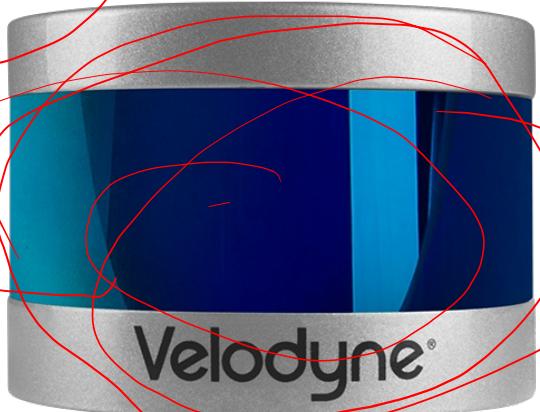


## Posicionamiento y Sensores

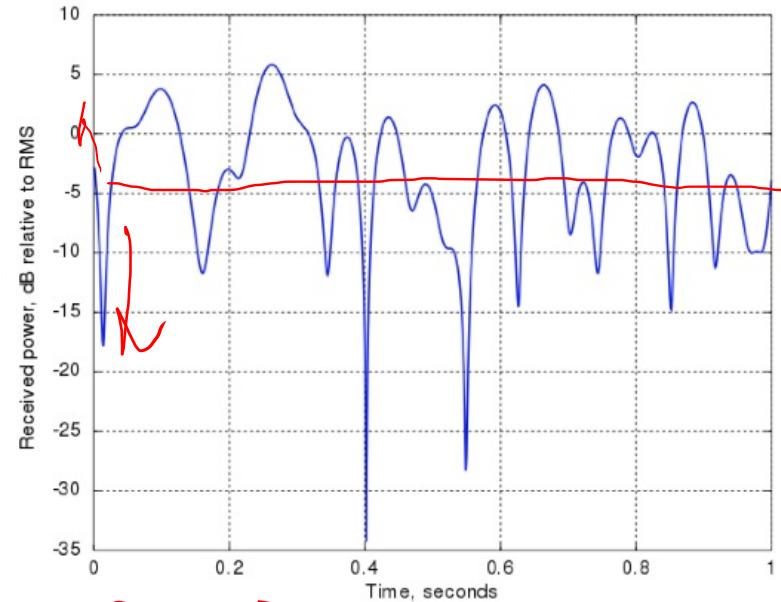
RF

30 m ~

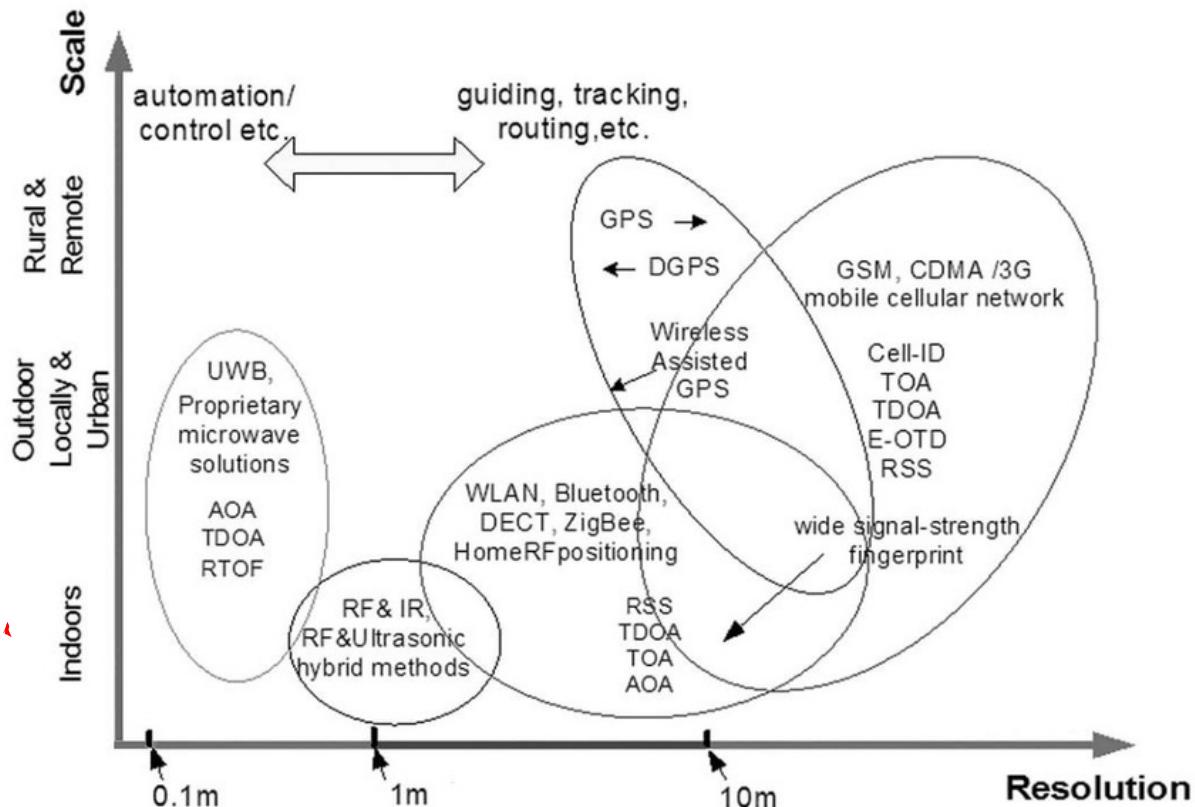


## Posicionamiento ubicuo

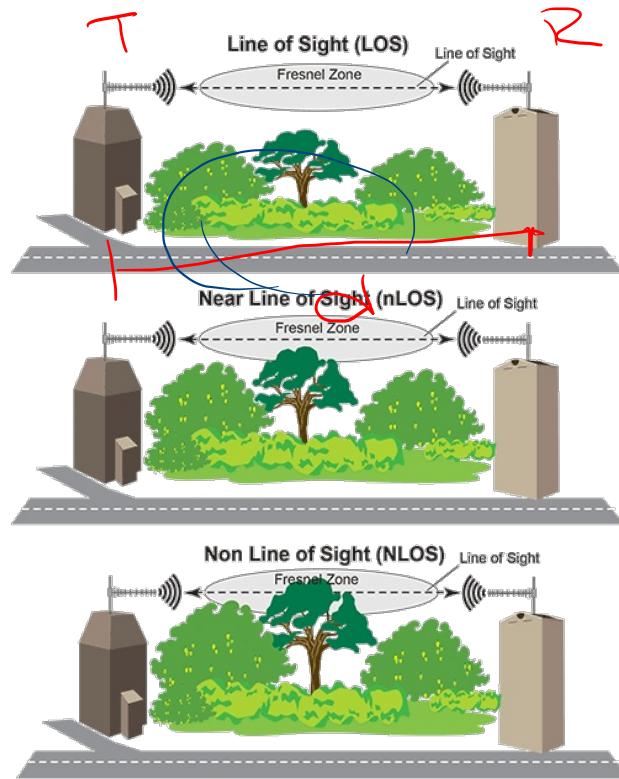
2.4 GHz (WiFi) 12 cm



# Sistemas de posicionamiento basado en RF



## Posicionamiento y RF: Introducción a la propagación de las señales



ESPACIO LIBRE  
FREE SPACE

LÍNEA DE VISTA

Line of sight.

