HW2_Estrada-Rand_Noah

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Problem Set 2

Problem 8

a) Basic Setup

```
setwd("C:/Users/noahe/Desktop/MGSC310")
college <-read.csv("College.csv")
dim(college)</pre>
```

[1] 777 19

b) First Few Columns of New Data Frame

```
View(college)
rownames(college) = college[,1]
View(college)
college <- college[,-1]
View(college)
head(college)</pre>
```

##		${\tt Private}$	Apps	Accept	Enroll	Top10pe	erc
##	Abilene Christian University	Yes	1660	1232	721		23
##	Adelphi University	Yes	2186	1924	512		16
##	Adrian College	Yes	1428	1097	336		22
##	Agnes Scott College	Yes	417	349	137		60
##	Alaska Pacific University	Yes	193	146	55		16
##	Albertson College	Yes	587	479	158		38
##		Top25per	rc F.	Undergra	ad P.Un	dergrad	Outstate
##	Abilene Christian University	52		288	35	537	7440
##	Adelphi University	29		268	33	1227	12280
##	Adrian College	50		103	36	99	11250
##	Agnes Scott College	89		5:	10	63	12960
##	Alaska Pacific University	44		24	19	869	7560
##	Albertson College	(62	6	78	41	13500
##		Room.Boa	ard B	ooks Per	rsonal	PhD Term	minal
##	Abilene Christian University	33	300	450	2200	70	78
##	Adelphi University	64	450	750	1500	29	30
##	Adrian College	37	750	400	1165	53	66
##	Agnes Scott College	54	450	450	875	92	97
##	Alaska Pacific University	4:	120	800	1500	76	72
##	Albertson College	33	335	500	675	67	73
##		S.F.Rat:	io pe	rc.alum	ni Expe	nd Grad	.Rate
##	Abilene Christian University	18	. 1	:	12 70	41	60
	Adelphi University	12.2		16 10527		56	
##	Adrian College	12	.9	3	30 87	35	54

```
## Agnes Scott College 7.7 37 19016 59
## Alaska Pacific University 11.9 2 10922 15
## Albertson College 9.4 11 9727 55
```

