

A **monoalphabetic substitution cipher** is a type of encryption where each letter of the plaintext is replaced with another letter from the alphabet. The substitution remains **consistent** throughout the message, meaning each letter always maps to the same substitute letter.

The **Vigenère cipher** is a **polyalphabetic substitution cipher**, meaning it uses multiple Caesar ciphers based on a keyword. It was designed to overcome the weaknesses of monoalphabetic ciphers like the one you asked about earlier.

Key Idea:

The Vigenère cipher shifts each letter of the plaintext by a different amount depending on a repeating **keyword**.

How It Works:

1. **Choose a keyword** (e.g., KEY).
2. Repeat the keyword to match the length of the plaintext:
 - Plaintext: HELLO
 - Keyword: KEYKE
3. Use Caesar shift for each letter:
 - Convert each letter to its position in the alphabet (A=0, B=1, ..., Z=25).
 - Add the positions of the plaintext letter and the keyword letter (mod 26).
 - Convert the result back to a letter.

Example:

- **Plaintext:** HELLO
- **Keyword:** KEYKE

Plaintext	H	E	L	L	O
Keyword	K	E	Y	K	E
Shift	10	4	24	10	4
Ciphertext	R	I	J	V	S

Ciphertext: RIJVS

The **Vernam cipher** is a special type of **stream cipher** invented by Gilbert Vernam in 1917. It forms the basis of the **One-Time Pad**, which is the only proven **unbreakable cipher** when used correctly.

Example:

Plaintext: HELLO
One-Time Pad (Key): XMCKL

Step 1: Letter → Number Mapping

Lette r	Plaintext (P)	Key (K)	P (num)	K (num)
H	H	X	7	23
E	E	M	4	12
L	L	C	11	2
L	L	K	11	10
O	O	L	14	11

Step 2: Add P + K (mod 26)

P + K	Su m	Mod 26	Cipher (number)	Cipher (letter)
H + X	30	4	4	E
E + M	16	16	16	Q
L + C	13	13	13	N
L + K	21	21	21	V
O + L	25	25	25	Z

Final Ciphertext: EQNVZ

The **Diffie-Hellman algorithm** is a **key exchange protocol** that allows two parties to securely share a **secret key** over an insecure channel (like the internet), **without actually transmitting the key itself**.

It's widely used in secure communications like HTTPS, VPNs, and messaging apps.



Key Concepts

- **Asymmetric key exchange** method (not encryption directly)
- Based on the **difficulty of computing discrete logarithms**
- Each party generates a private key and a corresponding public key
- Both parties combine their private key with the other's public key to compute the **same shared secret**



How It Works (Step-by-Step)

Let's say Alice and Bob want to share a secret key.

Publicly agreed values (known to both parties):

- A large **prime number** p
- A **primitive root modulo** p (called the generator) g

These can be sent in the open.



Step 1: Key Generation

Each party chooses a **private key**:

- Alice picks a secret number a
- Bob picks a secret number b

Then they compute their **public keys**:

- Alice computes: $A = g^a \bmod p$
- Bob computes: $B = g^b \bmod p$

They exchange A and B over the insecure channel.

Step 2: Compute Shared Secret

Now each side computes the shared key:

- Alice computes: $s = B^a \bmod p$
- Bob computes: $s = A^b \bmod p$

Since:

$$B^a \equiv (g^b)^a \equiv g^{(ab)} \bmod p$$

$$A^b \equiv (g^a)^b \equiv g^{(ab)} \bmod p$$

✓ Both sides compute the same value s , the **shared secret key**, without ever sending a or b .

Example (Small Numbers for Simplicity)

- Public values: $p = 23, g = 5$
- 1. Alice picks private key $a = 6$
→ Computes public key $A = 5^6 \bmod 23 = 15625 \bmod 23 = 8$
- 2. Bob picks private key $b = 15$
→ Computes public key $B = 5^{15} \bmod 23 = 759375 \bmod 23 = 2$
- 3. They exchange A and B
- 4. Alice computes: $s = B^a \bmod 23 = 2^6 \bmod 23 = 64 \bmod 23 = 18$
Bob computes: $s = A^b \bmod 23 = 8^{15} \bmod 23 = 18$

✓ Shared secret = **18**

The **RSA algorithm** is a **public-key cryptographic algorithm** used for secure data transmission. It is named after its inventors: **Rivest, Shamir, and Adleman**.

RSA is widely used for **encryption**, **digital signatures**, and **secure key exchange**.

Key Concepts

- **Asymmetric encryption**: uses a **public key** for encryption and a **private key** for decryption.
- Based on the difficulty of factoring large composite numbers.



