

An incomplete bibliography of network geometry

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Compiled on 2021-11-01

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The \mathbb{S}^1 and \mathbb{H}^2 models, their applications, and their variants

Models of undirected graphs

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Models of bipartite graphs

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Models of multiplex graphs

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