 \mathbf{c}

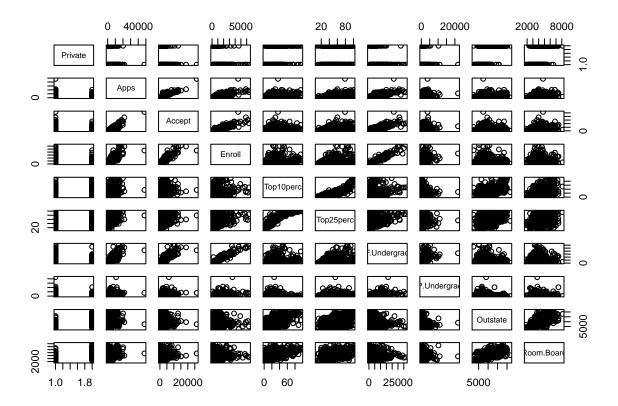
i) Summary Statistics

summary(college)

```
Private
                                   Accept
                                                    Enroll
                                                                 Top10perc
##
                   Apps
    No :212
                         81
                               Min.
                                      :
                                          72
                                                       : 35
                                                               Min.
                                                                     : 1.00
              Min.
                     :
                                               Min.
##
    Yes:565
              1st Qu.: 776
                               1st Qu.: 604
                                                1st Qu.: 242
                                                               1st Qu.:15.00
##
              Median: 1558
                               Median: 1110
                                               Median: 434
                                                               Median :23.00
##
              Mean
                     : 3002
                                      : 2019
                               Mean
                                               Mean
                                                       : 780
                                                               Mean
                                                                       :27.56
              3rd Qu.: 3624
                               3rd Qu.: 2424
                                                3rd Qu.: 902
                                                               3rd Qu.:35.00
##
##
              Max.
                      :48094
                               Max.
                                      :26330
                                               Max.
                                                       :6392
                                                               Max.
                                                                       :96.00
##
      Top25perc
                     F.Undergrad
                                      P.Undergrad
                                                           Outstate
##
    Min. : 9.0
                    Min.
                            : 139
                                     Min.
                                                  1.0
                                                               : 2340
                                            :
                                                        Min.
    1st Qu.: 41.0
                    1st Qu.:
                               992
                                     1st Qu.:
                                                 95.0
                                                        1st Qu.: 7320
    Median: 54.0
                    Median: 1707
                                               353.0
                                                        Median: 9990
##
                                     Median :
                                                               :10441
##
    Mean
           : 55.8
                    Mean
                           : 3700
                                     Mean
                                               855.3
                                                        Mean
    3rd Qu.: 69.0
                    3rd Qu.: 4005
                                                        3rd Qu.:12925
##
                                     3rd Qu.:
                                               967.0
                            :31643
##
    Max.
           :100.0
                    Max.
                                     Max.
                                             :21836.0
                                                        Max.
                                                               :21700
##
      Room.Board
                        Books
                                        Personal
                                                          PhD
##
    Min.
           :1780
                         : 96.0
                                            : 250
                                                            : 8.00
                   Min.
                                     Min.
                                                     Min.
    1st Qu.:3597
                   1st Qu.: 470.0
                                     1st Qu.: 850
                                                     1st Qu.: 62.00
    Median:4200
                   Median : 500.0
                                     Median:1200
                                                     Median : 75.00
##
##
    Mean
           :4358
                   Mean
                           : 549.4
                                     Mean
                                            :1341
                                                     Mean
                                                            : 72.66
##
    3rd Qu.:5050
                   3rd Qu.: 600.0
                                     3rd Qu.:1700
                                                     3rd Qu.: 85.00
##
    Max.
           :8124
                   Max.
                           :2340.0
                                     Max.
                                            :6800
                                                     Max.
                                                            :103.00
##
                      S.F.Ratio
                                      perc.alumni
       Terminal
                                                          Expend
                                            : 0.00
                                                             : 3186
          : 24.0
                           : 2.50
##
    Min.
                    Min.
                                     Min.
                                                      Min.
    1st Qu.: 71.0
                    1st Qu.:11.50
                                     1st Qu.:13.00
                                                      1st Qu.: 6751
    Median: 82.0
                    Median :13.60
                                     Median :21.00
                                                      Median: 8377
          : 79.7
##
    Mean
                    Mean
                            :14.09
                                     Mean
                                            :22.74
                                                             : 9660
                                                      Mean
    3rd Qu.: 92.0
##
                    3rd Qu.:16.50
                                     3rd Qu.:31.00
                                                      3rd Qu.:10830
##
    Max.
           :100.0
                            :39.80
                                            :64.00
                                                             :56233
                    Max.
                                     Max.
                                                      Max.
##
      Grad.Rate
##
    Min.
          : 10.00
##
    1st Qu.: 53.00
##
    Median : 65.00
    Mean
          : 65.46
##
    3rd Qu.: 78.00
    Max.
           :118.00
```

ii) Scatterplot Matrix

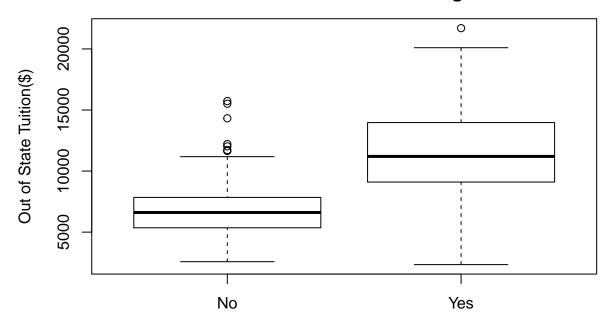
```
pairs(college[,1:10])
```



iii)

```
plot(college$Outstate~college$Private,
    main = "Boxplots of Out of State Cost\nFor Public and Private Colleges",
    ylab = "Out of State Tuition($)",xlab = "Whether or Not School is Private")
```

