

# Adding Stage of Infection to HIV Back-Calculation in WA State, 2005-2014

Martina Morris and Jeanette Birnbaum

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## 1 Overview

This report contains the initial results comparing the standard testing history model results for WA State undiagnosed estimates to an extended model incorporating stage of infection data.

## 2 Data

### 2.1 Description of analytic sample

Data from the advanced HIV/AIDS reporting system (eHARS) and the CDC treatment and testing history questionnaire (HIS) provided records for 26,134 HIV cases in WA state.<sup>1</sup>

#### 2.1.1 Exclusions

Figure 1 diagrams the construction of the analytic sample. We first restricted to cases diagnosed in WA state in the years 2005-2014. We further excluded cases diagnosed at age 16 or younger if their date of last negative test was missing, because the assumptions we use when date of last negative test is missing are not applicable to this age group.

The final sample includes 5,176 cases. In the 2014 report there were 4744 cases in the final sample across diagnosis years 2005-2013. Of the additional 447 diagnoses reported in 2014 eligible for this analysis, 432 met all our inclusion criteria.

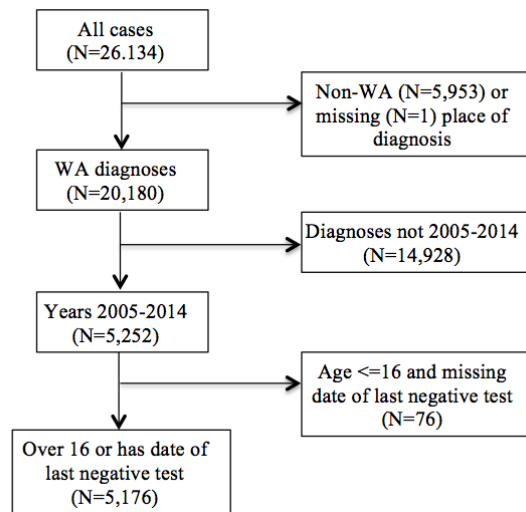


Figure 1: Construction of analytic sample

<sup>1</sup>Provided by Jason Carr, Washington State Department of Health, June 2015

### 2.1.2 Sample characteristics

This section focuses on the new characteristics we are working with: BED result and dual diagnosis.

Table 1: Cross-tabulation of BED and dual diagnoses, 2005-2014

	DD+		DD-		Total	
	N	Row %	N	Row %	N	Col %
BED -	382	27	1029	73	1411	27
BED +	101	11	779	89	880	17
BED Miss	1238	43	1647	57	2885	56
Total	1721	33	3455	67	5176	100

Table 2: Cross-tabulation of BED and dual diagnoses, 2014 only

	DD+		DD-		Total	
	N	Row %	N	Row %	N	Col %
BED -	2	6	32	94	34	8
BED +	2	6	29	94	31	7
BED Miss	119	32	257	68	376	85
Total	123	28	318	72	441	100

Table 3: Composition of analytic sample by BED and dual diagnosis status. Column % sums to 100 across the full sample. Availability of testing history data within each subgroup level is shown as row percents

		Ever Had a Negative Test				
BED Result	Dual Diagnosis	N	Column %	% Yes	% No	% Missing
BED +	DD +	101	2	43	18	40
	DD -	779	15	75	6	19
BED -	DD +	382	7	29	21	50
	DD -	1029	20	58	14	28
BED Miss	DD +	1238	24	33	18	49
	DD -	1647	32	39	7	54
Total		5176	100	46	12	42

The presence of an LNT ranges pretty dramatically across groups, from 29 to 75% (Table 3). Missingness also varies substantially, from 19 to 54%.

What are the implications of these associations, for example the fact that LNTs are much more common among the BED+DD- than the BEDm? Just that the BED information won't be as useful as it could be if it wasn't correlated with missing/no LNT?

Table 4 shows the same information for MSM vs non-MSM groups. The BED information is relatively more helpful in the non-MSM group, since there is more missingness among BED+ non-MSM than among BED+ MSM. But BED+ non-MSM only comprise 4% of the entire sample, so the absolute impact is minor.

### 2.1.3 Time trends

## 2.2 Stage of infection impact on infection window

The purpose of this section is to understand how many individuals will have their individual probabilities of infection altered due to a BED result and/or dual diagnosis, and to what extent.

We have 6 stage categories, 3 BED categories x 2 dual diagnosis subgroups. The table in Figure 3 is our original plan for the Base Case for each subgroup.

The following subsections detail the changes to the Base Case for each subgroup. Table 5 summarizes the distribution of cases by type of change. In this table, those changed by being BED+ are not only BED+ but also have a reported or imputed infection window that is greater than the BED window of 162 days.

### 2.2.1 BED+, DD+

How likely are the 101 (2% of the sample) are these cases to be false BED+?