$$d = \frac{C}{f}$$

$$P_r = P_t G_t G_r$$

$$\frac{\pi^2 d^2}{\left(\frac{4\pi d}{c}\right)^2}$$

$$P_r = P_t G_t G_r$$

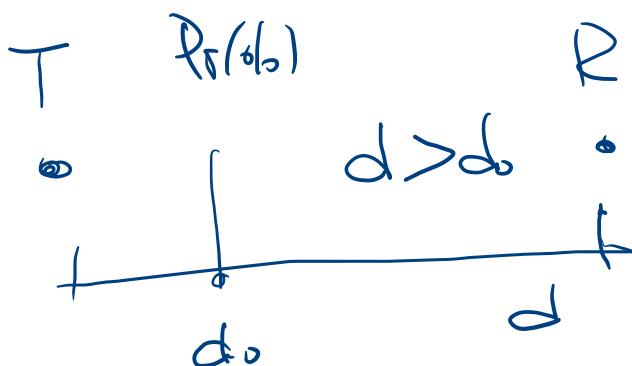
$$P_f = \frac{R_1 G_1 G_2 \lambda^2}{(4\pi d)^2}$$

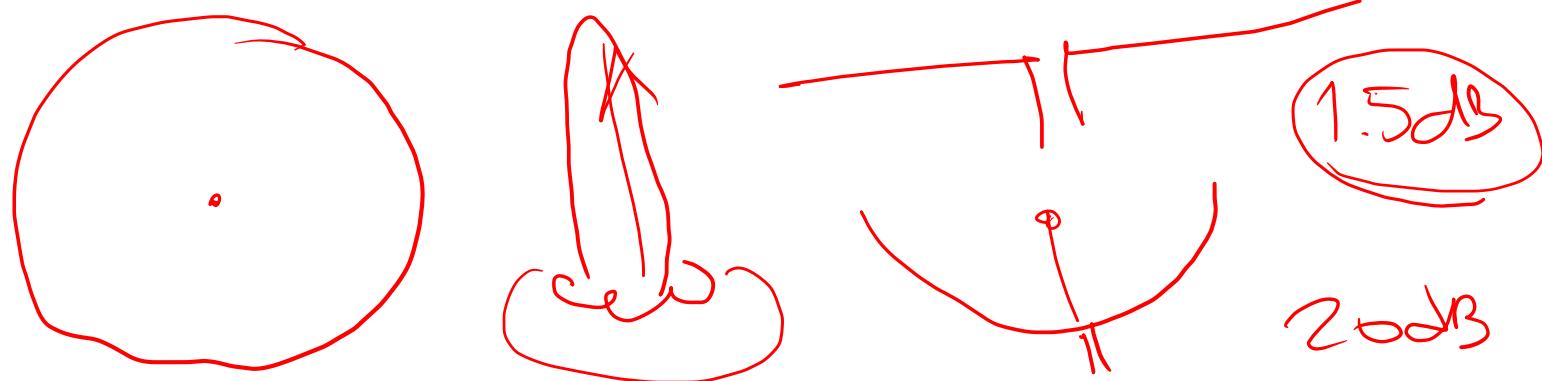
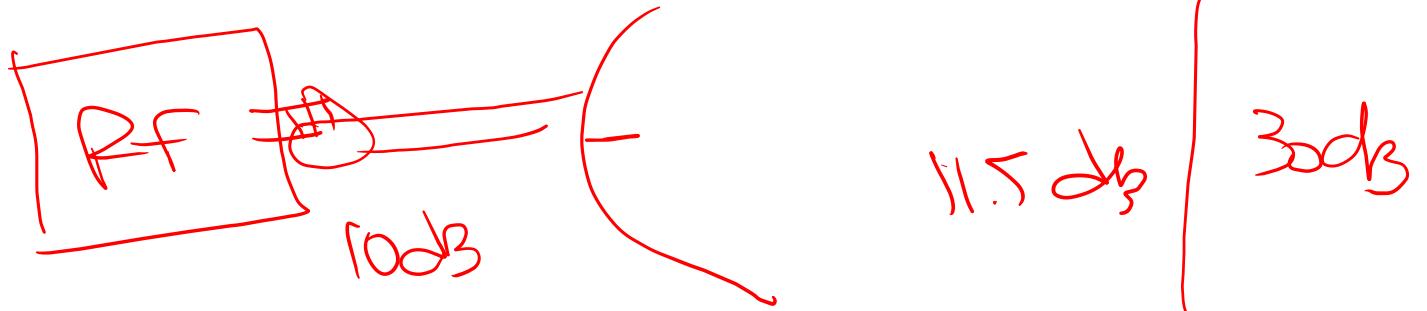
$$P_f = P_f(d_0) \left(\frac{d_0}{d}\right)^2$$

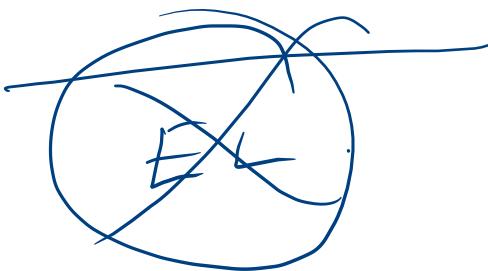
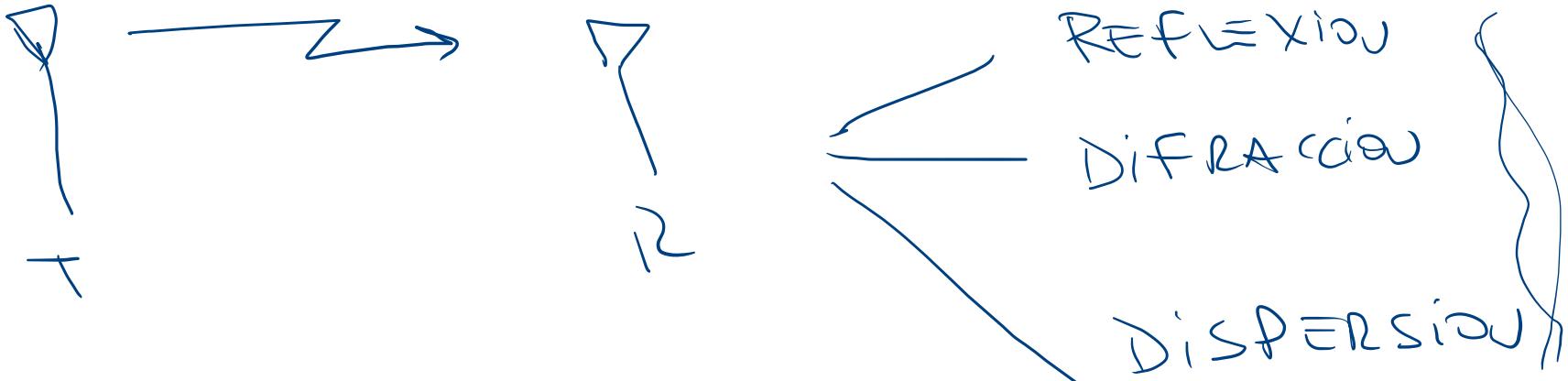
$$P_f = P_f(d_0) \cdot d_0^{-2}$$

$$P_f(d_0) = P_f(6r) \frac{\lambda^2}{(4\pi d_0)^2}$$

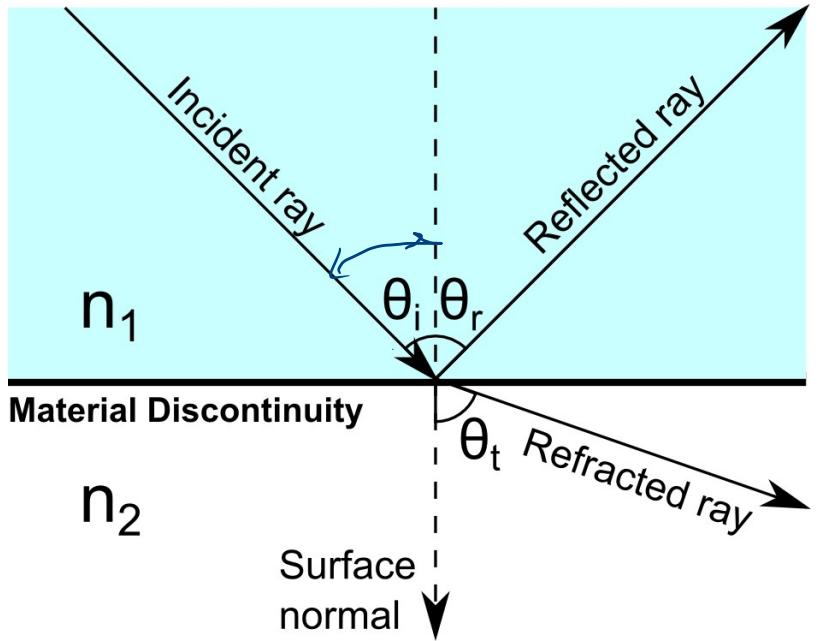
$$P_f(d_0) \cdot (d_0)^2 = \frac{P_f(6r)\lambda^2}{4\pi}$$



