

# CS201

## Data Structures and Algorithms

Revision Session 4

queue as array

queue as linked list

## Queue

### **implementation:**

queue as array

queue as linked list

### **algorithms:**

isFull

isEmpty

enqueue

dequeue

queue as array

implementation

```
public class QueueArray {
```

3 usages

```
Element[] array;
```

6 usages

```
int first;
```

6 usages

```
int last;
```

4 usages

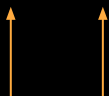
```
int N;
```

```
public QueueArray(int N){  
    array = new Element[N];  
    first = 0;  
    last = 0;  
    this.N = N;  
}
```

isEmpty

N = 10

0 1 2 3 4 5 6 7 8 9

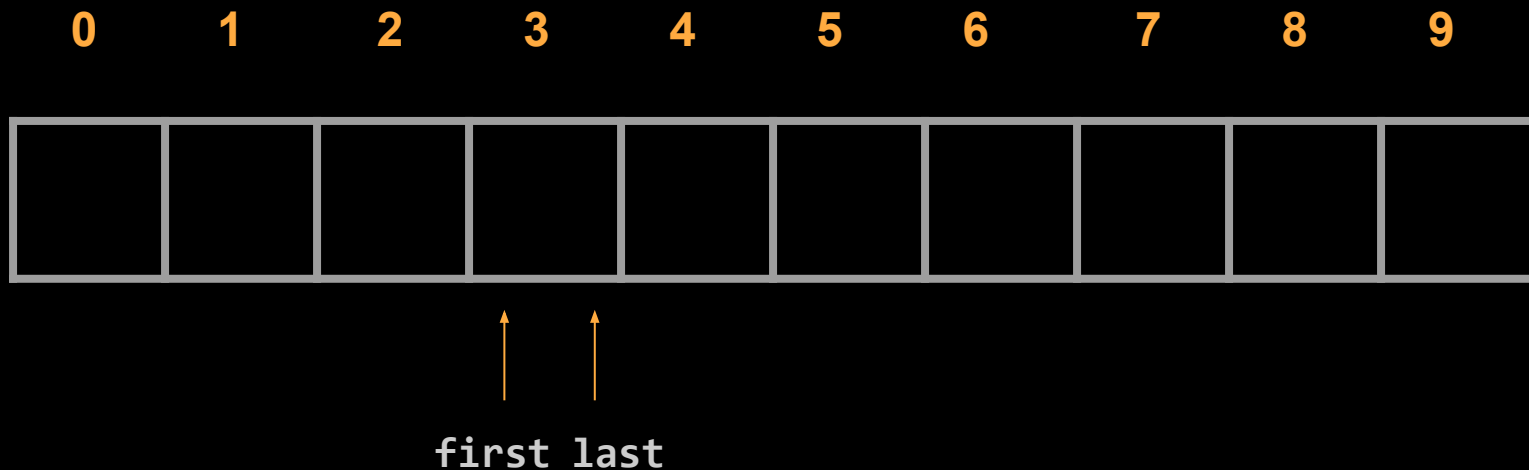


first last

If the first and last fields point to the same index, the queue is empty.

```
public boolean isEmpty(){  
    return first == last;  
}
```

N = 10



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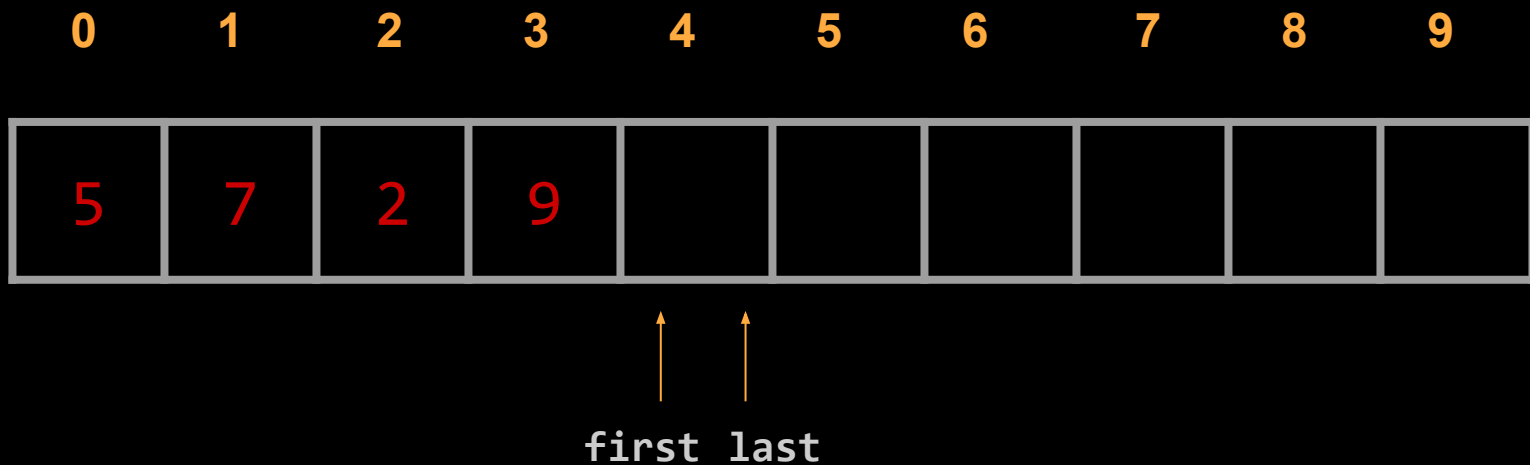
N = 10