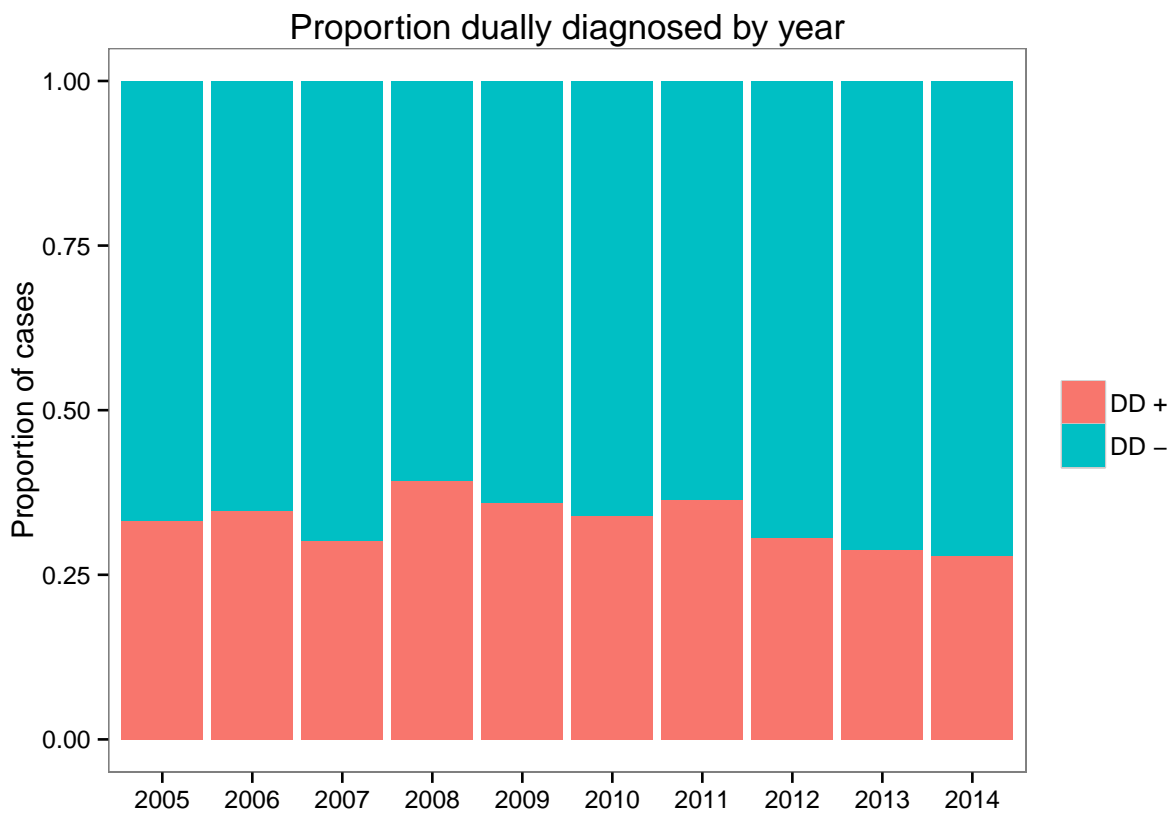


Figure 2: Percent of cases who are dual diagnoses by year

Table 4: Composition of analytic sample by MSM vs non-MSM, BED and dual diagnosis status. Column % sums to 100 across the full sample. Availability of testing history data within each subgroup level is shown as row percents

					Ever Had a Negative Test		
MSM	BED Result	Dual Diagnosis	N	Column %	% Yes	% No	% Missing
MSM	BED +	DD +	57	1	56	14	30
		DD -	628	12	82	4	15
	BED -	DD +	203	4	37	19	43
		DD -	669	13	71	10	19
	BED Miss	DD +	692	13	44	15	41
		DD -	1154	22	48	5	47
non-MSM	BED +	DD +	44	1	25	23	52
		DD -	151	3	46	16	38
	BED -	DD +	179	3	20	22	58
		DD -	360	7	33	21	46
	BED Miss	DD +	546	11	20	22	58
		DD -	493	10	19	10	71
Total			5176	100	46	12	42

BED Result	Dual Diagnosis	Status of LNT Data:	
		LNT Date Known	No Previous Test
+	Yes	$x_i^* = \min(x_i, x_{BED})$ $p(i,t)^* = Cp(i,t)p(AIDS)$	$x_i^* = x_{BED}$ $p(i,t)^* = Cp(i,t)p(AIDS)$
	No	$x_i^* = \min(x_i, x_{BED})$	$x_i^* = x_{BED}$
-	Yes	If $x_i > x_{BED}$ , $p(i,t) = p_{BED}(i,t)$ $p(i,t)^* = Cp(i,t)p(AIDS)$	$x_i = \min(\text{age}-16, 18)$ $p(i,t) = p_{BED}(i,t)$ $p(i,t)^* = Cp(i,t)p(AIDS)$
	No	If $x_i > x_{BED}$ , $p(i,t) = p_{BED}(i,t)$	$x_i = \min(\text{age}-16, 18)$ $p(i,t) = p_{BED}(i,t)$
Missing	Yes	$p(i,t)^* = Cp(i,t)p(AIDS)$	$p(i,t)^* = p(AIDS)$
	No	No change: $p(i,t) = 1/x_i$	No change: $p(i,t) = 1/x_i$ and $x_i = \min(\text{age}-16, 18)$

**Table 2. Impact of stage of infection data on the Base Case probability model of time from infection to diagnosis.** All stages of infection have a modified infection window  $x_i^*$  and/or modified probability model of time from infection to diagnosis  $p(i,t)^*$  except when BED status is missing and there is no dual diagnosis (final row). For the BED+, the modified  $x_i^*$  has a maximum value of the BED window  $x_{BED}=162$  days. Dual diagnoses have a  $p(i,t)$  modified by  $p(AIDS)$ , the AIDS incubation distribution (Figure 2), with a scalar  $C$  to constrain cumulative probability of infection over the window to 1. For the BED- with  $x_i > x_{BED}$ , their  $p(i,t) = p_{BED}(i,t) = I(t > x_{BED}) * (1/(x_i - x_{BED}))$ , i.e. all probability falls between  $x_{BED}$  and  $x_i$ . When LNT data are missing, they are considered missing at random conditional on the stage of infection.

