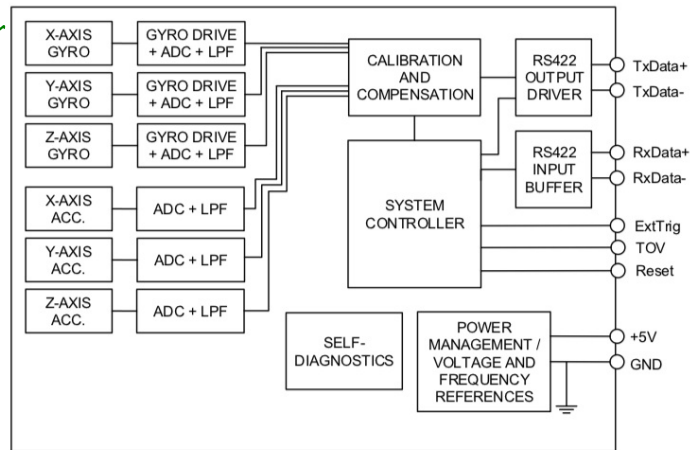


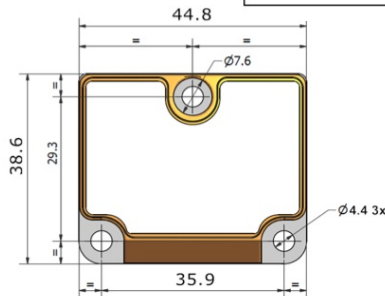
# Unidades Inerciales *3 ax*



FUNCTIONAL BLOCK DIAGRAM

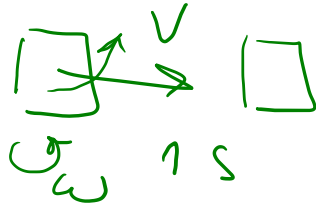
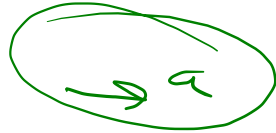


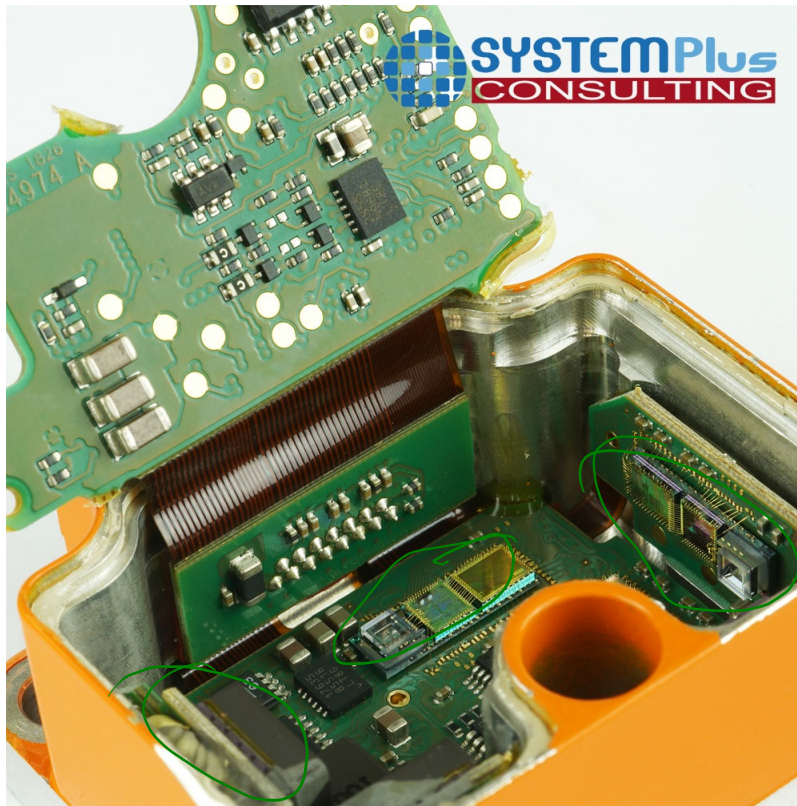
- ITAR free
- Low gyro bias instability ( $0.3^\circ/\text{h}$ )
- Low gyro noise ( $0.15^\circ/\sqrt{\text{h}}$ )
- Low accelerometer bias instability ( $0.003\text{mg}$ )
- Low accelerometer noise ( $0.015 \text{ m/s}/\sqrt{\text{h}}$ )
- $\pm 10\text{g}$  acceleration input range
- User programmable bias trim offset
- Customer configurable output format, sampling rate and filter settings
- Compensated digital output, RS422
- Continuous self-diagnostics
- Solid state - high reliability
- Insensitive to magnetic fields
- Weight:  $< 0.13 \text{ lbs}$  ( $< 57\text{g}$ )
- Volume:  $< 2.2 \text{ cu. in.}$  ( $35\text{cm}^3$ )



GPS  $\rightarrow$  SENSOR EVT.