Boxplots of Out of State Cost For Public and Private Colleges



Whether or Not School is Private

iv) Making New Variable for Levels of Elite Students

```
Elite <- rep("No",nrow(college))
Elite[college$Top10perc >50] <- "Yes"
Elite <- as.factor(Elite)
college <- data.frame(college,Elite)
summary(college)</pre>
```

```
Enroll
                                                                   Top10perc
##
    Private
                                    Accept
                    Apps
    No :212
                          81
                                                                        : 1.00
              Min.
                      :
                                Min.
                                       :
                                           72
                                                 Min.
                                                           35
                                                                 Min.
    Yes:565
               1st Qu.:
                         776
                                1st Qu.:
                                          604
                                                 1st Qu.: 242
                                                                 1st Qu.:15.00
##
              Median: 1558
                                Median: 1110
                                                 Median: 434
                                                                 Median :23.00
##
##
              Mean
                      : 3002
                                Mean
                                       : 2019
                                                 Mean
                                                         : 780
                                                                 Mean
                                                                         :27.56
##
               3rd Qu.: 3624
                                3rd Qu.: 2424
                                                 3rd Qu.: 902
                                                                 3rd Qu.:35.00
                                                         :6392
              Max.
                      :48094
                                       :26330
                                                 Max.
                                                                 Max.
                                                                         :96.00
##
                                Max.
##
      Top25perc
                      F. Undergrad
                                       P.Undergrad
                                                             Outstate
                                                                 : 2340
##
           : 9.0
                     Min.
                                139
                                      Min.
                                                   1.0
                                                         Min.
    1st Qu.: 41.0
                     1st Qu.:
                                992
                                                  95.0
                                                         1st Qu.: 7320
##
                                      1st Qu.:
##
    Median: 54.0
                     Median: 1707
                                      Median:
                                                 353.0
                                                         Median: 9990
           : 55.8
                            : 3700
                                                 855.3
##
    Mean
                     Mean
                                      Mean
                                                         Mean
                                                                 :10441
    3rd Qu.: 69.0
                     3rd Qu.: 4005
                                      3rd Qu.:
                                                 967.0
                                                         3rd Qu.:12925
                             :31643
                                              :21836.0
    Max.
           :100.0
                     Max.
                                                         Max.
                                                                 :21700
##
                                      Max.
##
      Room.Board
                        Books
                                         Personal
                                                           PhD
##
    Min.
           :1780
                    Min.
                           : 96.0
                                      Min.
                                              : 250
                                                      Min.
                                                              : 8.00
    1st Qu.:3597
                    1st Qu.: 470.0
                                      1st Qu.: 850
                                                      1st Qu.: 62.00
    Median:4200
                    Median : 500.0
                                      Median:1200
                                                      Median: 75.00
```

```
3rd Qu.: 85.00
    3rd Qu.:5050
                   3rd Qu.: 600.0
                                     3rd Qu.:1700
##
##
    Max.
           :8124
                           :2340.0
                                     Max.
                                            :6800
                                                            :103.00
##
       Terminal
                      S.F.Ratio
                                      perc.alumni
                                                          Expend
##
    Min.
           : 24.0
                    Min.
                           : 2.50
                                     Min.
                                            : 0.00
                                                     Min.
                                                             : 3186
    1st Qu.: 71.0
                    1st Qu.:11.50
                                     1st Qu.:13.00
                                                      1st Qu.: 6751
##
    Median: 82.0
                    Median :13.60
                                     Median :21.00
                                                      Median: 8377
           : 79.7
##
    Mean
                    Mean
                            :14.09
                                     Mean
                                            :22.74
                                                      Mean
                                                             : 9660
##
    3rd Qu.: 92.0
                    3rd Qu.:16.50
                                     3rd Qu.:31.00
                                                      3rd Qu.:10830
##
    Max.
           :100.0
                    Max.
                            :39.80
                                     Max.
                                           :64.00
                                                      Max.
                                                             :56233
##
      Grad.Rate
                     Elite
          : 10.00
                     No:699
##
   \mathtt{Min}.
   1st Qu.: 53.00
                     Yes: 78
##
  Median : 65.00
##
  Mean
           : 65.46
##
    3rd Qu.: 78.00
## Max.
           :118.00
plot(college$Outstate~college$Elite, main = "Boxplot of Schools With 50%+ Students\nFrom Top 10% of Hig
     xlab = "Whether or not >50% of students are from top 10%",
     ylab = "Cost of Out of State Tuition ($)")
```

