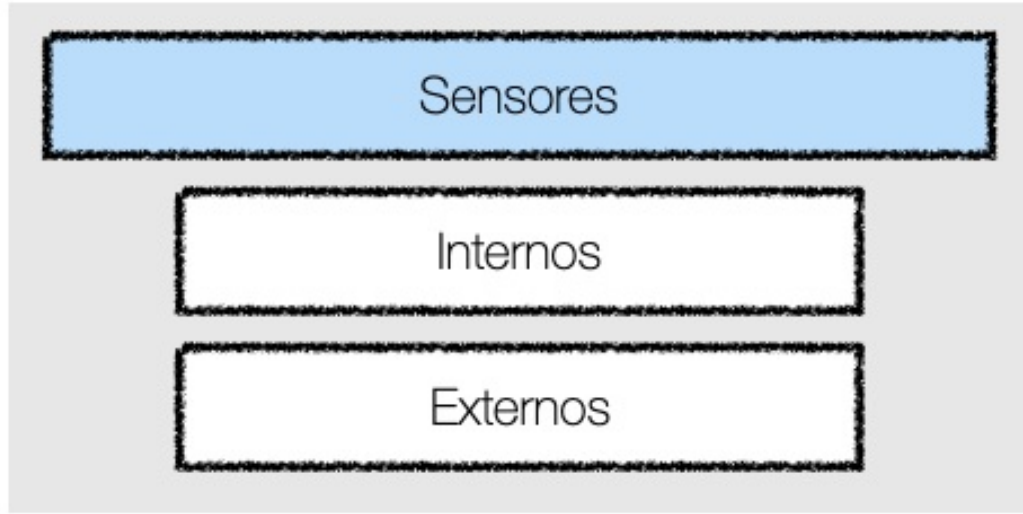
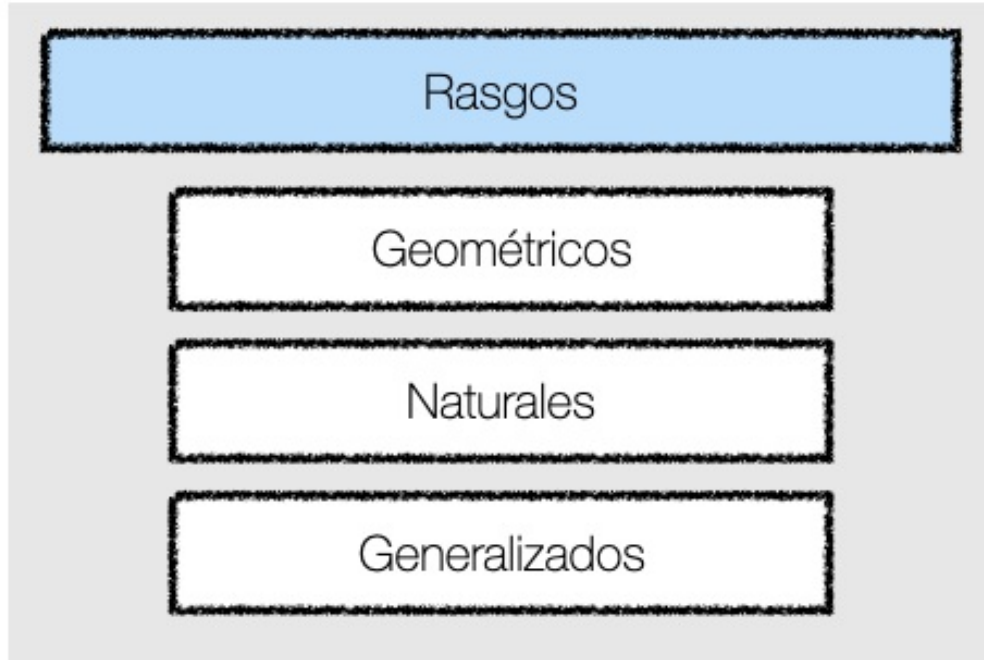