$\left. \begin{array}{l} VEL \\ Acc. \end{array} \right\}$  SENSOR. intervals





# Unidades Inerciales



Leading Inertial Measurement Unit Price to Performance

Gyro Bias Stability of  $1.08\text{ }^{\circ}/\text{h}$

Accelerometer Bias Stability of  $14.8\text{ }\mu\text{g}$

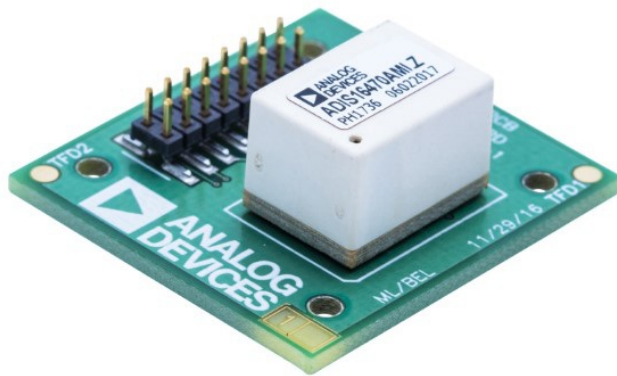
User configurable

No Export License Required

Miniature Package  $1.1 \times 1.1 \times 0.424$  inches,

Light Weight at 20 grams

# Unidades Inerciales



## Triaxial, digital gyroscope

$\pm 125^\circ/\text{sec}$ ,  $\pm 500^\circ/\text{sec}$ ,  $\pm 2000^\circ/\text{sec}$  range models

$2^\circ/\text{hr}$  in-run bias stability (ADIS16475-1)

$0.15^\circ/\sqrt{\text{hr}}$  angle random walk (ADIS16475-1 and ADIS16475-2)

$\pm 0.1^\circ$  axis to axis misalignment error

## Triaxial, digital accelerometer, $\pm 8 g$

$3.6 \mu g$  in-run bias stability

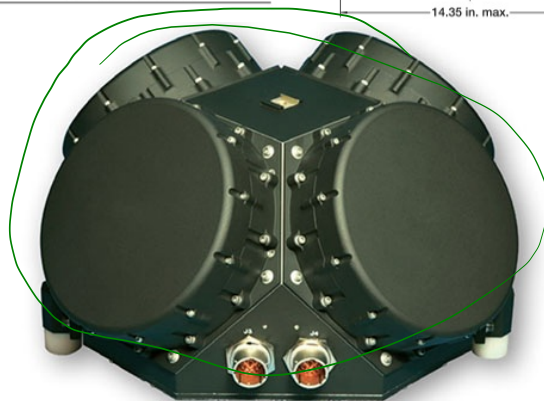
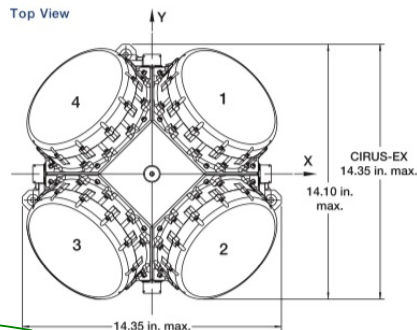
Triaxial, delta angle and delta velocity outputs

Factory calibrated sensitivity, bias, and axial alignment

Calibration temperature range:  $-40^\circ\text{C}$  to  $+85^\circ\text{C}$

# Unidades Inerciales

|                              | CIRUS  | CIRUS-EX   |
|------------------------------|--|--|
| Bias Stability ( $1\sigma$ ) | 0.0003 °/hr.   | 0.0003 °/hr.   |
| Angle Random Walk (EOL)      | 0.000190 °/√hr.<br>( $< 0.000150$ available)           | 0.000125 °/√hr.<br>( $< 0.000100$ available)           |
| Angle White Noise            | 0.000025 arc-sec./√Hz<br>(0.000006 typical)            | 0.000025 arc-sec./√Hz<br>(0.000006 typical)            |
| Angular Rate Range           | $> 30$ °/sec.  | $> 22$ °/sec.  |
| SF Stability                 | $\pm 2$ ppm  | $\pm 2$ ppm  |
| SF Linearity (maximum)       | 35 ppm (3 typical)                                     | 35 ppm (3 typical)                                     |
| Alignment Stability          | $< 3.5$ arc-sec. (long term)<br>$< 20$ arc-sec. (life) | $< 3.5$ arc-sec. (long term)<br>$< 20$ arc-sec. (life) |