Mean

: 72.66

##

Mean

:4358

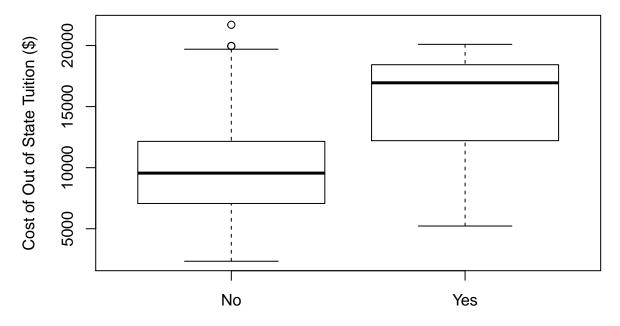
Mean

: 549.4

Mean

:1341

Boxplot of Schools With 50%+ Students From Top 10% of High School Class



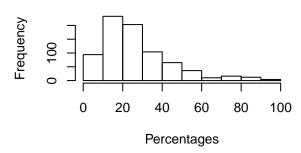
Whether or not >50% of students are from top 10%

```
v)
par(mfrow = c(2,2))
hist(college$Room.Board, main = "Histogram for Room and Board",
```

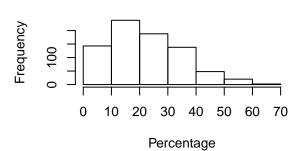
Histogram for Room and Board

2000 4000 6000 8000 Cost

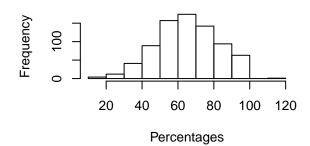
Histogram for Percentage of Students From top 10%



Histogram of % of Alumni Who Donate



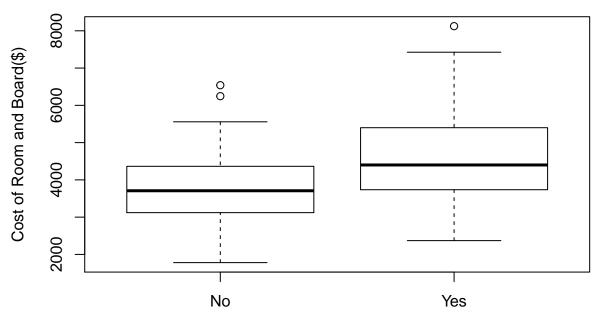
Histogram of Graduation Rates



vi)

```
boxplot(college$Room.Board~college$Private, xlab = "Whether School is Private or Not",
    ylab = "Cost of Room and Board($)",
    main = "Boxplots for Private and Public Schools \nand The distribution of Boarding Cost")
```