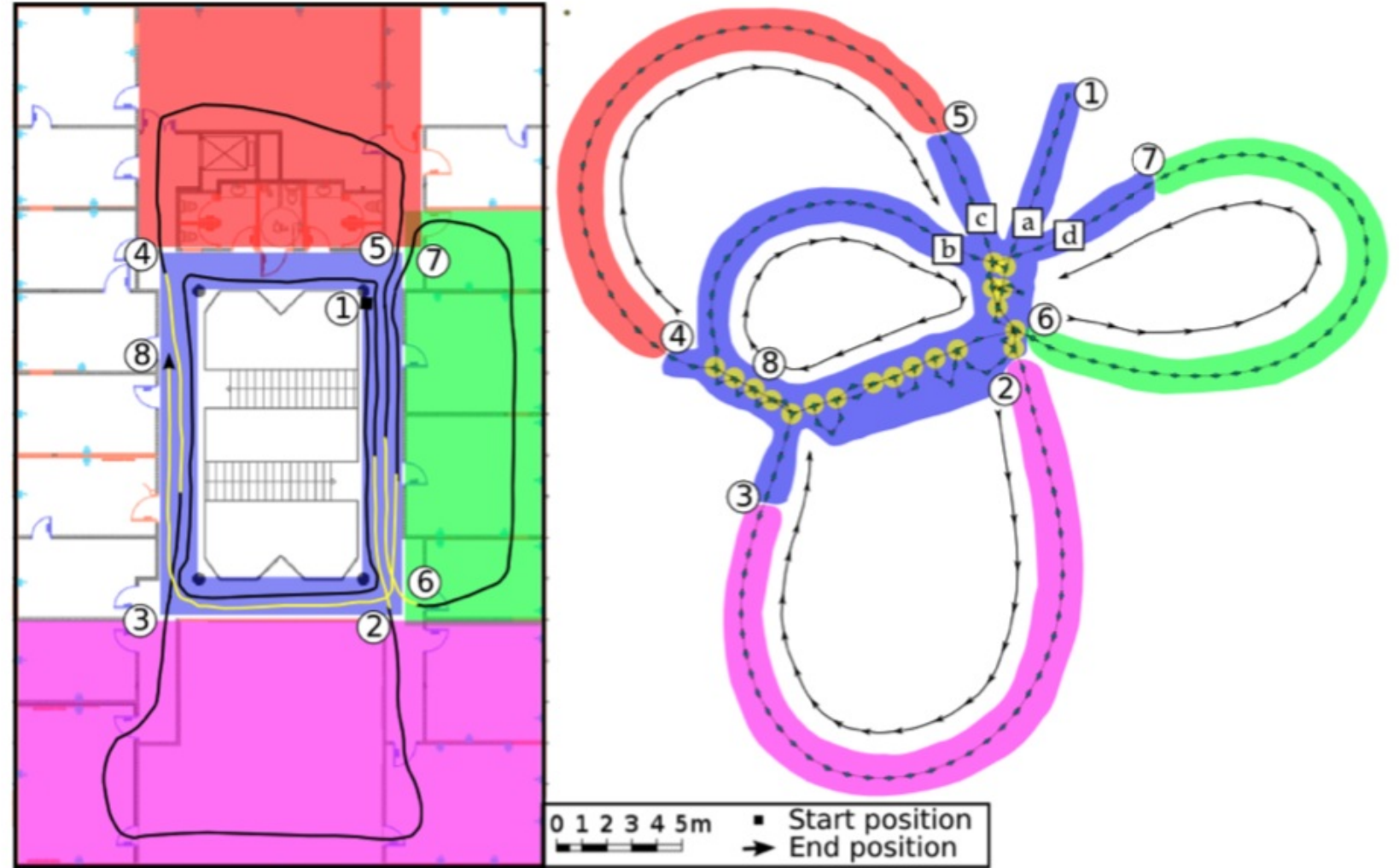
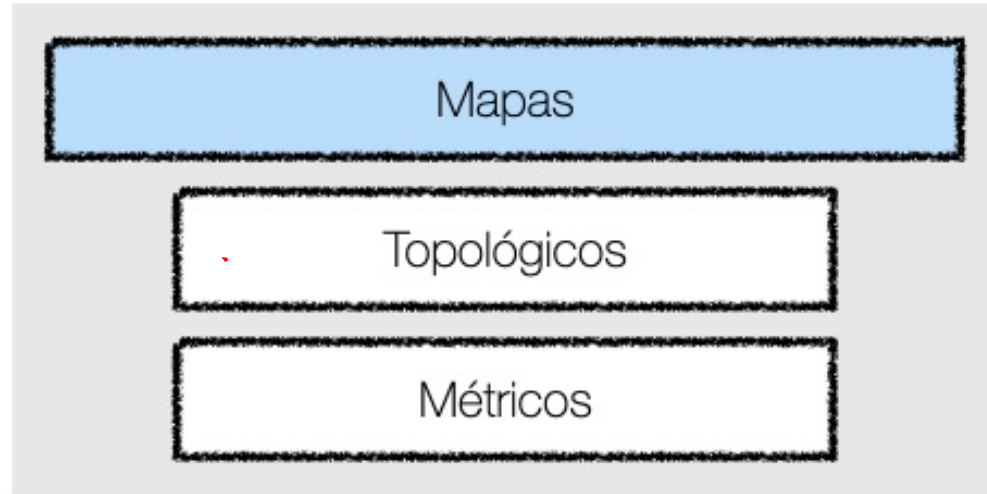
# Sensores