$\downarrow g$

~~$\vec{F}$~~   $\rightarrow a$



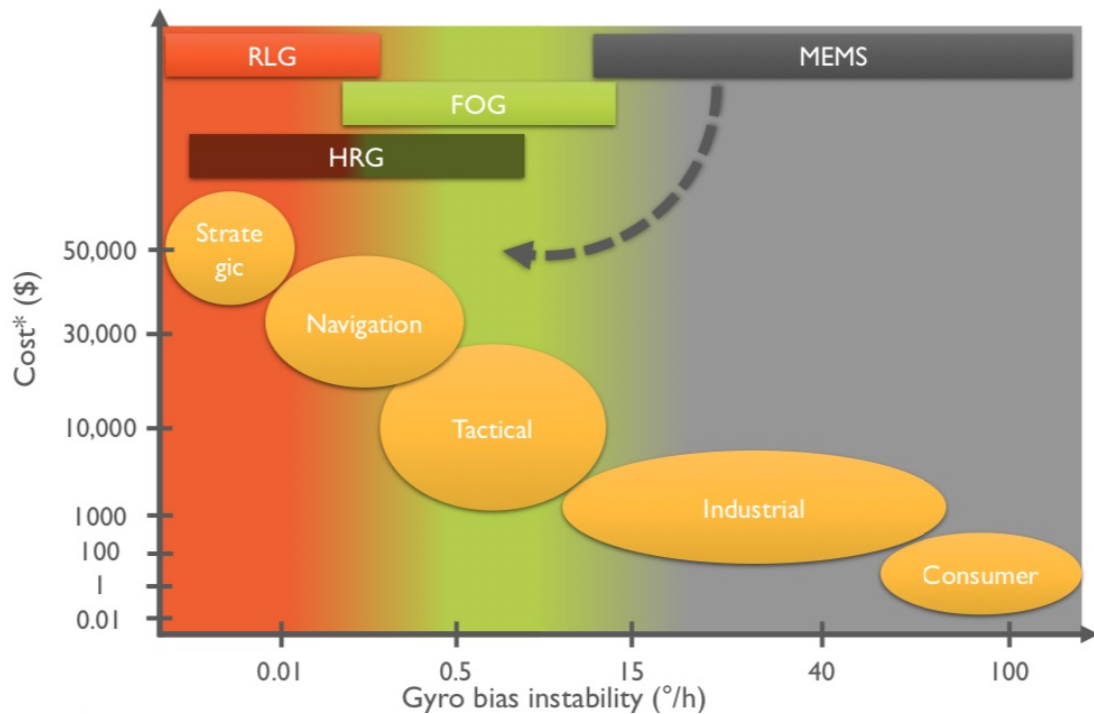
$$\textcircled{a_x} \rightarrow \int a_x = v_x \rightarrow \int v_x = p_x$$

$$\int a_x + \textcircled{v_x} = v_x + v_r$$

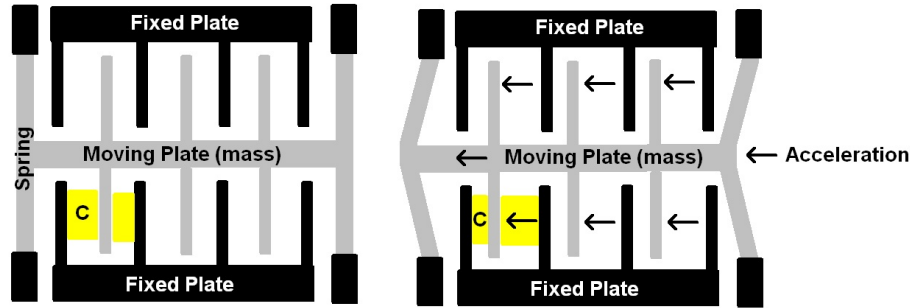
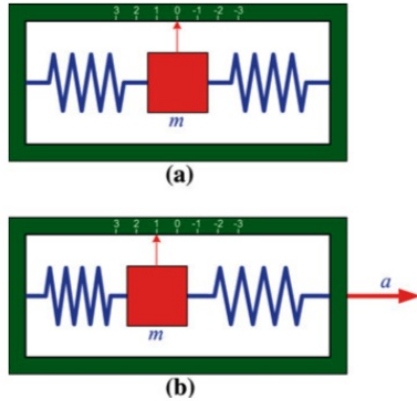
$$\int v_x + v_r = p_x + \textcircled{v_p}$$