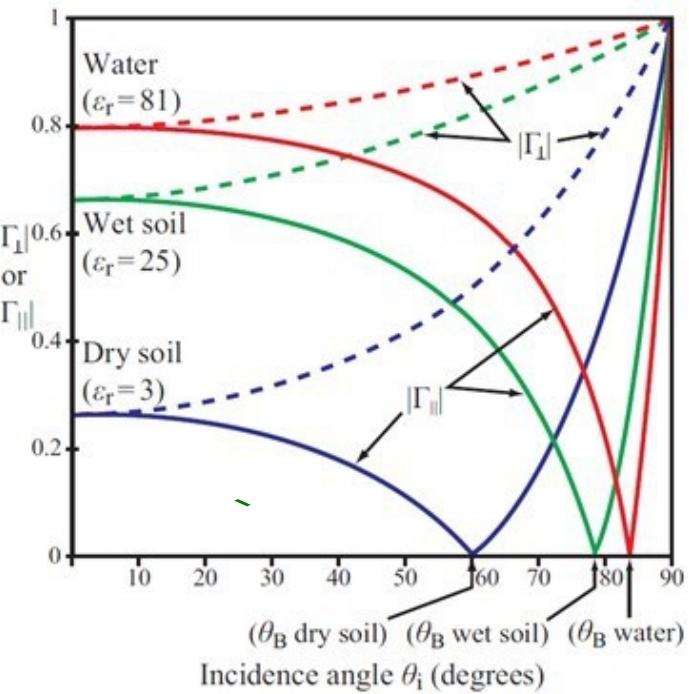




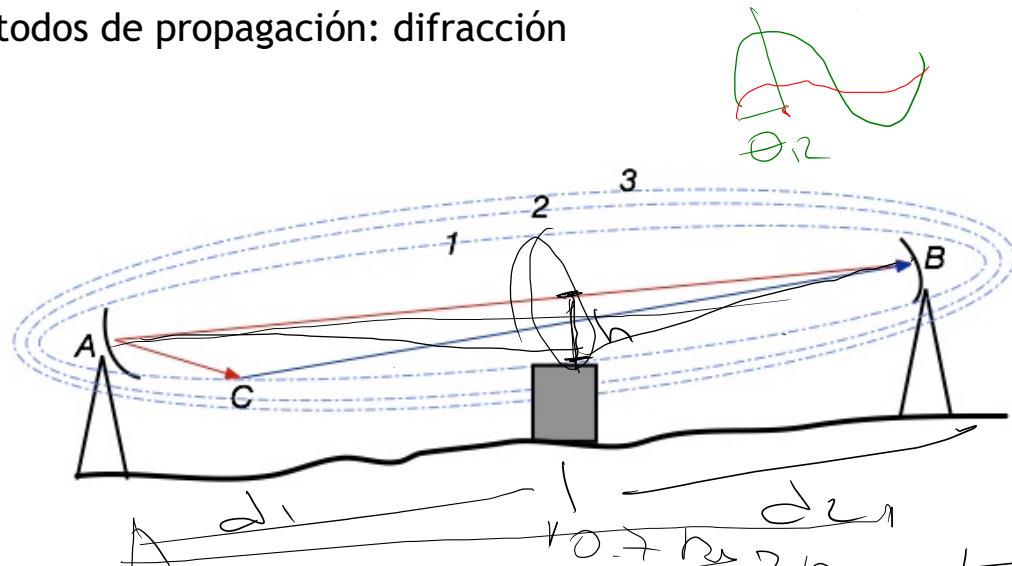
## Métodos de propagación: reflexión



$$\Gamma_{\perp} = \frac{-\epsilon_r \sin \theta_i + \sqrt{\epsilon_r - \cos^2 \theta_i}}{\epsilon_r \sin \theta_i + \sqrt{\epsilon_r - \cos^2 \theta_i}}$$



## Métodos de propagación: difracción

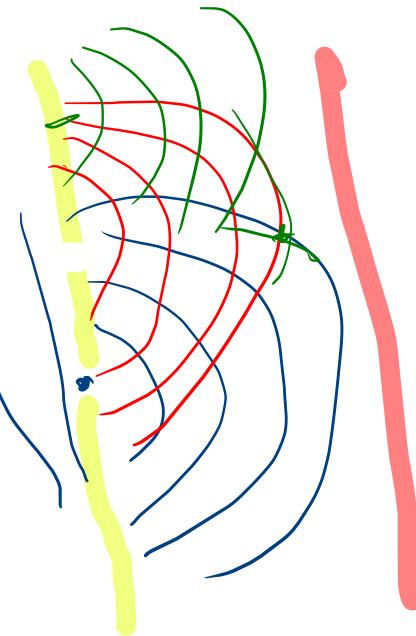


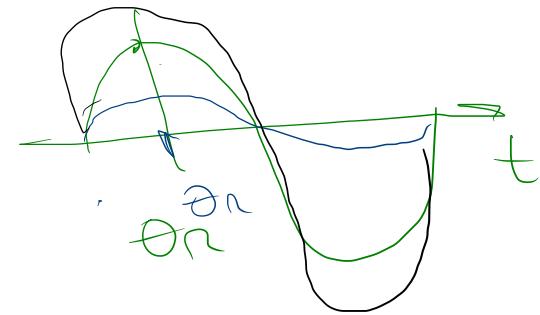
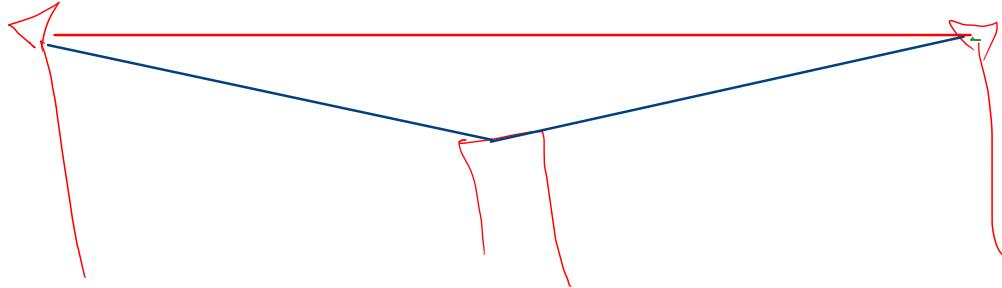
ZONAS DE FRESNEL

$$\begin{aligned}
 & d_1 = 0.7 h \quad d_2 = 2 km \\
 & D = h \quad \sqrt{2(d_1 + d_2)} \\
 & d_1 - d_2 = \frac{2(d_1 + d_2)}{D} \\
 & \Gamma = \sqrt{\frac{d_1}{d_2}} \quad \text{y} \quad \Gamma = \sqrt{\frac{d_2}{d_1}}
 \end{aligned}$$

