

## INDIAN INSTITUTE OF TECHNOLOGY KHARAGPUR

Stamp / Signature of the Invigilator

EXAMINATION ( End Semester )						er)			SEMESTER ( Autumn )				
Roll Number								Sectio	1	Name			
Subject Number	С	s	6	0	0	5	0	Subject N	me	MACHINE LEARNING			
Department / Cen	ter o	f the	Stu	iden	t					Additional sheets			

## Instructions and Guidelines to Students Appearing in the Examination

- 1. Ensure that you have occupied the seat as per the examination schedule.
- 2. Ensure that you do not have a mobile phone or a similar gadget with you even in switched off mode. Note that loose papers, notes, books should not be in your possession, even if those are irrelevant to the paper you are writing.
- 3. Data book, codes or any other materials are allowed only under the instruction of the paper-setter.
- Use of instrument box, pencil box and non-programmable calculator is allowed during the examination. However, exchange of these items is not permitted.
- 5. Additional sheets, graph papers and relevant tables will be provided on request.
- 6. Write on both sides of the answer script and do not tear off any page. Report to the invigilator if the answer script has torn page(s).
- 7. Show the admit card / identity card whenever asked for by the invigilator. It is your responsibility to ensure that your attendance is recorded by the invigilator.
- 8. You may leave the examination hall for wash room or for drinking water, but not before one hour after the commencement of the examination. Record your absence from the examination hall in the register provided. Smoking and consumption of any kind of beverages is not allowed inside the examination hall.
- 9. After the completion of the examination, do not leave the seat until the invigilator collects the answer script.
- 10. During the examination, either inside the examination hall or outside the examination hall, gathering information from any kind of sources or any such attempts, exchange or helping in exchange of information with others or any such attempts will be treated as adopting 'unfair means'. Do not adopt 'unfair means' and do not indulge in unseemly behavior as well.

Violation of any of the instructions may lead to disciplinary action.

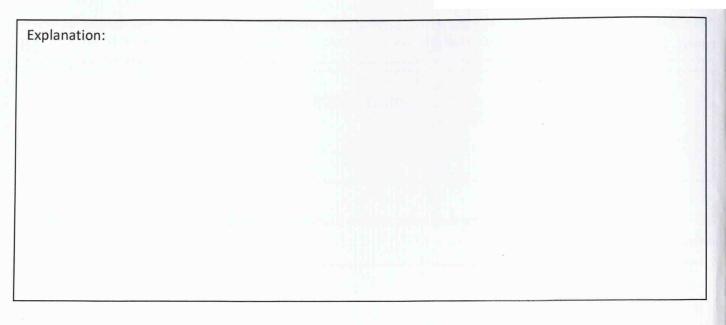
Signature of the Student

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Question Number	1	2	3	4	5	6	7	8	9	10	Total
Marks Obtained											
Marks ob	tained (in	words)		Sign	ature of	the Exam	niner	Sigi	nature of	the Scrut	ineer
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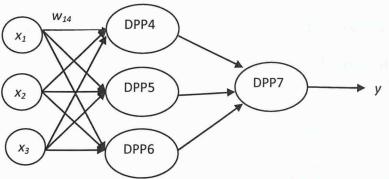
**Instructions**: Answer all FIVE questions. Time = 3hrs. Total marks = 5x20 = 100. Write your answers only in the space provided. Show the solution steps as required. The question paper has total 12 pages.

## **ROUGH WORK**

1.(a). Write the objective function for the primal optimization problem for soft margin SVM. Briefly, d terms.	[2]
a on the con-	
b). Write the objective function for the dual optimization problem for soft margin SVM. Briefly, define	e the
erms.	[2]
c). For support vectors $X_j$ in a hard margin SVM, $WX + b = 0$ , we have: $ WX + b  = $	[2
d). We are designing a SVM, $WX + b = 0$ , suppose $(X_j, y_j)$ 's are the support vectors and $\alpha_j$ 's the	
corresponding Lagrange multipliers, then $W$ =	[2
e). We are designing a SVM, $WX + b = 0$ , suppose $(X_j, y_j)$ 's are the support vectors and $\alpha_j$ 's the	
corresponding Lagrange multipliers, then $\sum lpha_j y_j =$	[2
f). Consider the following training data set of (seven) points $X$ 's in a plane and their binary class label	y's:
X (1, 0) (0, 1) (0, -1) (-1, 0) (0, 2) (0, -2) (-2, 0)   y -1 -1 -1 +1 +1 +1 +1	
We perform the following non-linear transform of the input vector $X = (x_1, x_2)$ to obtain the transform	ned
Feature vector $Z = (z_1, z_2) = (\phi_1(X), \phi_2(X))$ , with $\phi_1(X) = x_2^2 - 2x_1 + 3$ , $\phi_2(X) = x_1^2 - 2x_2 - 3$ .	
Write the equation of the optimal separating hyperplane in transformed space $\it Z$ . Explain your answe	r. [1
Write the equation of the optimal separating type plants.	
Equation of optimal separating hyperplane:	
	di. Ti



