

Probability that first head appears on n^{th} toss

Probability that first head appears on n^{th} toss

First try: $1/2$

Probability that first head appears on n^{th} toss

First try: $1/2$

Second try: $1/2 * 1/2 = 1/4$

Probability that first head appears on n^{th} toss

First try: $1/2$

Second try: $1/2 * 1/2 = 1/4$

Third try: $1/4 * 1/2 = 1/8$

Probability that first head appears on n^{th} toss

First try: $1/2$

Second try: $1/2 * 1/2 = 1/4$

Third try: $1/4 * 1/2 = 1/8$

...

Probability that first head appears on n^{th} toss

First try: $1/2$

Second try: $1/2 * 1/2 = 1/4$

Third try: $1/4 * 1/2 = 1/8$

...

n^{th} try: $1/2^n$

Probability that first head appears on n^{th} toss

First try: $1/2$

Second try: $1/2 * 1/2 = 1/4$

Third try: $1/4 * 1/2 = 1/8$

...

n^{th} try: $1/2^n$

Probability that it comes up heads at least one time =

$$1/2 + 1/4 + 1/8 + 1/16 + \dots$$

Probability that first head appears on n^{th} toss

First try: $1/2$

Second try: $1/2 * 1/2 = 1/4$

Third try: $1/4 * 1/2 = 1/8$

...

n^{th} try: $1/2^n$

Probability that it comes up heads at least one time =

$$s = 1/2 + 1/4 + 1/8 + 1/16 + \dots$$

Probability that first head appears on n^{th} toss

First try: $1/2$

Second try: $1/2 * 1/2 = 1/4$

Third try: $1/4 * 1/2 = 1/8$

...

n^{th} try: $1/2^n$

Probability that it comes up heads at least one time =

$$s = 1/2 + 1/4 + 1/8 + 1/16 + \dots$$

$$s = 1/2 + 1/2(1/2 + 1/4 + \dots)$$

Probability that first head appears on n^{th} toss

First try: $1/2$

Second try: $1/2 * 1/2 = 1/4$

Third try: $1/4 * 1/2 = 1/8$

...

n^{th} try: $1/2^n$

Probability that it comes up heads at least one time =

$$s = 1/2 + 1/4 + 1/8 + 1/16 + \dots$$

$$s = 1/2 + 1/2(s)$$

Probability that first head appears on n^{th} toss

First try: $1/2$

Second try: $1/2 * 1/2 = 1/4$

Third try: $1/4 * 1/2 = 1/8$

...

n^{th} try: $1/2^n$

Probability that it comes up heads at least one time =

$$s = 1/2 + 1/4 + 1/8 + 1/16 + \dots$$

$$s = 1/2 + 1/2(s)$$

$$s/2 = 1/2$$

$$s = 1$$

Probability that a grill lights on the n^{th} try

Probability that a grill lights on the n^{th} try

Suppose the probability that it lights on a single try is p

Probability that a grill lights on the n^{th} try

Suppose the probability that it lights on a single try is p

First try: p

Probability that a grill lights on the n^{th} try

Suppose the probability that it lights on a single try is p

First try: p

Second try: $(1-p)p$

Probability that a grill lights on the n^{th} try

Suppose the probability that it lights on a single try is p

First try: p

Second try: $(1-p)p$

Third try: $(1-p)^2p$

Probability that a grill lights on the n^{th} try

Suppose the probability that it lights on a single try is p

First try: p

Second try: $(1-p)p$

Third try: $(1-p)^2p$

Fourth try: $(1-p)^3p$

Probability that a grill lights on the n^{th} try

Suppose the probability that it lights on a single try is p

First try: p

Second try: $(1-p)p$

Third try: $(1-p)^2p$

Fourth try: $(1-p)^3p$

...

Probability that a grill lights on the n^{th} try

Suppose the probability that it lights on a single try is p

First try: p

Second try: $(1-p)p$

Third try: $(1-p)^2p$

Fourth try: $(1-p)^3p$

...

n^{th} try: $(1-p)^{n-1}p$

Probability that a grill lights on the n^{th} try

Suppose the probability that it lights on a single try is p

First try: p

Second try: $(1-p)p$

Third try: $(1-p)^2 p$

Fourth try: $(1-p)^3 p$

...

n^{th} try: $(1-p)^{n-1} p$

Probability that it lights at some point =

$$s = p(1 + (1-p) + (1-p)^2 + \dots)$$

Probability that a grill lights on the n^{th} try

Suppose the probability that it lights on a single try is p

First try: p

Second try: $(1-p)p$

Third try: $(1-p)^2 p$

Fourth try: $(1-p)^3 p$

...

n^{th} try: $(1-p)^{n-1} p$

Probability that it lights at some point =

$$s = p(1 + (1-p) + (1-p)^2 + \dots)$$

$$s = p + (1-p)*p*(1 + (1-p) + (1-p)^2 + \dots)$$

Probability that a grill lights on the n^{th} try

Suppose the probability that it lights on a single try is p

First try: p

Second try: $(1-p)p$

Third try: $(1-p)^2 p$

Fourth try: $(1-p)^3 p$

...

