm

JUMP(I_1)

MOVE(TEMP(t_{98}),CONST(1))

MOVE(MEM(CALL(f,TEMP(t_{98})),CONST(1))
```

IR-trees are the *abstract syntax* for the *abstract machine* instruction language!

Example

TEMP (t_{98})

tree.Exp

CONST(1)

```
TEMP(t_{98})
BINOP(+,CONST(1),TEMP(t_{98}))
CALL(f,TEMP(t_{98}))
MEM(CALL(f,TEMP(t_{98})))
```

tree.Stm

```
JUMP(I_1)
MOVE(TEMP(I_{98}),CONST(I_1))
MOVE(MEM(CALL(I_1,TEMP(I_{98}))),CONST(I_1))
```

IR-trees are the *abstract syntax* for the *abstract machine* instruction language!

Example

```
tree.Exp

CONST(1)

TEMP(t_{98})

BINOP(+,CONST(1),TEMP(t_{98}))

CALL(f,TEMP(t_{98}))

MEM(CALL(f,TEMP(t_{98})))

ESEQ(MOVE(TEMP(t_{98}),CONST(1)),TEMP(t_{98}))
```

```
tree.Stm
JUMP(I_1)
MOVE(TEMP(t_{98}),CONST(1))
MOVE(MEM(CALL(f,TEMP(t_{98})),CONST(1))
```

IR-trees are the *abstract syntax* for the *abstract machine* instruction language!

Example

 $JUMP(I_1)$

tree.Exp

```
CONST(1)
```

TEMP (t_{98})

BINOP $(+,CONST(1),TEMP(t_{98}))$ CALL $(f,TEMP(t_{98}))$

 $MEM(CALL(f,TEMP(t_{98})))$

 $ESEQ(MOVE(TEMP(t_{98}),CONST(1)),TEMP(t_{98}))$

tree.Stm

```
JUMP(I_1)
MOVE(TEMP(t_{98}),CONST(I)
```

IR-trees are the *abstract syntax* for the *abstract machine* instruction language!

Example

```
tree.Exp

CONST(1)

TEMP(t_{98})

BINOP(+,CONST(1),TEMP(t_{98}))

CALL(f,TEMP(t_{98}))

MEM(CALL(f,TEMP(t_{98})))

ESEQ(MOVE(TEMP(t_{98}),CONST(1)),TEMP(t_{98}))
```

```
tree.Stm

JUMP(I_1)

MOVE(TEMP(t_{98}),CONST(I))

MOVE(MEM(CALL(f_iTEMP(t_{98}))),CONST(I))
```

IR-trees are the *abstract syntax* for the *abstract machine* instruction language!

Example

 $BINOP(+,CONST(1),TEMP(t_{98}))$

tree.Exp

CONST(1) TEMP(t_{98})

BINOP(+,CONST(1),TEMP(t_{98}))

 $MEM(CALL(f,TEMP(t_{08})))$

ESEQ(MOVE(TEMP (t_{QR}) ,CONST(1)),TEMP (t_{QR}))

tree.Stm

 $JUMP(I_1)$

 $MOVE(TEMP(t_{98}),CONST(1))$

 $MOVE(MEM(CALL(f, TEMP(t_{98}))), CONST(1))$

IR-trees are the *abstract syntax* for the *abstract machine* instruction language!

Example

```
tree.Exp

CONST(1)

TEMP(t_{98})

BINOP(+,CONST(1),TEMP(t_{98}))

CALL(t_{7},TEMP(t_{98}))

MEM(CALL(t_{7},TEMP(t_{98})))

ESEQ(MOVE(TEMP(t_{98}),CONST(1)),TEMP(t_{98}))
```

```
tree.Stm
JUMP(I_1)
MOVE(TEMP(t_{98}),CONST(1))
MOVE(MEM(CALL(f,TEMP(t_{98}))),CONST(1))
```

IR-trees are the *abstract syntax* for the *abstract machine* instruction language!

Example

 $MOVE(TEMP(t_{98}),CONST(1))$

```
tree.Exp

CONST(1)

TEMP(t_{98})

BINOP(+,CONST(1),TEMP(t_{98}))

CALL(f,TEMP(t_{98}))

MEM(CALL(f,TEMP(t_{98})))

ESEQ(MOVE(TEMP(t_{98}),CONST(1)),TEMP(t_{98}))
```

```
tree.Stm

JUMP(I_1)

MOVE(TEMP(t_{98}),CONST(1))

MOVE(MEM(CALL(f,TEMP(t_{98}))),CONST(1))
```

IR-trees are the *abstract syntax* for the *abstract machine* instruction language!

Example

```
tree.Exp

CONST(1)

TEMP(t_{98})

BINOP(+,CONST(1),TEMP(t_{98}))

CALL(f,TEMP(t_{98}))

MEM(CALL(f,TEMP(t_{98}))

ESEQ(MOVE(TEMP(t_{98}),CONST(1)),TEMP(t_{98}))
```

```
tree.Stm

JUMP(I_1)

MOVE(TEMP(t_{98}),CONST(I))

MOVE(MEM(CALL(f_1TEMP(t_{98})),CONST(I))
```

IR-trees are the *abstract syntax* for the *abstract machine* instruction language!

Example

 $CALL(f, TEMP(t_{98}))$

tree.Exp

```
CONST(1)

TEMP(t_{98})

BINOP(+,CONST(1),TEMP(t_{98}))

CALL(f,TEMP(t_{98}))

MEM(CALL(f,TEMP(t_{98})))
```

tree. Stm

```
_{
m JUMP}(I_1)
_{
m MOVE}({
m TEMP}(t_{98}), {
m CONST}(1))
```

 $MOVE(MEM(CALL(f, TEMP(t_{98}))), CONST(1))$

IR-trees are the *abstract syntax* for the *abstract machine* instruction language!

Example

```
tree.Exp

CONST(1)

TEMP(t_{98})

BINOP(+,CONST(1),TEMP(t_{98}))

CALL(f,TEMP(t_{98}))

MEM(CALL(f,TEMP(t_{98}))

ESEQ(MOVE(TEMP(t_{98}),CONST(1)),TEMP(t_{98}))
```

```
tree.Stm
JUMP(I_1)
MOVE(TEMP(t_{98}),CONST(1))
MOVE(MEM(CALL(f,TEMP(t_{98})),CONST(1))
```

IR-trees are the *abstract syntax* for the *abstract machine* instruction language!

Example

 $MEM(CALL(f,TEMP(t_{98})))$

tree.Exp

```
CONST(1)

TEMP(t_{98})

BINOP(+,CONST(1),TEMP(t_{98}))

CALL(f,TEMP(t_{98}))

MEM(CALL(f,TEMP(t_{98})))
```

tree.Stm

```
_{
m JUMP}(I_1)
_{
m MOVE}({
m TEMP}(t_{98}), {
m CONST}(1))
```

 $MOVE(MEM(CALL(f, TEMP(t_{98}))), CONST(1))$

IR-trees are the *abstract syntax* for the *abstract machine* instruction language!

Example

tree.Exp CONST(1) TEMP(t_{08})

TEMP(t_{98})
BINOP(+,CONST(1),TEMP(t_{98}))
CALL(f,TEMP(t_{98}))

 $\texttt{MEM}(\texttt{CALL}(f,\texttt{TEMP}(t_{98})))$

 $\operatorname{ESEQ}(\operatorname{MOVE}(\operatorname{TEMP}(t_{98}),\operatorname{CONST}(1)),\operatorname{TEMP}(t_{98}))$

tree.Stm

 $JUMP(I_1)$

 $MOVE(TEMP(t_{98}),CONST(1))$

 $MOVE(MEM(CALL(f,TEMP(t_{98}))),CONST(1))$

IR-trees are the *abstract syntax* for the *abstract machine* instruction language!

Example

 $MOVE(MEM(CALL(f, TEMP(t_{98}))), CONST(1))$

tree.Exp

```
CONST(1)

TEMP(t_{98})

BINOP(+,CONST(1),TEMP(t_{98}))

CALL(f,TEMP(t_{98}))

MEM(CALL(f,TEMP(t_{98})))
```

ESEQ(MOVE(TEMP(t_{98}),CONST(1)),TEMP(t_{98}))

tree.Stm