# Unidades Inerciales

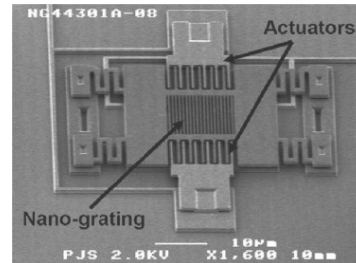


# Acelerómetro



Accelerometer Sensor MEM Mechanism

ElectronicWings.com



# Acelerómetro

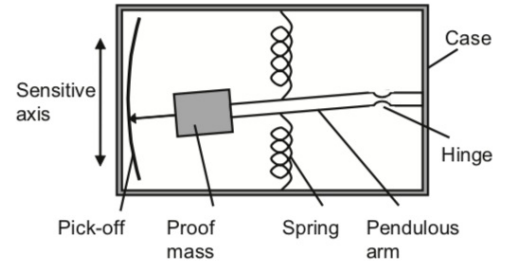
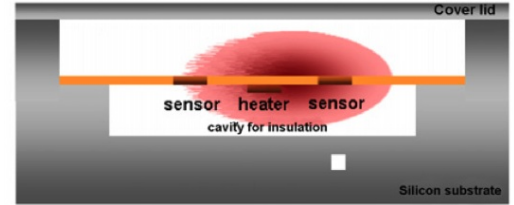
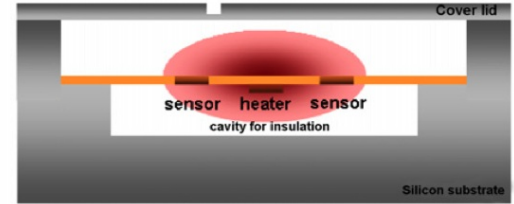
Electromecánico  
Piezoeléctrico

Desplazamiento / reequilibrio  
de masa traslacional / pendular

Frecuencia del elemento resonante

Térmicos

MEMS



## Modelo de Medida Acelerómetro

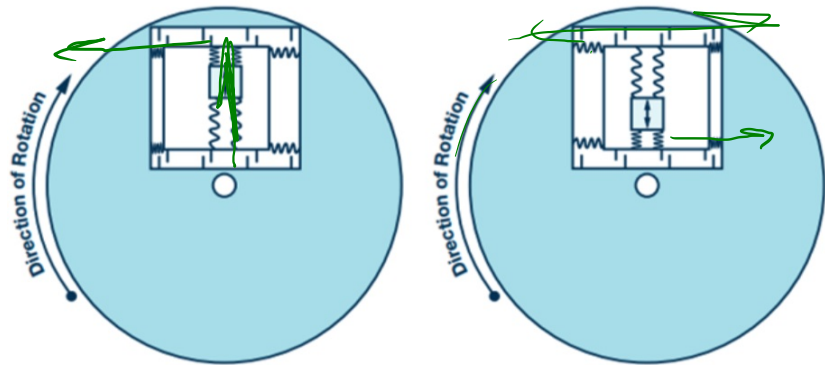
$$\tilde{\mathbf{f}}^b = \mathbf{f}^b + \mathbf{b}_a + S_1 \mathbf{f}^b + S_2 \mathbf{f}^{b^2} + N_a \mathbf{f}^b + \delta_g + \epsilon_a$$

## Calibración Acelerómetro

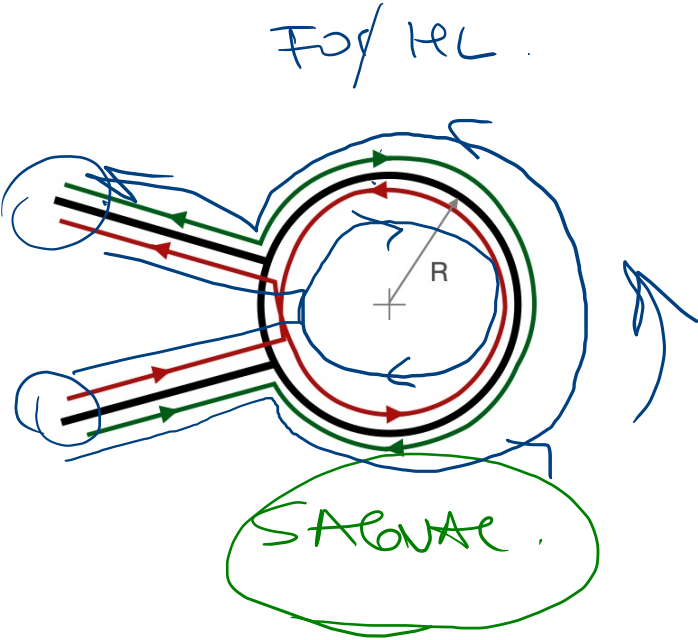
$$\tilde{\mathbf{f}}^b = \mathbf{f}^b + \mathbf{b}_a + S_1 \mathbf{f}^b + S_2 \mathbf{f}^{b^2} + N_a \mathbf{f}^b + \delta_g + \epsilon_a$$

$$f_{\text{up}} = b_a + (1 + S_a)g \quad \text{y} \quad f_{\text{down}} = b_a - (1 + S_a)g$$

