

The following exercises are related to the Racket programming language [3].

1. Re-write the following expressions in Racket and evaluate them using a Racket interpreter/compiler.

- (a)  $(3 \times (5 + (10 \div 5)))$
- (b)  $(2 + 3 + 4 + 5)$
- (c)  $(1 + (5 + (2 + (10 \div 3))))$
- (d)  $(1 + (5 + (2 + (10 \div 3.0))))$
- (e)  $(3 + 5) \times (10 \div 2)$
- (f)  $(3 + 5) \times (10 \div 2) + (1 + (5 + (2 + (10 \div 3))))$

**Solution:**

- (a) `(* 3 (+ 5 (/ 10 5)))`
- (b) `(+ 2 3 4 5)`
- (c) `(+ 1 (+ 5 (+ 2 (/ 10 3))))`
- (d) `(+ 1 (+ 5 (+ 2 (/ 10 3.0))))`
- (e) `(* (+ 3 5) (/ 10 2))`
- (f) `(+ (* (+ 3 5) (/ 10 2)) (+ 1 (+ 5 (+ 2 (/ 10 3)))))`

2. Define a procedure `discount` that takes two arguments: an item's initial price and a percentage discount [2]. It should return the new price:

```
> (discount 10 5)
9.50
> (discount 29.90 50)
14.95
```

**Solution:**

```
(define (discount p d)
  (* p (- 1 (/ d 100.0))))
```

3. Define a function `grcomdiv` that takes two integers and returns their greatest common divisor.

```
> (grcomdiv 10 15)
5
> (grcomdiv 64 30)
2
```

**Solution:**

```
(define (grcomdiv a b)
  (if (< a b)
      (grcomdiv b a)
      (if (= 0 b)
          a
          (grcomdiv b (modulo a b)))))
```

4. Write a function called `appearances` that returns the number of times its first argument appears as a member of its second argument [2].

**Solution:**

```
(define (appearances i l)
  (if (null? l)
      0
      (if (equal? i (car l))
          (+ 1 (appearances i (cdr l)))
          (appearances i (cdr l)))))
```

5. Write a procedure `inter` that takes two lists as arguments. It should return a list containing every element that appears in both lists, exactly once.

**Solution:**

```
; Use appearances from previous question.
(define (inter l1 l2)
  (if (null? l1)
      '()
      (if (> (appearances (car l1) l2) 0)
          (cons (car l1) (inter (cdr l1) l2))
          (inter (cdr l1) l2)))))
```

6. Write a procedure `noatoms` that takes a list and returns the number of atoms it contains.

**Solution:**

```
(define (noatoms l)
  (if (null? l)
```

```

0
(if (not (or (pair? (car l)) (null? (car l))))
    (+ 1 (noatoms (cdr l)))
    (noatoms (cdr l))))

```

7. Here is a Racket procedure that never finishes its job when  $n$  is not 0:

```

(define (forever n)
  (if (= n 0)
      1
      (+ 1 (forever n))))

```

Explain why it doesn't give any result[2].

**Solution:** The terminating condition is:  $n$  equals 0. However, each time `forever` is called,  $n$  is increased.

8. Write a function called `range` that takes an integer  $n$  and returns a list containing the atoms 1, 2, 3, ...,  $n$ .

**Solution:**

```

(define (range n)
  (if (= n 0)
      '()
      (append (range (- n 1)) (list n))))

```

9. Write a function called `reversel` that takes a list and returns it reversed.

**Solution:**

```

(define (reversel l)
  (define (reversel-aux l a)
    (if (null? l)
        a
        (reversel-aux (cdr l) (cons (car l) a))))
  (reversel-aux l null))

```

10. If we list all the natural numbers below 10 that are multiples of 3 or 5, we get 3, 5, 6 and 9. The sum of these multiples is 23. Write a procedure to find the sum of all the multiples of 3 or 5 below 1000 [1].

**Solution:**

```
(define
  (sum35 n)
    (if (= 0 n)
        0
        (if (= 0 (modulo n 3))
            (+ n (sum35 (- n 1)))
            (if (= 0 (modulo n 5))
                (+ n (sum35 (- n 1)))
                (sum35 (- n 1))))))

; Call this with 999 for < 1000.
(sum35 999)
```

11. Write a procedure called `flatten` that takes as its argument a list, possibly including sublists, but whose ultimate building blocks are atoms. It should return a sentence containing all the atoms of the list, in the order in which they appear in the original:

```
> (flatten '(((a b) c (d e)) (f g) (((h))) (i j) k)))
(a b c d e f g h i j k)
```

**Solution:**

```
(define (flatten l)
  (if (null? l)
      '()
      (if (pair? (car l))
          (append (flatten (car l)) (flatten (cdr l)))
          (cons (car l) (flatten (cdr l))))))
```

12. Each new term in the Fibonacci sequence is generated by adding the previous two terms. By starting with 1 and 2, the first 10 terms will be:

1, 2, 3, 5, 8, 13, 21, 34, 55, 89

By considering the terms in the Fibonacci sequence whose values do not exceed four million, find the sum of the even-valued terms [1].

**Solution:**

```
(define (sumflt total)
  (define (aux n-2 n-1 maxval total)
    (if (> n-1 maxval)
        total
        (aux n-1 (+ n-1 n-2) maxval (+ total n-1))))
```

```

    (if (> (+ n-2 n-1) maxval)
        total
        (if (= 0 (modulo (+ n-2 n-1) 2))
            (aux n-1 (+ n-2 n-1) maxval (+ total n-2 n-1))
            (aux n-1 (+ n-2 n-1) maxval total))))
    (aux 0 1 total 0))

```

13. Write a procedure `to-binary` that takes a decimal integer and converts it into a list of 0's and 1's representing the number in binary form. The least significant bit should be on the right of the list.

```

> (to-binary 9)
1001
> (to-binary 23)
10111

```

**Solution:**

```

(define (to-binary n) (if (= n 0)
    '() (append
        (to-binary (/ (- n (modulo n 2)) 2))
        (list (modulo n 2)))))

```

14. Write a function `select` that takes two elements, a list and a position in the list, and return the element of the list in that position.

```

> (select (list 1 2 3 4 5) 1)
2

```

**Solution:**

```

(define (select l i)
    (if (= 0 i)
        (car l)
        (select (cdr l) (- i 1))))

```

15. Write a function `perms` that takes a list as its only argument, and returns a list containing all permutations of that list.

**Solution:**

```
(define (perms l)
  (if (null? l)
      '()
      (apply append
        (map
          (lambda (i) (map
            (lambda (j)(cons i j))
            (perms (remove i l))))
          l))))
```

See the following URL for more information:

<https://see.stanford.edu/materials/icsppcs107/32-Scheme-Examples.pdf>

## References

- [1] Project Euler. Project euler.
- [2] Brian Harvey and Matt Wright. Simply scheme: Introducing computer science.
- [3] PLT Inc. Racket – a programmable programming language.