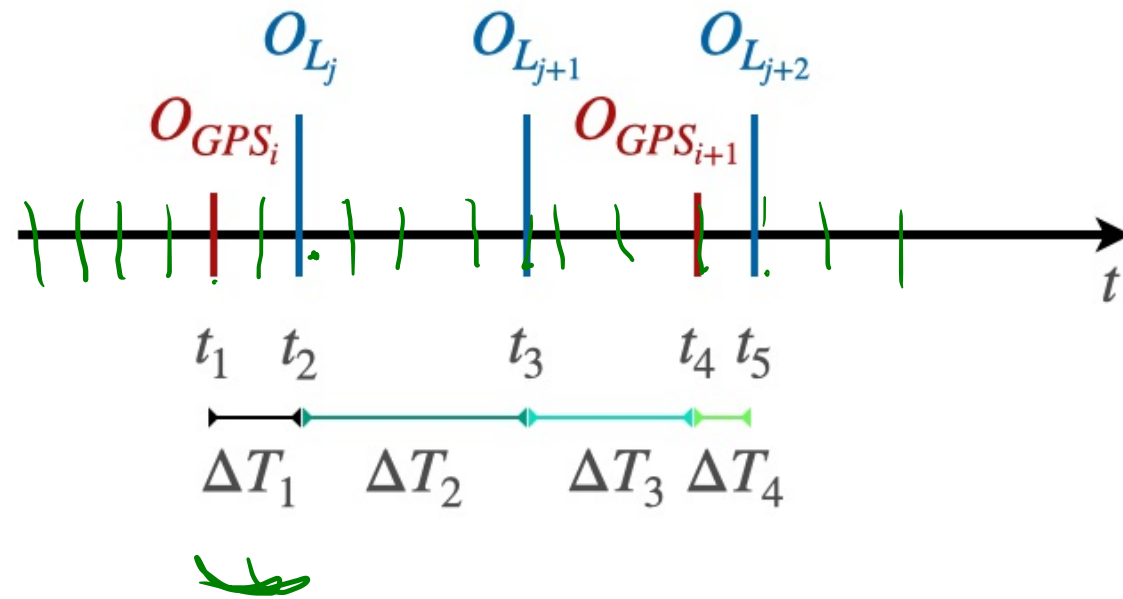
# Rasgos



# Mapas



# Integración GPS con otros sensores externos



# Predicción

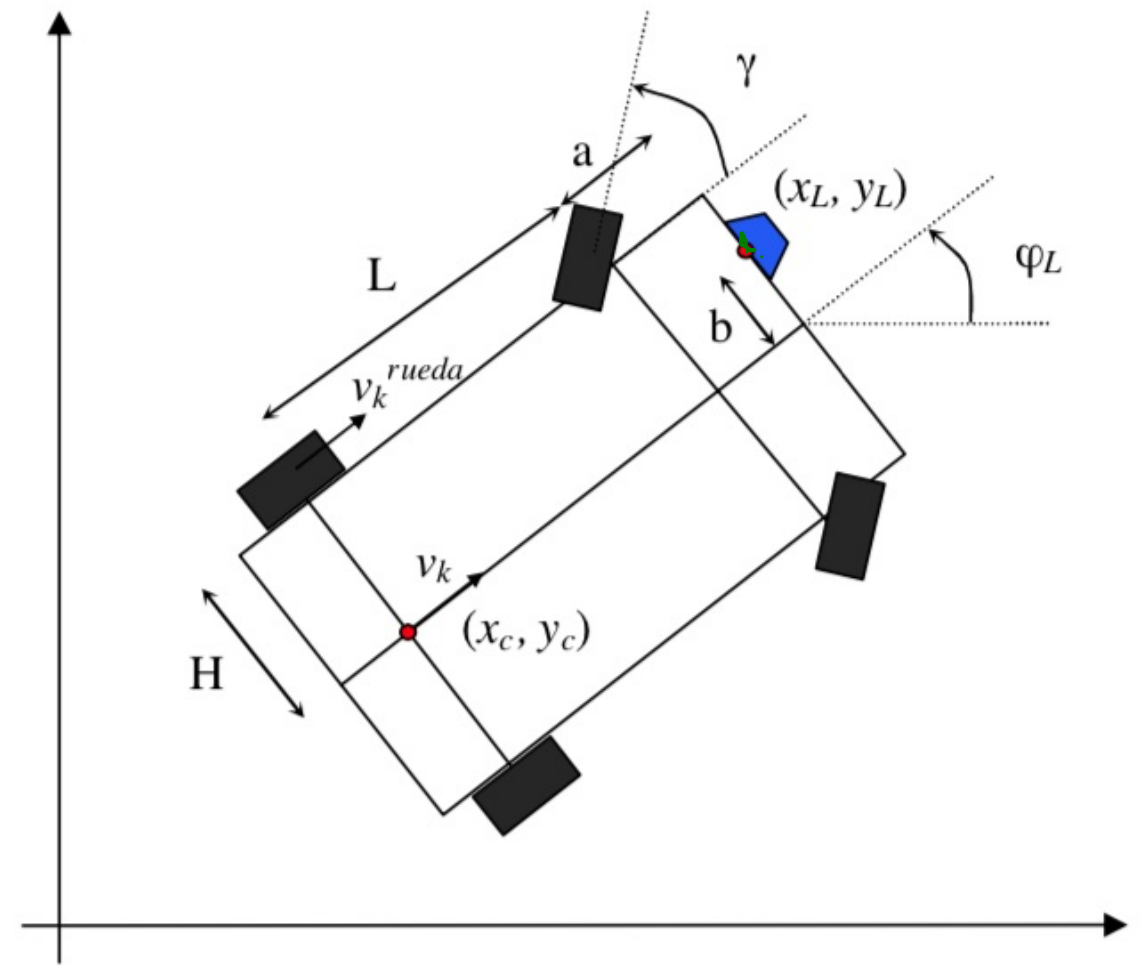
$$\hat{\mathbf{x}}_{k|k-1} = \mathbf{f}[\hat{\mathbf{x}}_{k-1|k-1}, \mathbf{u}_k]$$

$$\mathbf{P}_{k|k-1} = \nabla \mathbf{f}_x \mathbf{P}_{k-1|k-1} \nabla \mathbf{f}_x^T + \nabla \mathbf{f}_u \mathbf{U}_k \nabla \mathbf{f}_x^T + \mathbf{Q}_k$$

$$\mathbb{G} = \left( 1 - \frac{b \tan(\gamma_k)}{L} \right)$$

$$\mathbb{H} = \frac{(L + a) \tan(\gamma_k)}{L}$$

$$\begin{bmatrix} x_{Lk} \\ y_{Lk} \\ \varphi_{Lk} \end{bmatrix} = \begin{bmatrix} x_{Lk-1} + \Delta t \cdot v_k \cdot [\mathbb{G} \cos(\varphi_{Lk-1}) - \mathbb{H} \sin(\varphi_{Lk-1})] \\ y_{Lk-1} + \Delta t \cdot v_k \cdot [\mathbb{G} \sin(\varphi_{Lk-1}) + \mathbb{H} \cos(\varphi_{Lk-1})] \\ \varphi_{Lk-1} + \Delta t \cdot \frac{v_k}{L} \cdot \tan(\gamma_k) \end{bmatrix}$$



# Predicción

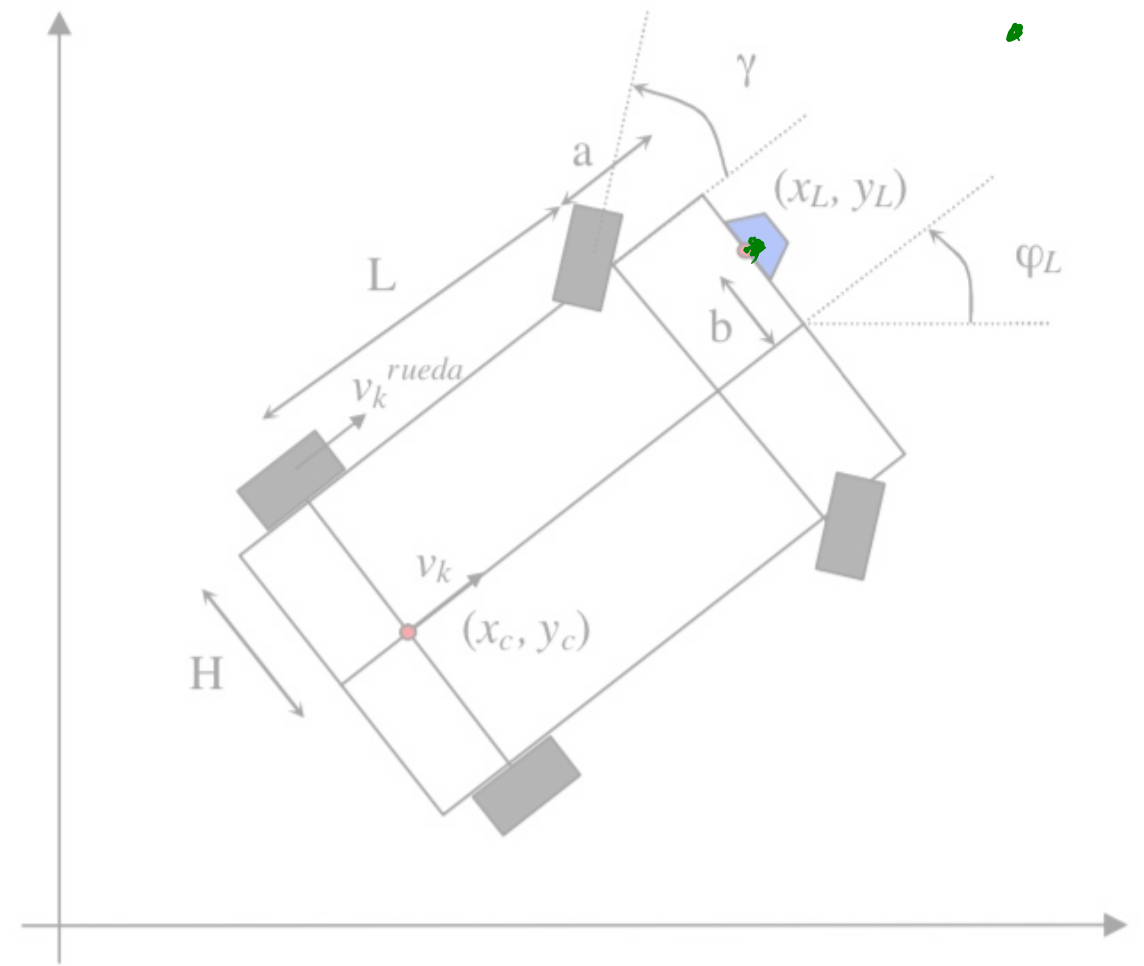
$$\hat{\mathbf{x}}_{k|k-1} = \mathbf{f}[\hat{\mathbf{x}}_{k-1|k-1}, \mathbf{u}_k]$$