2.(a). A dot product perceptron (DPP) has output  $y = W \cdot X$ , where W is the weight vector and X is the input vector. There is no bias input. Consider the network of dot product perceptrons shown below. The input (nodes) are numbered 1, 2, and 3. The other nodes are numbered (5-7) as shown in figure. Weight  $w_{ij}$  connects node i to node j. It can be shown that this network is equivalent to a single dot product perceptron. Draw the equivalent dot product perceptron showing its weights in terms of the original weights. [10]



c) is the corresponding or ceptron showing the weig	reignts of the	optimal perceptron fo	r this task. Draw
i			

3.(a). Consider a set D of six two-dimensional points: $a = (0, 0)$ , $b = (5, 0)$ , $c = (10, 0)$ , $d = (0, 5)$ , $e = (5, 8)$ , and $f = (10, 0)$ , $d = (10, $
(10, 8). We cluster these points using k-means algorithm with $k = 3$ and Euclidean as the distance metric. Ties
are broken in favor of the mean to the left/bottom. A "k-seed set" is a subset of D that form the initial means,
e.g. $\{a, b, c\}$ is a 3-seed set. A "k-clustering" is a partition of D into k non-empty subsets, e.g., $\{a, a, f\}$ $\{b, c\}$ , $\{e\}$
is a 3-clustering. Naturally, a k-clustering has a corresponding set of k means. A k-clustering is called stable if
an iteration of the k-means algorithm using the corresponding means leaves it unchanged. Fill in the following
table about the given 3-clusterings. [10]

3-clustering	Stable?	If stable, list all the k-seed sets that converge to the 3-clustering after some iterations of the k-means algorithm.
{a, b, e} {c, d} {f}		
{a, b, d} {e, f} {c}		
{a} {d} {b, c, e, f}		

(a) {d} {b, c, e, f}		
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o : I		
Consider a set of N one-dimensional point	its: $\{2^0, 2^1, 2^2,, 2^{N-1}\}$ , with Euclidean as the distant	ce metric. Drav
schematic of the dendogram for clustering	the points using single-linkage algorithm.	[5]
		1.0
		1
		12.20
Draw a schematic of the dendogram for o	clustering the above N points using complete-linkage	ge algorithm. [
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4.(a). In the following set of training examples, Feature F1 can take on the values a, b, or c; Feature F2 is Boolean-valued; and Feature F3 is always a real-valued number in [0, 1]. Using the decision stump (a single node decision tree) learner as weak learner, what would the weights be on each of the six training examples after one round of AdaBoost? Show your work.

	F1	F2	F3	Class		F1	F2	F3	Class
Example 1	a	Ţ	0.2	+	Example 4	b	T	0.6	-
Example 2	b	F	0.5	+	Example 5	а	F	0.1	-
Example 3	b	F	0.9	+	Example 6	а	Т	0.7	_

Weight of Example 1:

Weight on Example 2:

Weight on Example 3:

Weight on Example 4:

Weight on Example 5:

Weight on Example 6:

(b). The following data set has ten examples each with one real valued feature x and one binary output y. What is the leave-one-out cross validation error of 1-NN (nearest neighbor) classifier using Euclidean distance on this data set in terms of number of misclassified examples? Explain your answer briefly. [10]

X	-0.1	0.7	1.0	1.6	2.0	2.5	3.2	3.5	4.1	4.9
1/	_	+	+	-	+	+	-	-	+	+

ads to the minimum squared error loss. Briefly explain your answer.	[5]
. What is the amount of squared error loss due to this projection?	[5]
. Define Kullback-Liebler divergence between two distributions. Define the terms used.	[5]
When is a feature subset evaluation measure termed as "monotonic"?	[5]
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