```
_{
m JUMP}(I_1)
_{
m MOVE}({
m TEMP}(t_{98}), {
m CONST}(1))
```

 $MOVE(MEM(CALL(f, TEMP(t_{98}))), CONST(1))$

IR-trees are the *abstract syntax* for the *abstract machine* instruction language!

Example

tree.Exp

```
CONST(1)

TEMP(t_{98})

BINOP(+,CONST(1),TEMP(t_{98}))

CALL(f,TEMP(t_{98}))

MEM(CALL(f,TEMP(t_{98})))
```

ESEQ(MOVE(TEMP(t_{98}),CONST(1)),TEMP(t_{98}))

tree.Stm

```
JUMP(I_1)
MOVE(TEMP(t_{98}),CONST(I))
MOVE(MEM(CALL(f,TEMP(t_{98}))),CONST(I))
```

IR-trees (short reminder)

IR-trees are the *abstract syntax* for the *abstract machine* instruction language!

Example

 $ESEQ(MOVE(TEMP(t_{98}),CONST(1)),TEMP(t_{98}))$

tree.Exp

```
CONST(1)

TEMP(t_{98})

BINOP(+,CONST(1),TEMP(t_{98}))

CALL(f,TEMP(t_{98}))

MEM(CALL(f,TEMP(t_{98})))
```

 $ESEQ(MOVE(TEMP(t_{98}),CONST(1)),TEMP(t_{98}))$

tree.Stm

```
JUMP(I_1)
MOVE(TEMP(t_{98}),CONST(I))
MOVE(MEM(CALL(f,TEMP(t_{98}))),CONST(I))
```

IR-trees (short reminder)

IR-trees are the *abstract syntax* for the *abstract machine* instruction language!

Example

tree.Exp

```
CONST(1)

TEMP(t_{98})

BINOP(+,CONST(1),TEMP(t_{98}))

CALL(f,TEMP(t_{98}))

MEM(CALL(f,TEMP(t_{98})))
```

ESEQ(MOVE(TEMP(t_{QR}),CONST(1)),TEMP(t_{QR}))

tree.Stm

```
JUMP(I_1)
MOVE(TEMP(t_{98}),CONST(I))
MOVE(MEM(CALL(f,TEMP(t_{98}))),CONST(I))
```

- ESEQ(s,e)is very useful but introduces side effects when evaluating expressions!
- Many computer architectures support parallel evaluation of expressions. To exploit this, the order of evaluation of expressions should not influence the result! ESEQ(s,e) spoils this!
- We want to get rid of ESEQ(s,e) before generating code!
- We will subject each fragment to transformations that preserve meaning and result in IR-trees that are easier to translate to assembler!

- ESEQ(s,e)is very useful but introduces side effects when evaluating expressions!
- Many computer architectures support parallel evaluation of expressions. To exploit this, the order of evaluation of expressions should not influence the result! ESEQ(s,e) spoils this!
- We want to get rid of ESEQ(s,e) before generating code!
- We will subject each fragment to transformations that preserve meaning and result in IR-trees that are easier to translate to assembler!

- ESEQ(s,e)is very useful but introduces side effects when evaluating expressions!
- Many computer architectures support parallel evaluation of expressions. To exploit this, the order of evaluation of expressions should not influence the result! ESEQ(s,e) spoils this!
- We want to get rid of ESEQ(s,e) before generating code!
- We will subject each fragment to transformations that preserve meaning and result in IR-trees that are easier to translate to assembler!

- ESEQ(s,e)is very useful but introduces side effects when evaluating expressions!
- Many computer architectures support parallel evaluation of expressions. To exploit this, the order of evaluation of expressions should not influence the result! ESEQ(s,e) spoils this!
- We want to get rid of ESEQ(s,e) before generating code!
- We will subject each fragment to transformations that preserve meaning and result in IR-trees that are easier to translate to assembler!

- ESEQ(s,e)is very useful but introduces side effects when evaluating expressions!
- Many computer architectures support parallel evaluation of expressions. To exploit this, the order of evaluation of expressions should not influence the result! ESEQ(s,e) spoils this!
- We want to get rid of ESEQ(s,e) before generating code!
- We will subject each fragment to transformations that preserve meaning and result in IR-trees that are easier to translate to assembler!

- ESEQ(s,e)is very useful but introduces side effects when evaluating expressions!
- Many computer architectures support parallel evaluation of expressions. To exploit this, the order of evaluation of expressions should not influence the result! ESEQ(s,e) spoils this!
- We want to get rid of ESEQ(s,e) before generating code!
- We will subject each fragment to transformations that preserve meaning and result in IR-trees that are easier to translate to assembler!

- ESEQ(s,e)is very useful but introduces side effects when evaluating expressions!
- Many computer architectures support parallel evaluation of expressions. To exploit this, the order of evaluation of expressions should not influence the result! ESEQ(s,e) spoils this!
- We want to get rid of ESEQ(s,e) before generating code!
- We will subject each fragment to transformations that preserve meaning and result in IR-trees that are easier to translate to assembler!

- ESEQ(s,e)is very useful but introduces side effects when evaluating expressions!
- Many computer architectures support parallel evaluation of expressions. To exploit this, the order of evaluation of expressions should not influence the result! ESEQ(s,e) spoils this!
- We want to get rid of ESEQ(s,e) before generating code!
- We will subject each fragment to transformations that preserve meaning and result in IR-trees that are easier to translate to assembler!

- ESEQ(s,e)is very useful but introduces side effects when evaluating expressions!
- Many computer architectures support parallel evaluation of expressions. To exploit this, the order of evaluation of expressions should not influence the result! ESEQ(s,e) spoils this!
- We want to get rid of ESEQ(s,e) before generating code!
- We will subject each fragment to transformations that preserve meaning and result in IR-trees that are easier to translate to assembler!

- ESEQ(s,e)is very useful but introduces side effects when evaluating expressions!
- Many computer architectures support parallel evaluation of expressions. To exploit this, the order of evaluation of expressions should not influence the result! ESEQ(s,e) spoils this!
- We want to get rid of ESEQ(s,e) before generating code!
- We will subject each fragment to transformations that preserve meaning and result in IR-trees that are easier to translate to assembler!

- ESEQ(s,e)is very useful but introduces side effects when evaluating expressions!
- Many computer architectures support parallel evaluation of expressions. To exploit this, the order of evaluation of expressions should not influence the result! ESEQ(s,e) spoils this!
- We want to get rid of ESEQ(s,e) before generating code!
- We will subject each fragment to transformations that preserve meaning and result in IR-trees that are easier to translate to assembler!

• If ESEQ(s,e) is the main expression in a statement, as in

- So, if we manage to shift all ESEQ(s,e) to top level, then we can eliminate them! (we transform an IR-tree with an ESEQ(s,e) into another IR-tree that achieves the same results and does not contain the ESEQ(s,r))
- We have to provide the transformations that do the shift of subexpressions ESEQ(s,e) to top level!

• If $\mathrm{ESEQ}(s,e)$ is the main expression in a statement, as in

- So, if we manage to shift all ESEQ(s,e) to top level, then we can eliminate them! (we transform an IR-tree with an ESEQ(s,e) into another IR-tree that achieves the same results and does not contain the ESEQ(s,r))
- We have to provide the transformations that do the shift of subexpressions ESEQ(s,e) to top level!

• If $\mathrm{ESEQ}(s,e)$ is the main expression in a statement, as in $\mathrm{JUMP}(\mathrm{ESEQ}(s,e))$

- So, if we manage to shift all ESEQ(s,e) to top level, then we can eliminate them! (we transform an IR-tree with an ESEQ(s,e) into another IR-tree that achieves the same results and does not contain the ESEQ(s,r))
- We have to provide the transformations that do the shift of subexpressions ESEQ(s,e) to top level!

• If $\mathrm{ESEQ}(s,e)$ is the main expression in a statement, as in $\mathrm{JUMP}(\mathrm{ESEQ}(s,e))$

- So, if we manage to shift all ESEQ(s,e) to top level, then we can eliminate them! (we transform an IR-tree with an ESEQ(s,e) into another IR-tree that achieves the same results and does not contain the ESEQ(s,r))
- We have to provide the transformations that do the shift of subexpressions ESEQ(s,e) to top level!

• If $\mathrm{ESEQ}(s,e)$ is the main expression in a statement, as in $\mathrm{JUMP}(\mathrm{ESEQ}(s,e))$

we might replace it by

SEQ(s,JUMP(e))

- So, if we manage to shift all ESEQ(s,e) to top level, then we can eliminate them! (we transform an IR-tree with an ESEQ(s,e) into another IR-tree that achieves the same results and does not contain the ESEQ(s,r))
- We have to provide the transformations that do the shift of subexpressions ESEQ(s,e) to top level!

• If $\mathrm{ESEQ}(s,e)$ is the main expression in a statement, as in $\mathrm{JUMP}(\mathrm{ESEQ}(s,e))$

- So, if we manage to shift all ESEQ(s,e) to top level, then we can eliminate them! (we transform an IR-tree with an ESEQ(s,e) into another IR-tree that achieves the same results and does not contain the ESEQ(s,r))
- We have to provide the transformations that do the shift of subexpressions ESEQ(s,e) to top level!

• If ESEQ(s,e) is the main expression in a statement, as in JUMP(ESEQ(s,e))

- So, if we manage to shift all $\mathrm{ESEQ}(s,e)$ to top level, then we can eliminate them! (we transform an IR-tree with an $\mathrm{ESEQ}(s,e)$ into another IR-tree that achieves the same results and does not contain the $\mathrm{ESEQ}(s,r)$)
- We have to provide the transformations that do the shift of subexpressions ESEQ(s,e) to top level!

• If ESEQ(s,e) is the main expression in a statement, as in JUMP(ESEQ(s,e))

- So, if we manage to shift all ESEQ(s,e) to top level, then we can eliminate them! (we transform an IR-tree with an ESEQ(s,e) into another IR-tree that achieves the same results and does not contain the ESEQ(s,r))
- We have to provide the transformations that do the shift of subexpressions ESEQ(s,e) to top level!

• If $\mathrm{ESEQ}(s,e)$ is the main expression in a statement, as in

$$\mathtt{JUMP}\big(\mathtt{ESEQ}(s,e)\big)$$

- So, if we manage to shift all ESEQ(s,e) to top level, then we can eliminate them! (we transform an IR-tree with an ESEQ(s,e) into another IR-tree that achieves the same results and does not contain the ESEQ(s,r))
- We have to provide the transformations that do the shift of subexpressions ESEQ(s,e) to top level!

Some transformations that move $\mathrm{ESEQ}(s,e)$ to top leve

$$\mathrm{ESEQ}(s_1,\mathrm{ESEQ}(s_2,e)) \Rightarrow \mathrm{ESEQ}(\mathrm{SEQ}(s_1,s_2),e)$$

$$BINOP(op, ESEQ(s, e_1), e_2) \Rightarrow ESEQ(s, BINOP(op, e_1, e_2))$$

$$BINOP(op,e_1,ESEQ(s,e_2)) \Rightarrow ESEQ(s,BINOP(op,e_1,e_2))$$
 |F e_1 and s commute