Figure 3: Plan for the extended model, for each of the 6 stages of infection

“One important issue with antibody-based assays for recent infection, such as the BED assay, is that persons with advanced HIV disease (AIDS) will tend to be classified as having recent infections because of associated declines in anti-HIV antibody levels. Furthermore, persons receiving antiretroviral therapy may also be classified as having recent infection by some of these assays. This has led to the recommendation that it is necessary to exclude persons with AIDS or persons on antiretroviral therapy from being counted in the window period” (Brookmeyer 2010 Measuring the HIV-AIDS epidemic, citing a CDC factsheet that is no longer available).

The BED assay is known to overestimate HIV incidence under certain conditions and in certain settings. As a result there is some debate as to the best way to interpret BED results. One strategy “corrects for assay imperfection on the level of the individual by using additional information (eg, antiretroviral therapy ART utilization, AIDS diagnosis and previous HIV testing) to either reclassify or exclude individuals who are classified as recent by the BED assay but are obviously nonrecently infected (false-recent individuals). The second strategy corrects for assay imperfection at the population level, using incidence estimators that account for imperfect specificity of the BED assay” (Barnighausen 2010, HIV Incidence Estimation Using the BED Capture Enzyme Immunoassay).

This was my motivation for considering BED+, DD+ individuals to be likely false recent. Given the impression I get from the literature regarding the concern that BED overestimates recent infections, we may do well to err on the conservative side of treating the BED+ result as a true recent infection.

Table 5: Among the 3013 cases with non-missing testing history, row percents of each LNT/no LNT group not impacted by stage of infection data (No Change), impacted by being BED+ and having an infection window greater than 162 days (BED+ only), impacted by a dual diagnosis (DD+ only), or both (BED+ and DD+). Totals are row N.

	No Change	BED+ only	DD+ only	BED+ and DD+	Totals
LNT	60.4	15.9	22.3	1.3	2394.0
no LNT	40.7	7.6	48.8	2.9	619.0

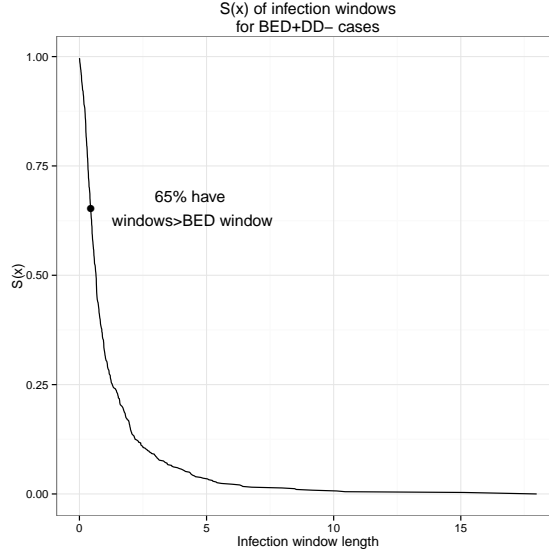


Figure 4: Infection windows of the BED+DD- who have observed windows

### 2.2.2 BED+, DD-

These 779 (15% of the sample) need their infection window modified to the BED window if it is longer than the BED window or they have no LNT.

We know that NA% of these NA cases have no LNT and will get a LNT of the BED window (Table 3). Another NA% of the cases have an infection window.

Figure 4 shows that 65% of the observed windows will be shortened by using the BED window as the max.

### 2.2.3 BED-, DD+

All of the NA cases (NA% of sample) will have their probabilities of infection distributed according to the AIDS incubation distribution rather than a uniform distribution.

The CDC model uses a probability distribution for annual diagnosis of AIDS that they say is “derived from the AIDS incubation distribution” and is gamma(shape=2, scale=4). For our PLoS One paper, we sourced a reference that estimated a Weibull(shape=2.516, scale=1/0.086). The two curves are compared in Figure 5. We’ll have to look at the references more closely to understand the differences.

Regarding the infection window, those with no LNT will get the usual assumption of  $\min(\text{age} - 16, 18)$ . But for those assumed windows as well as the observed windows, those longer than the BED window will have their probability distributed outside the window, that is, zero probability until 162 days (Figure 6).

### 2.2.4 BED-, DD-

These NA cases (NA% of sample) will have their probabilities of infection distributed outside of the BED window if their windows are longer than 162 days, as with the BED-DD+ (Figure 7).

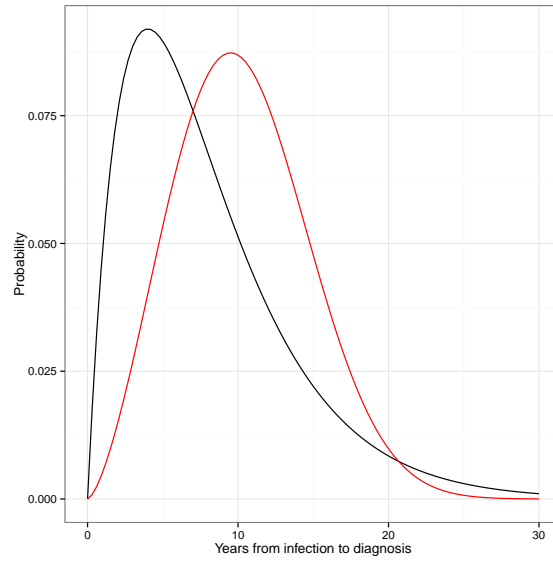


Figure 5: Probability of AIDS diagnosis by years since infection for  $\text{gamma}(2,4)$  and  $\text{weibull}(2.516, 1/0.086)$  - weibull in red