n^{th} try: $(1-p)^{n-1} p$

Probability that it lights at some point =

$$s = p(1 + (1-p) + (1-p)^2 + \dots)$$

$$s = p + (1-p)*p*(1 + (1-p) + (1-p)^2 + \dots)$$

$$s = p + (1-p)*s$$

Probability that a grill lights on the n^{th} try

Suppose the probability that it lights on a single try is p

First try: p

Second try: $(1-p)p$

Third try: $(1-p)^2 p$

Fourth try: $(1-p)^3 p$

...

n^{th} try: $(1-p)^{n-1} p$

Probability that it lights at some point =

$$s = p(1 + (1-p) + (1-p)^2 + \dots)$$

$$s = p + (1-p)*p*(1 + (1-p) + (1-p)^2 + \dots)$$

$$s = p + (1-p)*s$$

$$p*s = p$$

Probability that a grill lights on the n^{th} try

Suppose the probability that it lights on a single try is p

First try: p

Second try: $(1-p)p$

Third try: $(1-p)^2 p$

Fourth try: $(1-p)^3 p$

...

n^{th} try: $(1-p)^{n-1} p$

Probability that it lights at some point =

$$s = p(1 + (1-p) + (1-p)^2 + \dots)$$

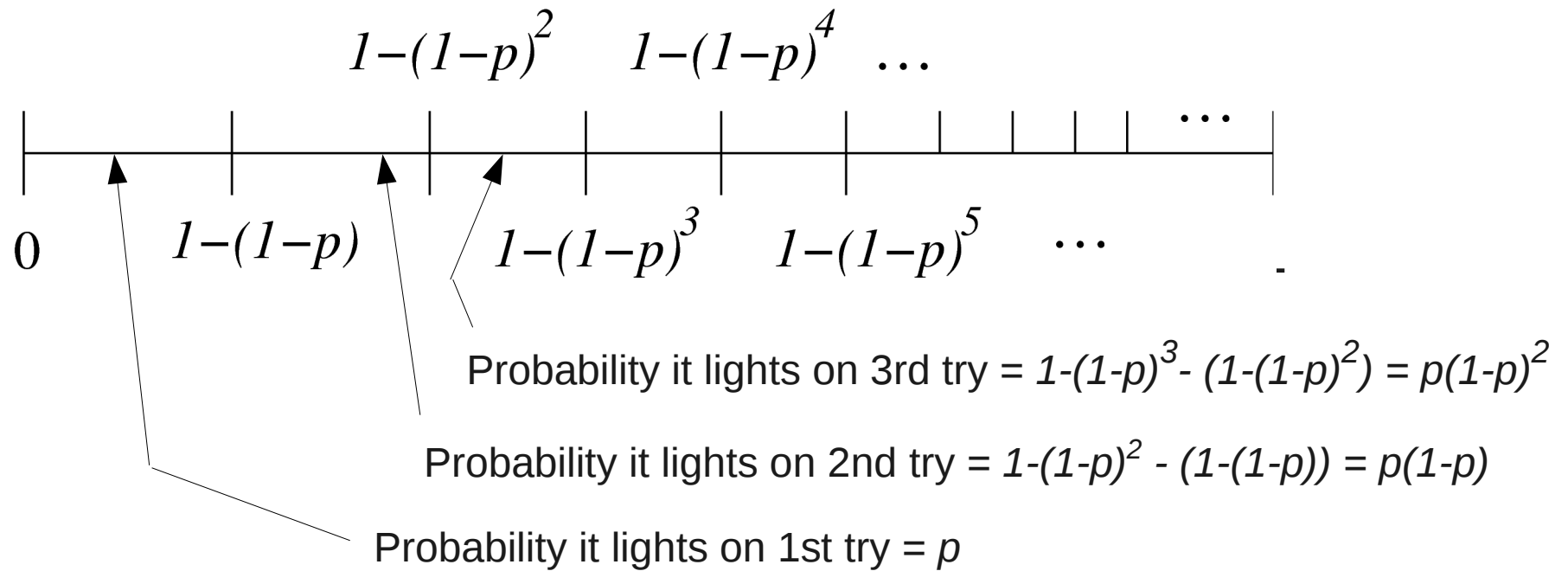
$$s = p + (1-p)*p*(1 + (1-p) + (1-p)^2 + \dots)$$