```
BINOP(op,e_1, \text{ESEQ}(s,e_2)) \Rightarrow

ESEQ(\text{SEQ}(\text{MOVE}(\text{TEMP}(t),e_1),s), \text{BINOP}(op, \text{TEMP}(t),e_2))
```

Some transformations that move $\mathrm{ESEQ}(s,e)$ to top level

```
\mathrm{ESEQ}(s_1,\mathrm{ESEQ}(s_2,e)) \Rightarrow \mathrm{ESEQ}(\mathrm{SEQ}(s_1,s_2),e)
```

$$BINOP(op, ESEQ(s,e_1),e_2) \Rightarrow ESEQ(s, BINOP(op,e_1,e_2))$$

$$\operatorname{BINOP}(\mathit{op}, e_1, \operatorname{ESEQ}(s, e_2)) \Rightarrow \operatorname{ESEQ}(s, \operatorname{BINOP}(\mathit{op}, e_1, e_2))$$
 |F e_1 and s

```
BINOP(op,e_1,ESEQ(s,e_2)) \Rightarrow ESEQ(SEQ(MOVE(TEMP(t),e_1),s),BINOP(op,TEMP(t),e_2))
```

Some transformations that move $\mathrm{ESEQ}(s,e)$ to top level

$$\mathrm{ESEQ}(s_1,\mathrm{ESEQ}(s_2,e)) \Rightarrow \mathrm{ESEQ}(\mathrm{SEQ}(s_1,s_2),e)$$

 $BINOP(op, ESEQ(s, e_1), e_2) \Rightarrow ESEQ(s, BINOP(op, e_1, e_2))$

 $\operatorname{BINOP}(op, e_1, \operatorname{ESEQ}(s, e_2)) \Rightarrow \operatorname{ESEQ}(s, \operatorname{BINOP}(op, e_1, e_2))$ IF e_1 and s_2 commute

BINOP
$$(op,e_1, \text{ESEQ}(s,e_2)) \Rightarrow$$

ESEQ $(\text{SEQ}(\text{MOVE}(\text{TEMP}(t),e_1),s), \text{BINOP}(op, \text{TEMP}(t),e_2)$

Some transformations that move $\mathrm{ESEQ}(s,e)$ to top level

$$\mathrm{ESEQ}(s_1,\mathrm{ESEQ}(s_2,e)) \Rightarrow \mathrm{ESEQ}(\mathrm{SEQ}(s_1,s_2),e)$$

 $BINOP(op, ESEQ(s, e_1), e_2) \Rightarrow ESEQ(s, BINOP(op, e_1, e_2))$

BINOP $(op,e_1, \text{ESEQ}(s,e_2)) \Rightarrow \text{ESEQ}(s, \text{BINOP}(op,e_1,e_2))$ | F e_1 and s commute

BINOP $(op,e_1, \text{ESEQ}(s,e_2)) \Rightarrow$ ESEQ $(\text{SEQ}(\text{MOVE}(\text{TEMP}(t),e_1),s), \text{BINOP}(op, \text{TEMP}(t),e_2)$

Some transformations that move $\mathrm{ESEQ}(s,e)$ to top level

$$\mathrm{ESEQ}\big(s_1, \mathrm{ESEQ}\big(s_2, e\big)\big) \Rightarrow \mathrm{ESEQ}\big(\mathrm{SEQ}\big(s_1, s_2\big), e\big)$$

$$BINOP(op,ESEQ(s,e_1),e_2) \Rightarrow ESEQ(s,BINOP(op,e_1,e_2))$$

BINOP $(op,e_1, \text{ESEQ}(s,e_2)) \Rightarrow \text{ESEQ}(s, \text{BINOP}(op,e_1,e_2))$ |F e_1 and s commute

```
BINOP(op,e_1,ESEQ(s,e_2)) \Rightarrow \\ ESEQ(SEQ(MOVE(TEMP(t),e_1),s),BINOP(op,TEMP(t),e_2)
```

Some transformations that move $\mathrm{ESEQ}(s,e)$ to top level

$$\mathrm{ESEQ}\big(s_1, \mathrm{ESEQ}\big(s_2, e\big)\big) \Rightarrow \mathrm{ESEQ}\big(\mathrm{SEQ}\big(s_1, s_2\big), e\big)$$

$${\tt BINOP}(\textit{op}, \texttt{ESEQ}(\textit{s}, e_1), e_2) \Rightarrow \texttt{ESEQ}(\textit{s}, \texttt{BINOP}(\textit{op}, e_1, e_2))$$

 $BINOP(op,e_1,ESEQ(s,e_2)) \Rightarrow ESEQ(s,BINOP(op,e_1,e_2))$ | F e_1 and s commute

$$\operatorname{BINOP}(op, e_1, \operatorname{ESEQ}(s, e_2)) \Rightarrow$$
 $\operatorname{ESEQ}(\operatorname{SEQ}(\operatorname{MOVE}(\operatorname{TEMP}(t), e_1), s), \operatorname{BINOP}(op, \operatorname{TEMP}(t), e_2)$

Some transformations that move $\mathrm{ESEQ}(s,e)$ to top level

$$\mathrm{ESEQ}\big(s_1, \mathrm{ESEQ}\big(s_2, e\big)\big) \Rightarrow \mathrm{ESEQ}\big(\mathrm{SEQ}\big(s_1, s_2\big), e\big)$$

$${\tt BINOP}(\textit{op}, \texttt{ESEQ}(\textit{s}, e_1), e_2) \Rightarrow \texttt{ESEQ}(\textit{s}, \texttt{BINOP}(\textit{op}, e_1, e_2))$$

$$BINOP(op,e_1,ESEQ(s,e_2)) \Rightarrow ESEQ(s,BINOP(op,e_1,e_2))$$
 | IF e_1 and s commute