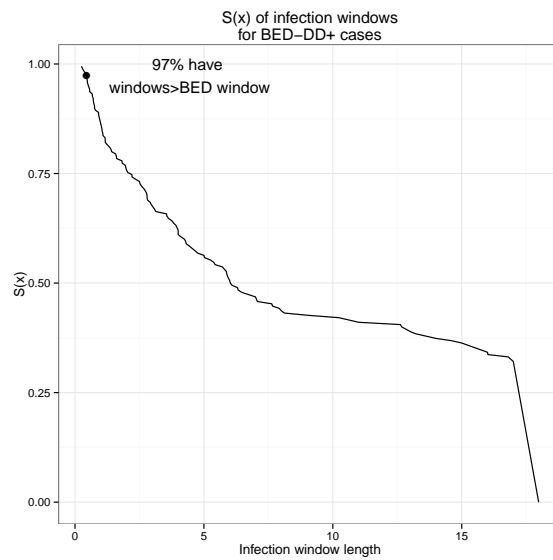


Figure 6: Infection windows of the BED-DD+, either observed or assumed as  $\min(\text{age}-16, 18)$  for those with no LNT

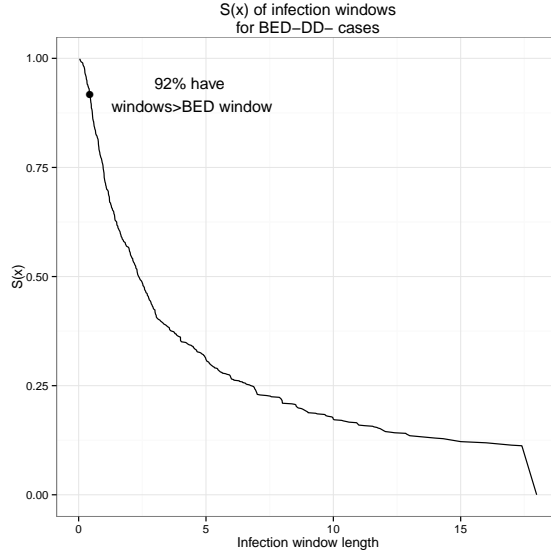


Figure 7: Infection windows of the BED-DD-, either observed or assumed as  $\min(\text{age}-16, 18)$  for those with no LNT

### 2.2.5 BEDm, DD+

The NA cases (NA% of sample) who are BEDmDD+ will either have their probability of infection distributed using the AIDS incubation distribution across their infection window (NA%) or, if they have no LNT, across the full length of the incubation window (NA%).

### 2.2.6 BEDm, DD-

These NA cases (NA% of sample) have no change to their infection window or probability of infection compared to the original Base Case.

### 2.2.7 Impact on Upper Bound

There is no impact of dual diagnosis on the upper bound case, since all probability is assumed to be immediately after the LNT. For the BED+DD-, the LNT will be modified to  $\min(\text{LNT}, \text{BED window}=162 \text{ days})$ .

## 3 Methodological Notes

1. The results in the next section are an abbreviated form of the changes described in the previous section. Only the BED-related modifications were made to the infection windows. The full plan for the Base Case involves altering the uniform probability distribution to the AIDS incubation curve, truncated to the infection window. This is not yet implemented.
2. We decided to treat missing testing histories as missing conditional on stage of infection. My current method for executing this assumption is to run the model on each subgroup. This approach computes the TID separately for each group and applies that TID to estimate incidence only on the diagnosis counts from that subgroup.
3. This is conceptually reasonable but poses sample size problems. The BED+DD+ and BED-DD+ groups were both too small to estimate quarterly incidence. Hence the decision to roll BED+DD+ in with BEDmDD+ and combine BED-DD+ with BED-DD-. I doubt this decision affected the total results much, given the relatively small sizes of those groups.

4. We will need to investigate the sample size limits of the method—they are currently unknown. When quarterly diagnoses are very small, we may want to consider increasing the time step to half or full years.
5. I also want to highlight that the way the method currently works is that the TID is generated from all the data used in the estimation. So here we use WA State data for 2005-2014.
6. A small percentage of BED- cases have LNTs that are shorter than 162 days, indicating false negatives or reporting error. (Figures 6 and 7). This leads to the next point:
7. I think we should work towards a way of incorporating BED results that better reflects the fact that it is intended for population-level interpretation, since the false positive and false negative rates are high but approximately equal. Something where we use the proportions of BED+/- cases rather than look at the individual BED results. However...
8. BED result is correlated with LNT presence/absence and length, so we'll have to think about that too.

## 4 Aggregating from six to four stage subgroups

We have to aggregate the two smallest BED-DD groups in order to have sufficient sample size. This is a short-term solution. Ultimately we should explore the sample size limits of the method, the impact of using a longer time-step than quarter-year, and ways that the TID can fairly reflect missing data without needing to stratify the estimation.

## 5 Results

### 5.1 Time from infection to diagnosis (TID)

Figure 8 shows, for each original stage subgroup, the estimated distribution of TID in the analytic sample for the Base Case under the original method and the Base Case under the extended method. Figure 9 shows the same information for the 4 final stage subgroups used in the analysis. Figure 10

### 5.2 Unstratified, Without-Stage Results

The estimated incidence and undiagnosed counts for each scenario are shown as quarterly counts in Figure 11 and summarized over all quarters in Table 6. These results are not stratified by any group, although we do have a version of the total results that reflects stratification by MSM and non-MSM.