$$s = p + (1-p)*s$$

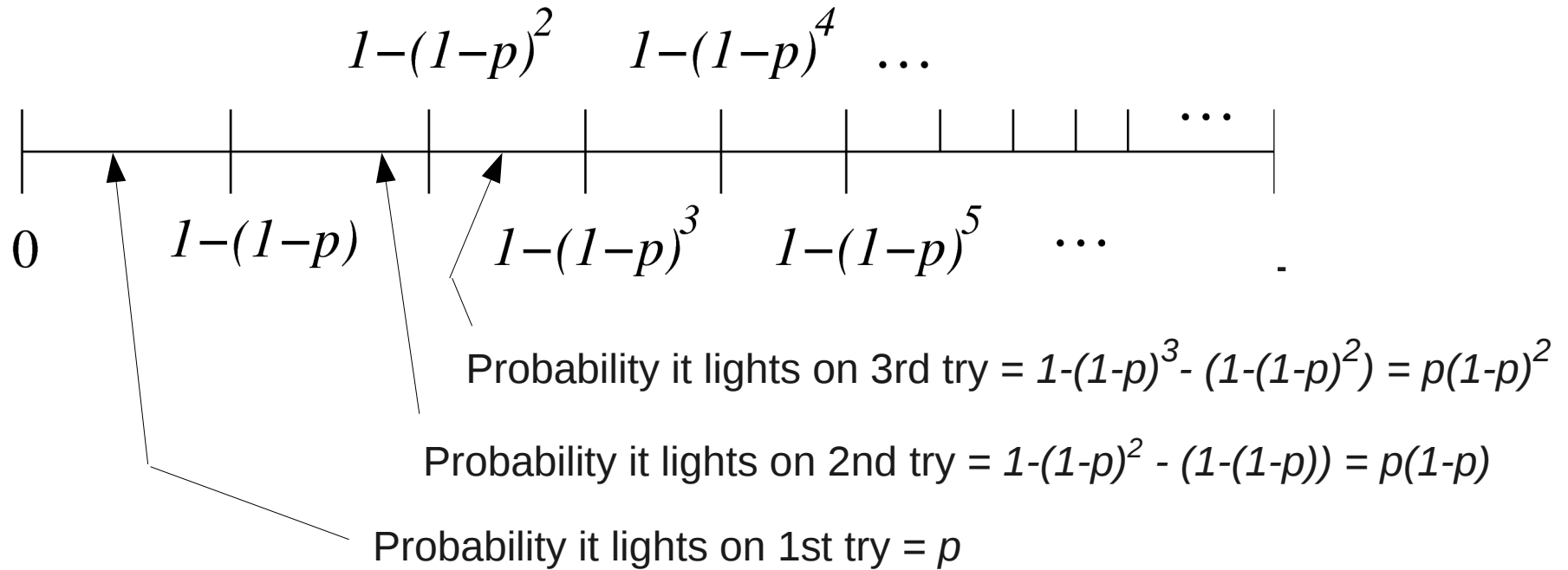
$$p*s = p$$

$$s = 1$$

How do we implement this in Matlab?



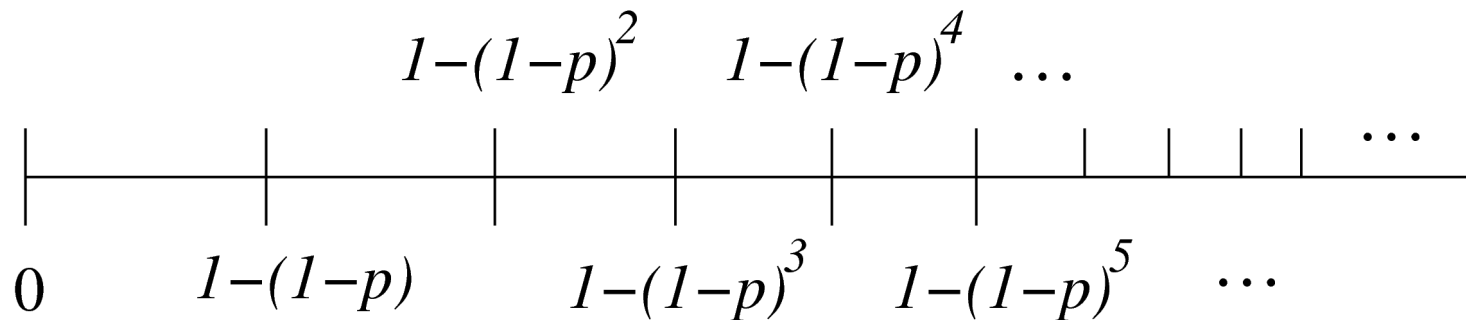
How do we implement this in Matlab?



Code that returns a geometrically distributed random number of mean $1/p$

```
function res = getRand (p)
    s = 1;
    t = rand(1);
    res = 1;
    while !(1-s <= t && t < 1-s*(1-p))
        s = s*(1-p);
        res = res+1;
    end
end
```

How do we implement this in Matlab?



But we use a continuous counterpart of the geometric distribution: if X is a random variable taken from a uniform distribution from 0 to 1, then relate X to n like this -

$$X = 1-(1-p)^n$$

where n is now a real number instead of an integer. Rearrange the equation above to get this:

$$n = \log(1-X)/\log(1-p)$$

The corresponding Matlab expression for generating n is:

```
n = log(rand(1))/log(1-(1/Mean));
```

since `rand(1)` and `1-rand(1)` give the same probabilities and $1/p$ is the **Mean** of the distribution above.