```
BINOP(op,e_1, \text{ESEQ}(s,e_2)) \Rightarrow

ESEQ(\text{SEQ}(\text{MOVE}(\text{TEMP}(t),e_1),s), \text{BINOP}(op, \text{TEMP}(t),e_2)
```

Some transformations that move $\mathrm{ESEQ}(s,e)$ to top level

$$\mathrm{ESEQ}\big(s_1, \mathrm{ESEQ}\big(s_2, e\big)\big) \Rightarrow \mathrm{ESEQ}\big(\mathrm{SEQ}\big(s_1, s_2\big), e\big)$$

$${\tt BINOP}(\textit{op}, \texttt{ESEQ}(\textit{s}, e_1), e_2) \Rightarrow \texttt{ESEQ}(\textit{s}, \texttt{BINOP}(\textit{op}, e_1, e_2))$$

$$BINOP(op,e_1,ESEQ(s,e_2)) \Rightarrow ESEQ(s,BINOP(op,e_1,e_2)) \mid F \mid e_1 \mid and \mid s \mid commute$$

```
BINOP(op,e_1,\text{ESEQ}(s,e_2)) \Rightarrow
ESEQ(\text{SEQ}(\text{MOVE}(\text{TEMP}(t),e_1),s),\text{BINOP}(op,\text{TEMP}(t),e_2)
```

Some transformations that move $\mathrm{ESEQ}(s,e)$ to top level

$$\mathrm{ESEQ}(s_1,\mathrm{ESEQ}(s_2,e)) \Rightarrow \mathrm{ESEQ}(\mathrm{SEQ}(s_1,s_2),e)$$

$${\tt BINOP}(\textit{op}, \texttt{ESEQ}(\textit{s}, e_1), e_2) \Rightarrow \texttt{ESEQ}(\textit{s}, \texttt{BINOP}(\textit{op}, e_1, e_2))$$

$$BINOP(op,e_1,ESEQ(s,e_2)) \Rightarrow ESEQ(s,BINOP(op,e_1,e_2))$$
 | IF e_1 and s commute

```
BINOP(op,e_1, \text{ESEQ}(s,e_2)) \Rightarrow
ESEQ(\text{SEQ}(\text{MOVE}(\text{TEMP}(t),e_1),s), \text{BINOP}(op, \text{TEMP}(t),e_2)
```

Some transformations that move $\mathrm{ESEQ}(s,e)$ to top level

$$\mathrm{ESEQ}(s_1,\mathrm{ESEQ}(s_2,e)) \Rightarrow \mathrm{ESEQ}(\mathrm{SEQ}(s_1,s_2),e)$$

$${\tt BINOP}(\textit{op}, \texttt{ESEQ}(\textit{s}, e_1), e_2) \Rightarrow \texttt{ESEQ}(\textit{s}, \texttt{BINOP}(\textit{op}, e_1, e_2))$$

 $BINOP(op,e_1,ESEQ(s,e_2)) \Rightarrow ESEQ(s,BINOP(op,e_1,e_2))$ | IF e_1 and s commute

BINOP
$$(op,e_1, \text{ESEQ}(s,e_2)) \Rightarrow$$

ESEQ $(\text{MOVE}(\text{TEMP}(t),e_1),s), \text{BINOP}(op, \text{TEMP}(t),e_2)$

Some transformations that move $\mathrm{ESEQ}(s,e)$ to top level

$$\mathrm{ESEQ}\big(s_1, \mathrm{ESEQ}\big(s_2, e\big)\big) \Rightarrow \mathrm{ESEQ}\big(\mathrm{SEQ}\big(s_1, s_2\big), e\big)$$

$${\tt BINOP}(\textit{op}, \texttt{ESEQ}(\textit{s}, e_1), e_2) \Rightarrow \texttt{ESEQ}(\textit{s}, \texttt{BINOP}(\textit{op}, e_1, e_2))$$

 $BINOP(op,e_1,ESEQ(s,e_2)) \Rightarrow ESEQ(s,BINOP(op,e_1,e_2))$ | IF e_1 and s commute

$$\begin{aligned} & \text{BINOP}(\textit{op}, e_1, \text{ESEQ}(\textit{s}, e_2)) \Rightarrow \\ & \text{ESEQ}(\text{SEQ}(\text{MOVE}(\text{TEMP}(t), e_1), \textit{s}), \text{BINOP}(\textit{op}, \text{TEMP}(t), e_2)) \end{aligned}$$

Some transformations that move $\mathrm{ESEQ}(s,e)$ to top level

$$\mathrm{ESEQ}\big(s_1, \mathrm{ESEQ}\big(s_2, e\big)\big) \Rightarrow \mathrm{ESEQ}\big(\mathrm{SEQ}\big(s_1, s_2\big), e\big)$$

$$\texttt{BINOP}(\textit{op},\texttt{ESEQ}(\textit{s},\textit{e}_1),\textit{e}_2) \Rightarrow \texttt{ESEQ}(\textit{s},\texttt{BINOP}(\textit{op},\textit{e}_1,\textit{e}_2))$$

 $BINOP(op,e_1,ESEQ(s,e_2)) \Rightarrow ESEQ(s,BINOP(op,e_1,e_2))$ | IF e_1 and s commute

```
\begin{aligned} & \text{BINOP}(\textit{op}, e_1, \text{ESEQ}(\textit{s}, e_2)) \Rightarrow \\ & \text{ESEQ}(\text{SEQ}(\text{MOVE}(\text{TEMP}(t), e_1), \textit{s}), \text{BINOP}(\textit{op}, \text{TEMP}(t), e_2)) \end{aligned}
```

The algorithm

Extract subexpressions

Given a *Tree.Exp* or a *Tree.Stm* the subexpressions can be extracted calling method abstract public LinkedList kids(); that is implemented adequately in each subclass of *Tree.Exp* and of *Tree.Stm*.

Example

CALL(NAME(f),CONST(3),MEM(CONST(4))). kids() will yield the list [NAME(f),CONST(3),MEM(CONST(4))].

The algorithm

Extract subexpressions

Given a *Tree.Exp* or a *Tree.Stm* the subexpressions can be extracted calling method abstract public LinkedList kids(); that is implemented adequately in each subclass of *Tree.Exp* and of *Tree.Stm*.

Example

$$\begin{split} & \text{CALL}(\text{NAME}(\textit{f}), \text{CONST}(\textit{3}), \text{MEM}(\text{CONST}(\textit{4}))) \text{. } \textit{kids}() \\ & \text{will yield the list} \\ & [\text{NAME}(\textit{f}), \text{CONST}(\textit{3}), \text{MEM}(\text{CONST}(\textit{4}))]. \end{split}$$

Reorder

A list of expressions can be reordered using the rewrite rules to one statement that does all the side effects and a list of expressions without ESEQ()s

Example

```
For the list [e_1,e_2,\mathrm{ESEQ}(s,e_3)] the statement s must be pulled to the left past e_1 and e_2 lf s commutes with e_1 and e_2 reordering will yield (s,[e_1,e_2,e_3]).
```

If s does not commute with e_1 and e_2 reordering will yield $(SEQ(MOVE(t_1,e_1),SEQ(MOVE(t_2,e_2),s)),[TEMP(t_1),TEMP(t_2),e_3])$

Reorder

A list of expressions can be reordered using the rewrite rules to one statement that does all the side effects and a list of expressions without ESEQ()s

Example

```
For the list
```

 $[e_1,e_2,\mathrm{ESEQ}(s,e_3)]$

the statement s must be pulled to the left past e_1 and e_2 .

If s commutes with e_1 and e_2 reordering will yield $(s, [e_1, e_2, e_3])$.

If s does not commute with e_1 and e_2 reordering will yield $(SEQ(MOVE(t_1,e_1),SEQ(MOVE(t_2,e_2),s)),[TEMP(t_1),TEMP(t_2),e_3])$

Building up

Once the expressions have been reordered they must be used to form back the corresponding $\mathit{Tree.Exp}$ or $\mathit{Tree.Stm}$. That is why we find methods

- public abstract Tree.Exp build(ExpList kids) in class Tree.Exp
- public abstract Tree.Stm build(ExpList kids) in class Tree.Stm

That are implemented adequtely in each of their subclasses.