Table 6: Observed diagnoses and estimated quarterly incidence and undiagnosed counts over 2005-2014 in WA state

Diagnoses/Case	Estimate	Min.	1st Qu.	Median	Mean	3rd Qu.	Max.
# Diagnosed	Diagnoses	91	120	129	129	140	163
Base Case	Incidence	108	115	126	124	134	138
Base Case	Undiagnosed Cases	1236	1303	1401	1371	1435	1461
Upper Bound	Incidence	105	109	121	120	130	135
Upper Bound	Undiagnosed Cases	2473	2575	2739	2704	2818	2870

Table 7: Estimated true prevalence and the undiagnosed fraction in WA state, limited to just 2014

Year	Diagnoses/Case	Estimate	Min.	1st Qu.	Median	Mean	3rd Qu.	Max.
2014.0	PLWHA	PLWHA				12691.0		
2014.0	Base Case	Undiagnosed Cases	1236.0	1243.0	1253.0	1251.0	1261.0	1262.0
2014.0	Base Case	True Prevalence	13927.0	13934.0	13944.0	13942.0	13952.0	13953.0
2014.0	Base Case	Undiagnosed Fraction (%)	8.9	8.9	9.0	9.0	9.0	9.0
2014.0	Upper Bound	Undiagnosed Cases	2473.0	2480.0	2494.0	2492.0	2507.0	2509.0
2014.0	Upper Bound	True Prevalence	15164.0	15171.0	15185.0	15183.0	15198.0	15200.0
2014.0	Upper Bound	Undiagnosed Fraction (%)	16.3	16.3	16.4	16.4	16.5	16.5



### 5.3 Stratified, Without- and With-Stage Results

When we run the model allowing stage (so far, just BED) to impact the TID, we also stratify by stage subgroups in order for the missing testing histories to be missing conditional on stage subgroup.

Quarterly incidence and undiagnosed counts are plotted in Figure 12. The summary results over 2005-2015 and for 2014 alone are given in Table 8. The mean without- and with-stage undiagnosed estimates for those two time periods are compared in Table 9. Table 10 shows the 2014 undiagnosed fraction results as well.

Regarding the impact on uncertainty, from Table 9 we can additionally calculate that the undiagnosed range in 2014 was 1,277-2,502 and adding stage decreased that to 1,195-2,344, which amounts to a difference of 76 cases. From Table 10 that amounts to a decrease from 7.2% to 6.9% for the range of the mean undiagnosed fraction.

Table 8: Observed diagnoses and estimated quarterly incidence and undiagnosed counts over 2005-2014 and just 2014 in WA state, using stage-subgroup strata

Year	Case	Estimate	Min.	1st Qu.	Median	Mean	3rd Qu.	Max.
2005-2014	Base Case	Undiagnosed Cases	1269	1372	1433	1403	1443	1467
2005-2014	Base Case using Stage	Undiagnosed Cases	1188	1288	1405	1350	1413	1432
2005-2014	Upper Bound	Undiagnosed Cases	2487	2640	2844	2756	2871	2901
2005-2014	Upper Bound using Stage	Undiagnosed Cases	2328	2448	2678	2599	2743	2757
2014	Base Case	Undiagnosed Cases	1269	1274	1279	1277	1280	1282
2014	Base Case using Stage	Undiagnosed Cases	1188	1192	1196	1195	1198	1200
2014	Upper Bound	Undiagnosed Cases	2487	2498	2509	2502	2510	2511
2014	Upper Bound using Stage	Undiagnosed Cases	2328	2339	2349	2344	2352	2354

Table 9: Impact of using BED result to modify the TID on mean undiagnosed estimates

Year	Case	With Stage	Without Stage	Difference	Percent Change
2005-2014	Base Case	1350.0	1403.0	-53.0	-4.0
2005-2014	Upper Bound	2599.0	2756.0	-157.0	-6.0
2014	Base Case	1195.0	1277.0	-82.0	-6.0
2014	Upper Bound	2344.0	2502.0	-158.0	-6.0

Table 10: Estimated true prevalence and the undiagnosed fraction for 2014 in WA state, using stage-subgroup strata

Year	Diagnoses/Case	Estimate	Min.	1st Qu.	Median	Mean	3rd Qu.	Max.
2014.0	PLWHA	PLWHA				12691.0		
2014.0	Base Case	Undiagnosed Cases	1269.0	1274.0	1279.0	1277.0	1280.0	1282.0
2014.0	Base Case using Stage	Undiagnosed Cases	1188.0	1192.0	1196.0	1195.0	1198.0	1200.0
2014.0	Upper Bound	Undiagnosed Cases	2487.0	2498.0	2509.0	2502.0	2510.0	2511.0
2014.0	Upper Bound using Stage	Undiagnosed Cases	2328.0	2339.0	2349.0	2344.0	2352.0	2354.0
2014.0	Base Case	True Prevalence	13960.0	13965.0	13970.0	13968.0	13971.0	13973.0
2014.0	Base Case using Stage	True Prevalence	13879.0	13883.0	13887.0	13886.0	13889.0	13891.0
2014.0	Upper Bound	True Prevalence	15178.0	15189.0	15200.0	15193.0	15201.0	15202.0
2014.0	Upper Bound using Stage	True Prevalence	15019.0	15030.0	15040.0	15035.0	15043.0	15045.0
2014.0	Base Case	Undiagnosed Fraction (%)	9.1	9.1	9.2	9.1	9.2	9.2
2014.0	Base Case using Stage	Undiagnosed Fraction (%)	8.6	8.6	8.6	8.6	8.6	8.6
2014.0	Upper Bound	Undiagnosed Fraction (%)	16.4	16.4	16.5	16.5	16.5	16.5
2014.0	Upper Bound using Stage	Undiagnosed Fraction (%)	15.5	15.6	15.6	15.6	15.6	15.6

## 6 Conclusion

It's my feeling that we should explore a more population-based approach to incorporating the BED results and one that doesn't involve stratifying the model runs by subgroup. We should also consider introducing

BED and DD in a stepwise fashion to understand their relative contributions, once the AIDS incubation distribution is incorporated.