Coeff. FRONTERA - FIN ALMOS

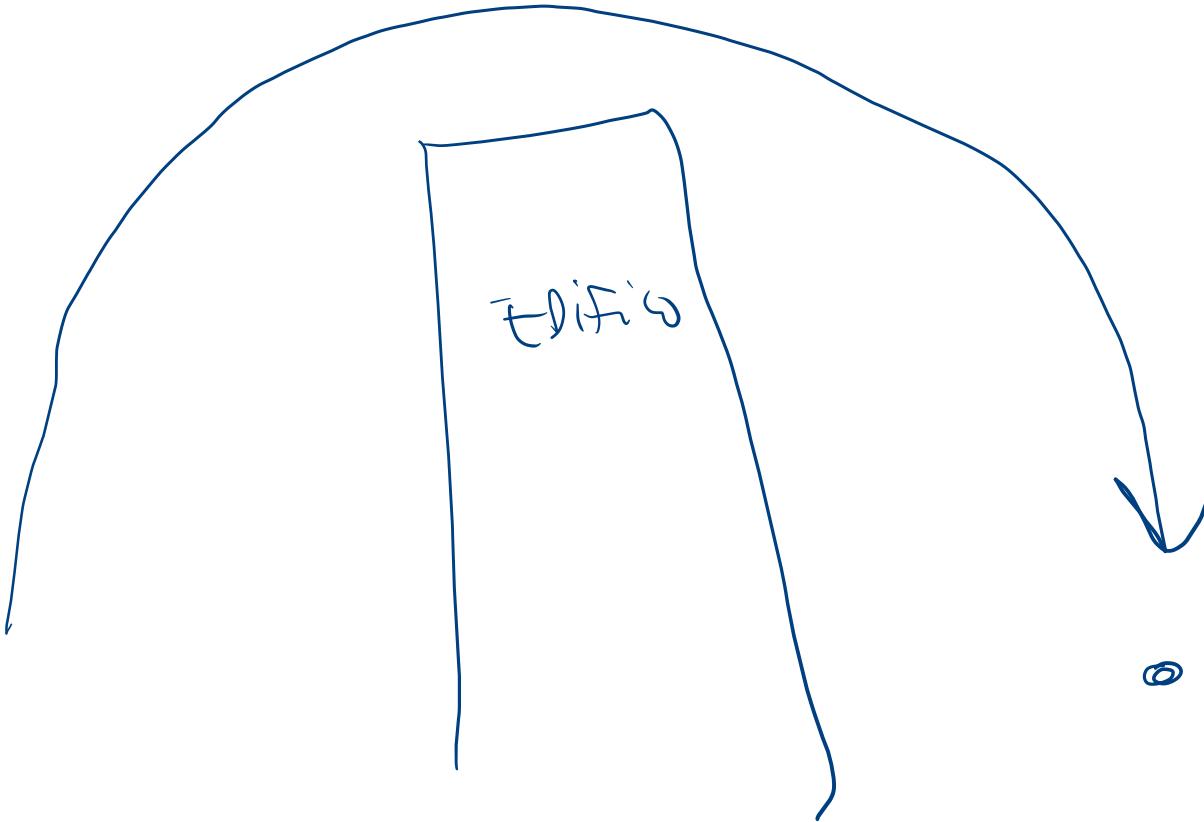
PRINCIPIO DE HUYGENS





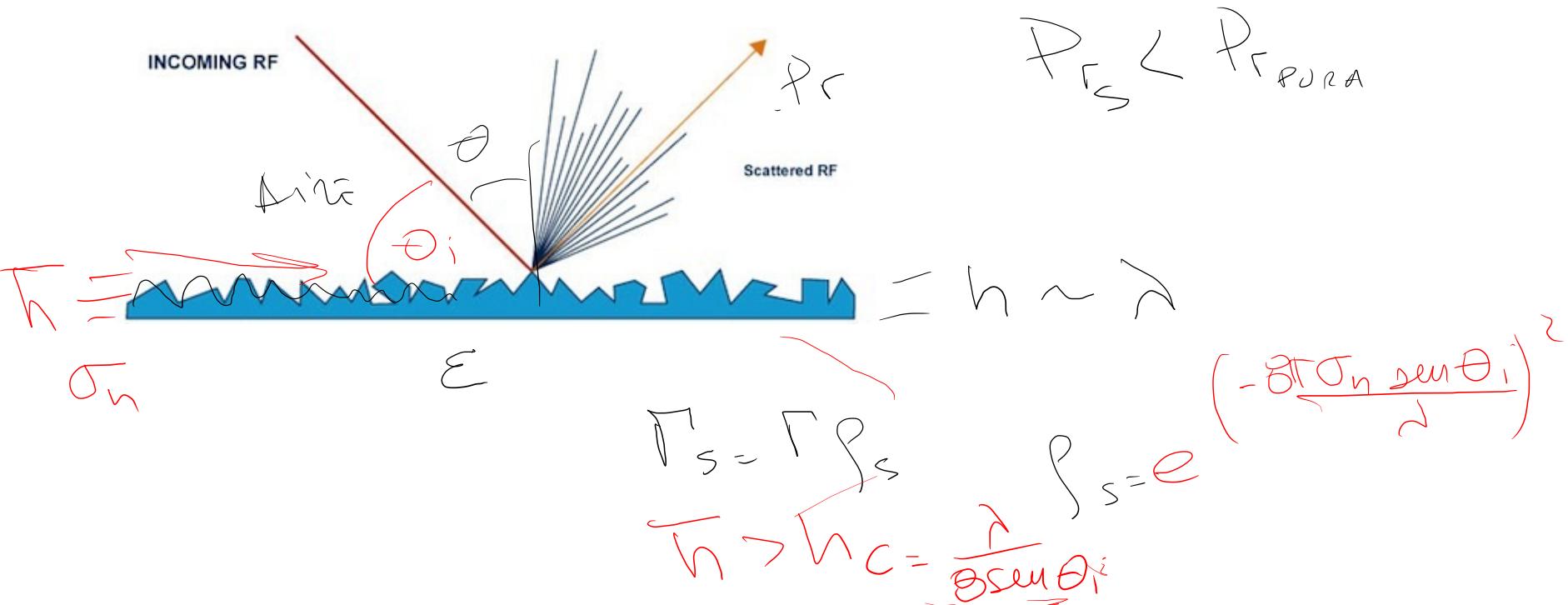


④



⑤

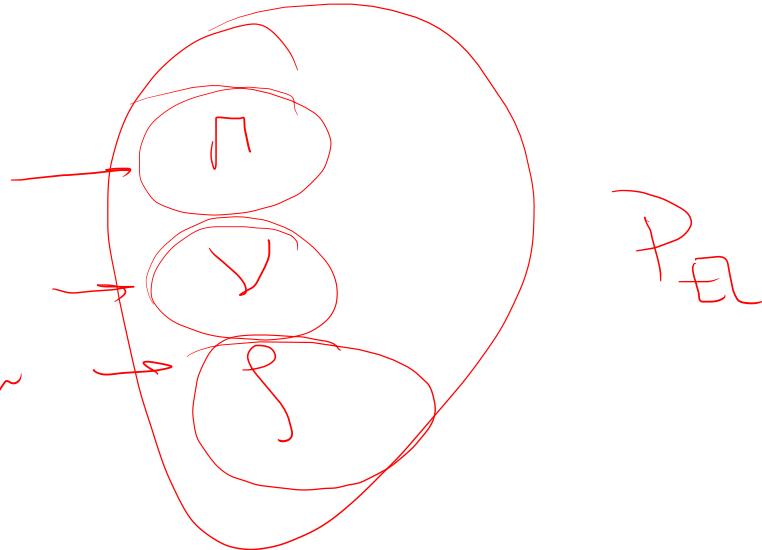
## Métodos de propagación: Scattering



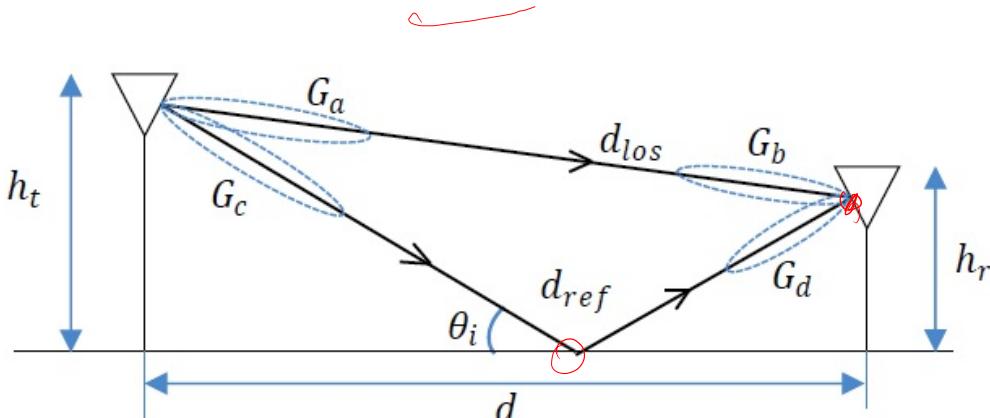
REFLEXION

DIFRACCIÓN

DISPERSIÓN

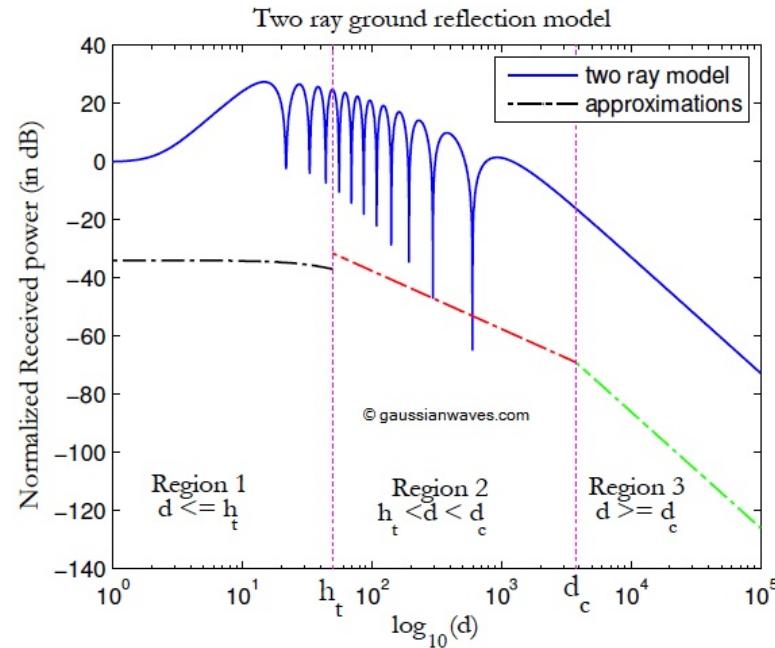


## Modelos de Propagación: 2 rayos



$$P_r = P_T G_t G_r \frac{4 \sin(\Theta_\Delta / \lambda)}{(4\pi d)^2} \frac{h_t h_r}{d^2}$$

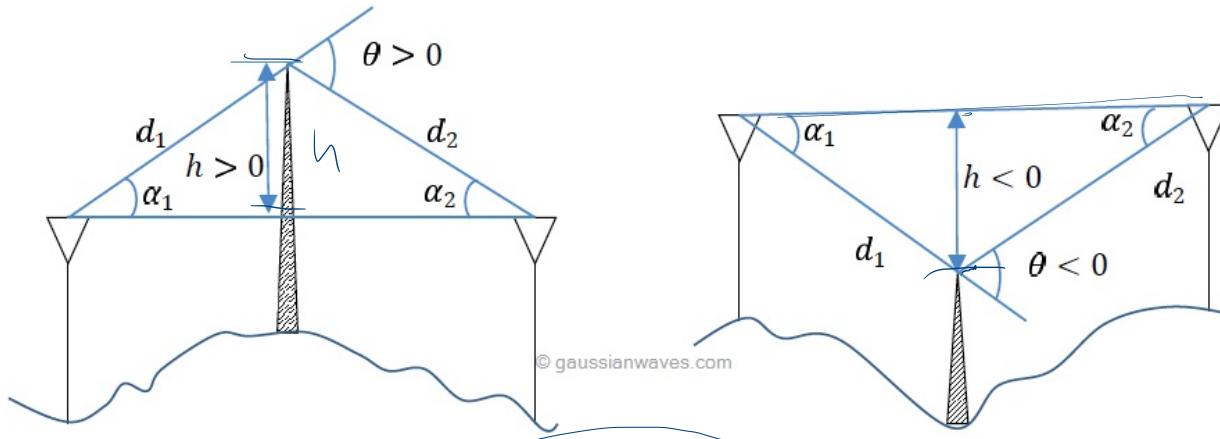
$$P_r = P_{TL} \cdot 4 \left( \frac{h_t + h_r}{d} \right)^2 = \frac{P_T G_t G_r (h_t h_r)^2}{4 d^4}$$



$$\Theta_\Delta < 0.2 \text{ rad}$$