```
class BINOP extends Exp{
  public Exp build(ExpList kids){
     return new BINOP(binop,kids.head,kids.tail.head);}
}
```

Building up

Once the expressions have been reordered they must be used to form back the corresponding $\mathit{Tree.Exp}$ or $\mathit{Tree.Stm}$. That is why we find methods

- public abstract Tree.Exp build(ExpList kids) in class Tree.Exp
- public abstract Tree.Stm build(ExpList kids) in class Tree.Stm

That are implemented adequtely in each of their subclasses.

```
class BINOP extends Exp{
  public Exp build(ExpList kids){
     return new BINOP(binop,kids.head,kids.tail.head);}
}
```

Building up

Once the expressions have been reordered they must be used to form back the corresponding $\mathit{Tree.Exp}$ or $\mathit{Tree.Stm}$. That is why we find methods

- public abstract Tree.Exp build(ExpList kids) in class Tree.Exp
- public abstract Tree.Stm build(ExpList kids) in class Tree.Stm

That are implemented adequtely in each of their subclasses.

```
class BINOP extends Exp{
   public Exp build(ExpList kids){
      return new BINOP(binop,kids.head,kids.tail.head);}
}
```

Building up

Once the expressions have been reordered they must be used to form back the corresponding $\mathit{Tree.Exp}$ or $\mathit{Tree.Stm}$. That is why we find methods

- public abstract Tree.Exp build(ExpList kids) in class Tree.Exp
- public abstract Tree.Stm build(ExpList kids) in class Tree.Stm

That are implemented adequtely in each of their subclasses.

```
class BINOP extends Exp{
  public Exp build(ExpList kids){
     return new BINOP(binop,kids.head,kids.tail.head);}
}
```

Building up

Once the expressions have been reordered they must be used to form back the corresponding *Tree.Exp* or *Tree.Stm*. That is why we find methods

- public abstract Tree.Exp build(ExpList kids) in class Tree.Exp
- public abstract Tree.Stm build(ExpList kids) in class Tree.Stm

That are implemented adequtely in each of their subclasses.

```
class BINOP extends Exp{
   public Exp build(ExpList kids){
      return new BINOP(binop,kids.head,kids.tail.head);}
}
```

Building up

Once the expressions have been reordered they must be used to form back the corresponding *Tree.Exp* or *Tree.Stm*. That is why we find methods

- public abstract Tree.Exp build(ExpList kids) in class Tree.Exp
- public abstract Tree.Stm build(ExpList kids) in class Tree.Stm

That are implemented adequtely in each of their subclasses.