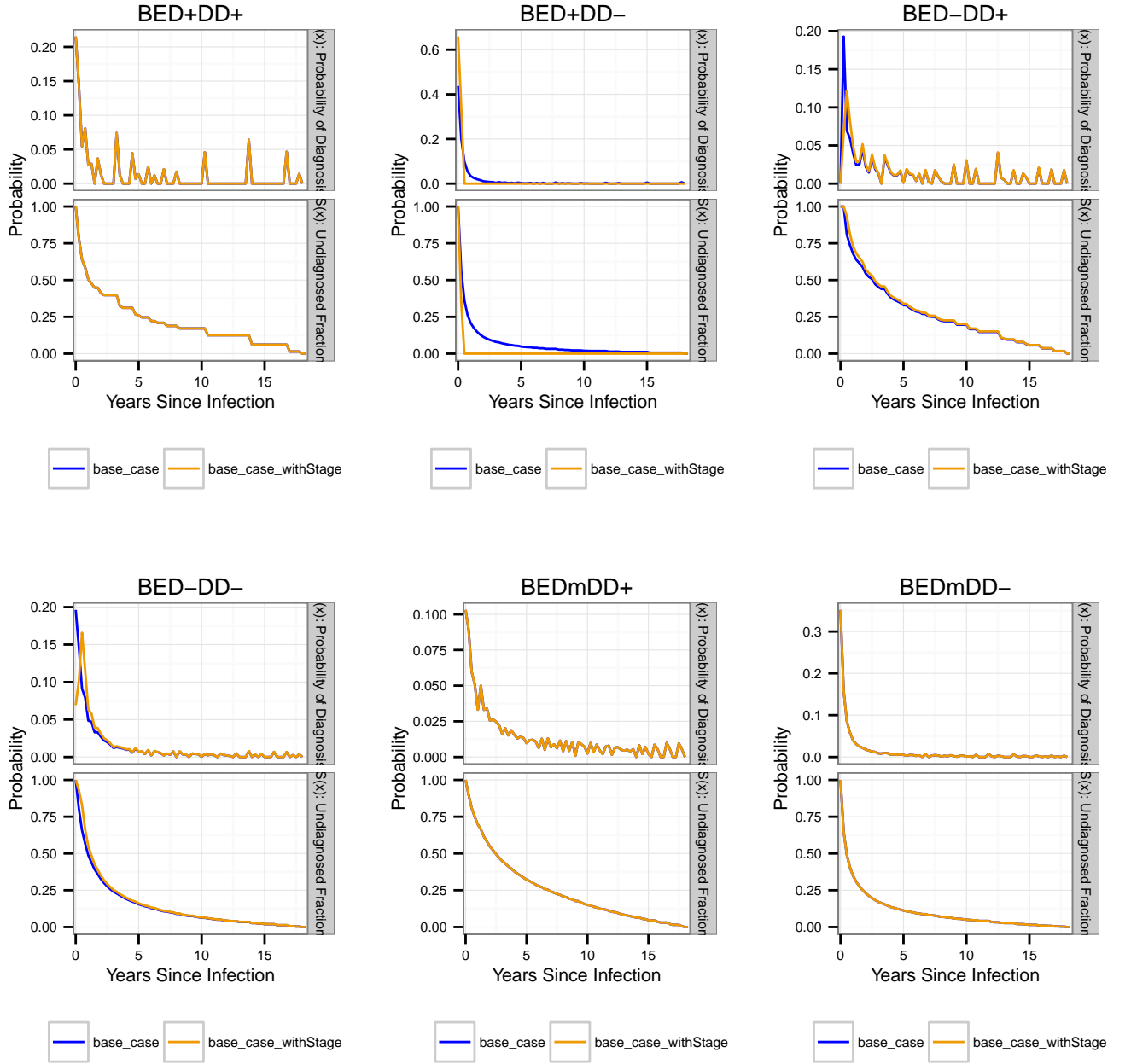


Figure 8: Time from infection to diagnosis (TID) for base case without and with stage, 6 groups