$$\mathbf{P}_{k|k-1} = \nabla \mathbf{f}_x \mathbf{P}_{k-1|k-1} \nabla \mathbf{f}_x^T + \nabla \mathbf{f}_u \mathbf{U}_k \nabla \mathbf{f}_x^T + \mathbf{Q}_k$$

$$\mathbb{G} = \left( 1 - \frac{b \tan(\gamma_k)}{L} \right)$$

$$\mathbb{H} = \frac{(L + a) \tan(\gamma_k)}{L}$$

$$\begin{bmatrix} x_{Lk} \\ y_{Lk} \\ \varphi_{Lk} \end{bmatrix} = \begin{bmatrix} x_{Lk-1} + \Delta t \cdot v_k \cdot [\mathbb{G} \cos(\varphi_{Lk-1}) - \mathbb{H} \sin(\varphi_{Lk-1})] \\ y_{Lk-1} + \Delta t \cdot v_k \cdot [\mathbb{G} \sin(\varphi_{Lk-1}) + \mathbb{H} \cos(\varphi_{Lk-1})] \\ \varphi_{Lk-1} + \Delta t \cdot \frac{v_k}{L} \cdot \tan(\gamma_k) \end{bmatrix}$$



# Predicción

$$\hat{\mathbf{x}}_{k|k-1} = \mathbf{f}[\hat{\mathbf{x}}_{k-1|k-1}, \mathbf{u}_k]$$

$$\mathbf{P}_{k|k-1} = \nabla \mathbf{f}_x \mathbf{P}_{k-1|k-1} \nabla \mathbf{f}_x^T + \nabla \mathbf{f}_u \mathbf{U}_k \nabla \mathbf{f}_x^T + \mathbf{Q}_k$$

$$\nabla \mathbf{f}_x = \begin{bmatrix} 1 & 0 & -\Delta t \cdot v_k \cdot [\mathbb{G} \sin(\varphi_{L_{k-1}}) - \mathbb{H} \cos(\varphi_{L_{k-1}})] \\ 0 & 1 & \Delta t \cdot v_k \cdot [\mathbb{G} \cos(\varphi_{L_{k-1}}) + \mathbb{H} \sin(\varphi_{L_{k-1}})] \\ 0 & 0 & 1 \end{bmatrix}$$

$$\mathbb{A} = \mathbb{G} \cos(\varphi_{L_{k-1}}) - \mathbb{H} \sin(\varphi_{L_{k-1}})$$

$$\mathbb{B} = \mathbb{G} \sin(\varphi_{L_{k-1}}) + \mathbb{H} \cos(\varphi_{L_{k-1}})$$

$$\mathbb{C} = -b \cos(\varphi_{L_{k-1}}) - (L + a) \sin(\varphi_{L_{k-1}})$$

$$\mathbb{D} = -b \sin(\varphi_{L_{k-1}}) + (L + a) \cos(\varphi_{L_{k-1}})$$

$$L = 2,38\text{m}$$

$$a = 0,95\text{m}$$

$$b = 0,5\text{m}$$

$$H = 0,75\text{m}$$

$$\nabla \mathbf{f}_u = \begin{bmatrix} \frac{\Delta t \cdot \mathbb{A}}{1 - \frac{H}{L} \tan(\gamma_k)} & \frac{\Delta t \cdot v_k^{\text{rueda}} \cdot \frac{H}{L} \cdot \mathbb{A}}{\left(1 - \frac{H}{L} \tan(\gamma_k)\right)^2 \cdot \cos^2(\gamma_k)} + \frac{\Delta t \cdot v_k \mathbb{C}}{L \cos^2(\gamma_k)} \\ \frac{\Delta t \cdot \mathbb{B}}{1 - \frac{H}{L} \tan(\gamma_k)} & \frac{\Delta t \cdot v_k^{\text{rueda}} \cdot \frac{H}{L} \cdot \mathbb{B}}{\left(1 - \frac{H}{L} \tan(\gamma_k)\right)^2 \cdot \cos^2(\gamma_k)} + \frac{\Delta t \cdot v_k \mathbb{D}}{L \cos^2(\gamma_k)} \\ \frac{\Delta t \cdot \tan(\gamma_k)}{L \cdot \left(1 - \frac{H}{L} \tan(\gamma_k)\right)} & \frac{\Delta t \cdot v_k^{\text{rueda}} \cdot \frac{H}{L} \cdot \tan(\gamma_k)}{L \cdot \left(1 - \frac{H}{L} \tan(\gamma_k)\right)^2 \cdot \cos^2(\gamma_k)} + \frac{\Delta t \cdot v_k}{L \cos^2(\gamma_k)} \end{bmatrix}$$



# Actualización Laser

$$\hat{\mathbf{x}}_{k|k} = \hat{\mathbf{x}}_{k|k-1} + \mathbf{W}_k (\mathbf{z}_k - \mathbf{h}[\hat{\mathbf{x}}_{k|k-1}])$$