Boxplots for Private and Public Schools and The distribution of Boarding Cost



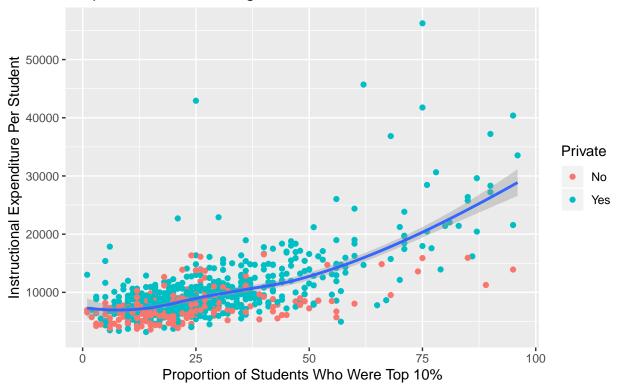
Whether School is Private or Not

Further analysis of college data highlighted the fact that private schools have a higher room and board cost on average. Moreover, it appears that although both distributions overlap significantly, the inner quartile range of private colleges is significantly higher than that of public schools. Thus, when one attends a private school they should expect higher room and board costs.

```
ggplot(college,aes(Top10perc,Expend)) + geom_point(aes(Top10perc,Expend,color = Private)) +
   geom_smooth() + labs(title = "Expenditure Per Student vs \nProportion of 10% of High School Class")+
   xlab("Proportion of Students Who Were Top 10%") + ylab("Instructional Expenditure Per Student")
```

`geom_smooth()` using method = 'loess' and formula 'y ~ x'

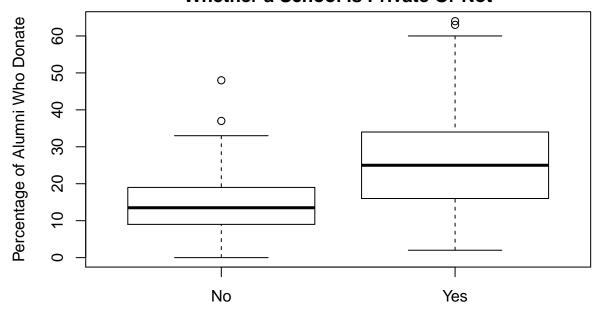
Expenditure Per Student vs Proportion of 10% of High School Class



In looking at the percentage of new students taken from the top 10% of their high school class, it was found that this particular variable held a strong positive correlation with instructional expenditure per student. This points to a positive linear relationship in which the higher the percetage of elite students, the higher the instructional expenditure per student. Thus, schools with higher achieving individuals spend more on their instruction than schools with lower achieving students. Furthermore this plot serves to illustrate that the majority of the higher spending schools are private institutions.

```
boxplot(college$perc.alumni~college$Private, xlab = "Whether College is Private or Not",
    ylab = "Percentage of Alumni Who Donate",
    main = "Boxplots of % of Alumni Who Donate\nvs\nWhether a School is Private Or Not")
```

Boxplots of % of Alumni Who Donate vs Whether a School is Private Or Not



Whether College is Private or Not

In once again considering the variable of private versus public institutions, it becomes apparent that private schools garner much higher amounts of alumni donations than do public institutions. However, this does not necessarily mean that private institutions dominate this metric. Looking at the boxplots one can observe that private institutions also have a much larger range of proportions of alumni who donate in comparison to public institutions. Yet, it still remains true that private institutions garner a higher percentage of alumni donations on average.

Problem 10

a)

[1] 14

The boston data set has 506 rows and 14 columns. In this particular dataset, each row delineates a different town while each column is a different metric of each town.

```
library(MASS)
?Boston

## starting httpd help server ... done
bos <- Boston
nrow(bos)

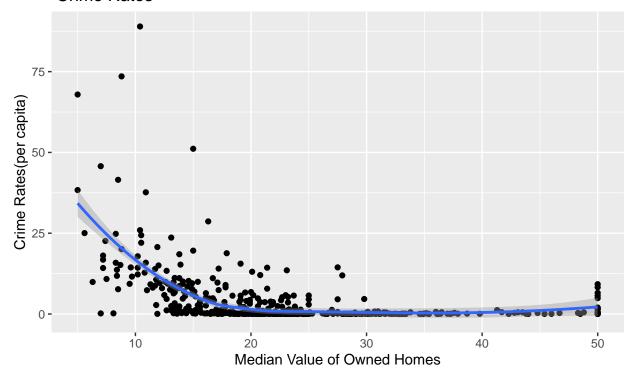
## [1] 506
ncol(bos)
```

b)

```
ggplot(bos,aes(medv,crim)) + geom_point(aes(medv,crim)) + xlab("Median Value of Owned Homes")+
ylab("Crime Rates(per capita)") + geom_smooth()+
labs(title = "Scatterplot for Median Value of Owned Homes\nvs\n Crime Rates")
```