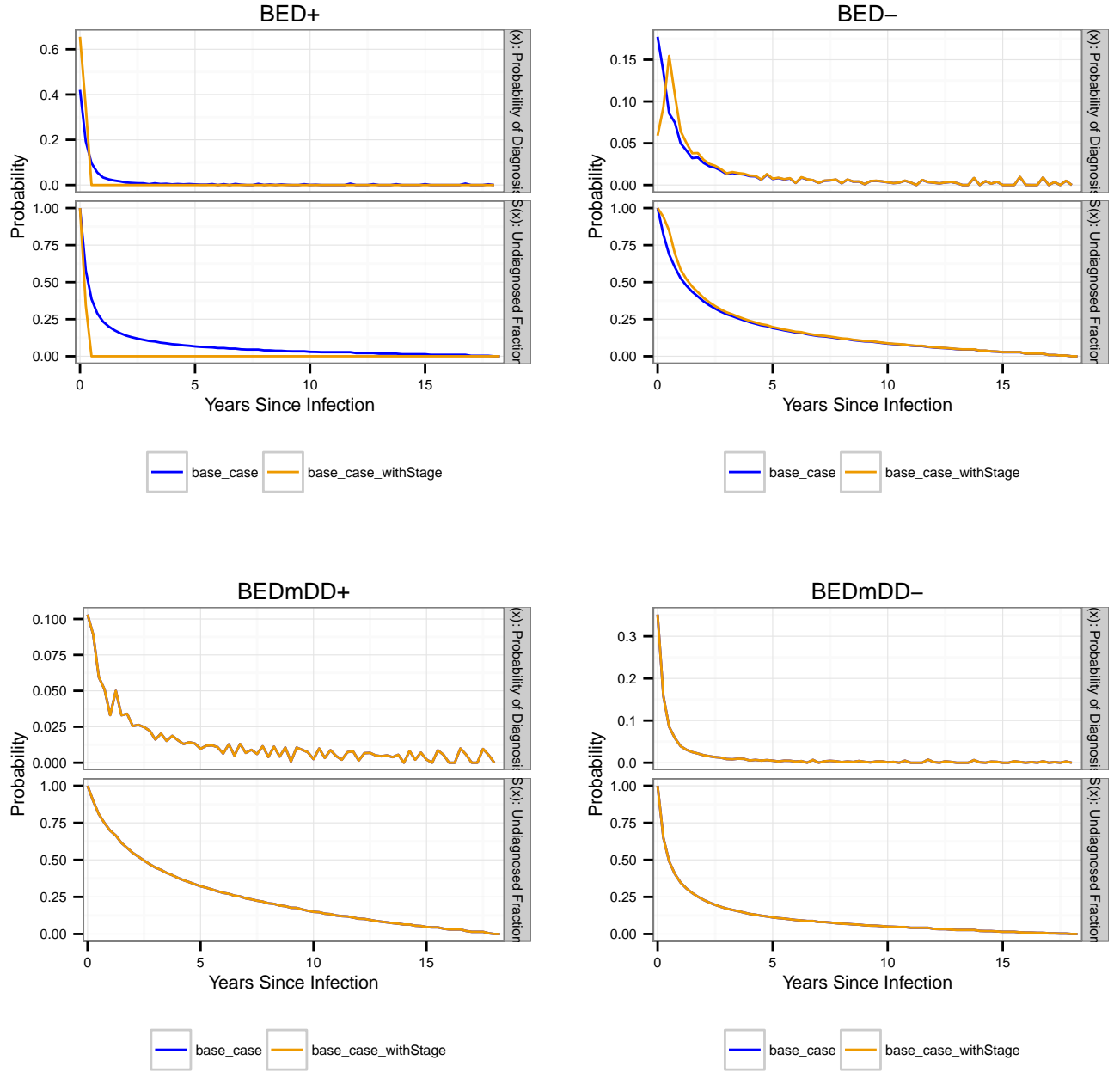


Figure 9: Time from infection to diagnosis (TID) for base case without and with stage, 4 groups

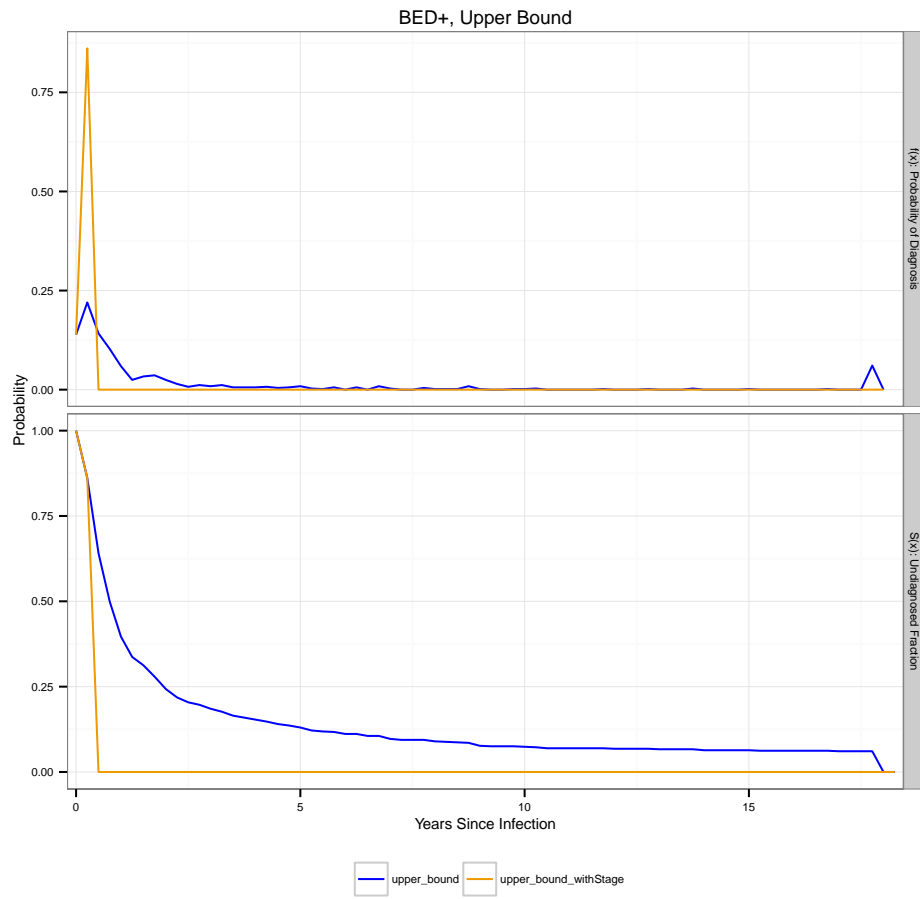


Figure 10: Time from infection to diagnosis (TID) for upper bound without and with stage, BED+DD-