RSA Algorithm Steps

► Step 1: Key Generation

1. Choose two **distinct large prime numbers**, p and q
 2. Compute:

$$n = p * q$$

$$\phi(n) = (p - 1) * (q - 1) \text{ (Euler's totient)}$$
 3. Choose an integer e such that:

$$1 < e < \phi(n) \text{ and } \gcd(e, \phi(n)) = 1$$
 (e is the **public exponent**)
 4. Compute d as the **modular inverse** of e modulo $\phi(n)$

$$\rightarrow d \equiv e^{-1} \pmod{\phi(n)}$$
- **Public Key** = (e, n)
 - **Private Key** = (d, n)

► Step 2: Encryption

To encrypt a message M :

- Convert plaintext to an integer m such that $0 < m < n$
- Ciphertext $c = m^e \pmod{n}$

► Step 3: Decryption

To decrypt ciphertext c :

- Plaintext $m = c^d \pmod{n}$



Example (using small numbers for clarity)



Key Generation:

- $p = 61, q = 53$
- $n = p * q = 61 * 53 = 3233$
- $\phi(n) = (p - 1)(q - 1) = 60 * 52 = 3120$

Choose $e = 17$ (a common public exponent)

Find d such that $d * e \equiv 1 \pmod{3120}$

$\rightarrow d = 2753$

- Public Key: $(e=17, n=3233)$
- Private Key: $(d=2753, n=3233)$



Encrypt message $M = 65$:

$$c = 65^{17} \pmod{3233} = 2790$$



Decrypt ciphertext $c = 2790$:

$$m = 2790^{2753} \pmod{3233} = 65$$



Original message retrieved

The **Caesar Cipher** is one of the **simplest and oldest** encryption techniques. It's a type of **substitution cipher** in which each letter in the plaintext is **shifted a fixed number of places** down the alphabet.



Caesar Cipher Basics

- Invented by **Julius Caesar**
- It uses a single key: the **shift amount** (usually from 1 to 25)
- For example, with a shift of **+3**:
 - $A \rightarrow D$
 - $B \rightarrow E$
 - $C \rightarrow F$
 - ...
 - $X \rightarrow A$
 - $Y \rightarrow B$
 - $Z \rightarrow C$



Encryption Formula:

pgsql

CopyEdit

Encrypted letter = (plaintext_letter + shift) mod 26

Assuming:

- A=0, B=1, ..., Z=25



Decryption Formula:

bash

CopyEdit

Decrypted letter = (cipher_letter - shift + 26) mod 26



Example

► Plaintext: **HELLO**

► Shift: **3**

Letter	Position	3	Ciphertext
H	7	10	K
E	4	7	H
L	11	14	O
L	11	14	O
O	14	17	R



Ciphertext: **KHOOR**

The **DES (Data Encryption Standard)** is a symmetric-key block cipher developed in the 1970s. It was once the gold standard for secure data encryption but is now considered insecure due to its short key length.



DES at a Glance

Feature	Detail
Algorithm type	Symmetric block cipher
Block size	64 bits (8 bytes)

Key size	56 bits (plus 8 parity bits)
Rounds	16 rounds
Encryption method	Feistel structure (split & process)
Status	Obsolete (replaced by AES)

How DES Works

1. Initial Permutation (IP)

- The 64-bit plaintext block undergoes an initial permutation.

2. 16 Rounds of Processing

Each round involves:

- Splitting the block into **Left (L)** and **Right (R)** halves.
- Using a **round key** (generated from the main key).
- Applying a **function $f(R, K)$** that:
 - Expands R from 32 to 48 bits.
 - XORs it with the round key.
 - Applies **S-box substitution** and **permutation**.
- Swapping and recombining L and R after each round.

3. Final Permutation (IP^{-1})

- After 16 rounds, the halves are recombined and a final permutation is applied.

The **AES (Advanced Encryption Standard)** is the current **U.S. federal standard** for encrypting data, and it's one of the most widely used **symmetric encryption algorithms** in the world today.



AES at a Glance

Feature	Detail
Type	Symmetric-key block cipher
Block size	128 bits (16 bytes)
Key sizes	128, 192, or 256 bits

Rounds	10 (128-bit), 12 (192-bit), 14 (256-bit)
Structure	Substitution–Permutation Network (SPN)
Standardized by	NIST in 2001
Replaces	DES

AES Encryption Steps (128-bit key)

AES works on a **4×4 matrix of bytes** called the **state**.

Each round includes:

1. **SubBytes** – Each byte is replaced using an S-box (substitution)
2. **ShiftRows** – Rows of the matrix are cyclically shifted
3. **MixColumns** – Columns are mixed using matrix multiplication over $GF(2^8)$
4. **AddRoundKey** – Each byte is XORed with a round key

The **first round** starts with AddRoundKey.

The **last round** skips MixColumns.

Key Expansion

- The input key is expanded into multiple **round keys** using a **key schedule**
- Number of rounds depends on key size:
 - 128-bit key → 10 rounds
 - 192-bit key → 12 rounds
 - 256-bit key → 14 rounds

Example (Conceptual)

Let's say you want to encrypt:

Plaintext: "HelloWorld123456" (16 bytes)

Key: "That'sMyAESKey123" (16 bytes = 128 bits)

AES will:

1. Convert the plaintext and key into byte matrices

2. Apply 10 rounds of transformations as described above
3. Output the ciphertext (also 16 bytes)

Note: Actual encrypted text will look like unreadable binary or hex — not regular characters.



AES Advantages

- Fast and secure even on limited-resource devices
- Resistant to all known practical attacks (when implemented correctly)
- Supports multiple key lengths