$$\sin(\Theta_\Delta / \lambda) \approx \frac{\Theta_\Delta}{\lambda}$$

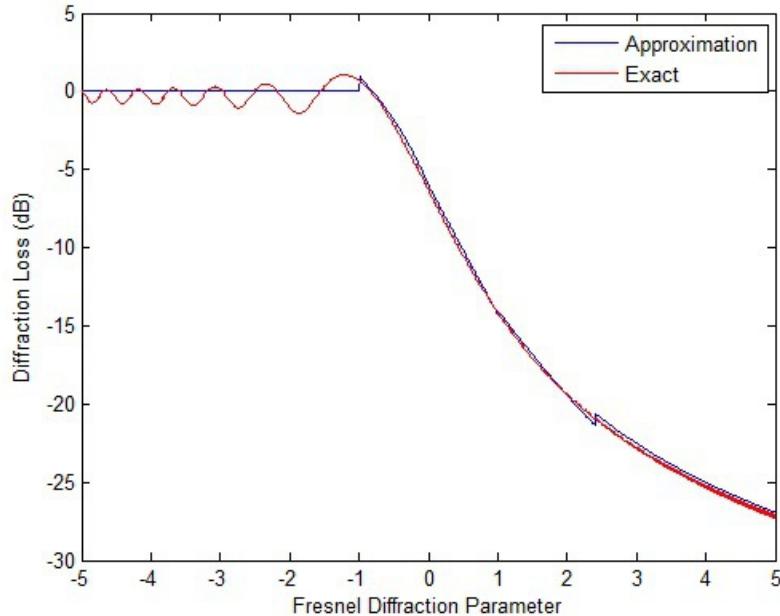
## Modelos de Propagación: Filo de Cuchillo



(a) (b)

$$d = h \sqrt{\frac{2(d_1 + d_2)}{d_1 \cdot d_2}}$$

## Modelos de Propagación: Filo de Cuchillo



$$\left. \begin{array}{ll} G_d(\text{dB}) = 0 & \nu \leq -1 \\ = 20 \log(0,5 - 0,62\nu) & \nu \in (-1; 0] \\ = 20 \log(0,5 \exp(-0,95\nu)) & \nu \in (0; 1] \\ = 20 \log(0,4 - \sqrt{0,1184 - (0,38 - 0,1\nu)^2}) & \nu \in (1; 2,4] \\ = 20 \log(0,225/\nu) & \nu > 2,4 \end{array} \right\}$$

$$P_r = P_{el} + G_{dif}$$

## Modelos de Propagación: Filo de Cuchillo

Multiple knife-edge diffraction –  
used to calculate propagation in rough terrain