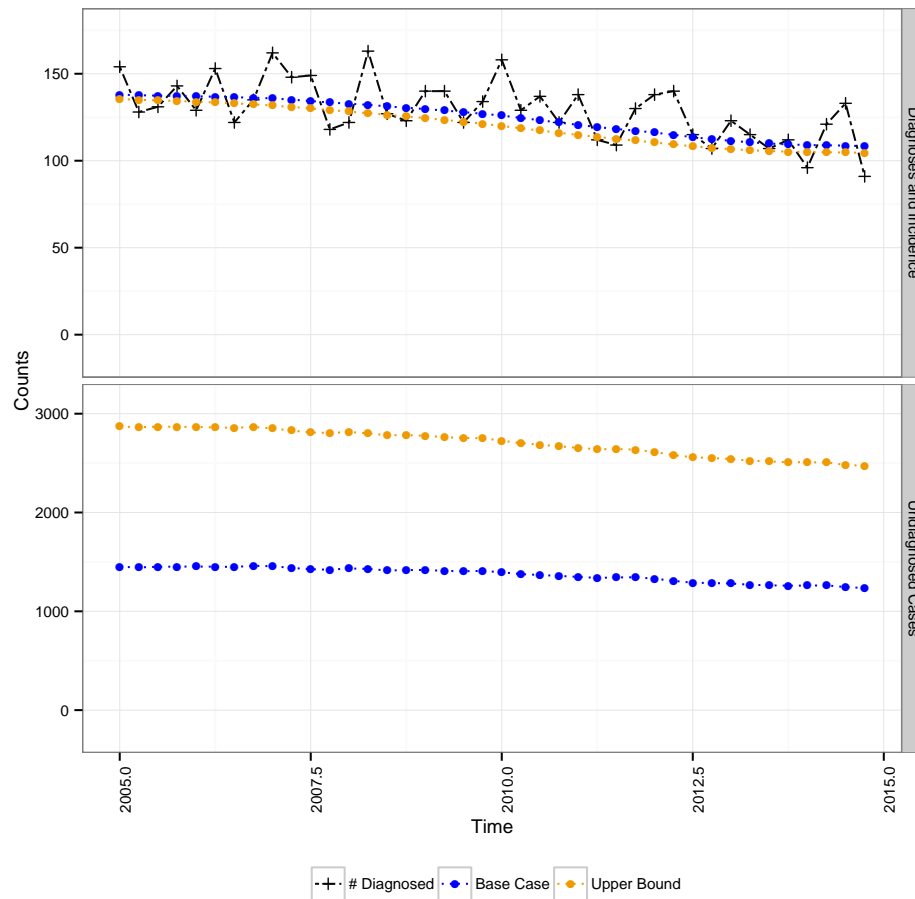


Figure 11: Observed diagnoses and estimated quarterly and undiagnosed counts over 2005-2014 in WA state

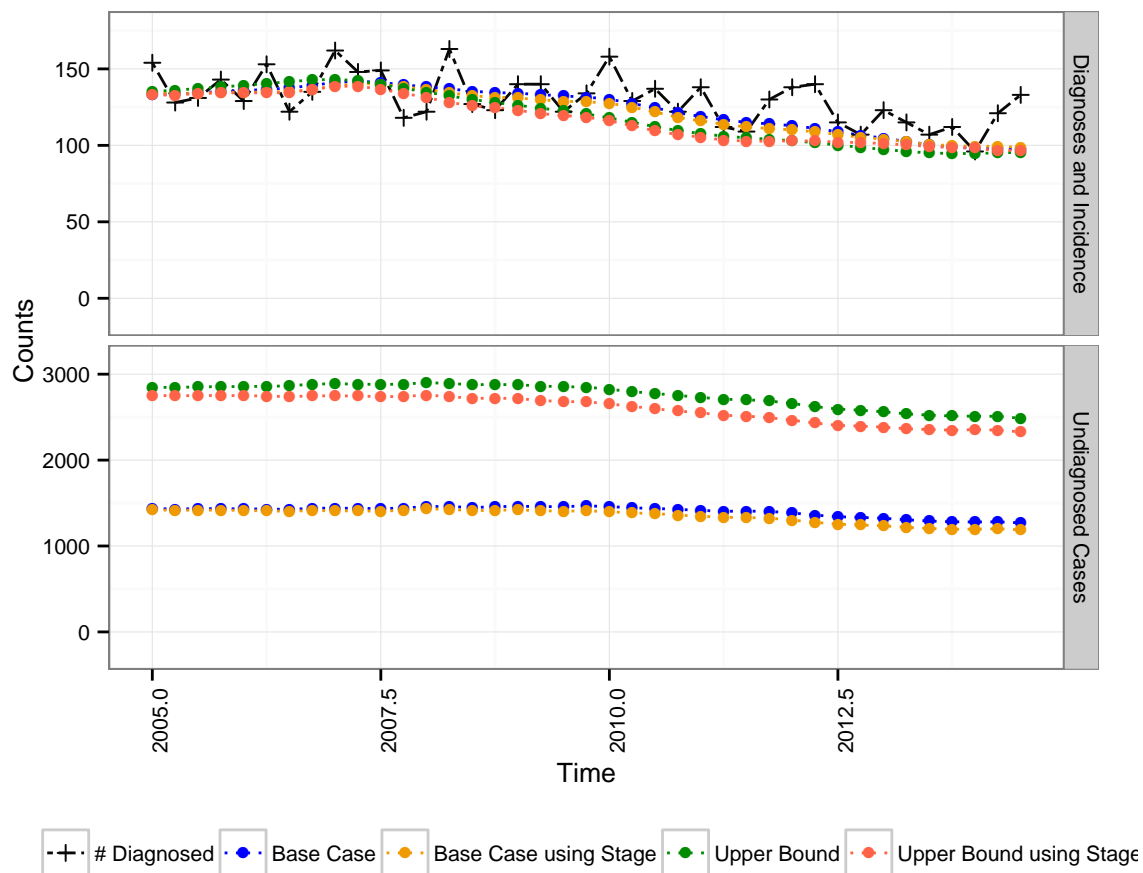


Figure 12: Observed diagnoses and estimated quarterly and undiagnosed counts over 2005-2014 in WA state, using stage-subgroup strata