`geom_smooth()` using method = 'loess' and formula 'y ~ x'

Scatterplot for Median Value of Owned Homes vs Crime Rates

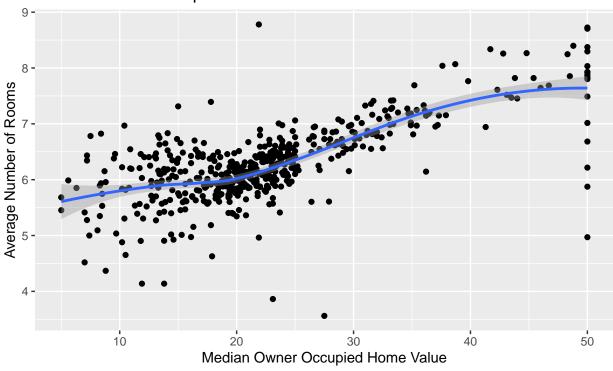


From the above graph there appears to a weak negative correlation between the median value of owned homes in the town and the crime rate in the town. When looking at the plot it becomes apparent that the highest crime rates exist in the lower range of median values of owned homes, indicating that wealthier neighborhoods have lower crime rates.

```
ggplot(bos,aes(medv,rm)) + geom_point(aes(medv,rm)) + geom_smooth() +
labs(title = "Number of Rooms on Average\nvs\nMedian Owner Occupied Home Value") +
xlab("Median Owner Occupied Home Value") + ylab("Average Number of Rooms")
```

`geom_smooth()` using method = 'loess' and formula 'y ~ x'

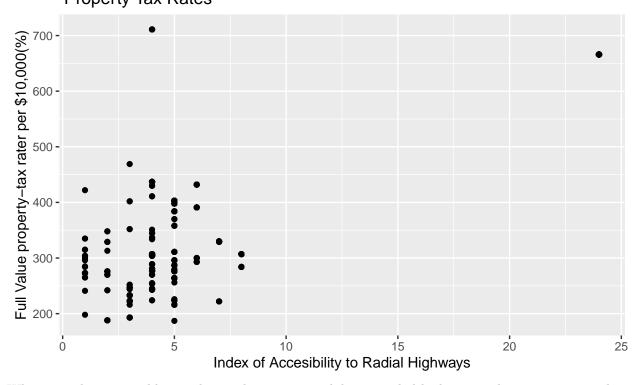
Number of Rooms on Average vs Median Owner Occupied Home Value



As illustrated by the above scatterplot, it becomes apparent that there is a strong positive correlation between median home values and the number of rooms per dwelling. This points to the idea that higher valued homes tend to have more rooms.

```
ggplot(bos,aes(rad,tax)) + geom_point(aes(rad,tax)) + xlab("Index of Accesibility to Radial Highways")
ylab("Full Value property-tax rater per $10,000(%)") +
labs(title = "Scatterplot for Accesibility to Radial Highways\nvs\n Property Tax Rates")
```

Scatterplot for Accesibility to Radial Highways vs Property Tax Rates



When considering possible correlations between accesibility to radial highways and property taxes, there appears to be little correlation if any. While calculating the pearson's correlation coefficient for the two variables indicates a strong positive linear relationship between the two, graphical analysis indicates that the relationship may not necessarily be significant in relation to the real world.

$\mathbf{c})$

cor(bos\$crim,bos)

```
##
                              indus
        crim
                                            chas
                      zn
                                                       nox
                                                                    rm
                                                                              age
##
             -0.2004692 0.4065834 -0.05589158 0.4209717 -0.2192467 0.3527343
##
                dis
                                     tax
                                            ptratio
                                                                    lstat
                          rad
                                                         black
##
        -0.3796701
                    0.6255051 0.5827643 0.2899456 -0.3850639 0.4556215
##
               medv
  [1,] -0.3883046
```