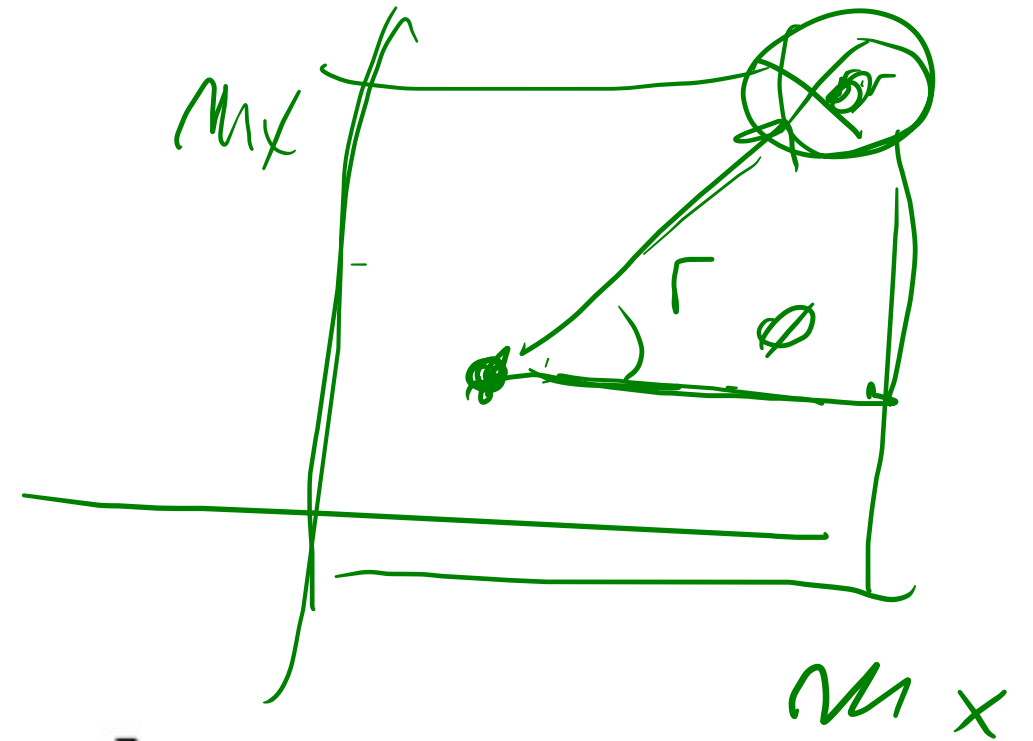
$$\mathbf{P}_{k|k} = \mathbf{P}_{k|k-1} - \mathbf{W}_k \mathbf{S}_k \mathbf{W}_k^T$$

$$\mathbf{W}_k = \mathbf{P}_{k|k-1} \nabla \mathbf{h}_x^T \mathbf{S}_k^{-1}$$

$$\mathbf{S}_k = \nabla \mathbf{h}_x \mathbf{P}_{k|k-1} \nabla \mathbf{h}_x^T + \mathbf{R}_k$$

$$\mathbf{h}[\hat{\mathbf{x}}_{k|k-1}] = \begin{bmatrix} \cos(\varphi_{Lk-1}) & -\sin(\varphi_{Lk-1}) \\ \sin(\varphi_{Lk-1}) & \cos(\varphi_{Lk-1}) \end{bmatrix} \cdot \begin{bmatrix} m_{xi} - x_L \\ m_{yi} - y_L \end{bmatrix}$$

$$\mathbf{z}_k = \begin{bmatrix} z_{x,k} \\ z_{y,k} \end{bmatrix} = \begin{bmatrix} z_{r,k} \cos(z_{\theta,k}) \\ z_{r,k} \sin(z_{\theta,k}) \end{bmatrix}$$





# Actualización Laser

$$\mathbf{W}_k = \mathbf{P}_{k|k-1} \nabla \mathbf{h}_x^T \mathbf{S}_k^{-1}$$

$$\mathbf{S}_k = \nabla \mathbf{h}_x \mathbf{P}_{k|k-1} \nabla \mathbf{h}_x^T + \mathbf{R}_k$$

$$\nabla \mathbf{h}_x = \begin{bmatrix} -\cos(\varphi_{Lk-1}) & -\text{sen}(\varphi_{Lk-1}) & \mathbb{K}_1 \\ \text{sen}(\varphi_{Lk-1}) & -\cos(\varphi_{Lk-1}) & \mathbb{K}_2 \end{bmatrix}$$

$$h = \begin{bmatrix} 0 & 0 \\ 0 & 1 \end{bmatrix}$$

$$\begin{aligned} \mathbb{K}_1 &= -(m_{xi} - x_L) \text{sen}(\varphi_{Lk-1}) + (m_{yi} - y_L) \cos(\varphi_{Lk-1}) \\ \mathbb{K}_2 &= (m_{xi} - x_L) \cos(\varphi_{Lk-1}) - (m_{yi} - y_L) \text{sen}(\varphi_{Lk-1}) \end{aligned}$$

$$\mathbf{R}_k = \nabla \mathbf{z}_{z_r, k, z_{\theta, k}} \cdot \begin{bmatrix} \sigma_{z_r, k}^2 & 0 \\ 0 & \sigma_{z_{\theta, k}}^2 \end{bmatrix} \cdot \nabla \mathbf{z}_{z_r, k, z_{\theta, k}}^T$$

$$\nabla \mathbf{z}_{z_r, k, z_{\theta, k}} = \begin{bmatrix} \cos(z_{\theta, k}) & -z_{r, k} \text{sen}(z_{\theta, k}) \\ \text{sen}(z_{\theta, k}) & z_{r, k} \cos(z_{\theta, k}) \end{bmatrix}$$

# Actualización GPS

$$\hat{\mathbf{x}}_{k|k} = \hat{\mathbf{x}}_{k|k-1} + \mathbf{W}_k (\mathbf{z}_k - \mathbf{h}[\hat{\mathbf{x}}_{k|k-1}])$$

$$\mathbf{P}_{k|k} = \mathbf{P}_{k|k-1} - \mathbf{W}_k \mathbf{S}_k \mathbf{W}_k^T$$

$$\mathbf{W}_k = \mathbf{P}_{k|k-1} \nabla \mathbf{h}_x^T \mathbf{S}_k^{-1}$$

$$\mathbf{S}_k = \underbrace{\nabla \mathbf{h}_x \mathbf{P}_{k|k-1}} \underbrace{\nabla \mathbf{h}_x^T} + \mathbf{R}_k$$

[60]

$$\mathbf{z}_k = \begin{bmatrix} z_{x,k} \\ z_{y,k} \end{bmatrix}$$

$$\mathbf{h}[\hat{\mathbf{x}}_{k|k-1}] = \begin{bmatrix} \hat{x}_{L_{k|k-1}} \\ \hat{y}_{L_{k|k-1}} \end{bmatrix}$$