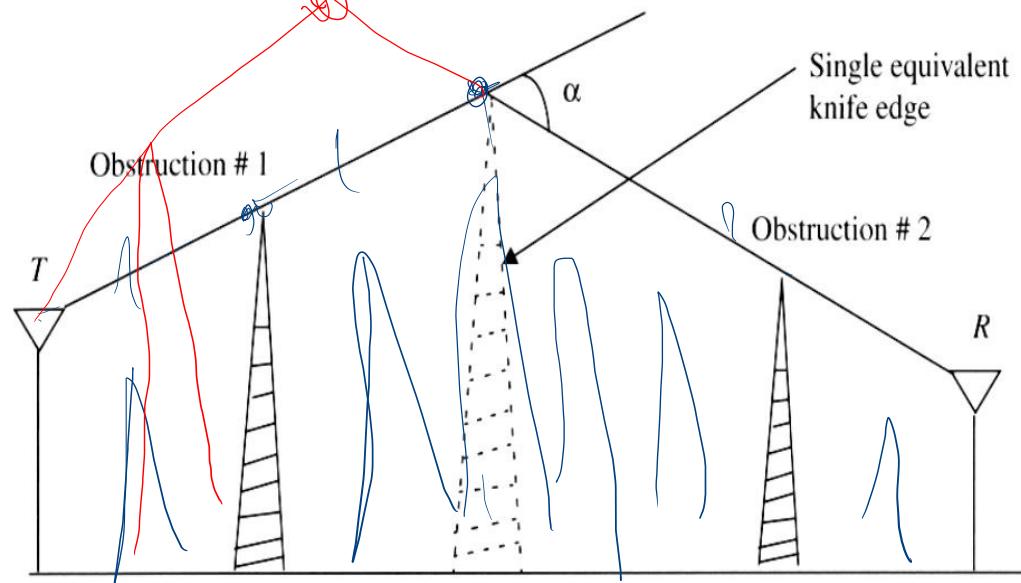
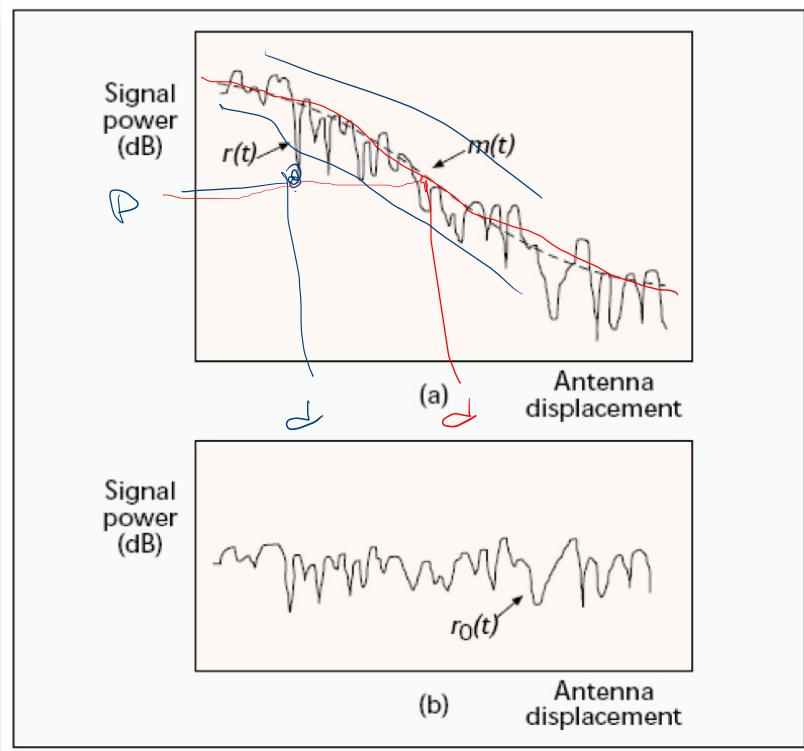


Figure 4.15 Bullington's construction of an equivalent knife edge [from [Bul47] © IEEE].

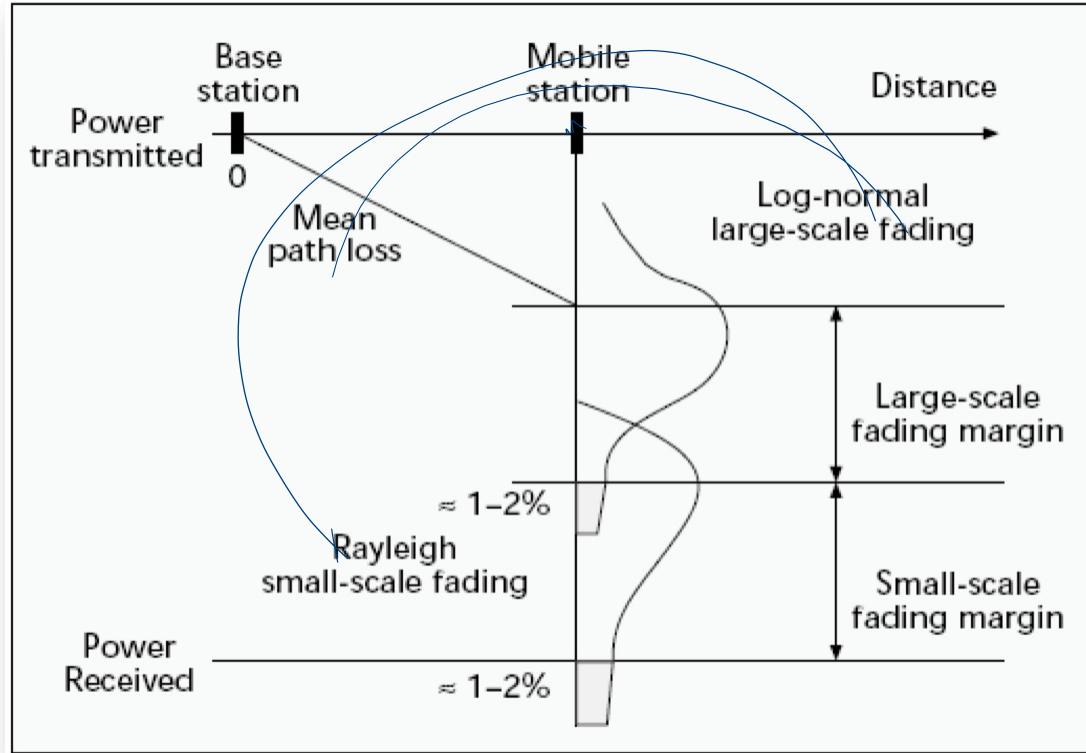
# Potencia vs. Distancia



GRAN ESPECTRO ( $d > 2\lambda$ )