```
class BINOP extends Exp{
   public Exp build(ExpList kids){
      return new BINOP(binop,kids.head,kids.tail.head);}
}
```

- Another issue is the possibility of using CALL(f, args) as subexpressions.
- All functions return their result in the dedicated register RV.Thus, in

the second call will overwrite RV before the operation can be executed!

 \bullet All CALL(f, args) are replaced by

ESEQ(MOVE(TEMP(
$$t$$
),CALL(f ,args)),TEMP(t)

before eliminating ESEQ()s

- Another issue is the possibility of using CALL(f, args) as subexpressions.
- All functions return their result in the dedicated register RV.Thus, in

the second call will overwrite RV before the operation can be executed!

 All CALL(f,args) are replaced by ESEQ(MOVE(TEMP(t),CALL(f,args)),TEMP(t) before eliminating ESEQ()s

- Another issue is the possibility of using CALL(f, args) as subexpressions.
- All functions return their result in the dedicated register RV. Thus, in

the second call will overwrite RV before the operation can be executed!

All CALL(f,args) are replaced by
 ESEQ(MOVE(TEMP(t),CALL(f,args)),TEMP(t)
 before eliminating ESEQ()s

- Another issue is the possibility of using CALL(f, args) as subexpressions.
- All functions return their result in the dedicated register RV.Thus, in

the second call will overwrite RV before the operation can be executed!

All CALL(f,args) are replaced by
 ESEQ(MOVE(TEMP(t),CALL(f,args)),TEMP(t)
 before eliminating ESEQ()s

- Another issue is the possibility of using CALL(f, args) as subexpressions.
- All functions return their result in the dedicated register RV.Thus, in

the second call will overwrite RV before the operation can be executed!

All CALL(f,args) are replaced by
 ESEQ(MOVE(TEMP(t),CALL(f,args)),TEMP(t)
 before eliminating ESEQ()s

- Another issue is the possibility of using CALL(f, args) as subexpressions.
- All functions return their result in the dedicated register RV.Thus, in

the second call will overwrite RV before the operation can be executed!

All CALL(f,args) are replaced by
 ESEQ(MOVE(TEMP(t),CALL(f,args)),TEMP(t))
 before eliminating ESEQ()s

- After these transformations, SEQ() nodes can only appear as children to other SEQ() nodes. As no expressions remain that have statements as children, and only the SEQ() statement has statements as children!
- The transformation

$$\operatorname{SEQ}(\operatorname{SEQ}(a,b),c) \Rightarrow \operatorname{SEQ}(a,\operatorname{SEQ}(b,c))$$

can be used to linearize the sequence structure.

- After these transformations, SEQ() nodes can only appear as children to other SEQ() nodes. As no expressions remain that have statements as children, and only the SEQ() statement has statements as children!
- The transformation

$$SEQ(SEQ(a,b),c) \Rightarrow SEQ(a,SEQ(b,c))$$

can be used to linearize the sequence structure.

- After these transformations, SEQ() nodes can only appear as children to other SEQ() nodes. As no expressions remain that have statements as children, and only the SEQ() statement has statements as children!
- The transformation

$$SEQ(SEQ(a,b),c) \Rightarrow SEQ(a,SEQ(b,c))$$

can be used to linearize the sequence structure.

- After these transformations, SEQ() nodes can only appear as children to other SEQ() nodes. As no expressions remain that have statements as children, and only the SEQ() statement has statements as children!
- The transformation

$$SEQ(SEQ(a,b),c) \Rightarrow SEQ(a,SEQ(b,c))$$

can be used to linearize the sequence structure.

- After these transformations, SEQ() nodes can only appear as children to other SEQ() nodes. As no expressions remain that have statements as children, and only the SEQ() statement has statements as children!
- The transformation

$$SEQ(SEQ(a,b),c) \Rightarrow SEQ(a,SEQ(b,c))$$

can be used to linearize the sequence structure.

- After these transformations, SEQ() nodes can only appear as children to other SEQ() nodes. As no expressions remain that have statements as children, and only the SEQ() statement has statements as children!
- The transformation

$${\scriptstyle \operatorname{SEQ}\left(\operatorname{SEQ}(a,b),c\right) \Rightarrow \operatorname{SEQ}\left(a,\operatorname{SEQ}(b,c)\right)}$$

can be used to linearize the sequence structure.

- After these transformations, SEQ() nodes can only appear as children to other SEQ() nodes. As no expressions remain that have statements as children, and only the SEQ() statement has statements as children!
- The transformation

$$SEQ(SEQ(a,b),c) \Rightarrow SEQ(a,SEQ(b,c))$$

can be used to linearize the sequence structure.

- After these transformations, SEQ() nodes can only appear as children to other SEQ() nodes. As no expressions remain that have statements as children, and only the SEQ() statement has statements as children!
- The transformation

$$SEQ(SEQ(a,b),c) \Rightarrow SEQ(a,SEQ(b,c))$$

can be used to linearize the sequence structure.

- To resume,
 - the translation phase resulted in an IR-tree statement for every method body,
 - the transformations sketched turned each such statement into a list of atomic statements without ESEQ() expression nodes.
- Before producing assembler we will rearange the lists of statements so that all

$$CJUMP(op,e_1,e_2,l_t,l_f)$$

To resume,

- the translation phase resulted in an IR-tree statement for every method body,
- the transformations sketched turned each such statement into a list of atomic statements without ESEQ() expression nodes.
- Before producing assembler we will rearange the lists of statements so that all

$$CJUMP(op,e_1,e_2,l_t,l_f)$$

- To resume,
 - the translation phase resulted in an IR-tree statement for every method body,
 - the transformations sketched turned each such statement into a list of atomic statements without ESEQ() expression nodes.
- Before producing assembler we will rearange the lists of statements so that all

$$CJUMP(op,e_1,e_2,l_t,l_f)$$

- To resume,
 - the translation phase resulted in an IR-tree statement for every method body,
 - the transformations sketched turned each such statement into a list of atomic statements without ESEQ() expression nodes.
- Before producing assembler we will rearrange the lists of statements so that all

$$CJUMP(op,e_1,e_2,l_t,l_f)$$

- To resume,
 - the translation phase resulted in an IR-tree statement for every method body,
 - the transformations sketched turned each such statement into a list of atomic statements without ESEQ() expression nodes.
- Before producing assembler we will rearange the lists of statements so that all

$$CJUMP(op,e_1,e_2,l_t,l_f)$$

- To resume,
 - the translation phase resulted in an IR-tree statement for every method body,
 - the transformations sketched turned each such statement into a list of atomic statements without ESEQ() expression nodes.
- Before producing assembler we will rearange the lists of statements so that all

$$CJUMP(op,e_1,e_2,l_t,l_f)$$

- To resume,
 - the translation phase resulted in an IR-tree statement for every method body,
 - the transformations sketched turned each such statement into a list of atomic statements without ESEQ() expression nodes.
- Before producing assembler we will rearrange the lists of statements so that all

$$CJUMP(op,e_1,e_2,l_t,l_f)$$

are followed by the statement under I_f

(so that they can be translated with the more commor jumps!)

- To resume,
 - the translation phase resulted in an IR-tree statement for every method body,
 - the transformations sketched turned each such statement into a list of atomic statements without ESEQ() expression nodes.
- Before producing assembler we will rearrange the lists of statements so that all

$$\mathrm{CJUMP}(op,e_1,e_2,l_t,l_f)$$

- To implement this last transformation of the list of statements, a bit of control flow analysis is done.
- First, basic blocks of statements are identified and put together. A basic block is a list of statements where
 - the first statement is a LABEL()
 - the last statement is a JUMP() or CJUMP()
 - there are no other LABEL(), JUMP() or CJUMP() in it.
 - a basic block is entered at the begining and exited at the end
- Basic blocks can be rearanged in any order without altering results!

- To implement this last transformation of the list of statements, a bit of control flow analysis is done.
- First, basic blocks of statements are identified and put together. A basic block is a list of statements where
 - the first statement is a LABEL()
 - the last statement is a JUMP() or CJUMP()
 - there are no other LABEL(), JUMP() or CJUMP() in it.
 - a basic block is entered at the begining and exited at the end!
- Basic blocks can be rearanged in any order without altering results!

- To implement this last transformation of the list of statements, a bit of control flow analysis is done.
- First, basic blocks of statements are identified and put together. A basic block is a list of statements where
 - the first statement is a LABEL()
 - the last statement is a JUMP() or CJUMP()
 - there are no other LABEL(), JUMP() or CJUMP() in it.
 - basic block is entered at the begining and exited at the end!
- Basic blocks can be rearanged in any order without altering results!

- To implement this last transformation of the list of statements, a bit of control flow analysis is done.
- First, basic blocks of statements are identified and put together. A basic block is a list of statements where
 - the first statement is a LABEL()
 - the last statement is a JUMP() or CJUMP()
 - there are no other LABEL(), JUMP() or CJUMP() in it.
 - a basic block is entered at the begining and exited at the end!
- Basic blocks can be rearanged in any order without altering results!

- To implement this last transformation of the list of statements, a bit of control flow analysis is done.
- First, basic blocks of statements are identified and put together. A basic block is a list of statements where
 - the first statement is a LABEL()
 - the last statement is a JUMP() or CJUMP()
 - there are no other LABEL(), JUMP() or CJUMP() in it.
 - a basic block is entered at the begining and exited at the end!
- Basic blocks can be rearanged in any order without altering results!

- To implement this last transformation of the list of statements, a bit of control flow analysis is done.
- First, basic blocks of statements are identified and put together. A basic block is a list of statements where
 - the first statement is a LABEL()
 - the last statement is a JUMP() or CJUMP()
 - there are no other LABEL(), JUMP() or CJUMP() in it.
 - a basic block is entered at the begining and exited at the end!
- Basic blocks can be rearanged in any order without altering results!

- To implement this last transformation of the list of statements, a bit of control flow analysis is done.
- First, basic blocks of statements are identified and put together. A basic block is a list of statements where
 - the first statement is a LABEL()
 - the last statement is a JUMP() or CJUMP()
 - there are no other LABEL(), JUMP() or CJUMP() in it.
 - a basic block is entered at the begining and exited at the end!
- Basic blocks can be rearanged in any order without altering results!

- To implement this last transformation of the list of statements, a bit of control flow analysis is done.
- First, basic blocks of statements are identified and put together. A basic block is a list of statements where
 - the first statement is a LABEL()
 - the last statement is a JUMP() or CJUMP()
 - there are no other LABEL(), JUMP() or CJUMP() in it.
 - a basic block is entered at the begining and exited at the end!
- Basic blocks can be rearanged in any order without altering results!

Splitting

The list of canonical IR-trees corresponding to a function body is inspected from first to last element.

- On a LABEL(), start a new block!
- On a JUMP() or CJUMP(), end a block!
- On any other statement, add it to the current block!

- If a block doesn't end with a JUMP() or CJUMP() add to it a JUMP() to the label of the following block.
- If a block doesn't start with a LABEL(), create one and stick it to it!

Splitting

The list of canonical IR-trees corresponding to a function body is inspected from first to last element.

- On a LABEL(), start a new block!
- On a JUMP() or CJUMP(), end a block!
- On any other statement, add it to the current block!

- If a block doesn't end with a JUMP() or CJUMP() add to it a JUMP() to the label of the following block.
- If a block doesn't start with a LABEL(), create one and stick it to it!

Splitting

The list of canonical IR-trees corresponding to a function body is inspected from first to last element.

- On a LABEL(), start a new block!
- On a JUMP() or CJUMP(), end a block!
- On any other statement, add it to the current block!

- If a block doesn't end with a JUMP() or CJUMP() add to it a JUMP() to the label of the following block.
- If a block doesn't start with a LABEL(), create one and stick it to it!

Splitting

The list of canonical IR-trees corresponding to a function body is inspected from first to last element.

- On a LABEL(), start a new block!
- On a JUMP() or CJUMP(), end a block!
- On any other statement, add it to the current block!

Completing

 If a block doesn't end with a JUMP() or CJUMP() add to it a JUMP() to the label of the following block.

 If a block doesn't start with a LABEL(), create one and stick it to it!

Splitting

The list of canonical IR-trees corresponding to a function body is inspected from first to last element.

- On a LABEL(), start a new block!
- On a JUMP() or CJUMP(), end a block!
- On any other statement, add it to the current block!

- If a block doesn't end with a JUMP() or CJUMP() add to it a JUMP() to the label of the following block.
- If a block doesn't start with a LABEL(), create one and stick it to it!

Splitting

The list of canonical IR-trees corresponding to a function body is inspected from first to last element.

- On a LABEL(), start a new block!
- On a JUMP() or CJUMP(), end a block!
- On any other statement, add it to the current block!

- If a block doesn't end with a JUMP() or CJUMP() add to it a JUMP() to the label of the following block.
- If a block doesn't start with a LABEL(), create one and stick it to it!

Splitting

The list of canonical IR-trees corresponding to a function body is inspected from first to last element.

- On a LABEL(), start a new block!
- On a JUMP() or CJUMP(), end a block!
- On any other statement, add it to the current block!

- If a block doesn't end with a JUMP() or CJUMP() add to it a JUMP() to the label of the following block.
- If a block doesn't start with a LABEL(), create one and stick it to it!

- Basic blocks are put together into a traces.
- A trace is a sequence of statements that could be executed sequentialy.
- We want to produce a set of traces such that
 - every basic block is in some trace,
 - every CJUMP() is followed by its false label
 - many JUMP()s are followed by the label they jump to (because they can then be eliminated!)
- First, a covering set of traces is built by starting with an arbitrary block and adding its execution successors to the trace until there are no more successors to add. Then another trace is started.

- Basic blocks are put together into a traces.
- A trace is a sequence of statements that could be executed sequentialy.
- We want to produce a set of traces such that
 - every basic block is in some trace,
 - every CJUMP() is followed by its false label
 - many JUMP()s are followed by the label they jump to (because they can then be eliminated!)
- First, a covering set of traces is built by starting with an arbitrary block and adding its execution successors to the trace until there are no more successors to add. Then another trace is started.

- Basic blocks are put together into a traces.
- A trace is a sequence of statements that could be executed sequentialy.
- We want to produce a set of traces such that
 - every basic block is in some trace,
 - every CJUMP() is followed by its false label
 - many JUMP()s are followed by the label they jump to (because they can then be eliminated!)
- First, a covering set of traces is built by starting with an arbitrary block and adding its execution successors to the trace until there are no more successors to add. Then another trace is started.

- Basic blocks are put together into a traces.
- A trace is a sequence of statements that could be executed sequentialy.
- We want to produce a set of traces such that
 - every basic block is in some trace,
 - every CJUMP() is followed by its false label
 - many JUMP()s are followed by the label they jump to (because they can then be eliminated!)
- First, a covering set of traces is built by starting with an arbitrary block and adding its execution successors to the trace until there are no more successors to add. Then another trace is started.

- Basic blocks are put together into a traces.
- A trace is a sequence of statements that could be executed sequentialy.
- We want to produce a set of traces such that
 - every basic block is in some trace,
 - every CJUMP() is followed by its false label
 - many JUMP()s are followed by the label they jump to (because they can then be eliminated!)
- First, a covering set of traces is built by starting with an arbitrary block and adding its execution successors to the trace until there are no more successors to add. Then another trace is started.

- Basic blocks are put together into a traces.
- A trace is a sequence of statements that could be executed sequentialy.
- We want to produce a set of traces such that
 - every basic block is in some trace,
 - every CJUMP() is followed by its false label
 - many JUMP()s are followed by the label they jump to (because they can then be eliminated!)
- First, a covering set of traces is built by starting with an arbitrary block and adding its execution successors to the trace until there are no more successors to add. Then another trace is started.

- Basic blocks are put together into a traces.
- A trace is a sequence of statements that could be executed sequentialy.
- We want to produce a set of traces such that
 - every basic block is in some trace,
 - every CJUMP() is followed by its false label
 - many JUMP()s are followed by the label they jump to (because they can then be eliminated!)
- First, a covering set of traces is built by starting with an arbitrary block and adding its execution successors to the trace until there are no more successors to add. Then another trace is started.

- Basic blocks are put together into a traces.
- A trace is a sequence of statements that could be executed sequentialy.
- We want to produce a set of traces such that
 - every basic block is in some trace,
 - every CJUMP() is followed by its false label
 - many JUMP()s are followed by the label they jump to (because they can then be eliminated!)
- First, a covering set of traces is built by starting with an arbitrary block and adding its execution successors to the trace until there are no more successors to add. Then another trace is started.

- Then these traces are further adjusted by considering the CJUMP()s in them:
 - A CJUMP() followed by its false label is left untouched.
 - For a CJUMP() followed by its true label, labels are switched and the condition negated.
 - For a CJUMP() followed by neither label