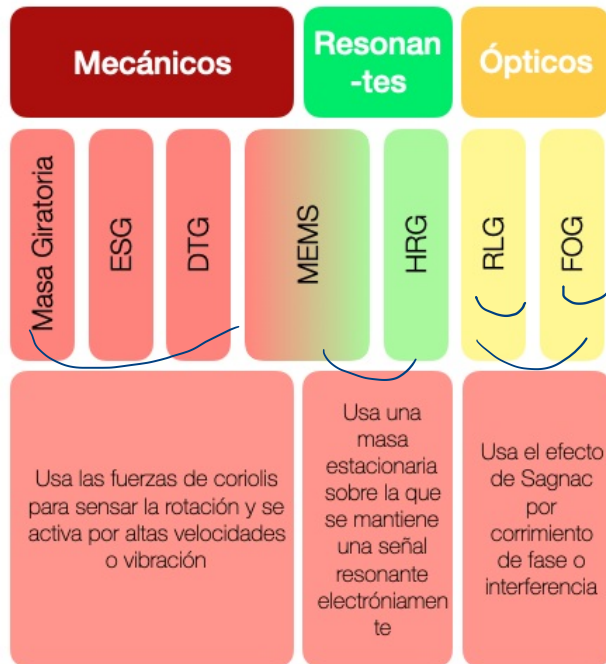
# Giróscopio



Coriolis  
EFFECT



# Giróscopio



## Modelo de Medida Giros

$$\tilde{\omega}_{ib}^b = \omega_{ib}^b + \mathbf{b}_g + \mathbf{S}_g \omega_{ib}^b + \mathbf{N}_g \omega_{ib}^b + \epsilon_g$$



## Calibración Giro

$$\omega_x = 0; \quad \omega_y = \omega_e \cos \phi_{lat}; \quad \omega_z = \omega_e \sin \phi_{lat}$$

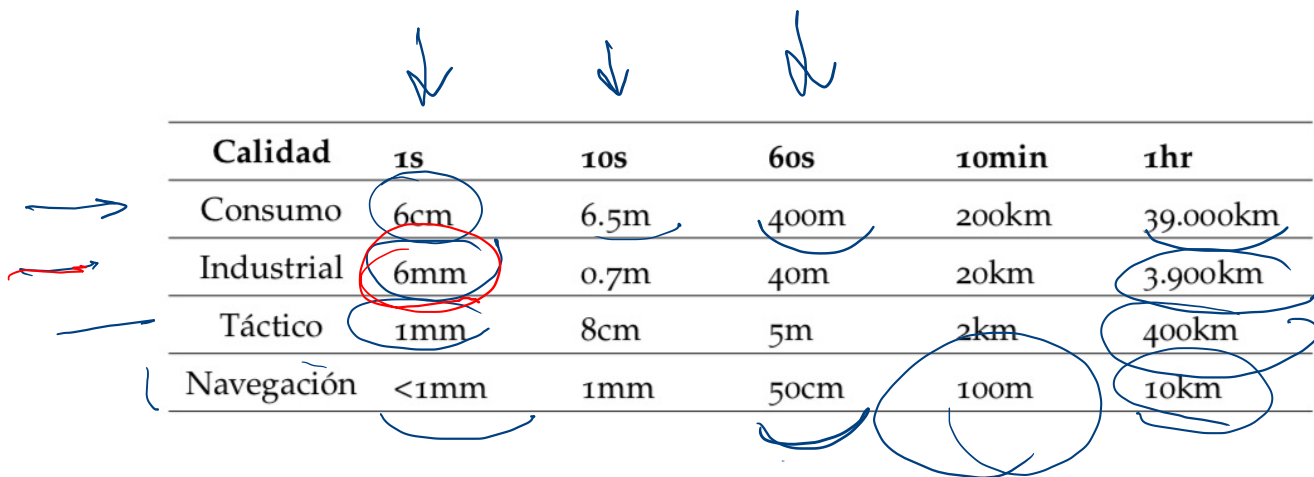
$$\omega_{up} = b_{go} + (1 + S_g) \omega_e \sin \phi_{lat} \quad y \quad \omega_{down} = b_{go} - (1 + S_g) \omega_e \sin \phi_{lat}$$




# IMU

| Calidad    | Costo            | Estabilidad del sesgo del gyro | Tiempo de navegación sin GPS | Aplicaciones |
|------------|------------------|--------------------------------|------------------------------|--------------|
| Consumo    | <\$10            | -                              | -                            | Smartphones  |
| Industrial | \$100-\$1.000    | $< 10^\circ/\text{hora}$       | <1 minuto                    | UAV/UGV      |
| Táctico    | \$5.000-\$50.000 | $< 1^\circ/\text{hora}$        | <10 minutos                  | Municiones   |
| Navegación | \$100.000        | $< 0,1^\circ/\text{hora}$      | Varias horas                 | Militar      |

