Sketch of solutions.	
Sketch of solutions.  1. a.) Eigenvalues: $\lambda = 2 \pm 2i$	
Eigenvector cy'n: $\begin{bmatrix} -1-2i & -5 \end{bmatrix}$ $\begin{bmatrix} -1-2i & -5 \end{bmatrix}$ $\begin{bmatrix} -5 & 7 \\ 1+2i \end{bmatrix}$	
[-1-21 -5]	0,7 [0]
1-21	J2 J - [0]
Tale v = 5 7	
[l+Zi]	
Soly: x(4) = v e(2+2i)+	
×(+) = v e	
= e <sup>24</sup> [ -5 cos (2+) - 5isin(2+	1
$[\cos(2t) - 2\sin(2t) + i(\sin(2t))$	7 7
Take real kimaginany parts:	sols:
$\chi_{i}(t) = e^{2t} \left[ -5\cos(2t) \right]$	7
= L cos (2t) -28iy	(21)
$\chi_2(t) = e^{2t} \left[ -5 \sin \theta \right]$	
siu (2+)	
Cheek lineary indep: Wro.	
W(x, x2) = e4 - 5cos (2+)	-5 Sin (2+)
cos(zt) -zsin	(2+) sin (2+) + 2cos(24)

$$= e^{4t} \left( -5\cos(2tt\sin(2t) - 10\cos^{2}(2t) \right)$$

$$+5\sin(2tt\cos(2t) - 10\sin^{2}(2t) \right)$$

$$= -10e^{4t} \neq 0 = s \text{ liq. indep.}$$

$$b. \text{ Fig. 1 (spiral source)}.$$

$$2. \text{ Evgenvalues: } \lambda_{i} = -2, \lambda_{i} = 5$$

$$\text{ for } \lambda_{i} = -2, \quad \forall_{i} = \begin{bmatrix} 1 \\ -6 \end{bmatrix}$$

$$\text{ for } \lambda_{i} = 5, \quad \forall_{i} = \begin{bmatrix} 1 \\ -6 \end{bmatrix} + c_{1}c^{5t} \begin{bmatrix} 1 \\ 1 \end{bmatrix}$$

$$\text{ gen. sol'u: } \quad \times : c_{1}e^{-2t} \begin{bmatrix} 1 \\ -6 \end{bmatrix} + c_{2}c^{5t} \begin{bmatrix} 1 \\ 1 \end{bmatrix}$$

$$\text{ years sol'u: } \quad \times : c_{1}e^{-2t} \begin{bmatrix} 1 \\ -6 \end{bmatrix} + c_{2}c^{5t} \begin{bmatrix} 1 \\ 1 \end{bmatrix}$$

$$\text{ years sol'u: } \quad \times : c_{1}e^{-2t} \begin{bmatrix} 1 \\ -6 \end{bmatrix} + c_{2}c^{5t} \begin{bmatrix} 1 \\ 1 \end{bmatrix}$$

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$$\text{ years sol'u: } \quad \times : c_{1}e^{-2t} \begin{bmatrix} 1 \\ -6 \end{bmatrix} + c_{2}e^{-2t} \begin{bmatrix} 1 \\ 1 \end{bmatrix}$$

$$\text{ years sol'u: } \quad \times : c_{1}$$

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$$\frac{x}{y} = c_{1}e^{2t} \begin{bmatrix} 21 \\ -51 \end{bmatrix} + c_{2}e^{2t} \begin{bmatrix} 21 \\ -51 \end{bmatrix} + \begin{bmatrix} 4 \\ -11 \end{bmatrix} \\
+ c_{3}e^{2t} \begin{bmatrix} 21 \\ -51 \end{bmatrix} + \begin{bmatrix} 4 \\ -11 \end{bmatrix} + \begin{bmatrix} 4 \\ -11 \end{bmatrix} \\
+ c_{3}e^{2t} \begin{bmatrix} 21 \\ -51 \end{bmatrix} + \begin{bmatrix} 4 \\ -11 \end{bmatrix} + \begin{bmatrix} 4 \\ -11 \end{bmatrix} \\
+ c_{3}e^{2t} \begin{bmatrix} 21 \\ -51 \end{bmatrix} + \begin{bmatrix} 4 \\ -51 \end{bmatrix} + \begin{bmatrix} 4 \\ -11 \end{bmatrix} + \begin{bmatrix} 6 \\ -11 \end{bmatrix} \\
+ c_{3}e^{2t} \begin{bmatrix} 21 \\ -51 \end{bmatrix} + \begin{bmatrix} 21 \\ -51 \end{bmatrix} + \begin{bmatrix} 4 \\ -11 \end{bmatrix} + \begin{bmatrix} 4 \\ -11 \end{bmatrix} + \begin{bmatrix} 6 \\ -11 \end{bmatrix} \\
+ c_{3}e^{2t} \begin{bmatrix} 21 \\ -51 \end{bmatrix} + \begin{bmatrix} 21 \\ -51 \end{bmatrix} + \begin{bmatrix} 4 \\ -11 \end{bmatrix} + \begin{bmatrix} 4 \\ -11 \end{bmatrix} + \begin{bmatrix} 6 \\ -11 \end{bmatrix}$$

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