If the first and last fields point to the same index, the queue is empty.

```
public boolean isEmpty(){  
    return first == last;  
}
```

N = 10



If the first and last fields point to the same index, the queue is empty.

```
public boolean isEmpty(){  
    return first == last;  
}
```

isFull

N = 12

0 1 2 3 4 5 6 7 8 9 10 11



last first

$$5 = (4 + 1) \% 12$$

$$5 = 5 \% 12$$

$$5 = 5$$

```
public boolean isFull(){  
    return (first == (last + 1) % N);  
}
```

If the first field comes right after the last field, the queue is full.

Why do we need the modulus operator?

N = 12

0 1 2 3 4 5 6 7 8 9 10 11



first



last

```
public boolean isFull(){  
    return (first == (last + 1) % N);  
}
```

$$0 = (11 + 1) \% 12$$

$$0 = 12 \% 12$$

$$0 = 0$$

If the first field comes right after the last field, the queue is full.



enqueue

N = 10

0 1 2 3 4 5 6 7 8 9



↑  
**first**

↑  
**last**

$N = 10$

0 1 2 3 4 5 6 7 8 9

			6	2	8	4	7		
--	--	--	---	---	---	---	---	--	--

↑  
first

↑  
last

N = 10

0 1 2 3 4 5 6 7 8 9

			6	2	8	4	7		
--	--	--	---	---	---	---	---	--	--

↑  
first

↑  
last

How do we pass from index 9 to index 0?

N = 10

0 1 2 3 4 5 6 7 8 9

			6	2	8	4	7	9	
--	--	--	---	---	---	---	---	---	--

↑  
first

↑  
last

$N = 10$

0 1 2 3 4 5 6 7 8 9



↑  
first

$(\text{last} + 1) \% N$

↑  
last

Until it reaches  $N-1$ , it will  
always give the value itself.

$(N-1 + 1) \% N$

$6 \% 10 = 6$

$N \% N$

N = 10

0 1 2 3 4 5 6 7 8 9

			6	2	8	4	7	9	1
--	--	--	---	---	---	---	---	---	---



last



first



```
public void enqueue(Element newElement){  
  
    if (!isFull()){  
        array[last] = newElement;  
        last = (last + 1) % N;  
    } else  
        System.out.println("Queue is full!");  
}
```

If the queue is not full:

put the new element in last

shift the last field by one (it should wrap around when it reaches the end)

dequeue

```
public Element dequeue(){  
  
    Element dequeued = null;  
  
    if (isEmpty()){  
        System.out.println("Queue is empty!");  
    } else {  
        dequeued = array[first];  
        first = (first + 1) % N;  
    }  
    return dequeued;  
}
```

If the list is not empty, store the first element in another variable. Then, shift the first field to the left. If the old first was at  $N-1$ , the modulus will shift it to index 0.

$N = 10$

0

1

2

3

4

5

6

7

8

9



↑  
last

↑  
first

$N = 10$

0

1

2

3

4

5

6

7

8

9



first last

queue as linked list

implementation

```
public class QueueLinked {
```

```
    7 usages
```

```
    Node first;
```

```
    4 usages
```

```
    Node last;
```

```
no usages  ⓘ neslihancesurr
```

```
    public QueueLinked(){
```

```
        first = null;
```

```
        last = null;
```

```
    }
```



first → null

last → null

# isEmpty?

```
public boolean isEmpty(){  
    return first == null;  
}
```

If the first element is null,  
the queue is empty.