# Resultado

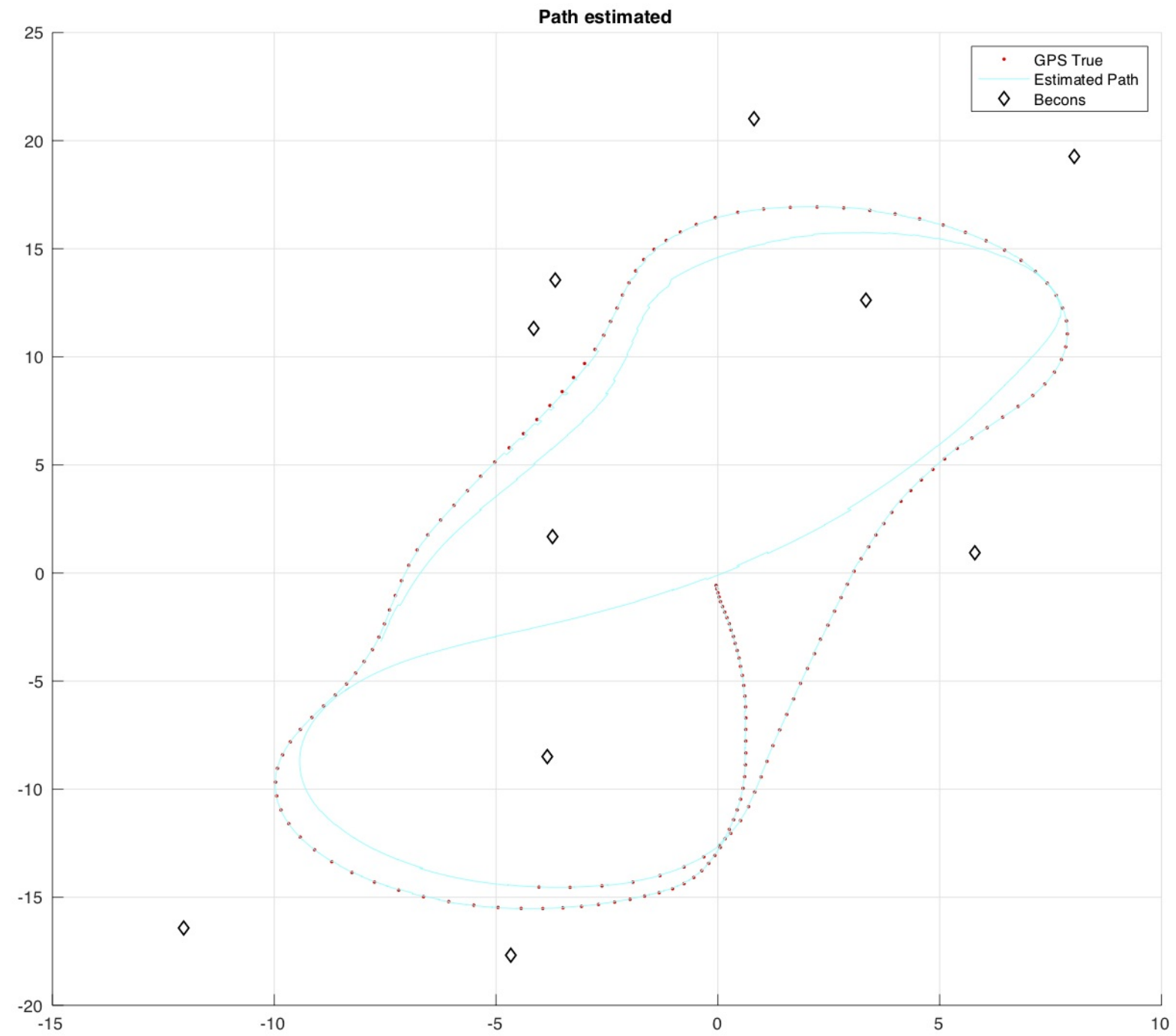




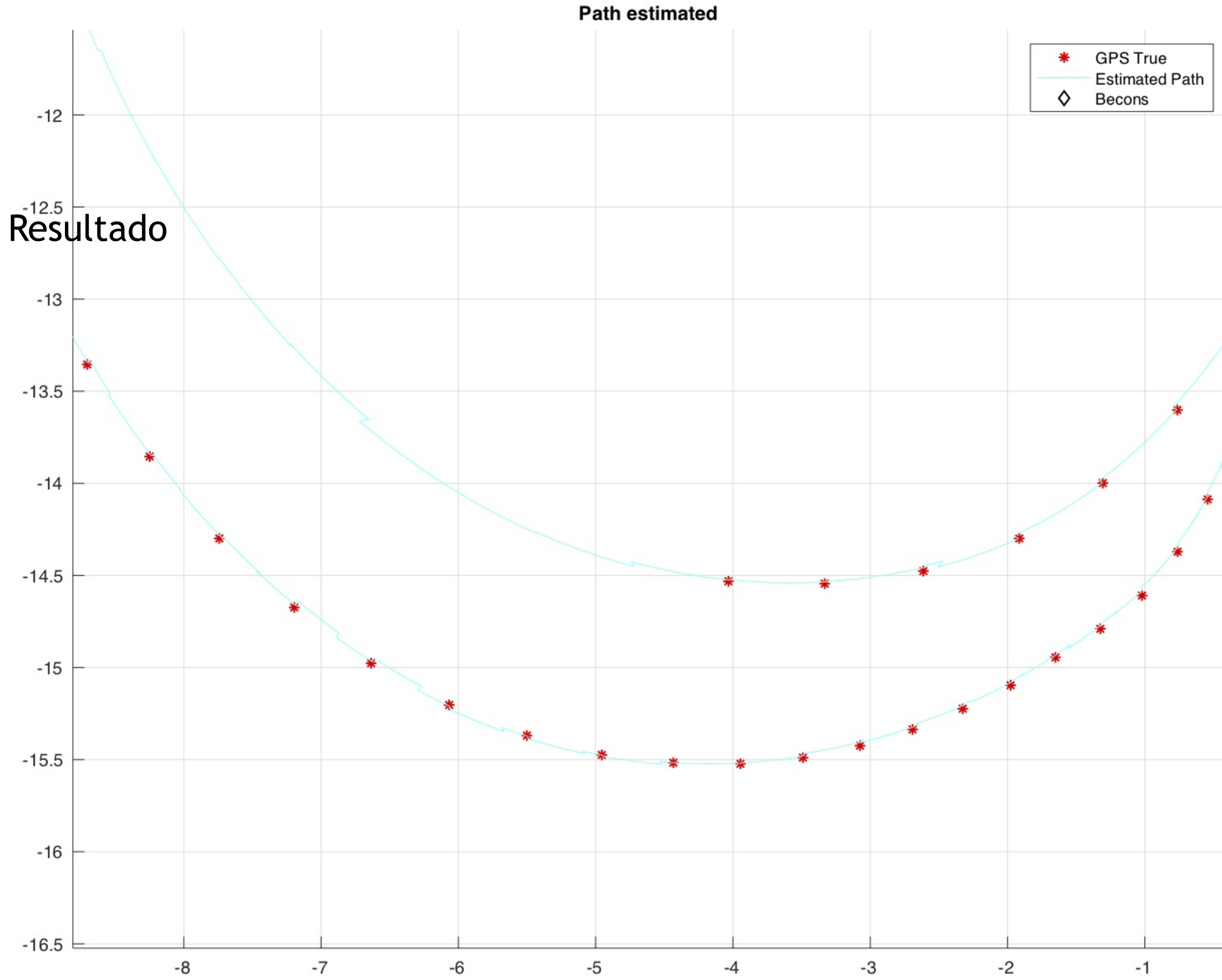
Resultado



