

HASHING

- 1) Open Hashing (closed addressing)
- 2) Closed Hashing (open addressing)

key = 6, 26

$$h(k_i) = k_i \% m$$

$$m = 10$$

$$6 \% 10 = 6$$

$$26 \% 10 = 6$$



→ Open Hashing - chaining method

→ Closed Hashing (open addressing)

Linear Probing

Quadratic Probing

Double Hashing

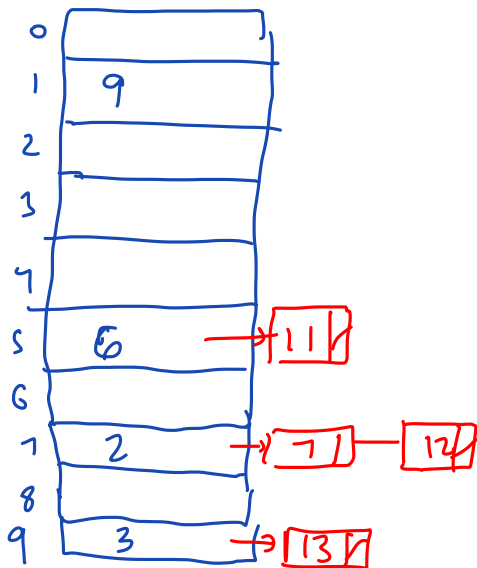
to resolve collision

① A = 3, 2, 9, 6, 11, 13, 7, 12] key value

$$h(k) = 2k + 3$$

m = 10 (size of hash table)

use division method & closed addressing technique to store these values



closed addressing / chaining

→ create linked list when collision occurs

$$h(k) = k_i \% m$$

key	location
3	$[2(3) + 3] \% 10 = 9 \% 10 = 9$
2	$7 \% 10 = 7$
9	$21 \% 10 = 1$
6	$6(2) + 3 = 15 \% 10 = 5$
11	$25 \% 10 = 5$
13	$29 \% 10 = 9$
7	$17 \% 10 = 7$
12	$27 \% 10 = 7$

→ Linear Probing Method / Open addressing

0	13
1	9
2	12
3	
4	
5	6
6	11
7	2
8	7
9	3

key	Location	Probes
3	9	1
2	7	1
9	1	1
6	5	1
11	5	2
13	9	2
7	7	2
12	7	6

Collision at 5th place so go to next place

Order of elements: 13, 9, 12, —, —, 6, 11, 2, 7, 3

→ Insert k_i at first free location from $(u + i) \% m$ where $i = 0$ to $(m - 1)$

$$\begin{aligned}
 \text{for } 11 &= (u + i) \% m \\
 &= (5 + 0) \% 10 = 5 \% 10 = 5 \\
 &\text{so not free so } i = 1 \\
 (5 + i) \% m &= 6 \% 10 = 6 \checkmark \\
 &= \text{free}
 \end{aligned}$$

Double Hashing

$A = 3, 2, 9, 6, 11, 13, 7, 12$

$h_1(k) = 2k + 3 \quad m = 10$

$h_2(k) = 3k + 1$

if collision,
insert K_i at first free place
from $(u + v * i) \% m$

$[i = 0 + (m-1)]$

$(u + i) \% m$
 $(u + i^2) \% m$

Calculate v
using 2nd
hash function
 $v = h_2(k) \% m$

↓
apply only
during
collision

0	
1	9
2	
3	11
4	12
5	6
6	
7	2
8	
9	3

key	location (u)	v	Probe
3	$(2(3)+3)\%10 = 9$	—	1
2	7	—	1
9	1	—	1
6	5	—	1
11	5 (collision)	$v = 3(11)+1$ $34\%10 = 4$	3
x 13	9	$v = 3(13)+1$ $39\%10 = 9$	—
x 7	7	$v = 3(7)+1$ $22\%10 = 2$	—
12	7	$v = 3(12)+1$ $37\%10 = 7$	2 (i=0 i=1)

always
get 9
so can't
insert 13
into hash
table

- ① $(9 + (0 * 7)) \% 10$
 $9 \% 10 \rightarrow \text{not}$
- ② $(9 + (0 * \text{anything times over})) \% 10$
 \downarrow
be 0