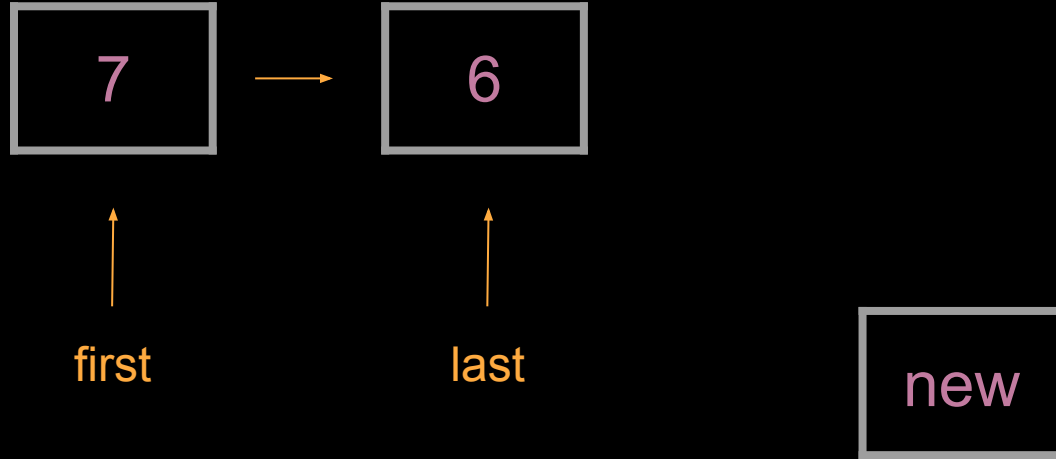
enqueue

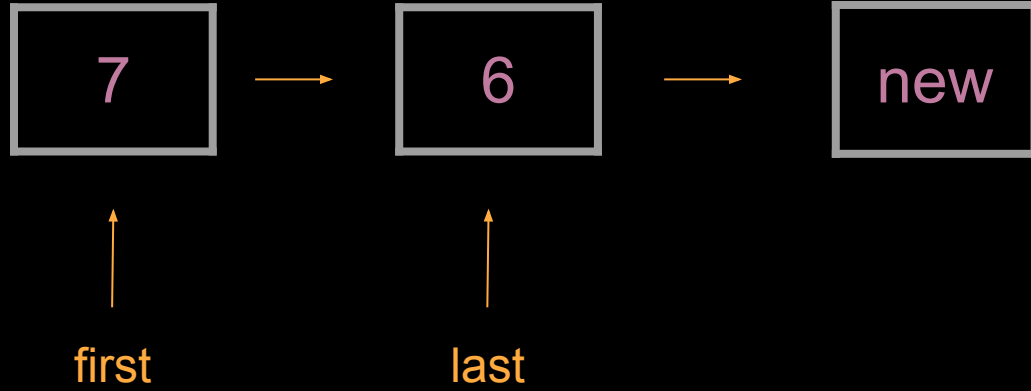


first

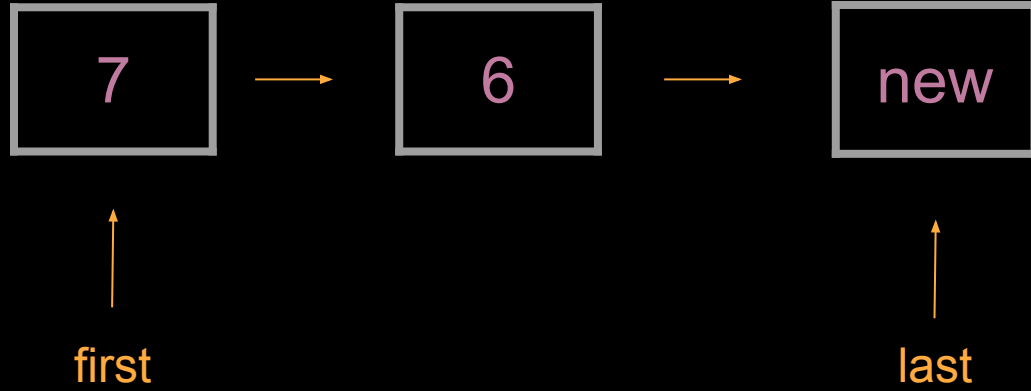


last





```
last.next = newNode;
```



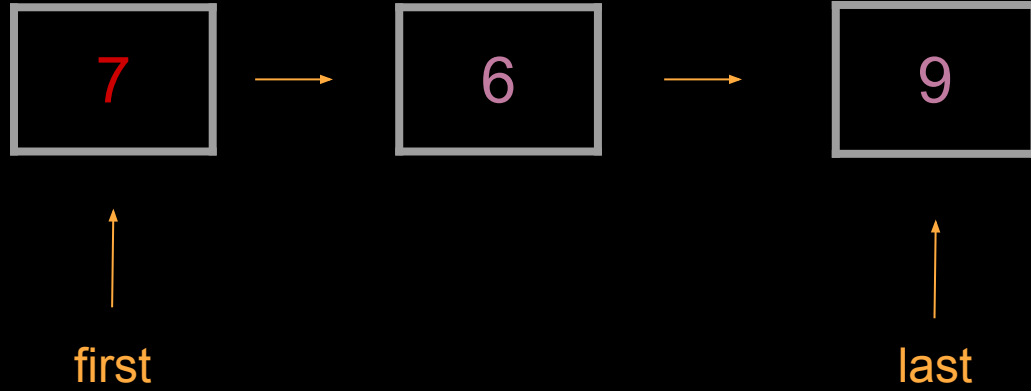
```
last = newNode;
```

```
public void enqueue(Node newNode){  
    if (isEmpty()){  
        first = newNode;  
    } else {  
        last.next = newNode;  
    }  
    last = newNode;  
}
```

If queue is empty, the new node will be first and last. If it is not empty next field of last will point to the new node and the new last will be the new node.

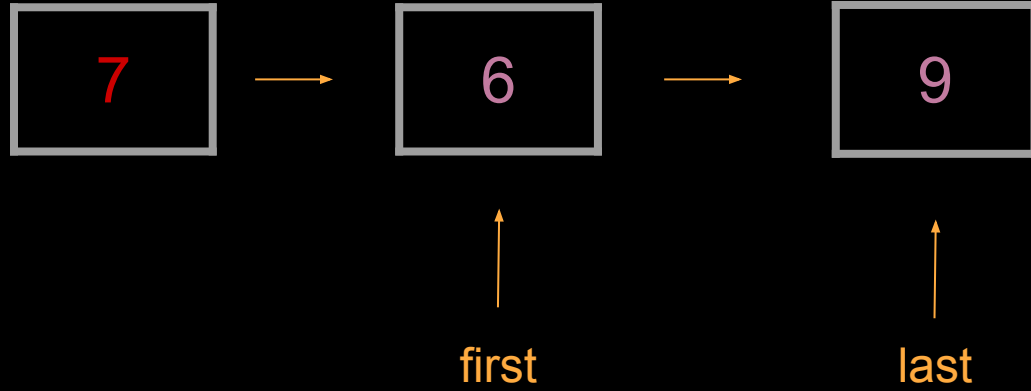


dequeue



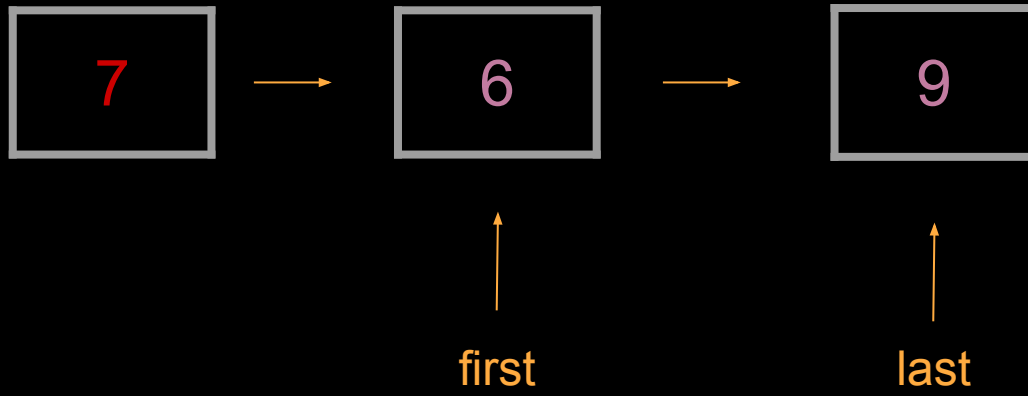
Node dequeued = first;





```
first = first.next;
```





return dequeued; 

Keep the first node to return it later.

If the link is not empty shift first to its next.

If its next is full (only one element), make the only element last.

Return the old first.

```
public Node dequeue(){  
  
    Node dequeued = first;  
  
    if (!isEmpty()){  
        first = first.next;  
        if (first == null){  
            last = null;  
        }  
    } else {  
        System.out.println("Queue is empty!");  
    }  
  
    return dequeued;  
}
```

# Queue exercise

Write a function that moves the element currently at the front of the queue to the rear of the queue. Write the function for both array and linked list implementations.

```
public void moveToRear()
```

before moveToRear(): first 5 6 8 3 4 last

after moveToRear(): first 6 8 10 3 4 5 last