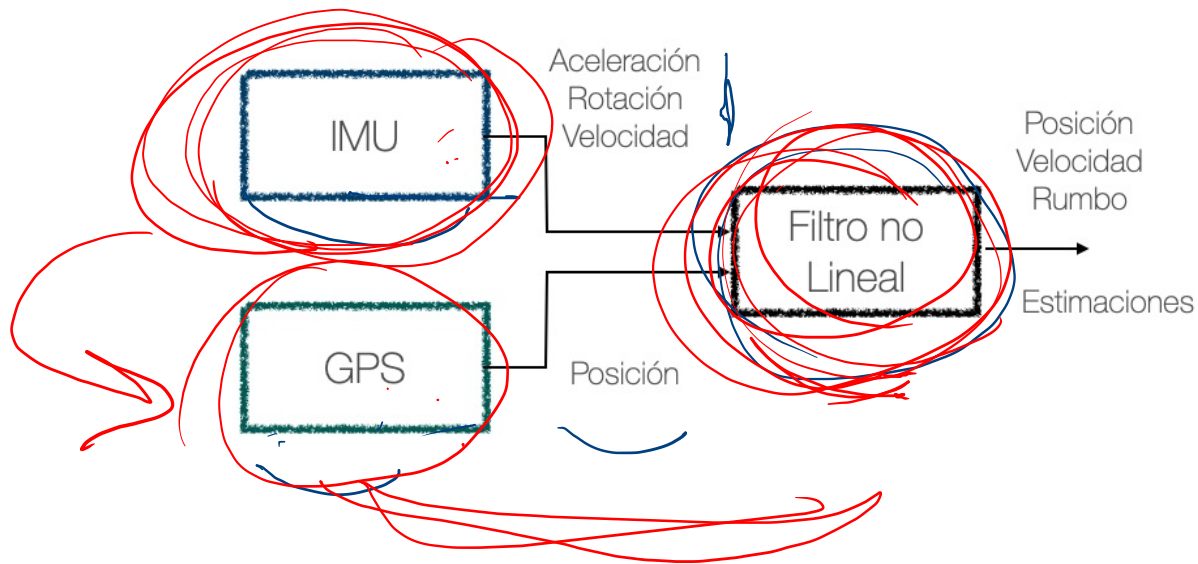
| Calidad    | Sesgo Acelerómetro (mg) | Random Walk de velocidad ( $\text{m/s}/\sqrt{\text{hr}}$ ) | Sesgo Giro (grado/hr) | Random Walk de ángulo ( $\text{grado}/\sqrt{\text{hr}}$ ) |
|------------|-------------------------|--|-----------------------|---|
| Consumo    | 10                      | 1  | 100                   | 2   |
| Industrial | 1                       | 0.1  | 10                    | 0.2   |
| Táctico    | 0.1                     | 0.03   | 1                     | 0.05  |
| Navegación | 0.01                    | 0.01   | 0.01                  | 0.01  |

# IMU



|            |  |  |  |       |          |
|------------|---|---|--|-------|----------|
| Calidad    | 1s  | 10s   | 60s  | 10min | 1hr      |
| Consumo    | 6cm   | 6.5m  | 400m   | 200km | 39.000km |
| Industrial | 6mm   | 0.7m  | 40m  | 20km  | 3.900km  |
| Táctico    | 1mm   | 8cm   | 5m   | 2km   | 400km    |
| Navegación | <1mm  | 1mm   | 50cm   | 100m  | 10km     |

# Integración directa IMU+GPS

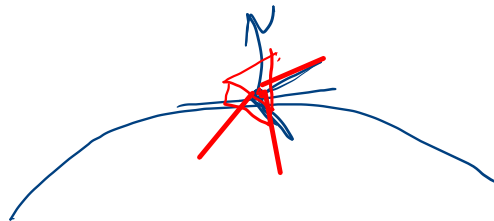
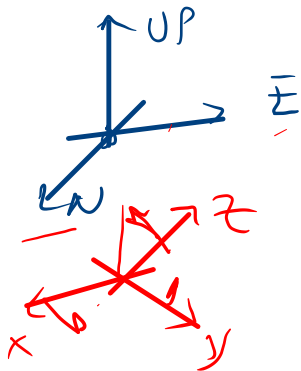


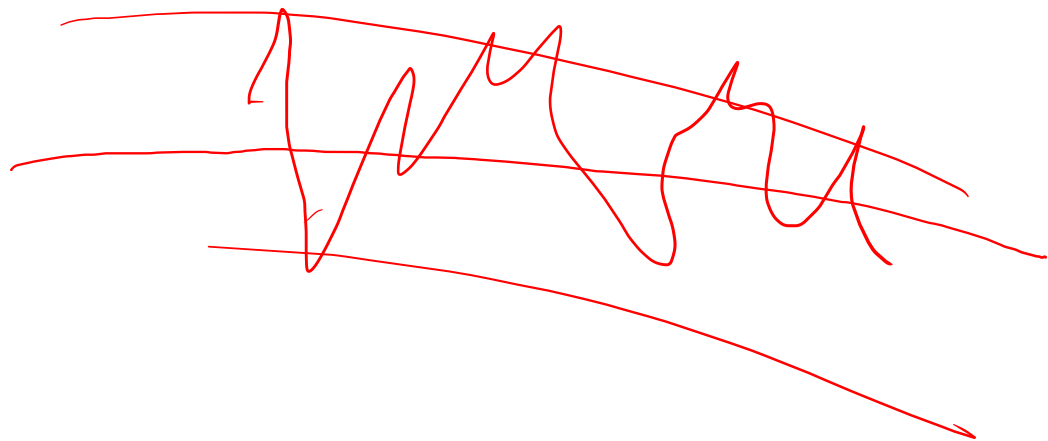
(GPS  
(NAV))