Looking at the correlation between crime rates and all other variables in the dataset, a few interesting trends emerge. First and foremost, it appears that crime rates have a moderate strength correlation with tax rates in each town. Furthermore, there is a similar correlational relationship between crime rates and percent of the lower status of the population. Yet, the strongest correlation concerning crime rates is found between crime and accesibility to radial highways. A decently strong positive correlation is found between these two variables indicating a positive linear relationship between accesibility to highways and crime. Thus, it would be somewhat reasonable to assume that the closer a town is to highways, the higher the level of crime. When Looking at negative correlations, median value of owner occupied homes and the proportion of blacks per town are negatively correlated to the level of crime in each town. Thus, crime rate has a negative linear relationship with both the level of black citizens and median home value in each city. This implies that the wealthier the neighborhood, the less crime, as highlighted earlier in this report. These findings present

significant implications when looking at predictors of crime throughout Boston.

d)

```
range(bos$crim)
## [1] 0.00632 88.97620
boxplot.stats(bos$crim)
## $stats
## [1] 0.00632 0.08199 0.25651 3.67822 8.98296
##
## $n
## [1] 506
##
## $conf
  [1] 0.00391236 0.50910764
##
##
## $out
##
    [1] 13.52220 9.23230 11.10810 18.49820 19.60910 15.28800 9.82349
   [8] 23.64820 17.86670 88.97620 15.87440 9.18702 20.08490 16.81180
  [15] 24.39380 22.59710 14.33370 11.57790 13.35980 38.35180 9.91655
  [22] 25.04610 14.23620 9.59571 24.80170 41.52920 67.92080 20.71620
  [29] 11.95110 14.43830 51.13580 14.05070 18.81100 28.65580 45.74610
  [36] 18.08460 10.83420 25.94060 73.53410 11.81230 11.08740 12.04820
## [43] 15.86030 12.24720 37.66190 9.33889 10.06230 13.91340 11.16040
## [50] 14.42080 15.17720 13.67810 9.39063 22.05110 9.72418 9.96654
## [57] 12.80230 10.67180 9.92485
                                   9.32909 9.51363 15.57570 13.07510
## [64] 15.02340 10.23300 14.33370
```

When weighing the range of crime rates in suburbs throughout Boston, it becomes glaringly apparent that there are numerous outliers in this dataset. In looking at the list of outliers, the list is extensive, detailing that numerous suburbs have abnormally high levels of crime when compared to the bulk of the remaining data. Furthermore, the range of this metric is large, ranging from .6% to 88.97% per capita indicative of a very large range of crime rates throughout Boston.

```
range(bos$tax)
```

```
## [1] 187 711
boxplot.stats(bos$tax)
```

```
## $stats
## [1] 187 279 330 666 711
##
## $n
## [1] 506
##
## $conf
## [1] 302.8173 357.1827
##
## pout
## numeric(0)
```

When considering the range of values for property taxes, there do not appear to be any outliers in the given data. In this case, the lowest tax rate per \$10,000 is \$187 while the highest is \$711.

Now, in consideration of pupil-teacher ratios a few outliers appear when alayzing the range of the predictor. In this case, however, the outliers exist on the lower end of the metric, with only abnormally low values existing. Overall, however, the pupil teacher ratio values range from 12.6 to 22.0 students per teacher in Boston.

e)

[15] 13.0

There are 35 tracts that bound the river.

```
sum(bos$chas ==1)
## [1] 35
```

f)

The median pupil to teacher ratio across all towns is 19.05 pupils per teacher.

```
median(bos$ptratio)
```

```
## [1] 19.05
```

\mathbf{g}

There are two suburbs in Boston with the lowest median value of owner occupied homes is a median value of \$5,000. These entries are entries 399 and 406.

```
min(bos$medv)
```

```
## [1] 5
```

The values of the remaining predictors in the suburbs with the lowest median value of owner occupied homes are shown below:

```
bos[bos$medv == min(bos$medv),]
```

```
crim zn indus chas
                               nox
                                      rm age
                                                 dis rad tax ptratio black
## 399 38.3518 0
                  18.1
                           0 0.693 5.453 100 1.4896
                                                      24 666
                                                                20.2 396.90
## 406 67.9208 0
                   18.1
                           0 0.693 5.683 100 1.4254 24 666
                                                                20.2 384.97
##
       1stat medv
## 399 30.59
```

