

sine series

$$\sum_{n=1}^{\infty} b_n \sin\left(\frac{n\pi x}{L}\right)$$

$$= \frac{1}{10} \sin\left(\frac{\pi x}{10}\right)$$

$$\Rightarrow b_4 = \frac{1}{10}$$

$$\Rightarrow b_6 = 0, b_8 = 0, \dots$$

lowest freq: $n=1$:

$$\text{fundamental freq} = \frac{\pi}{2L} = \frac{\pi}{2 \times 10} = \frac{\pi}{20} \text{ Hz}$$

All other freqs are constant
multiples of fundamental freq.

High D: 523

$$\frac{\pi L}{3} = \frac{\pi \times 10}{3} \text{ cm to Hz} = \frac{3}{2} \times 523$$

$$\text{long: } 292 \approx \frac{1}{2} \times 523$$

Music & vibrating
strings

$$y(x,t) = \sum_{n=1}^{\infty} A_n \cos\left(\frac{n\pi t}{T}\right) \sin\left(\frac{n\pi x}{L}\right)$$

fix x : solution of
time freqs w/ max
frequency

$$v_n = \frac{1}{2\pi} \frac{n\pi}{L} \alpha = \left(\frac{\pi}{L} \right) \frac{n}{2} \alpha$$