(~~AGE~~  
(INERC))

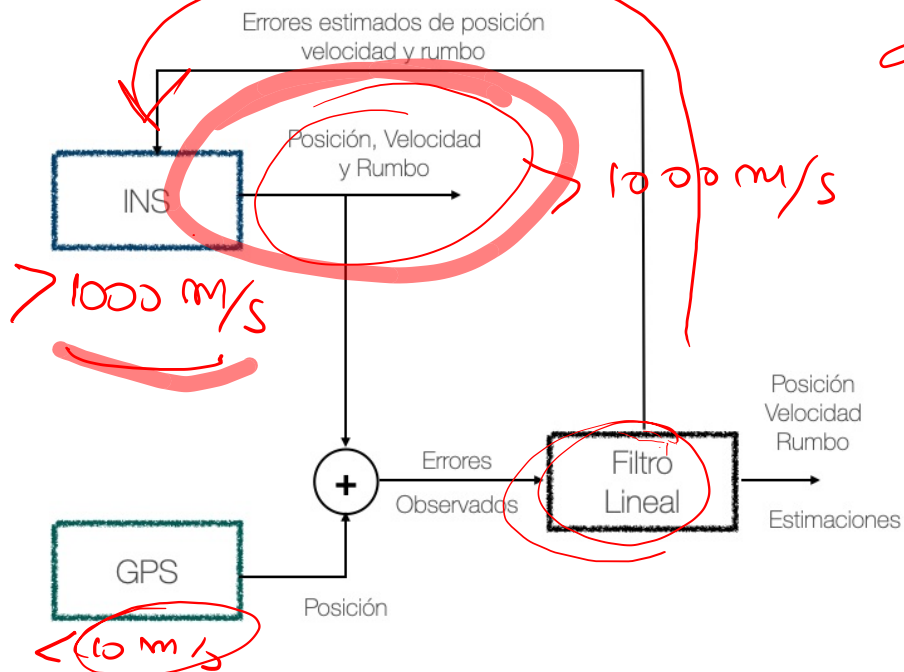
Gyro

$$\begin{aligned} \int \omega_D &= \varphi_D \\ \int \omega_A &= \varphi_A \\ \int \omega_C &= \varphi_C \end{aligned}$$





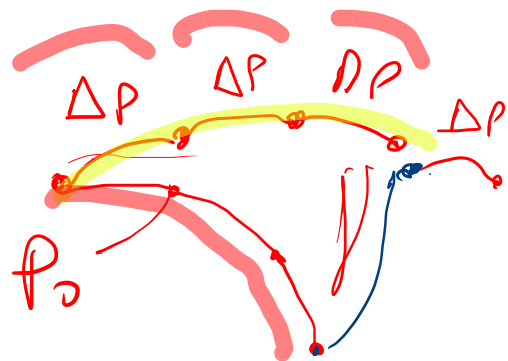
# Integración realimentación directa INS+GPS