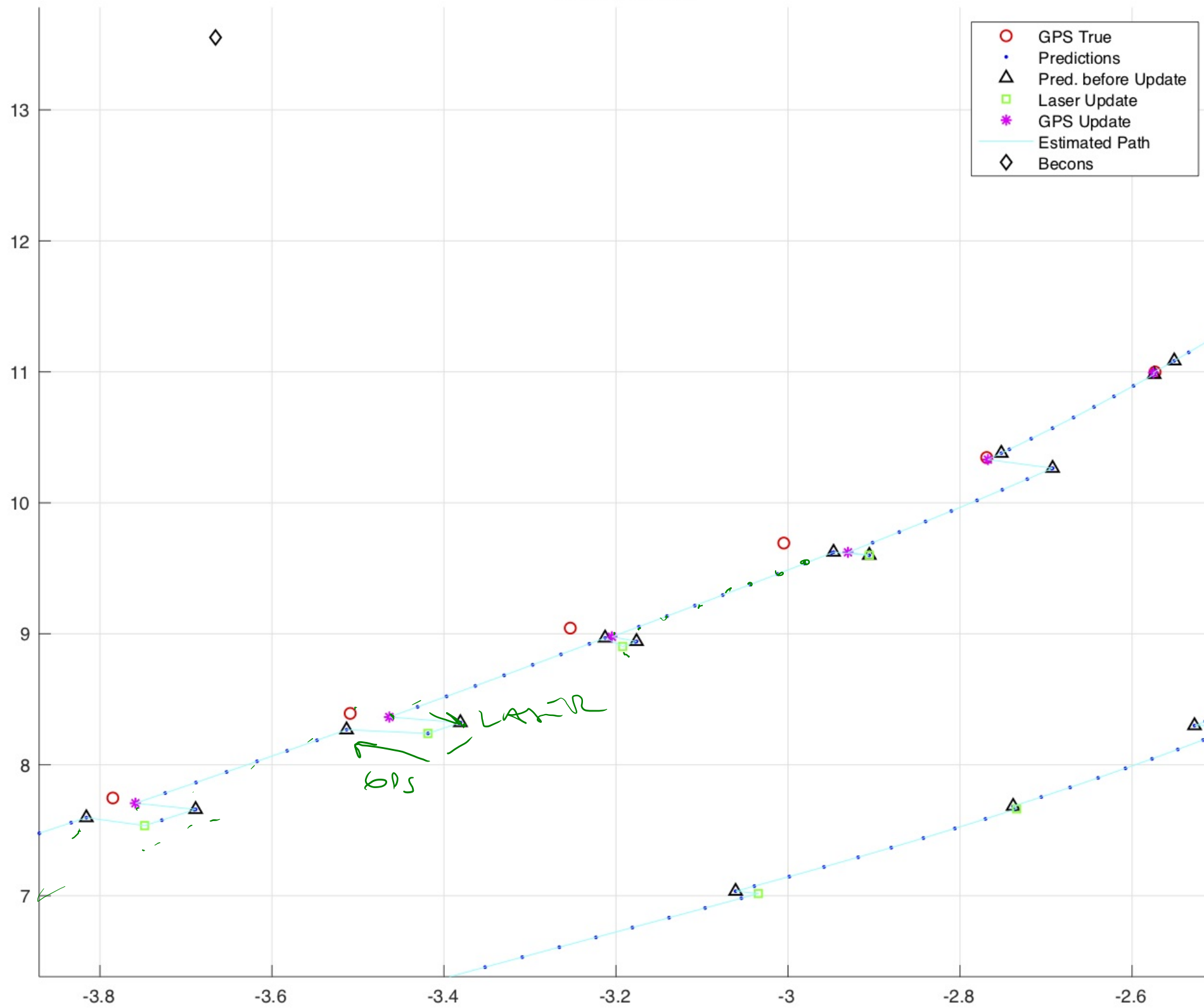
# Resultado



Resultado

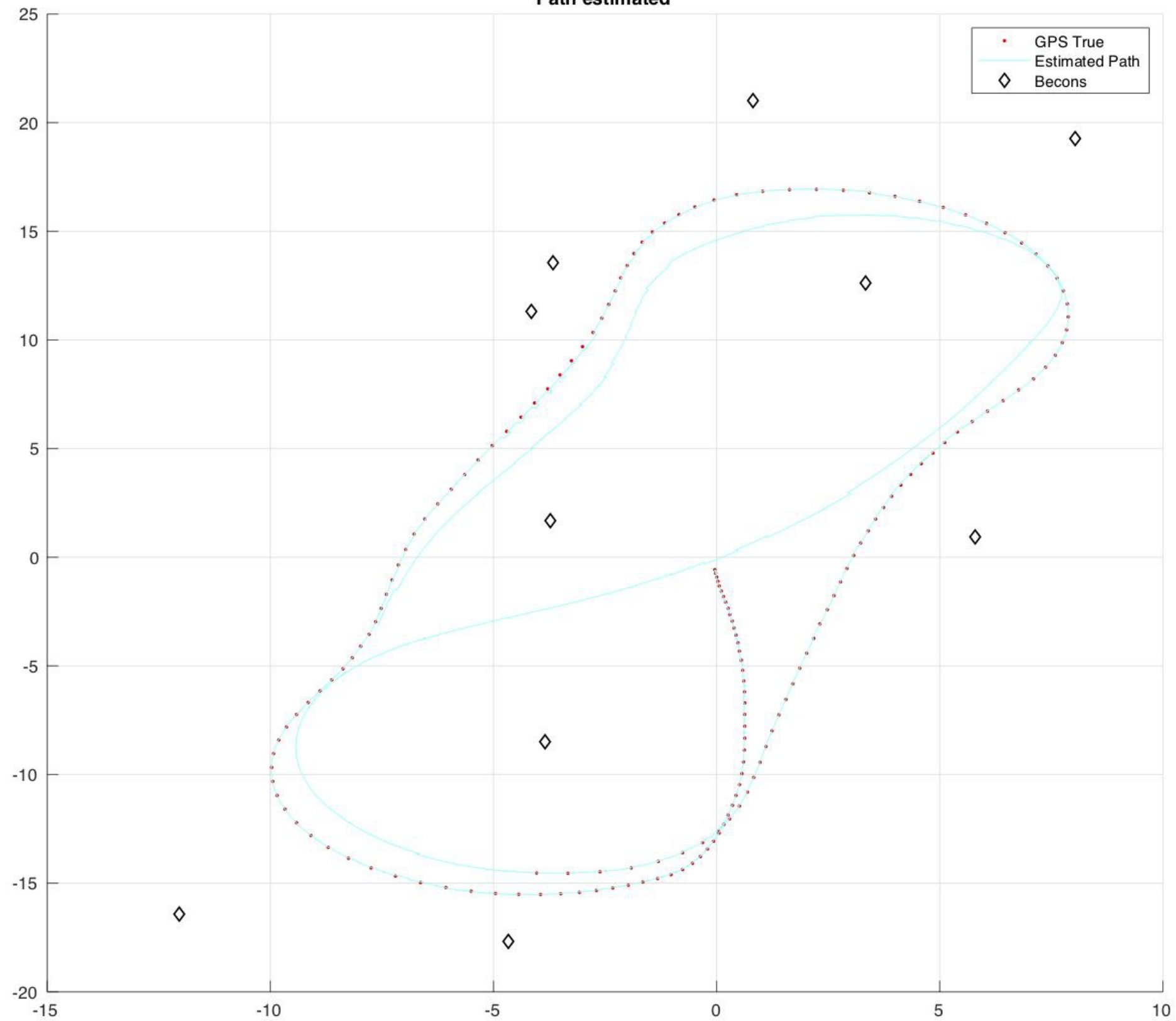