③ $(7 + (2 * 0)) \% 10$
 $7 \% 10 = 7 \rightarrow \text{not free}$

④ $(7 + (2 * 1)) \% 10$
 $9 \% 10 \rightarrow \text{not}$

⑤ $(7 + 4) \% 10 = 11$
 $11 \% 10 = 1 \rightarrow \text{not}$

⑥ $(7 + 6) \% 10 = 13$
 $13 \% 10 = 3 \rightarrow \text{not}$

⑦ $(7 + 8) \% 10 = 15$
 $15 \% 10 = 5 \rightarrow \text{not}$

⑧ $(7 + 10) \% 10 = 17$
 $17 \% 10 = 7 \rightarrow \text{not}$

⑨ $(7 + 2(6)) \% 10 = 19$
 $19 \% 10 = 9$

⑩ $(7 + 2(7)) \% 10 = 21$
 $21 \% 10 = 1$

⑪ $(7 + 2(8)) \% 10 = 23$
 $23 \% 10 = 3$

⑫ $(7 + 2(9)) \% 10 = 25$
 $25 \% 10 = 5 \rightarrow \text{not free}$

$(u + v * i) \% m$
 $(5 + (4 * 0)) \% 10$
Probe 1 $(5 + 0) \% 10$
 $5 \% 10 = 5 \rightarrow \text{not free}$

Probe 2 $(5 + (4 * 1)) \% 10$
 $9 \% 10 = 9 \rightarrow \text{not free}$

Probe 3 $(5 + (4 * 2)) \% 10$
 $13 \% 10 = 3 \rightarrow \text{Free}$

* Order of elements:

—, 9, —, 11, 12, 6, —, 2, —, 3

also calculate
sum
insertion

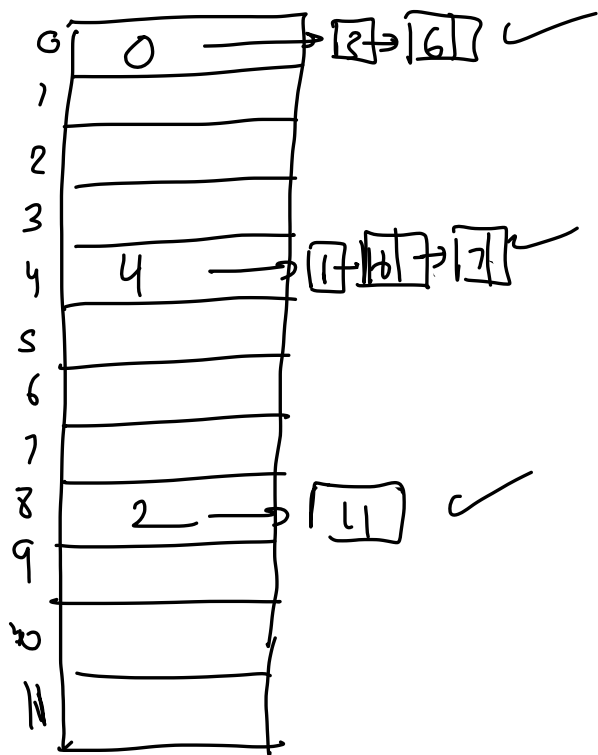
Hashing Practice Problems

0, 4, 7, 1, 2, 3, 6, 11, 16

$m = 12$

$h(x) = 4x$

CHaining



Key	Location
0	$4(0) \% 12 = 0$
4	$16 \% 12 = 4$
7	$28 \% 12 = 4$
1	$4 \% 12 = 4$
2	$8 \% 12 = 8$
3	$12 \% 12 = 0$
6	$24 \% 12 = 0$
11	$44 \% 12 = 8$
16	$64 \% 12 = 4$

$$\begin{array}{r} 12 \overline{) 28} \\ 24 \\ \hline 4 \end{array}$$

$$\begin{array}{r} 12 \overline{) 28} \\ 24 \\ \hline 4 \end{array}$$

$$\begin{array}{r} 12 \overline{) 24} \\ 24 \\ \hline 0 \end{array}$$

$6(4) = 24$
 $24 \% 12 = 0$

LINEAR PROBING

2, 4, 6, 7, 15, 13, 19

$m = 13$

$h(x) = 3x$

Key	hash	Pro
2	$3(2) \% 13 = 6$	6
4	12	12
6	18	5
7	21	8
15	45	6
13	39	0
19	57	5

0	13
1	/
2	/
3	/
4	/
5	6
6	2
7	15
8	7
9	19
10	/
11	/
12	4

$$\begin{array}{r} 12 \overline{) 36} \\ 36 \\ \hline 0 \end{array}$$

$$\begin{array}{r} 12 \overline{) 39} \\ 36 \\ \hline 3 \end{array}$$

Double Hashing
 $m = 11$

keys to insert: 20, 34,