PEQUEÑA EXALTA  $\Delta \ll d$

## Enlace de RF



T<sup>0</sup>



## Modelo de gran escala: Log-Normal

$$\text{El } n = 2$$

$$\text{Ran } n = 4$$

$$\overline{PL}[dB] = \overline{PL}(d_0) + 10n \log \frac{d}{d_0} + X_{\sigma}$$

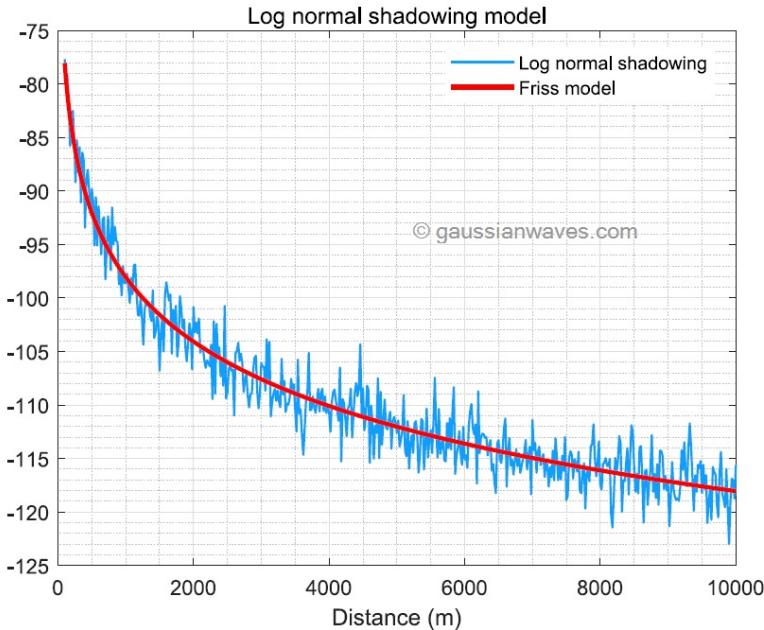
[2, 16]

$$P_r[dB] = P_t[dB] - \overline{PL}[dB]$$

Path loss

Distancia

$$n = [2.4, 6]$$

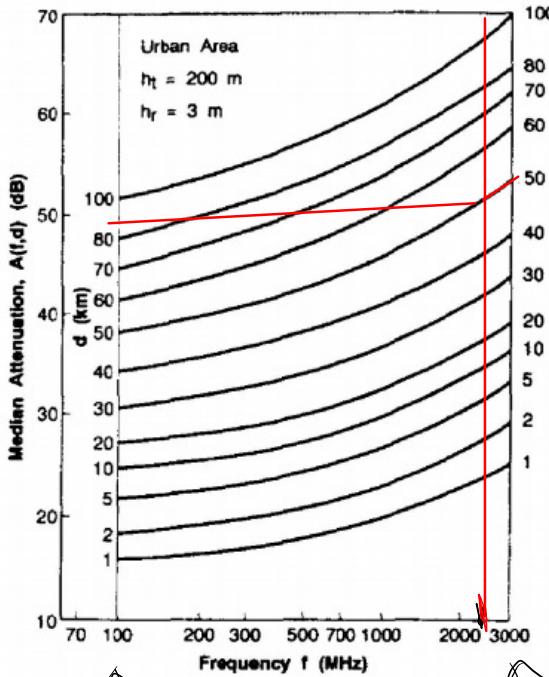


© gaussianwaves.com

# Modelo de gran escala: Okumura

MEDIA

$$L_{50}[dB] = L_F + A_{mu}(f, d) - G(h_{re}) - G(h_{te}) - G_{AREA}$$



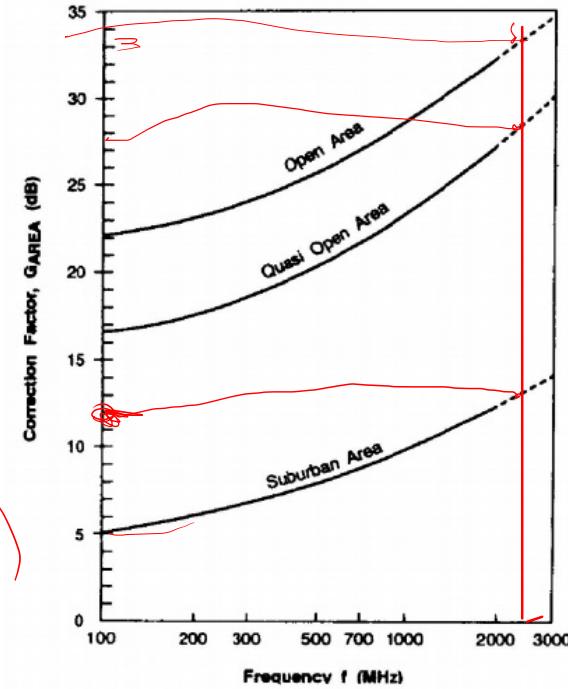
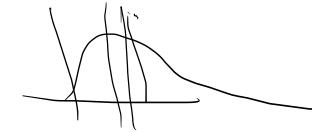
$$G(h_{re}) = 10 \log \left( \frac{h_{re}}{3} \right)$$