```
a new label is invented l' the CJUMP() is replaced by CJUMP(op,e_1,e_2,l_t,l')
LABEL(l')
JUMP(l_f)
```

- Then these traces are further adjusted by considering the CJUMP()s in them:
 - A CJUMP() followed by its false label is left untouched.
 - For a CJUMP() followed by its true label, labels are switched and the condition negated.
 - For a CJUMP() followed by neither label

```
a new label is invented l' the CJUMP() is replaced by CJUMP(op,e_1,e_2,l_t,l')
LABEL(l')
JUMP(l_f)
```

- Then these traces are further adjusted by considering the CJUMP()s in them:
 - A CJUMP() followed by its false label is left untouched.
 - For a CJUMP() followed by its true label, labels are switched and the condition negated.
 - For a CJUMP() followed by neither label

```
a new label is invented l' the CJUMP() is replaced by CJUMP(op,e_1,e_2,l_t,l')
LABEL(l')
JUMP(l_f)
```

- Then these traces are further adjusted by considering the CJUMP()s in them:
 - A CJUMP() followed by its false label is left untouched.
 - For a CJUMP() followed by its true label, labels are switched and the condition negated.
 - For a CJUMP() followed by neither label

```
a new label is invented l' the CJUMP() is replaced by CJUMP(op,e_1,e_2,l_t,l')
LABEL(l')
JUMP(l_f)
```

- Then these traces are further adjusted by considering the CJUMP()s in them:
 - A CJUMP() followed by its false label is left untouched.
 - For a CJUMP() followed by its true label, labels are switched and the condition negated.
 - For a CJUMP() followed by neither label

```
a new label is invented l' the CJUMP() is replaced by CJUMP(op,e_1,e_2,l_t,l')
LABEL(l')
JUMP(l_f)
```

- Then these traces are further adjusted by considering the CJUMP()s in them:
 - A CJUMP() followed by its false label is left untouched.
 - For a CJUMP() followed by its true label, labels are switched and the condition negated.
 - For a CJUMP() followed by neither label

```
a new label is invented l' the CJUMP() is replaced by: CJUMP(op,e_1,e_2,l_t,l')
LABEL(l')
JUMP(l_f)
```

- Then these traces are further adjusted by considering the CJUMP()s in them:
 - A CJUMP() followed by its false label is left untouched.
 - For a CJUMP() followed by its true label, labels are switched and the condition negated.
 - For a CJUMP() followed by neither label

```
a new label is invented l' the CJUMP() is replaced by: CJUMP(op,e_1,e_2,l_t,l')
LABEL(l')
JUMP(l_f)
```

- Then these traces are further adjusted by considering the CJUMP()s in them:
 - A CJUMP() followed by its false label is left untouched.
 - For a CJUMP() followed by its true label, labels are switched and the condition negated.
 - For a CJUMP() followed by neither label

```
a new label is invented l' the CJUMP() is replaced by: CJUMP(op,e_1,e_2,l_t,l')
LABEL(l')
JUMP(l_f)
```

There is an implementation of these transformations that comes with the book. For it to run with the rest of the compiler I've made some small modifications (you will get it with the distribution for part five of the project)

package canon;

Canon removes ESEQ(), assigns CALL() to registers and returns a list of atomic statements

BasicBlocks puts together statements into basic blocks
TraceSchedule puts together blocks into traces and flattens
back to a list of statements

There is an implementation of these transformations that comes with the book. For it to run with the rest of the compiler I've made some small modifications (you will get it with the distribution for part five of the project)

package canon;

There is an implementation of these transformations that comes with the book. For it to run with the rest of the compiler I've made some small modifications (you will get it with the distribution for part five of the project)

package canon;

Canon removes ESEQ(), assigns CALL() to registers and returns a list of atomic statements

BasicBlocks puts together statements into basic blocks
TraceSchedule puts together blocks into traces and flattens
back to a list of statements

There is an implementation of these transformations that comes with the book. For it to run with the rest of the compiler I've made some small modifications (you will get it with the distribution for part five of the project)

package canon;

Canon removes ESEQ(), assigns CALL() to registers and returns a list of atomic statements

BasicBlocks puts together statements into basic blocks

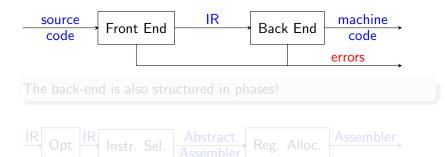
There is an implementation of these transformations that comes with the book. For it to run with the rest of the compiler I've made some small modifications (you will get it with the distribution for part five of the project)

package canon;

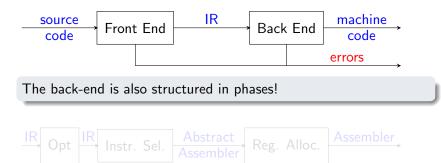
Canon removes ESEQ(), assigns CALL() to registers and returns a list of atomic statements

BasicBlocks puts together statements into basic blocks TraceSchedule puts together blocks into traces and flattens back to a list of statements

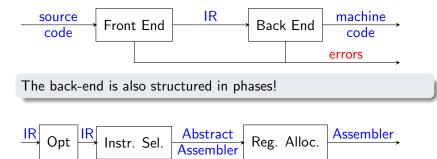
The back-end



The back-end



The back-end



Observation

For the back-end we no longer look at *minijava*! We compile IR-trees to assembler.

A small minijava program