$$a \rightarrow \int a = v \rightarrow \int v = p$$

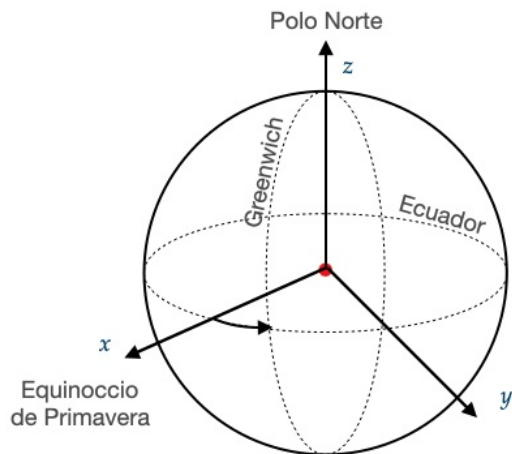
$$\int a_x = \Delta N$$

$$\int \Delta N = \Delta p$$

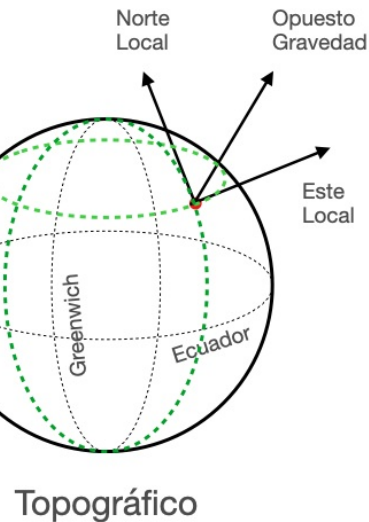
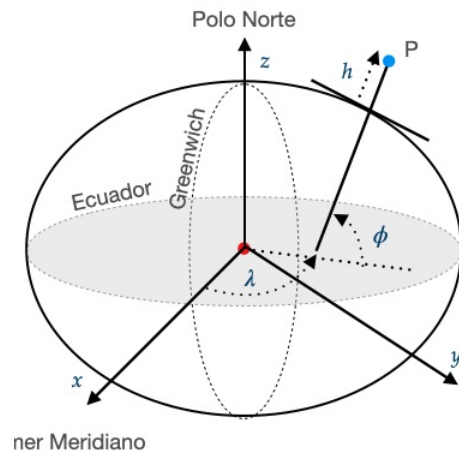




# Marcos de Referencia/Ejes de Referencia



ECI



Topográfico

## Teorema de Coriolis

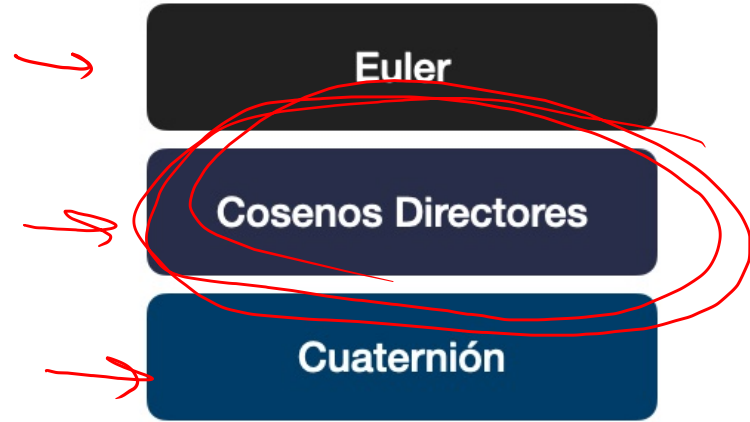
$$\mathbf{v}_i = \mathbf{v}_e + \boldsymbol{\omega}_{ie} \times \mathbf{r}$$

## Navegación en áreas locales (ERN/ERT)

$$\dot{\mathbf{v}}_{e/e} = \dot{\mathbf{v}}_{e/i} - \boldsymbol{\omega}_{ie} \times \mathbf{v}_e$$

$$\dot{\mathbf{v}}_{e/i} = \mathbf{f} - [\boldsymbol{\omega}_{ie} \times \mathbf{v}_e] + [\mathbf{g} - \boldsymbol{\omega}_{ie} \times [\boldsymbol{\omega}_{ie} \times \mathbf{r}]]$$

# Propagación de la matriz de Transformación



invariant: body  
NAUT.

# Matriz de Cosenos Directores

$$\mathbf{C}_{b}^n = \begin{bmatrix} \gamma_c & -\gamma_s & 0 \\ \gamma_s & \gamma_c & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \beta_c & 0 & \beta_s \\ 0 & 1 & 0 \\ -\beta_s & 0 & \beta_c \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & \theta_c & -\theta_s \\ 0 & \theta_s & \theta_c \end{bmatrix}$$

$$= \begin{bmatrix} \beta_c \gamma_c & -\theta_c \gamma_s + \theta_s \beta_s \gamma_c & \theta_s \gamma_s + \theta_c \beta_s \gamma_c \\ \beta_c \gamma_s & \theta_c \gamma_c + \theta_s \beta_s \gamma_s & -\theta_s \gamma_c + \theta_c \beta_s \gamma_s \\ -\beta_s & \theta_s \beta_c & \theta_c \beta_c \end{bmatrix}$$

$$\mathbf{C}_b^N \mathbf{f}_b = \mathbf{f}_N$$

$$\mathbf{f}_b = \begin{bmatrix} a_x \\ a_y \\ a_z \end{bmatrix}$$

$$\beta_c = \cos \beta$$

$$\beta_s = \sin \beta$$

$$\gamma_s = \sin \gamma$$

$$\gamma_c = \cos \gamma$$

$$f_N = \begin{bmatrix} a_E \\ a_N \\ a_u \end{bmatrix} \rightarrow \begin{matrix} \kappa_E \\ \kappa_N \\ \kappa_u \end{matrix} \rightarrow \begin{matrix} p_E \\ p_N \\ p_u \end{matrix}$$

## Matriz de Cosenos Directores

$$\mathbf{f}_n = \mathbf{C}_b^n(i+1)\mathbf{f}_b$$