$$h_{re} < 3 \text{ m}$$

$$G(h_{re}) = 20 \left( \frac{h_{re}}{3} \right)$$

$$G(h_t) = 20 \log \left( \frac{h_t}{200} \right)$$

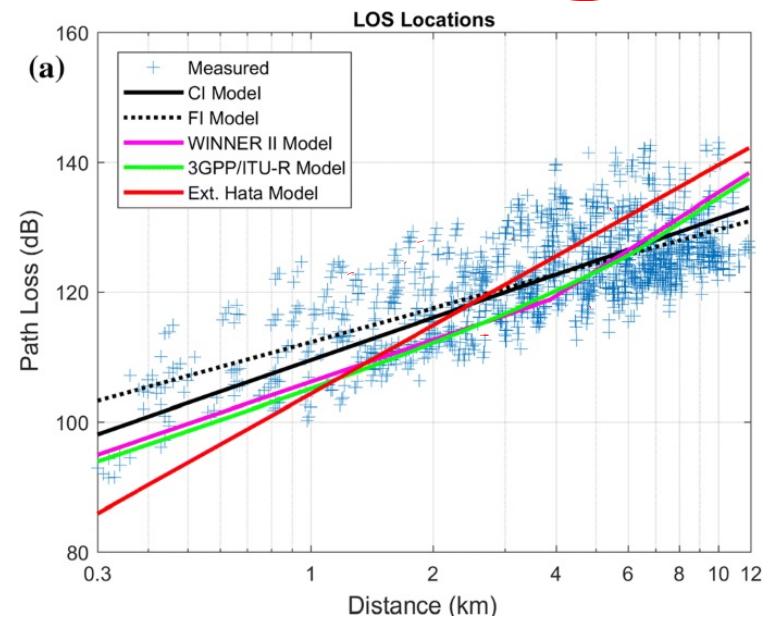
↑  
24



## Modelo de gran escala: Hata

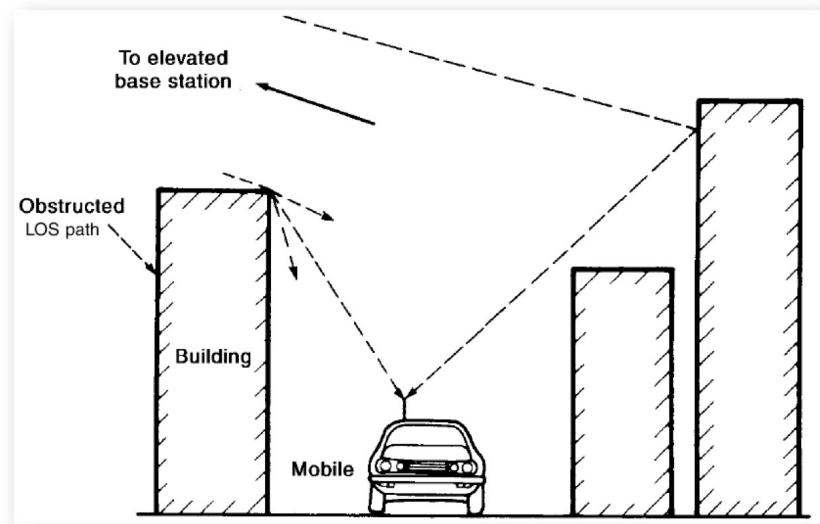
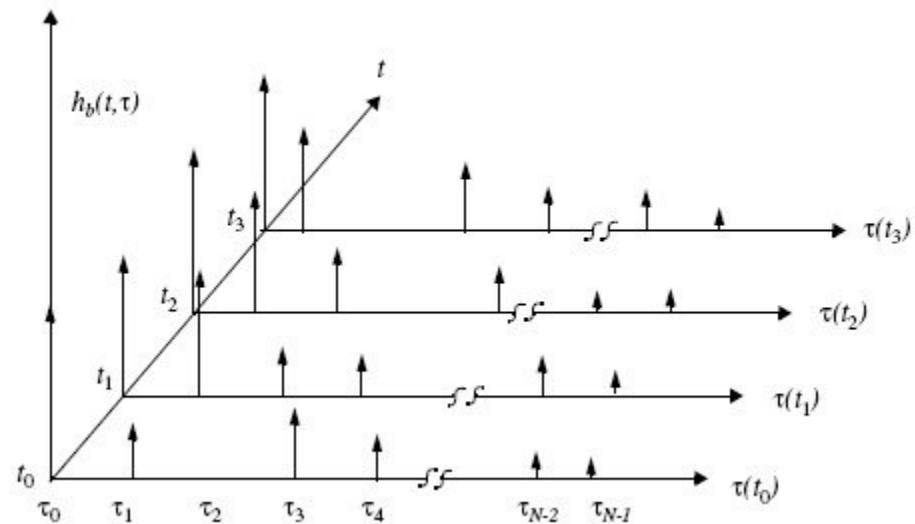
$$L_{50}[dB] = L_{50}[urbana, dB] - 2(\log(f_c/28))^2 - 5.4$$

$$L_{50}[urbana, dB] = 69.55 + 26.16 \log(f_c) - 13.82 \log(h_{te}) - a(h_{re}) + (44.9 - 6.55 \log(h_{te})) \log(d)$$

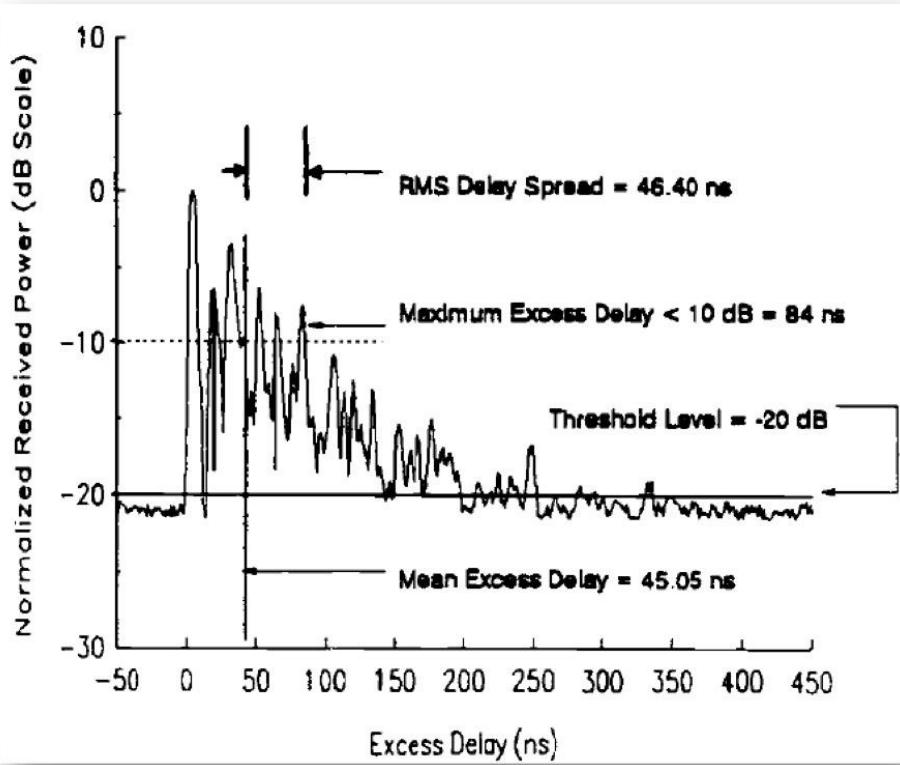


Measurements and path loss models for a TD-LTE network at 3.7 GHz in rural areas

## Modelo de pequeña escala



## Modelo de pequeña escala

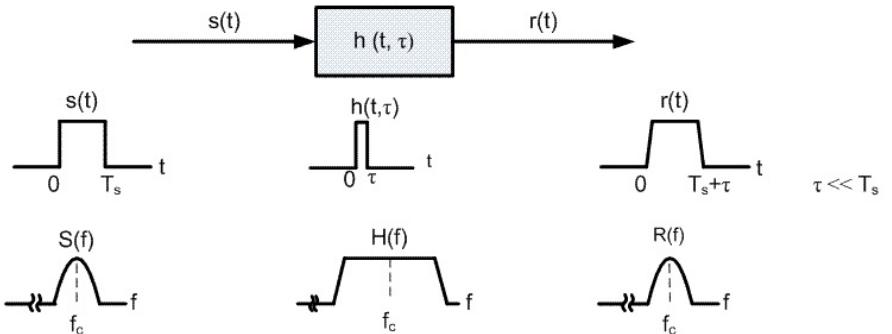


$$\bar{\tau} = \frac{\sum_k (p(\tau_k) \cdot \tau_k)}{\sum_k p(\tau_k)}$$

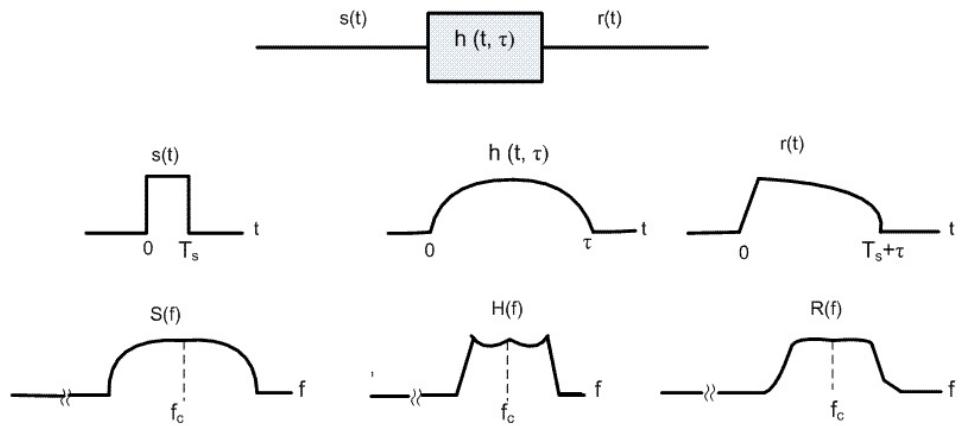
$$\overline{\tau^2} = \frac{\sum_k (p(\tau_k) \cdot \tau_k^2)}{\sum_k p(\tau_k)}$$

$$\sigma_\tau = \sqrt{\overline{\tau^2} - \bar{\tau}^2}$$

## Modelo de pequeña escala



(a) Flat fading channel characteristics



(b) Frequency selective fading channel characteristics

# Modelo de pequeña escala

## **Small-Scale Fading**

(Based on multipath time delay spread)

### **Flat Fading**

1. BW of signal < BW of channel
2. Delay spread < Symbol period

### **Frequency Selective Fading**

1. BW of signal > BW of channel
2. Delay spread > Symbol period

## **Small-Scale Fading**

(Based on Doppler spread)

### **Fast Fading**

1. High Doppler spread
2. Coherence time < Symbol period
3. Channel variations faster than baseband signal variations

### **Slow Fading**

1. Low Doppler spread
2. Coherence time > Symbol period
3. Channel variations slower than baseband signal variations

## Efectos en el Posicionamiento