```
class A{
   public static void main(String[] a){
      System.out.println(new B().f(3).f());
class B{
   int x;
   int y;
   public C f(int z){
      if (x < y) x=z+1; else x=z+x;
      return new C();
class C{
   public int f(){return 3;}
```

The result of translating it

```
PROCEDURE :main
EXPS(
CALL(
  NAME _printint,
  CONST 0,
  CALL(
   NAME C_f,
   CALL(
    NAME B_f,
    CALL(
     NAME _malloc,
     CONST 0,
     CONST 8),
    CONST 3))))
```

The result of translating it

```
PROCEDURE :B_f
PROCEDURE :main
                      MOVE(
EXPS(
                       TEMP t32,
CALL(
                       ESEQ(
  NAME _printint,
                        SEQ(
  CONST 0,
                         SEQ(
  CALL(
                          CJUMP(LT,
   NAME C_f,
                           MEM(
   CALL(
                             BINOP (PLUS,
    NAME B_f,
                              TEMP t64,
    CALL(
                              CONST 0)).
     NAME _malloc,
                            MEM(
     CONST 0,
                             BINOP (PLUS,
     CONST 8),
                              TEMP t64,
    CONST 3))))
                              CONST 4)),
                            LO,L1),
```

The result of translating it

```
PROCEDURE :B_f
PROCEDURE :main
                      MOVE(
EXPS(
                       TEMP t32,
CALL(
                       ESEQ(
  NAME _printint,
                        SEQ(
  CONST 0,
                         SEQ(
  CALL(
                                             PROCEDURE : C_f
                          CJUMP(LT,
   NAME C_f,
                                             MOVE (
                           MEM(
   CALL(
                                              TEMP t32,
                             BINOP(PLUS.
                                              CONST 3)
    NAME B_f,
                              TEMP t64,
    CALL(
                              CONST 0)).
     NAME _malloc,
                            MEM(
     CONST 0,
                             BINOP (PLUS.
     CONST 8),
                              TEMP t64,
    CONST 3))))
                              CONST 4)),
                            LO,L1),
```

(almost)All of B_f

```
MOVE(
 TEMP t32,
 ESEQ(
  SEQ(
   SEQ(
    CJUMP(LT,
     MEM(
      BINOP (PLUS,
       TEMP t64,
       CONST 0)),
     MEM(
      BINOP (PLUS,
       TEMP t64,
       CONST 4)),
     LO,L1),
```

(almost)All of B_f

```
MOVE(
                      SEQ(
 TEMP t32,
                       SEQ(
 ESEQ(
                        SEQ(
  SEQ(
                         LABEL LO,
   SEQ(
                         MOVE(
    CJUMP(LT,
                           MEM(
     MEM(
                            BINOP (PLUS,
      BINOP (PLUS,
                             TEMP t64,
       TEMP t64,
                             CONST 0)),
       CONST 0)),
                          BINOP (PLUS,
     MEM(
                            TEMP t65,
      BINOP (PLUS,
                            CONST 1))),
       TEMP t64,
                        JUMP (
       CONST 4)),
                         NAME L2)),
     LO,L1),
```

(almost)All of B_f

```
SEQ(
MOVE(
                      SEQ(
                                              SEQ(
 TEMP t32,
                        SEQ(
                                               LABEL L1,
 ESEQ(
                         SEQ(
                                               MOVE(
  SEQ(
                          LABEL LO,
                                                 MEM(
   SEQ(
                          MOVE(
                                                  BINOP (PLUS,
    CJUMP(LT,
                           MEM(
                                                   TEMP t64,
     MEM(
                            BINOP (PLUS,
                                                   CONST 0)),
      BINOP (PLUS,
                             TEMP t64,
                                                 BINOP (PLUS,
       TEMP t64,
                             CONST 0)),
                                                  TEMP t65,
       CONST 0)),
                           BINOP (PLUS,
                                                  MEM(
     MEM(
                            TEMP t65,
                                                   BINOP (PLUS,
      BINOP (PLUS,
                            CONST 1))),
                                                    TEMP t64,
       TEMP t64,
                         JUMP (
                                                    CONST 0)))),
       CONST 4)),
                          NAME L2)),
                                              JUMP (
     LO,L1),
```

NAME L2)))).

```
LABEL L6 MOVE(
CJUMP(LT, MEM( LABEL L2
MEM (
 BINOP(PLUS, TEMP t64, TEMP t32,
  TEMP t64, CONST 0)). CALL(
  CONST 0)), BINOP(PLUS, NAME _malloc,
MEM(
 BINOP(PLUS, MEM( CONST 0))
  TEMP t64, BINOP(PLUS, JUMP(
  CONST 4)), TEMP t64, NAME L5)
LO,L1)
```

```
LABEL L1
LABEL L6
             MOVE (
CJUMP(LT,
              MEM(
MEM (
               BINOP(PLUS, MOVE(
 BINOP (PLUS,
                TEMP t64, TEMP t32,
  TEMP t64,
                CONST 0)), CALL(
  CONST 0)), BINOP(PLUS, NAME _malloc,
MEM(
               TEMP t65, CONST 0,
 BINOP(PLUS,
               MEM(
  TEMP t64,
             BINOP(PLUS, JUMP(
  CONST 4)),
                 TEMP t64, NAME L5)
LO,L1)
                 CONST 0)))
```

```
LABEL L1
LABEL L6
             MOVE (
CJUMP(LT,
                         LABEL L2
             MEM(
MEM (
               BINOP(PLUS, MOVE(
 BINOP (PLUS,
             TEMP t64, TEMP t32,
  TEMP t64,
                CONST 0)), CALL(
  CONST 0)), BINOP(PLUS, NAME _malloc,
MEM(
               TEMP t65, CONST 0,
                         CONST 0))
 BINOP(PLUS,
               MEM(
  TEMP t64, BINOP(PLUS, JUMP(
  CONST 4)),
                TEMP t64, NAME L5)
LO,L1)
                CONST ())))
```

What is left: code generation

Purpose: Generate a file with assembler code for a target machine

Instruction Selection

- Study the instructions of the target architecture.
- Program how to match each IR statement with machine instructions.
- For each instruction keep a list of the temporaries used.

Register Allocation

- Build a *flow graph* where instructions are nodes and edges reflect usage of temporaries.
- Color the graph to find independent temporaries.
- Assign registers to instructions.

What is left: code generation

Purpose: Generate a file with assembler code for a target machine

Instruction Selection

- Study the instructions of the target architecture.
- Program how to match each IR statement with machine instructions.
- For each instruction keep a list of the temporaries used.

Register Allocation

- Build a *flow graph* where instructions are nodes and edges reflect usage of temporaries.
- Color the graph to find independent temporaries.
- Assign registers to instructions.

What is left: code generation

Purpose: Generate a file with assembler code for a target machine

Instruction Selection

- Study the instructions of the target architecture.
- Program how to match each IR statement with machine instructions.
- For each instruction keep a list of the temporaries used.

Register Allocation

- Build a *flow graph* where instructions are nodes and edges reflect usage of temporaries.
- Color the graph to find independent temporaries.
- Assign registers to instructions.