Path estimated

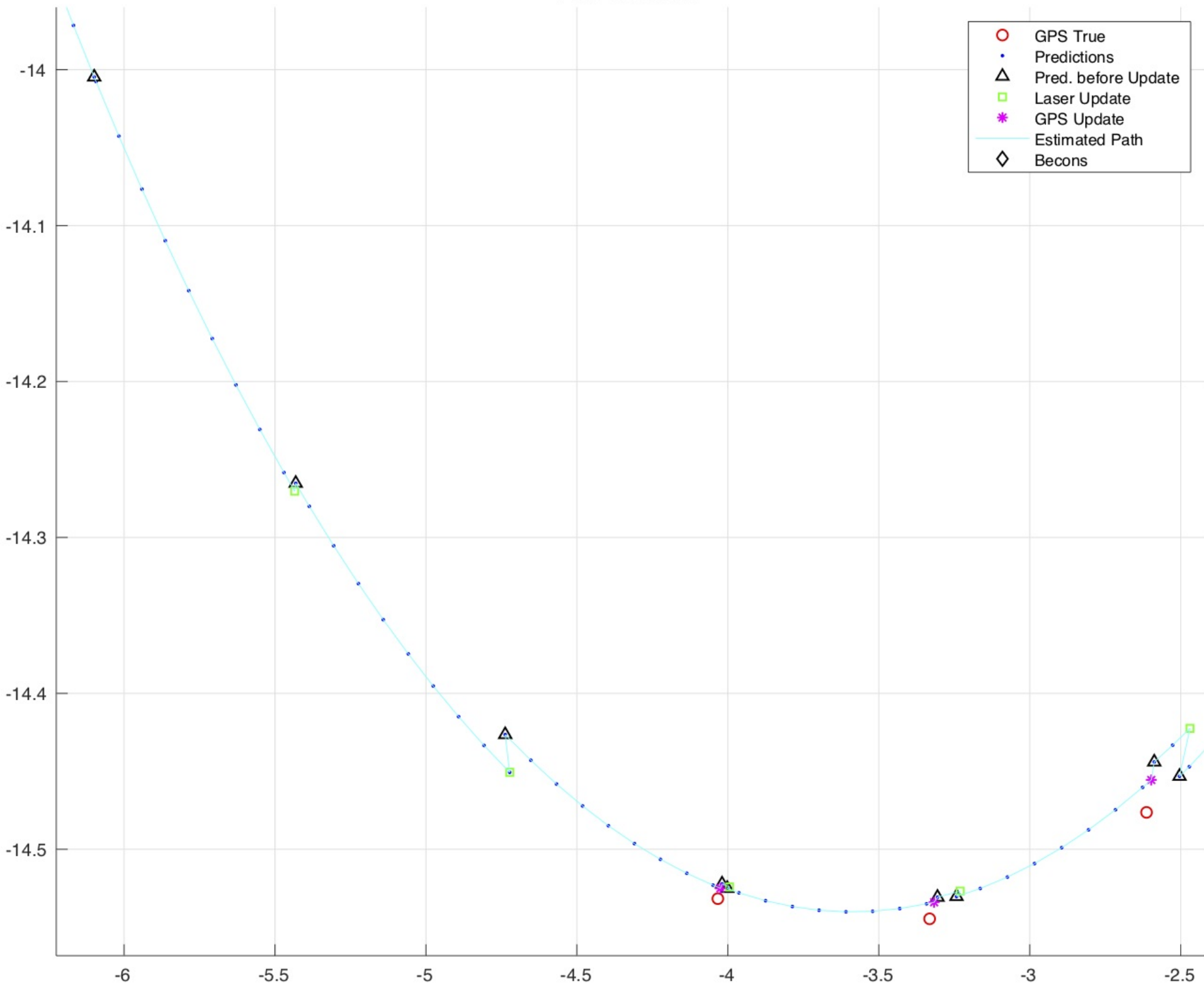




Path estimated



Path estimated



Path estimated

R