406 22.98

The corresponding ranges are also below:

5

When comparing the crime rate of the suburbs with the two lowest median value of owner occupied homes to the entire range of crime rates, it becomes clear that suburb 399 is in the lower half of the range while suburb 406 is in the upper half of the range. This is curious as this is the only variable where the two suburbs differ significantly, while all other variables are nearly identical.

range(bos\$crim)

[1] 0.00632 88.97620

When looking at proportion of residential lan zoned for lots over 25,00 square feet, the values of suburbs 399 and 406 score the lowest score possible, 0. This indicates that no lots of residential land are zoned for over 25,000 square feet, indicating that homes and housing may only comprise a small portion of the land in these two suburbs.

range(bos\$zn)

[1] 0 100

Regarding the proportion of non-reatail business acres per town, suburbs 399 and 406 fall in the middle of the overall range with both scoring values of 18.1% of land belonging to non-retail businesses. This indicates that the majority of businesses in these areas are retail based businesses.

range(bos\$indus)

[1] 0.46 27.74

When analyzing the average number of rooms per dwelling, the suburbs with the lowest median value of owner occupied homes fall close to the middle of the range of values, both around an average of 5 rooms per dwelling.

range(bos\$rm)

[1] 3.561 8.780

When considering the predictor of age, suburbs 399 and 406 have 100% of their owner-occupied dwellings built before 1940, indicating that both are older suburbs in the Boston area.

range(bos\$age)

[1] 2.9 100.0

In regards to the weighted mean of distance to five Boston employment centers, suburbs 399 and 406 score close to the minimum value, indicating that they are close to places of employment.

range(bos\$dis)

[1] 1.1296 12.1265

However, when considering accesibility from these suburbs to raidal highways, they score the highest value of 24, indicating that they are not conveniently located near radial highways.

range(bos\$rad)

[1] 1 24

When considering the full-value property tax rate, suburbs 399 and 406 have among the highest tax rate per \$10000. This indicates that while the neighborhood may be older and not as highly appraised as other suburbs, they still experience relatively high rates of property tax.

range(bos\$tax)

[1] 187 711

When weighing the pupil to teacher ratio in these suburbs, they score among the highest ratios both town having a pupil to teacher ratio of 20.2 students per teacher.

```
range(bos$ptratio)
```

```
## [1] 12.6 22.0
```

Further analyzing other predictor variables for suburbs 399 and 406, it appears that these two suburbs score close to the highest score for the proportion of blacks per town.

```
range(bos$black)
```

```
## [1] 0.32 396.90
```

Overall these findings present curious implications. While the two suburbs analyzed above have the lowest median value of owner-occupied homes, they are among one of the highest taxed within the data set. Furthermore, the fact that zero percent of both suburbs are zone for residential lots over 25,000 square feet, it becomes apparent that the homes there are smaller.

H)

From the dataset, there are 64 total suburbs which average more than 7 rooms per dwelling.

```
nrow(bos[bos$rm >7,])
```

```
## [1] 64
```

Further analyses revealed that only 13 suburbs average more than 8 rooms per dwelling. This is only a small proportion of the total neighborhoods, indicating that far fewer rooms is the norm. However, when looking at other predictors of these neighborhoods, it becomes clear that these neighborhoods also have other distinct characteristics. For instance, their crime rate are nearly zero, indicating a safer environment overall. Furthermore, the median value of owner occupied homes ranges from \$21,000 to \$50,000 in value. Lastly, the pupil teacher ratios are also in the lower end of that predictors values, indicating a more personalized education for the children therein. Observing the trends in this data regarding these suburbs with homes averaging more than 8 rooms, it becomes clear that these suburbs are much wealthier overall with many of the variables supporting this conclusion.

```
nrow(bos[bos$rm >8,])
```

[1] 13